

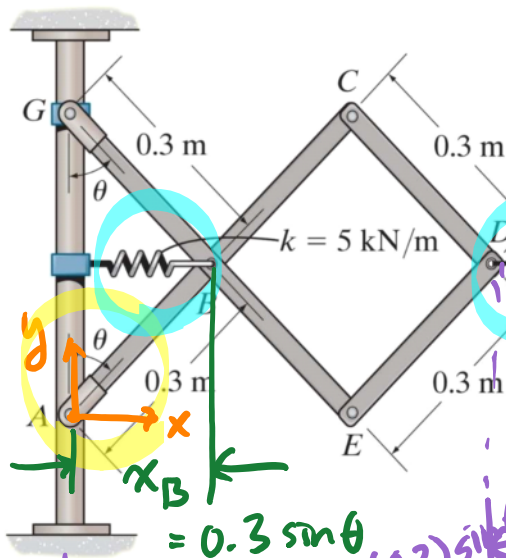
Announcements

- CBTF Quiz 5 retry starts tomorrow (Thursday)
- Last day of class: Monday, April 29
- No discussion sections next week
- Last day of office hours and Piazza help: Wednesday, May 1
- CBTF (last) Quiz 6 starts Thursday, May 2

□ Upcoming deadlines:

- Friday (4/26): Written Assignment
- Wednesday (5/1): Last PL HW





Determine the required force P needed to maintain equilibrium of the scissors linkage when the angle is 60 degrees.

The spring is unstretched when the angle is 30 degrees.

$$F_{\text{spring}} = k s = k(l - l_0)$$

$$\begin{cases} l_0 = 0.3 \sin 30^\circ \\ l = 0.3 \sin \theta \end{cases}$$

$$\rightarrow F_{\text{spring}} = k(0.3)(\sin \theta - \sin 30^\circ)$$

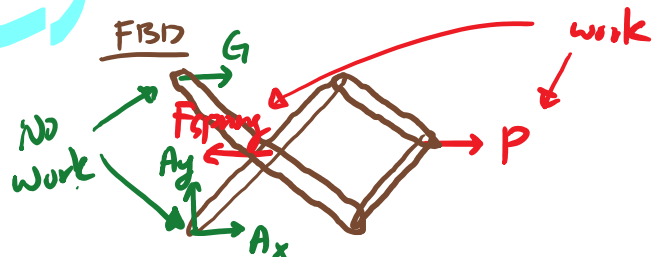
$$\frac{\delta}{\delta \theta} (x_B) = 0.3 \cos \theta$$

$$\frac{\delta}{\delta \theta} (x_D) = 0.9 \cos \theta$$

$$\Sigma dU = 0 = -k(0.3)(\sin \theta - \sin 30^\circ)(0.3 \cos \theta) + P(0.9 \cos \theta)$$

$$k(0.3)(\sin \theta - \sin 30^\circ)(0.3 \cos \theta) = 0.9 P \cos \theta$$

$$\sin \theta - \sin 30^\circ = \frac{0.9 P}{(0.3)(0.3)k} \rightarrow \boxed{\sin \theta = \frac{10P}{k} + \sin 30^\circ}$$



Virtual Work

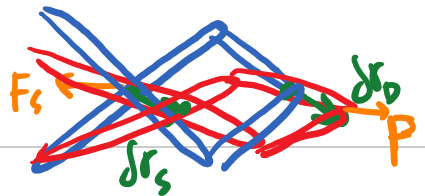
$$\Sigma dU = 0 = dU_{\text{spring}} + dU_P$$

$$dU_{\text{spring}} = \vec{F}_{\text{spring}} \cdot \delta \vec{r}_B$$

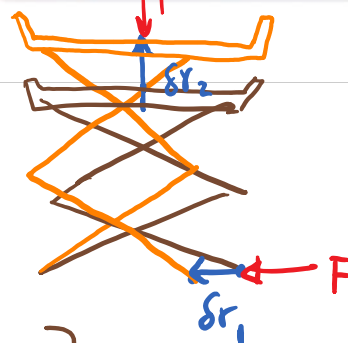
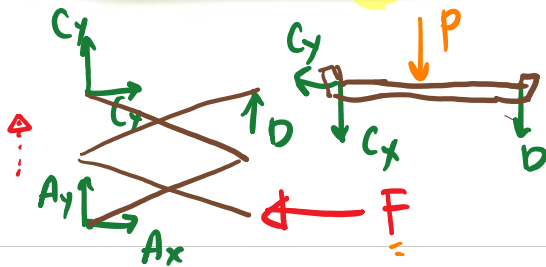
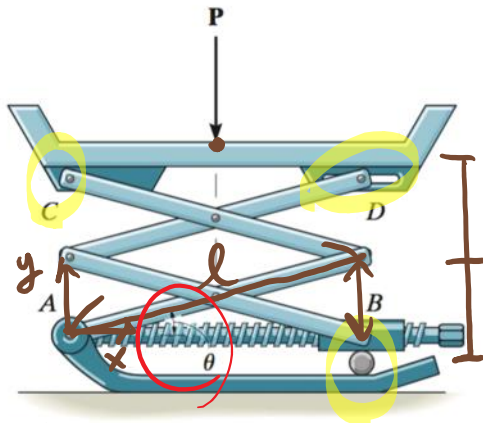
$$\text{or} = F_{\text{spring}} \delta x_B$$

$$dU_P = \vec{P} \cdot \delta \vec{r}_D$$

$$\text{or} = P \delta x_D$$



The scissors jack supports a load P . Determine the axial force in the screw necessary for equilibrium when the jack is in the position shown. Each of the four links has a length L and is pin-connected at its center. Points B and D can move horizontally.



$$\delta U_p = -P \delta y_2$$

$$\delta U_F = -F \delta x_1$$

$$x_1 = L \cos \theta \rightarrow \frac{\delta x_1}{\delta \theta} = -L \sin \theta$$

$$y_2 = 2L \sin \theta \rightarrow \frac{\delta y_2}{\delta \theta} = 2L \cos \theta$$

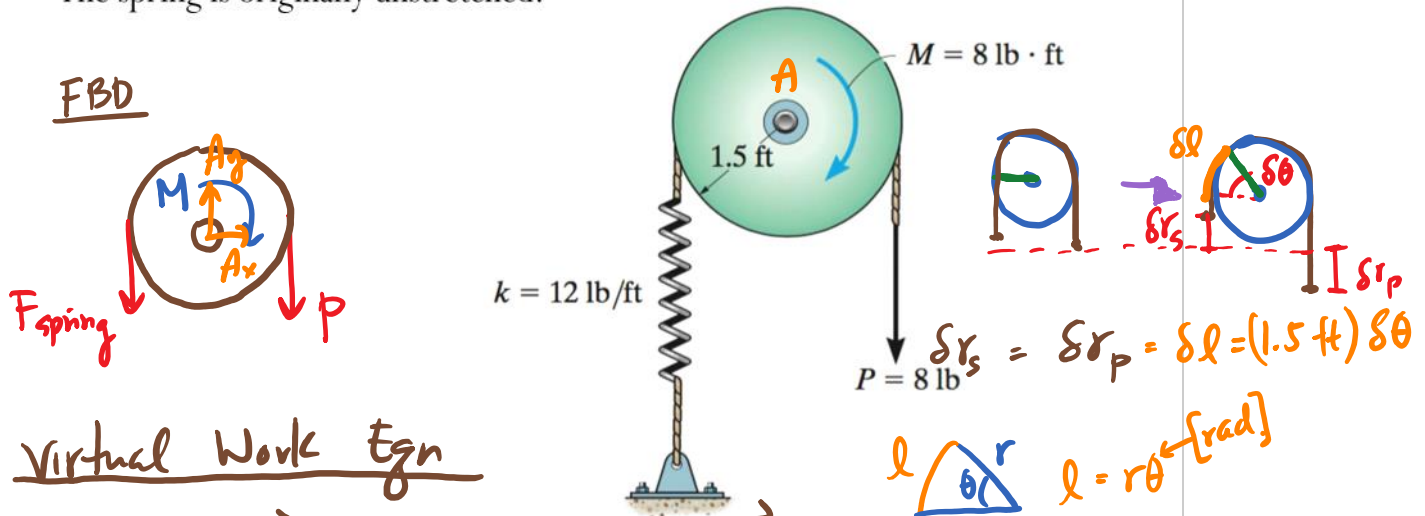
$$-P(2L \cos \theta) + (-F)(-L \sin \theta) = 0$$

$$P = \frac{F}{2} \tan \theta$$

$$\theta \leq 45^\circ \quad \text{if } \theta = 45^\circ, \tan \theta = 1.$$

$$P = \frac{F}{2}$$

The disk has a weight of 10 lb and is subjected to a vertical force $P = 8$ lb and a couple moment $M = 8$ lb ft. Determine the disk's rotation θ if the end of the spring wraps around the periphery of the disk as the disk turns. The spring is originally unstretched.



Virtual Work Eqn

$$\sum \delta U = 0 = \vec{F}_{\text{spring}} \cdot \delta \vec{r}_s + M \delta \theta + \vec{P} \cdot \delta \vec{r}_p$$

$$F_{\text{spring}} = ks$$

$$\delta \vec{r}_s = ? = (1.5 \text{ ft}) \delta \theta$$

$$\delta \vec{r}_p = ? = (1.5 \text{ ft}) \delta \theta$$

$$\delta \theta \quad \checkmark$$

$$s = \frac{M + 1.5P}{1.5k}$$

$$\rightarrow s = r\theta \rightarrow \underline{\underline{\theta = \frac{s}{r} \quad \checkmark}}$$