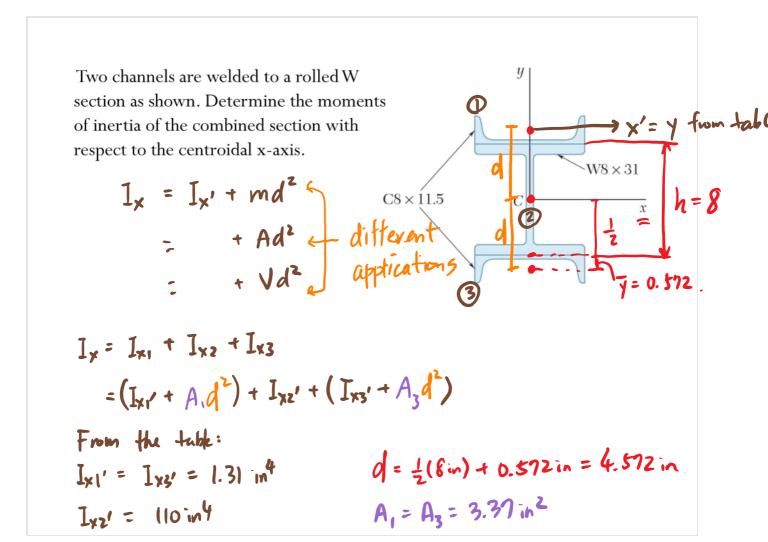
### Announcements

• CBTF Quiz 5 continues.

- ☐ Upcoming deadlines:
- Friday (4/19): Written Assignment
- Tuesday (4/23): PL HW

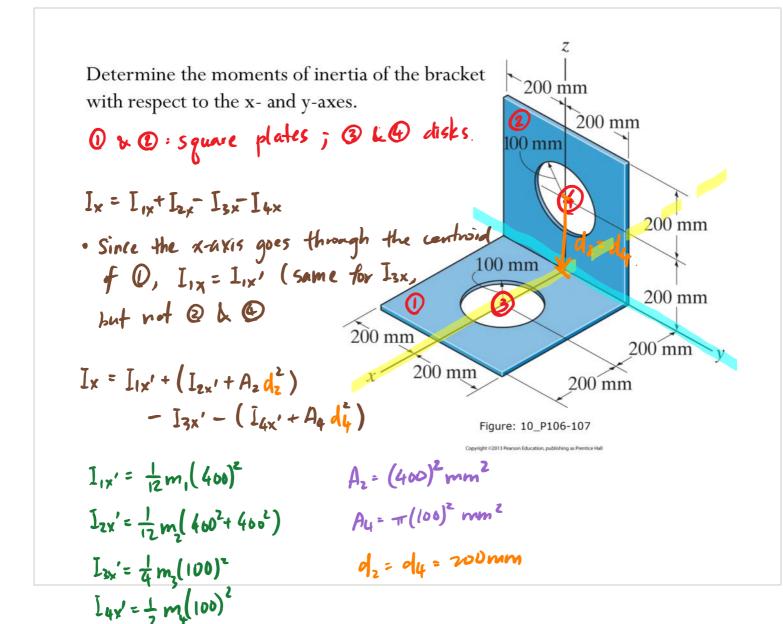


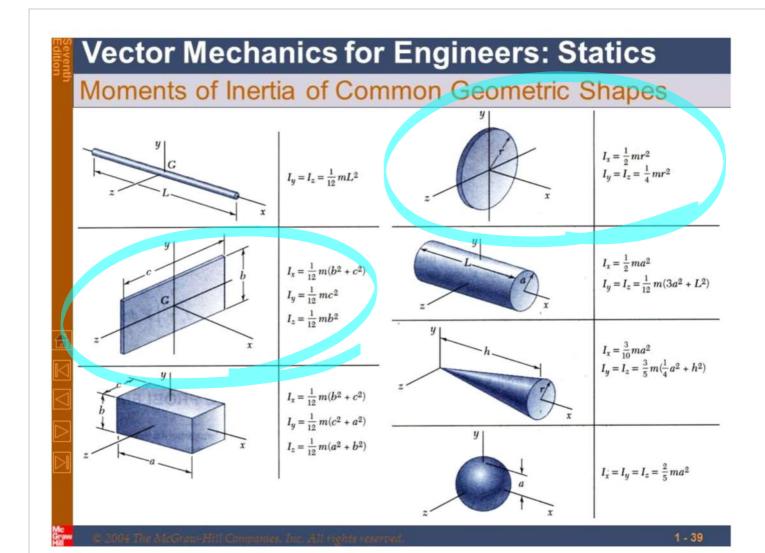


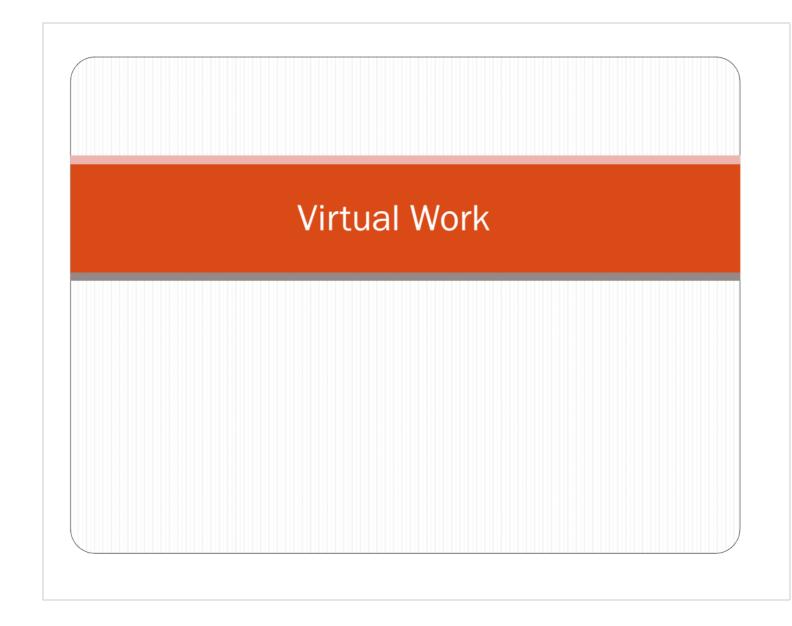


Wide-Flange Chapes   X				Donah	unda		Axis X-X		-	Axis Y-Y	
Wishapes Wide-Flange (Wide-Flange) (Wide-Fla		Designation				$\overline{I}_x$ , in <sup>4</sup>	$\overline{k}_{\mathrm{r}}$ , in.	y, in.	$\overline{I}_y$ , in <sup>4</sup>	$\overline{k}_g$ , in.	₹, in.
S Shapes American Standard Channels)  Y  S18 × 54.7†  16.0  18.0  6.00  801  7.07  20.7  1.14  9.33  1.00  6.73  9.33  1.00  6.73  9.93  1.00  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  6.73  9.90  1.80  7.70  6.73  9.80  9.33  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.00  6.73  9.93  1.80  0.707  0.698  2.27  0.711  0.634  CS×11.5  CS×11.5  3.37  8.00  2.26  6.00  1.92  13.1  2.34  0.687  0.536  0.512	W Shapes (Wide-Flange	W16 × 57 W14 × 38	16.8 11.2	16.4 14.1	7.12 6.77	758 385 110	6.72 5.87		43.1 26.7 37.1	1.60 1.55	
Shapes American Standard (Shapes)  X  X  X  X  X  X  X  X  X  X  X  X  X	Y		A			Ix'			=		/
American Standard Cax X X X X X X X X X X X X X X X X X X X	American Standard Thispes)	\$12 × 31.8 \$10 × 25.4	9.31 7.45	12.0 10.0	5.00 4.66	217 123	4.83 4.07		9.33 6.73	1.00 0.950	
	American Standard Channels)  X  X  X	C10 × 15.3 C8 × 11.5	4.48 3.37	10.0 8.00	2.60 2.26	67.3 32.5	3.87		2.27 1.31	0.711	0.634

	<u></u>					A	ods X-X	Axis Y-Y			
		Designation	Area mm²	Depth mm	Width mm	\overline{I_x} 106 mm <sup>4</sup>	$\overline{k}_{x}$ mm	y mm	100 mm4	$\overline{k}_y$	mm
W Shapes (Wide-Flange Shapes)	x x	W460 × 113† W410 × 85 W360 × 57.8 W200 × 46.1	14400 10900 7230 5890	462 417 358 203	279 181 172 203	554 316 160 45.8	196 171 149 88.1		63.3 17.9 11.1 15.4	66.3 40.6 39.4 51.3	
S Shapes (American Standard Shapes)	xx	\$460 × 81.4† \$310 × 47.3 \$250 × 37.8 \$150 × 18.6	10300 6010 4810 2360	457 305 254 152	152 127 118 84.6	333 90.3 51.2 9.16	180 123 103 62.2		8.62 3.88 2.80 0.749	29.0 25.4 24.1 17.8	
C Shapes (American Standard Channels)	$x \xrightarrow{\Upsilon} x$	C310 × 30.8† C250 × 22.8 C200 × 17.1 C150 × 12.2	3920 2990 2170 1540	305 254 203 152	74.7 66.0 57.4 48.8	53.7 28.0 13.5 5.45	117 98.3 79.0 59.4		1.61 0.945 0.545 0.296	20.2 18.1 15.8 13.6	17.7 16.1 14.5 13.0
Angles X	<u> </u>	L152 × 152 × 25.4‡ L102 × 102 × 12.7 L76 × 76 × 6.4 L152 × 102 × 12.7 L127 × 76 × 12.7 L76 × 51 × 6.4	7100 2420 929 3060 2420 768			14.7 2.30 0.512 7.20 3.93 0.454	45.5 30.7 23.5 48.5 40.1 24.2	47.2 30.0 21.2 50.3 44.2 24.9	14.7 2.30 0.512 2.59 1.06 0.162	45.5 30.7 23.5 29.0 20.9 14.5	47.2 30.0 21.2 24.9 18.9 12.4







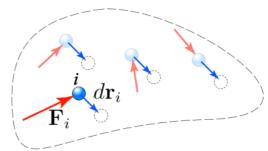
### Main goals and learning objectives

- Introduce the principle of virtual work
- Show how it applies to determining the equilibrium configuration of a series of pin-connected members

## **Definition of Work**

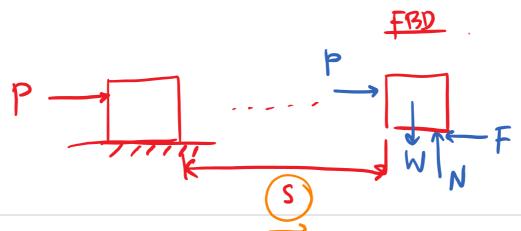
#### Work of a force

A force does work when it undergoes a displacement in the direction of the line of action.



The work dU produced by the force  ${\pmb F}$  when it undergoes a differential displacement  $d{\pmb r}$  is given by

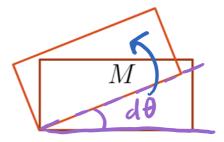
$$dU = \mathbf{F} \cdot d\mathbf{r}$$



W&N: did no work.

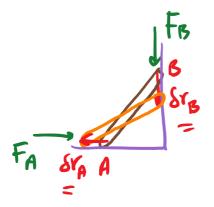
# **Definition of Work**

Work of a couple  $dU = M\mathbf{k} \cdot d\theta \, \mathbf{k} = M \, d\theta$ 



# Virtual Displacements

A *virtual displacement* is a conceptually possible displacement *or* rotation of all *or* part of a system of particles. The movement is assumed to be possible, but actually does not exist.

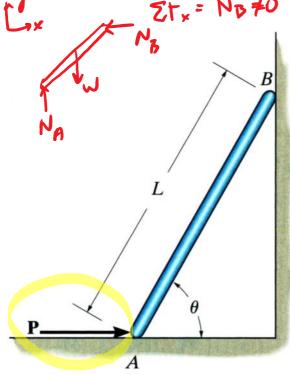


## Principle of Virtual Work

The principle of virtual work states that if a body is in equilibrium, then the algebraic sum of the virtual work done by all the forces and couple moments acting on the body is zero for any virtual displacement of the body. Thus,

ZFx=NB =0 -) Pis required for equilibrium

干PD



The thin rod of weight *W* rests against the smooth wall and floor. Determine the magnitude of force *P* needed to hold it in equilibrium.

P SUAT NO WORK

Virtual Work egn.

Na: I SUB - no work. Na: I SUB - no work. W: do some work.