2.3 Interaction of Photons
Interactions of Photons with Matter

Reading Material:

- Chapter 5 in "Introduction to Health Physics", Third edition, by Cember.
- Chapter 8 in "Atoms, Radiation, and Radiation Protection", by James E Turner.
# Classification of Photon Interactions

## Table 1. Classification of elementary photon interactions.

<table>
<thead>
<tr>
<th>Type of interaction</th>
<th>Absorption</th>
<th>Scattering</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Elastic (Coherent)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Inelastic (Incoherent)</td>
</tr>
<tr>
<td>Interaction with:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Atomic electrons</td>
<td><strong>Photoelectric effect</strong></td>
<td>Rayleigh scattering</td>
</tr>
<tr>
<td></td>
<td>$\sigma_{pe} \begin{cases} \sim Z^4 (L.E.) \ \sim Z^5 (H.E.) \end{cases}$</td>
<td>$\sigma_R \sim Z^2$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\text{(L.E.)}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\sigma_C \sim Z$</td>
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<tr>
<td>Nucleus</td>
<td><strong>Photonuclear reactions</strong></td>
<td>Elastic nuclear</td>
</tr>
<tr>
<td></td>
<td>$(\gamma, n), (\gamma, p)$, photofission, etc.</td>
<td>scattering</td>
</tr>
<tr>
<td></td>
<td>$\sigma_{ph.n.} \sim Z$</td>
<td>$(\gamma, \gamma) \sim Z^2$</td>
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<tr>
<td></td>
<td>$(h\nu \geq 10\text{MeV})$</td>
<td>$\text{(\gamma, \gamma')}$</td>
</tr>
<tr>
<td>Electric field</td>
<td><strong>Electron-positron pair production in field of</strong></td>
<td></td>
</tr>
<tr>
<td>surrounded by</td>
<td>nucleus, $\sigma_{pair} \sim Z^2$</td>
<td></td>
</tr>
<tr>
<td>charged particles</td>
<td>$(h\nu \geq 1.02\text{MeV})$</td>
<td></td>
</tr>
</tbody>
</table>
Coherent or Raleigh Scattering

Rayleigh scattering

- Rayleigh scattering results from the interaction between the incident photons and the target atoms as a whole.
- There is no appreciable energy loss by the photon to the atom.
- The scattering angle is very small.
Photoelectric Effect

In photoelectric process, an incident photon transfer its energy to an orbital electron, causing it to be ejected from the atom.

\[ E_{e^-} = h \nu - E_b \]

- \( h \) is the Planck's constant
- \( \nu \) is the frequency of the photon

- Photoelectric interaction is **with the atom in a whole** and can not take place with free electrons.
- Photoelectric effect **creates a vacancy in one of the electron shells**, which leaves the atom at an excited state.
Photoelectric Effect Cross Section

Probability of photoelectric absorption per atom is

\[ \sigma \propto \begin{cases} 
\frac{Z^4}{(hv)^{3.5}} & \text{low energy} \\
\frac{Z^5}{(hv)^{3.5}} & \text{high energy}
\end{cases} \]

- The interaction cross section for photoelectric effect depends strongly on Z.

- Photoelectric effect is favored at lower photon energies. It is the major interaction process for photons at low hundred keV energy range.
Photoelectric Effect – Absorption Edges

Requires **sufficient photon energy** for P.E. interaction.

Interaction probability decreases dramatically with increasing energy.

P.E. interaction is significant only for low energy photons, when the photon energy is close to the binding energies of the target atoms.

Figure 2: Total and partial atomic photoeffect of Ag.
Relaxation Processes after Photoelectric Interaction

The excited atoms will **de-excite** through one of the following processes:

- **Auger electron** emission dominates in low-\(Z\) elements. **Characteristic X-ray** emission dominates in higher-\(Z\) elements.

![Diagram showing processes](image)

Generation of characteristic X-rays

Generation of Auger electrons

NPRE 441, Principles of Radiation Protection, Spring 2022
Auger Electrons

The relative probability of the emission of characteristic radiation to the emission of an Auger electron is called the fluorescent yield, $\omega$:

$$\omega_K = \frac{\text{Number K x ray photons emitted}}{\text{Number K shell vacancies}}$$  \hspace{1cm} (3-12)

Values for $\omega_K$ are given in Table 3-1. We see that for large Z values fluorescent radiation is favored, while for low values of Z Auger electrons tend to be produced.

From this table we see that if a nucleus with $Z = 40$ had a K shell hole, then on the average 0.74 fluorescent photons and 0.26 Auger electrons would be emitted.

<p>| TABLE 3-1 |
| Fluorescent Yield |</p>
<table>
<thead>
<tr>
<th>Z</th>
<th>$\omega_K$</th>
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<td>35</td>
<td>.63</td>
<td>65</td>
<td>.90</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

From Evans (E1)
Compton Scattering

In Compton scattering, the incident gamma ray photon is **deflected by an orbital electron** in the absorbing material.

Part of the **energy** carried by the incident photon is **transferred to the target electron** in the atom, causing it to be ejected from the atom.

**FIGURE 8.2.** Compton measured the intensity of scattered photons as a function of their wavelength \( \lambda' \) at various scattering angles \( \theta \). Incident radiation was molybdenum K\( \alpha \) X rays, having a wavelength \( \lambda = 0.714 \) Å.
Basic Kinematics in Compton Scattering

The **energy transfer** in Compton scattering may be derived as the following:

- Assuming that the **electron binding energy is small** compared with the energy of the incident photon – **elastic scattering**.

- Write out the **conservation of energy and momentum**:

\[
\begin{align*}
\text{Conservation of energy} & \quad h\nu + mc^2 = h\nu' + E' \\
\text{Conservation of momentum} & \quad \frac{h\nu}{c} = \frac{h\nu'}{c} \cos \theta + P' \cos \phi \\
& \quad \frac{h\nu'}{c} \sin \theta = P' \sin \phi
\end{align*}
\]
Energy Transfer in Compton Scattering

If we assume that the electron is free and at rest, the scattered gamma ray has an energy

\[
hv' = \frac{hv}{1 + \frac{hv}{m_0c^2}(1 - \cos \theta)},
\]

Initial photon energy, \(v\): photon frequency

mass of electron Scattering angle

and the photon transfers part of its energy to the electron (assumed to be at rest before the collision), which is known as the *recoil electron*. Its energy is simply

\[
E_{\text{recoil}} = hv - hv' = hv - \frac{hv}{1 + \frac{hv}{m_0c^2}(1 - \cos(\theta))}
\]

assuming the binding energy of the electron is negligible.

In the simplified elastic scattering case, there is an one-to-one relationship between scattering angle and energy loss!!
Energy Transfer in Compton Scattering

The scattering angles of the photon and the recoil electron is related by

\[
\cot \frac{\theta}{2} = \left( 1 + \frac{h\nu}{mc^2} \right) \tan \varphi
\]

- The electron recoil angle \( \varphi \) is confined to the forward direction (\( 0 \leq \varphi \leq 90^\circ \)).
- The scattering angle of the photon can take any value between 0 and 180°.
Energy Transfer in Compton Scattering

The maximum energy carried by the recoil electron is obtained by setting $\theta$ to $180^\circ$,

$$E_{\text{max}} = \frac{2h \nu}{2 + mc^2/h \nu}$$

The maximum energy transfer is exemplified by the Compton edge in measured gamma ray energy spectra.

Figure 8.5. Relative number of Compton recoil electrons as a function of their energy for 1-MeV photons.
Energy Transfer in Compton Scattering

Example

In the previous example a 1.332-MeV photon from $^{60}$Co was scattered by an electron at an angle of 140°. Calculate the energy acquired by the recoil electron. What is the recoil angle of the electron? What is the maximum fraction of its energy that this photon could lose in a single Compton scattering?

$$
\cot \frac{\theta}{2} = \left(1 + \frac{hv}{mc^2}\right) \tan \phi
$$

$$
E_{\text{recoil}} = hv - hv' = hv - \frac{hv}{1 + \frac{hv}{m_0c^2(1 - \cos(\theta))}}
$$
Energy Transfer in Compton Scattering

Solution
Substitution into Eq. (8.19) gives the electron recoil energy,

$$T = 1.332 \frac{1 - (-0.766)}{0.511/1.332 + 1 - (-0.766)} = 1.094 \text{ MeV.} \quad (8.25)$$

Note from Eq. (8.15) that \(T + h\nu' = 1.332 \text{ MeV} = h\nu\), as it should. The angle of recoil of the electron can be found from Eq. (8.24). We have

$$\tan \varphi = \frac{\cot (140^\circ/2)}{1 + 1.332/0.511} = 0.101, \quad (8.26)$$

from which it follows that \(\varphi = 5.76^\circ\). This is a relatively hard collision in which the photon is backscattered, retaining only the fraction \(0.238/1.332 = 0.179\) of its energy and knocking the electron in the forward direction. From Eq. (8.20),

$$T_{\text{max}} = \frac{2 \times 1.332}{2 + 0.511/1.332} = 1.118 \text{ MeV.} \quad (8.27)$$

The maximum fractional energy loss is \(T_{\text{max}}/h\nu = 1.118/1.332 = 0.839\).
Energy Transfer in Compton Scattering

Small angle scattering:
Energy carried by the scattered gamma ray depends strongly on scattering angle.

Large angle scattering:
Energy carried by the scattered gamma ray depends only weakly on scattering angle.
Derivation of the Relationship Between Scattering Angle and Energy Loss

The relation between energy the scattering angle and energy transfer are derived based on the conservation of energy and momentum:

\[ \vec{p}_{hv} + \vec{p}_e = \vec{p}_{hv'} + \vec{p}_{e'} \]

\[ E_{hv} + E_e = E_{hv'} + E_{e'} \]

Are those terms truly zero?
Compton Scattering with Non-stationary Electrons – Doppler Broadening

- It is so far assumed that (a) the electron is free and stationary and (b) the incident photon is unpolarized.

- When an incident photon is reflected by a non-stationary electron, for example an bond electron, an extra uncertainty is added to the energy of the scattered photon. This extra uncertainty is called Doppler broadening.

\[
\Delta v' = \frac{h v}{1 + \frac{h v}{m_0 c^2} (1 - \cos(\theta))} \pm \sigma(h v')
\]

The one-to-one relationship between scattering angle and energy loss holds only when incident photon energy is far greater than the bonding energy of the electron...
Compton Scattering with Non-stationary Electrons

– Doppler Broadening

Comparison of the energy spectra for the photons scattered by C and Cu samples. $E_{hv} = 40\text{keV}$, $\theta = 90$ degrees

The Doppler broadening is stronger in Cu than in C because of the Cu electrons have greater bonding energy.
Angular Distribution of the Scattered Gamma Rays

The differential scattering cross section of per electron is given by the Klein-Nishina formula:

\[
\frac{d\sigma}{d\Omega}(\theta) = r_e^2 \left( \frac{1}{1 + \alpha(1 - \cos \theta)} \right)^2 \left( \frac{1 + \cos^2 \theta}{2} \right) \left( 1 + \frac{\alpha^2(1 - \cos \theta)^2}{(1 + \cos^2 \theta)[1 + \alpha(1 - \cos \theta)]} \right) \text{ (m}^2 \text{s}^{-1})
\]

where

\[\alpha = \frac{hv}{m_0c^2}\] and \[r_e = \frac{k_0e^2}{m_0c^2}\] is the classic electron radius \((2.818 \times 10^{-15} \text{ m})\)
Angular Distribution of the Scattered Gamma Rays

The differential scattering cross section per electron — the probability of a photon scattered into a unit solid angle around the a given scattering angle $\theta$, when the incident photon is passing normally through a thin layer of scattering material that contains one electron per unit area.

$$\frac{d\sigma}{d\Omega} (\theta) = r_e^2 \left( \frac{1}{1 + \alpha (1 - \cos \theta)} \right)^2 \left( \frac{1 + \cos^2 \theta}{2} \right) \left( 1 + \frac{\alpha^2 (1 - \cos \theta)^2}{(1 + \cos^2 \theta)[1 + \alpha (1 - \cos \theta)]} \right) (m^2 sr^{-1})$$

where $\alpha = \frac{hv}{m_0 c^2}$ and $r_e$ is the classical electron radius.

Fig. 5.15. Compton scattering diagram to illustrate differential scattering cross section. $S$ is a sphere of unit radius whose center is the scattering electron.
Angular Distribution of the Scattered Gamma Rays

Incident photons with higher energies tend to scatter with smaller angles (forward scattering).

Incident photons with lower energy (a few hundred keV) have greater chance of undergoing large angle scattering (back scattering).

Radial distance represents the differential cross section.

The higher the energy carried by an incident gamma ray, the more likely that the gamma ray undergoes forward scattering ...
Total Compton Collision Cross Section for an Electron

Compton Collision Cross Section is defined as the total cross section per electron for Compton scattering. It can be derived by integrating the differential cross section, $\frac{d\sigma}{d\Omega}$, over $4\pi$ solid angle.

Since

$$d\Omega = 2\pi \sin \theta \, d\theta,$$

then the Compton scattering cross section per electron is given by

$$\sigma = 2\pi \int_{\Omega} \frac{d\sigma}{d\Omega} \cdot \sin \theta \cdot d\theta \quad (m^2)$$

Note that the Compton scattering cross section per electron is given in unit of $m^2$. 
Energy Distribution of Compton Recoil Electrons

Given the Klein-Nishina formula, how do we derive the energy spectrum of recoil electrons? In other words, how do we derive the probability of a gamma-ray undergoing a Compton scattering and transferring an energy falling into an energy window, \( E_{\text{recoil}} \in \left[ E' - \frac{1}{2} \Delta E, E' + \frac{1}{2} \Delta E \right] \)?

\[
\frac{d\sigma}{d\Omega}(\theta) = r_e^2 \left( \frac{1}{1 + \alpha(1 - \cos \theta)} \right)^2 \left( \frac{1 + \cos^2 \theta}{2} \right) \left( 1 + \frac{\alpha^2(1 - \cos \theta)^2}{(1 + \cos^2 \theta)[1 + \alpha(1 - \cos \theta)]} \right) \left( m^2 sr^{-1} \right)
\]

Fig. 5.15. Compton scattering diagram to illustrate differential scattering cross section. \( S \) is a sphere of unit radius whose center is the scattering electron.
Energy Distribution of Compton Recoil Electrons

Klein-Nishina formula can be used to derive the energy spectrum of recoil electrons as the following:

\[
\frac{d\sigma}{dE_{\text{recoil}}} = \frac{d\sigma}{d\Omega} \cdot \frac{d\Omega}{d\theta} \cdot \frac{d\theta}{dE_{\text{recoil}}} (m^2 \cdot \text{keV}^{-1})
\]

If a gamma-ray underwent a Compton Scattering, then probability of the gamma-ray transferring a given amount of energy falling into a small energy window, \(E_{\text{recoil}} \in \left[ E' - \frac{1}{2} \Delta E, E' + \frac{1}{2} \Delta E \right] \) would be proportional to

\[
p \propto \Delta E \cdot \left( \frac{d\sigma}{dE_{\text{recoil}}} \right)_{E'}
\]
Energy Distribution of Compton Recoil Electrons

The energy distribution for the recoil electrons could be derived with the following differential cross section

\[
\frac{d\sigma}{dE_{\text{recoil}}} = \frac{d\sigma}{d\Omega} \frac{d\Omega}{d\theta} \frac{d\theta}{dE_{\text{recoil}}}
\]

The three partial derivative terms on the right-hand side of the equation can be derived from the following relationships:

- **From Klein-Nishina formula:**

\[
\frac{d\sigma}{d\Omega}(\theta) = r_e^2 \left( \frac{1}{1+\alpha(1-\cos \theta)} \right)^2 \left( \frac{1+\cos^2 \theta}{2} \right) \left( 1 + \frac{\alpha^2(1-\cos \theta)^2}{(1+\cos^2 \theta)[1+\alpha(1-\cos \theta)]} \right)
\]

- **From Compton equation:**

\[
E_{\text{recoil}} = h\nu - h\nu' = h\nu - \frac{h\nu}{1 + \frac{h\nu}{m_0c^2(1-\cos \theta)}} \Rightarrow
\]

\[
\frac{d\theta}{dE_{\text{recoil}}} = - \frac{m_0c^2}{(h\nu - E_{\text{recoil}}^2) \cdot \sin \theta} = \frac{m_0c^2}{(h\nu)^2 \cdot \sin \theta} \left[1 + \frac{h\nu}{m_0c^2(1-\cos \theta)} \right]^2
\]

- **From the known scattering geometry:**

\[
d\Omega = 2\pi \sin \theta \, d\theta \quad \Rightarrow \frac{d\Omega}{d\theta} = 2\pi \sin \theta
\]
Energy Distribution of Compton Recoil Electrons

Therefore, the differential cross section becomes

$$\frac{d\sigma}{dE_{recoil}} = \frac{d\sigma}{d\Omega} \frac{d\Omega}{d\theta} \frac{d\theta}{dE_{recoil}}$$

$$= \left[ r_e^2 \left( \frac{1}{1+\alpha(1-\cos \theta)} \right)^2 \left( \frac{1+\cos^2 \theta}{2} \right) \left( 1 + \frac{\alpha^2(1-\cos \theta)^2}{(1+\cos^2 \theta)[1+\alpha(1-\cos \theta)]} \right) \right] \times$$

$$\left[ \frac{m_0 c^2}{(\nu)^2 \cdot \sin \theta} \left[ 1 + \frac{\nu}{m_0 c^2} (1 - \cos \theta) \right]^2 \right] \times$$

$$[2\pi \sin \theta]$$

Remember that

$$E_{recoil} = \nu - \nu' = \nu - \frac{\nu}{1+\frac{\nu}{m_0 c^2}(1-\cos \theta)} ,$$

Then $\frac{d\sigma}{dE_{recoil}}$ could be written as an explicit function of $E_{recoil}$.

$$\frac{d\sigma}{dE_{recoil}}(\theta) \Rightarrow \frac{d\sigma}{dE_{recoil}}(E_{recoil})$$
Energy Distribution of Compton Recoil Electrons

Klein-Nishina formula can be used to calculate the energy spectrum of recoil electrons as the following:

\[
\frac{d\sigma}{dE_{\text{recoil}}} = \frac{d\sigma}{d\Omega} \cdot \frac{d\Omega}{d\theta} \cdot \frac{d\theta}{dE_{\text{recoil}}} \quad (\text{m}^2 \cdot \text{keV}^{-1})
\]

If a gamma-ray underwent a Compton Scattering, then probability of the gamma-ray transferring a given amount of energy that fall into a small energy window, \( E_{\text{recoil}} \in \left[ E' - \frac{1}{2} \Delta E, E' + \frac{1}{2} \Delta E \right] \) would be proportional to

\[ P \propto \Delta E \cdot \left( \frac{d\sigma}{dE_{\text{recoil}}} \right) \bigg|_{E_{\text{recoil}}=E'} \]
Energy Distribution of Compton Recoil Electrons

Remember that the maximum amount of energy that a photon can transfer to an electron in a single Compton scattering is given by:

$$E_{\text{max}} = \frac{2h \nu}{2 + mc^2/h \nu}$$

The energy distribution of the recoil electrons derived using the Klein-Nishina formula is closely related to the energy spectrum measured with “small” detectors (in particular, the so-called Compton continuum).

Average fraction of energy transfer to the recoil electron through a single Compton Collision

Average recoil electron energy \( E_{\text{avg}_{-}\text{recoil}} \) is of special interest for dosimetry is the, since it is an approximation of the radiation dose delivered by each photon through a single Compton scattering interaction.

The average fraction of energy transfer to the recoil electron through a single Compton scattering is given by

\[
\frac{E_{\text{avg}_{-}\text{recoil}}}{h\nu} = \int_{E_{\text{recoil}}} \frac{E_{\text{recoil}}}{h\nu} \cdot \left[ \frac{d\sigma}{dE_{\text{recoil}}} / \sigma \right] \cdot dE_{\text{recoil}},
\]

where \( \sigma \) is the Compton scattering cross section per electron and is given by

\[
\sigma = 2\pi \int_{\Omega} \frac{d\sigma}{d\Omega} \cdot \sin \theta \cdot d\theta \ (m^2).
\]
Average fraction of energy transfer to the recoil electron through a single Compton Collision

TABLE 8.1. Average Kinetic Energy, $T_{\text{avg}}$, of Compton Recoil Electrons and Fraction of Incident Photon Energy, $h\nu$

<table>
<thead>
<tr>
<th>Photon Energy $h\nu$ (MeV)</th>
<th>Average Recoil Electron Energy $T_{\text{avg}}$ (MeV)</th>
<th>Average Fraction of Incident Energy $T_{\text{avg}}/h\nu$</th>
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Total Compton Collision Cross Section for an Electron

Compton Collision Cross Section is defined as the total cross section per electron for Compton scattering. It can be derived by integrating the differential cross section, $\frac{d\sigma}{d\Omega}$, over $4\pi$ solid angle.

Since

$$d\Omega = 2\pi \sin \theta \, d\theta,$$

the total Compton scattering cross section per electron is given by

$$\sigma = 2\pi \int_{\Omega} \frac{d\sigma}{d\Omega} \cdot \sin \theta \cdot d\theta \ (m^2)$$

Note that the Compton scattering cross section per electron is given in unit of $m^2$. 

![Diagram of Compton scattering](image)
Linear Attenuation Coefficient through Compton Scattering

The differential Compton cross section given by the Klein-Nishina Formula can also be related to another important parameter for gamma ray dosimetry – the linear attenuation coefficient.

Note that $\sigma$ is the Compton scattering cross section per electron and is given by

$$\sigma = 2\pi \int_{\Omega} \frac{d\sigma}{d\Omega} \cdot \sin \theta \cdot d\theta \ (m^2).$$

Linear attenuation coefficient through Compton scattering: the probability of a photon interacting with the absorber through Compton scattering while traversing a unit distance.

$$\sigma_{linear} = NZ\sigma (m^{-1}),$$

Where NZ is the electron density of the absorber materials (number of electrons per $m^3$)
Pair Production

Definition:
Pair production refers to the creation of an electron-positron pair by an incident gamma ray in the vicinity of a nucleus.

Characteristics
☞ The minimum energy required is

\[ E_\gamma \geq 2m_e c^2 + \frac{2m_e^2 c^2}{m_{\text{nucleus}}} \approx 2m_e c^2 = 1.022\text{MeV} \]

☞ The process is more probable with a heavy nucleus and incident gamma rays with higher energies.

☞ The positrons emitted will soon annihilate with ordinary electrons near by and produces two 511keV gamma rays.
Photonuclear Reaction

A photon can be absorbed by an atomic nucleus and knock out a nucleon. This process is called photonuclear reaction. For example,

\[ ^9_4 Be + hv \rightarrow ^8_4 Be + ^1_0 n, \quad Q-value: -1.666\text{MeV} \]

\[ ^2_1 H + hv \rightarrow ^1_1 H + ^1_0 n, \quad Q-value: -2.226\text{MeV} \]

The photon must possess enough energy to overcome the nuclear binding energy, which is generally several MeV.

The threshold, or the minimum photon energy required, for \((\gamma,p)\) reaction is generally higher than that for \((\gamma,n)\) reactions. Since the repulsive Coulomb barrier that a proton must overcome to escape from the nucleus.

Other nuclear reaction s are also possible, such as \((\gamma, 2n)\), \((\gamma, np)\), \((\gamma, \alpha)\) and photon induced fission reaction.
Interaction of Photons in Matter

Figure 2.18 Energy dependence of the various gamma-ray interaction processes in sodium iodide. (From The Atomic Nucleus by R. D. Evans Copyright 1955 by the McGraw-Hill Book Company. Used with permission.)
The Relative Importance of the Three Major Types of X and Gamma Ray Interactions
A few things to follow up from the discussions on interactions of photons with matter:

- Photon attenuation coefficients.
- Energy transfer and energy absorption coefficients.