# MODULE I: INTRODUCTION

Linux & bash shell

# I. Linux

### What is Linux?

- Linux is an operating system (OS) developed by Linus Torvalds in 1991
- Based on UNIX developed in response to closing legal loophole that made UNIX free
- Many "distributions" Fedora, RedHat, CentOS, Debian, Ubuntu
- Typically free and open source GNU licensing
- Command line interface (CLI) and graphical desktop environments (GDE)



Tux



Linus Torvalds



Richard Stallman

# Why Linux?

- Developed by Bell Labs in 1969, and initially free, UNIX was quickly adopted as de facto scientific computing OS
- Powerful CLI enables direct low level access GDE provides simplicity and usability
- Free and open source makes code development easy
- Linux is everywhere
  - 90% of supercomputers run Linux (incl. Blue Waters)
  - Android OS is based on a Linux kernel
  - Ubuntu distro is the most popular OS in the world

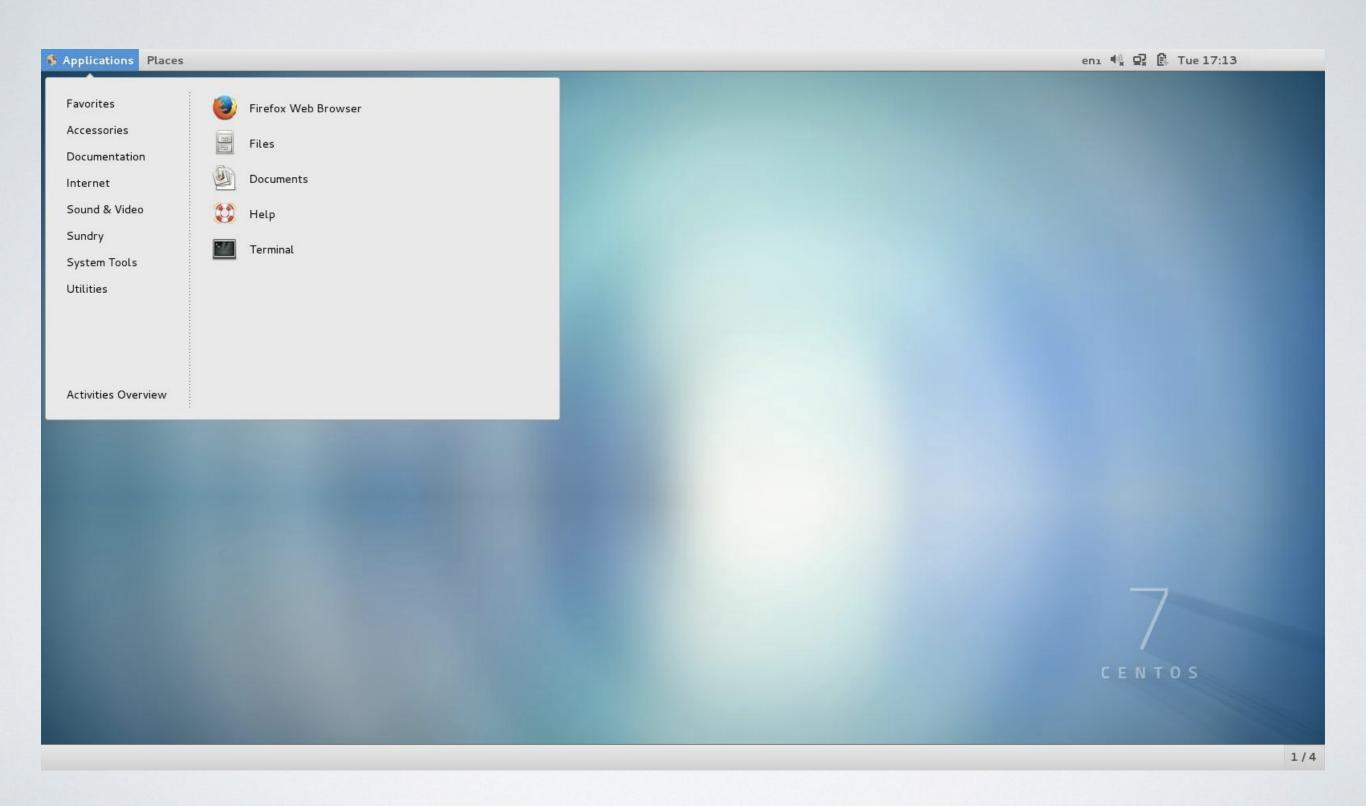
### Can't I use Windows / Mac OS X?

- Maybe.
- Some software have Mac OS X / Windows / Windows + Cygwin versions to install on your local machine
- Remote login via Mac OS X terminal / [Windows + Cygwin / Putty] to SSH into EWS Linux
- A key learning objectives of this course is to develop familiarity and competence using Linux Bon Courage!



# What distro are we using?

### EWS Linux machines run CentOS 7



### II. bash shell

### The command line

- CLI and GDE offer alternatives to interact with a machine
- Switching to a CLI can be very intimidating for new users!
- CLI interaction is powerful, concise, and efficient
- CLI scripting enables task automation
  - e.g. Download of 1500 daily NASDAQ stock prices
  - GDE: Point and click file download extremely tedious!
  - CLI: Trivially automated using CLI wget loop

#### bash shell

- "Command line interpreters" or "shells" convert text inputs into OS commands
- Many flavors: sh, bash, ksh, csh, zsh, tcsh
- The bash shell ("Bourne-again shell") is one of the most popular, and the default on many Linux distros

```
marsmain " $ cd /usr/portage/app-shells/bash
          smain /usr/portage/app-shells/bash $ is -al
 rwxr-xr-x 3 portage portage 1024 Jul 25 10:06
rwxr-xr-x 33 portage portage 1024 Aug 7 22:39
                                    35888 Jul 25 10:06 ChangeLog
                                    27002 Jul 25 10:06 Manifest
                                    4645 Mar 23 21:37 bash-3.1_p17.ebuild
5977 Mar 23 21:37 bash-3.2_p39.ebuild
                                    6151 Apr 5 14:37 bash-3.2_p48-r1.ebuild
5988 Mar 23 21:37 bash-3.2_p48.ebuild
5643 Apr 5 14:37 bash-4.0_p10-r1.ebuild
6230 Apr 5 14:37 bash-4.0_p10.ebuild
                                     5532 Apr 8 10:21 bash-4.0_p17.ebuild
                                     5660 May 30 03:35 bash-4.0_p24.ebuild
5660 Jul 25 09:43 bash-4.0_p28.ebuild
              2 portage portage 2048 May 30 03:35 ft
                                     468 Feb 9 04:35 metadata.xml
  xml version="1.0" encoding="UTF-8"?>
 DOCTYPE pkgmetadata SYSTEM "http://www.gentoo.org/dtd/metadata.dtd">
 herd>base-system</herd>
  <flag name='bashlogger'>Log ALL commands typed into bash; should ONLY be
   used in restricted environments such as honeypots</flag>
  <flag name='net'>Enable /dev/tcp/host/port redirection</flag>
  <flag name='plugins'>Add support for loading builtins at runtime via 
'enable'</flag>
      marsmain /usr/portage/app-shells/bash $ sudo /etc/init.d/bluetooth status
 assword:
mars@marsmain /usr/portage/app-shells/bash $ ping -q -cl en.wikipedia.org
PING rr.esams.wikimedia.org (91.198.174.2) 56(84) bytes of data.
    rr.esams.wikimedia.org ping statistics ---
 packets transmitted, 1 received, 0% packet loss, time 2ms
 tt min/avg/max/mdev = 49.820/49.820/49.820/0.820 ms
              n /usr/portage/app-shells/bash $ grep -i /dev/sda /etc/fstab | cut --fields=-3
                            none
                /usr/portage/app-shells/bash $ date
iat Aug 8 02:42:24 MSD 2009
                             Size Used by
rndis_wlan
                                   1 rndis_wlan
                                   1 rndis_host
                                    3 rndis_wlan,rndis_host,cdc_ether
usbnet
                                   1 parport_pc
   s@marsmain /usr/portage/app-shells/bash 🛊 📗
```

### III. bash basics

- Pop a bash terminal by clicking on or navigating Applications Accessories Terminal
- show path to present working directory
- 1s list contents of current directory
  - list <u>all</u> contents of cdir in <u>l</u>ong form with human readable file sizes
  - 1s /sw/q list contents of directory /sw/q
- cd <path> change directory into <path>
  - cd . . change directory up one level
  - cd ../.. change directory up two levels

- touch <file> make new file <file> or update last access of existing file
- mkdir <dir> make directory
- chmod 755 <file> change file permissions to

  r+w+x (user), r+x (group, world)

  chmod 644 <file> change file permissions to

  r+w (user), r (group, world)

  [N.B. r=4, w=2, x=1]
- var=ferrari42 assign ferrari42 to var
- echo \$var print \$var

./<execFile>
<path>/<execFile>

- execute execFile in cdir
- execute execFile in path

which <cmd>

- location of command cmd

clear

- clear terminal
- wget -0 <file> <url> download url data into file
  - e.g. wget -O myProf.png http://bit.ly/2jt9NAl

- cp <source> <target> copy file source to target e.g. cp myFile /apps/doc/
- mv <source> <target> move source to target (same for files and directories)
- rm <file> remove file rm -r <directory> - remove recursively directory

# bash: safety!

- cp / rm / mv These do exactly what you ask
  - They do not ask for permission
- Furthermore, there is no Trash/Recycling
- Once you remove / overwrite a file, it's gone.
- Standard "safety" choices: use alias in your .bashrc

```
alias cp='cp -i'
alias rm='rm -i'
alias mv='mv -i'
setopt noclobber
```

You don't have to do this, but you may breathe a little easier with some safety.

- whoami show your login username
  - who show everyone currently logged in
- cat <file> show file contents
- less <file> show file contents (spacebar ♥, b ♠)
- head <file> show head of file
  - tail <file> show tail of file
  - tail -n <nLines> <file> show tail nLines of file
  - tail -f <file> show tail of file and follow

- zip <archive> <file1 file2 ...>
  - create zip file archive.zip containing file I, file 2, ...
    unzip <archive>
    - unzip zip file archive.zip

- tar cvzf <archive.tgz> <file1 file2 ...>
  - create gzip compressed tape archive archive.tgz containing file I, file 2, ...

### tar xvzf <archive.tgz>

- uncompress end extracted compressed tape archive archive.tgz

- grep <str> <file> return lines in file containing string str
- find <path> -name <\*str\*> -print
  - print all files in path containing str in their name
- < cmd> -help help for cmd
  man < cmd> manual for cmd (spacebar ♥, b ♠)
- Google is your friend for bash help!

# bash: special symbols

- ~ your home directory
  - current directory
- directory one level up
  - \* wildcard character
  - escape succeeding character e.g. mkdir My\ Directory
- e.g. cat <file> | grep tungsten

# bash: special symbols

- > redirect standard output and overwrite
  - >> redirect standard output and append
  - e.g. echo "Today was great!" >> myDiary.txt
- **\$var** dereference variable var
  - enclose text string but expand \$
    - enclose text string but do not expand \$
    - e.g. myVar="My String With Spaces" echo "This is \$myVar"
- `<stuff>` execute stuff first
  - e.g. echo `expr 1 + 1`

### IV. bash utilities

# bash: integer arithmetic

expr - integer arithmetic engine e.g. \$ echo `expr 1 + 1` \$ var1=`expr 10 \\* 2` \$ var2=`expr 21 / 7` \$ echo \$var1 \$var2 `expr \$var1 / \$var2` 20 3 6

## bash: quick calculator

```
bc -1
          - arbitrary precision calculator (w/ math lib)
$ bc -1
2/3
.6666666666666666666
2^3
e(1)
2.71828182845904523536
pi=a(1)*4
pi
3.14159265358979323844
s(pi/6)
.499999999999999999
c(pi/6)
.86602540378443864676
```

### bash: ssh & scp

SSH CLI remote login is supported by ssh (secure shell)
ssh <user>@<hostname> - login to host
ssh -Y <user>@<hostname> - login to host w/
secure X forwarding (use this to get graphics via SSH!)

N.B. For EWS, hostname=remlnx.ews.illinois.edu

## bash: ssh & scp

- ssh and scp are prepackaged with Linux / Mac OS X and are accessible directly from the bash terminal
- On Windows, you need to download a **third party ssh client** in order to make a ssh connection with EWS

```
- - X
nova.kettering.edu - PuTTY
login as: thajek
ccess to this server is restricted to authorized personnel of
Kettering University. Your activity on this system may be monitored.
Using keyboard-interactive authentication.
Last login: Mon Nov 1 13:54:45 2010 from thajek-xp.kette
For enhanced support services help, please visit
          http://www.kettering.edu/it/
Please NOTE: As of May 23, 2009, Nova has been
          switched to a virtual machine running Solaris 10.
          If you experience any problems, please contact
          the help desk @ x8324 or 810-237-8324.
nova{thajek}41%
```





www.putty.org

https://answers.uillinois.edu/illinois.engineering/page.php?id=81727

## bash: sftp

SFTP more sophisticated alternative to scp (secure file transfer protocol)

```
sftp <user>@<hostname>
15
11s
pwd
lpwd
cd
1cd
get <file>
put <file>
quit
```

- login to host
- remote Is
- local Is
- remote pwd
- local pwd
- remote cd
- local cd
- download file
- upload file
- logout

- Two built-in CLI text editors: vi/vim & emacs
  Seem slow and painful, but invaluable for on-the-fly edits
- Use whichever you prefer, I use both.

  (It is very fashionable to argue over which is better...)
- vi/vim is fast for text manipulation, uses two modes
- emacs is has lots of built-in modules, more "Word"-like
- Two-modes: navigation for moving insertion for editing
- Nav mode is the default mode, and can be accessed by hitting **Esc**
- Ins mode is accessed by hitting i

#### Nav mode

```
    ↑↓←→ - single char / single line movement
    gg - go to top of file
    ^ - go to beginning of line
    $ - go to end of line
    <n>G - go to line n
    skip forward one word
```

b - skip backward one word

#### Nav mode

- x delete character
  - create new line below and enter insert mode
    - enter insert mode to left of current character
    - enter insert mode at beginning of line
    - enter insert mode to right of current character
    - enter insert mode at end of line

#### Nav mode

```
dd or d$ - delete current line
```

d<n>
d - delete next n lines

u - undo

Ctrl+r - redo

#### Nav mode

```
/<str><Enter> - search forward for str
?<str><Conter> - search backward for str
```

<N>n

- go to next match
- go to Nth match

#### Nav mode

- :w writes file
- :w! writes file even if read only
- :q quit
- q! quit and don't question me(good way to mess things up)
- :wq write quit
- :wq! write quit and don't question me(very good way to mess things up)

Ins mode

Type normally - what you enter appears on screen

↑↓←→ work as in nav mode

Hit Esc to get back to nav mode

# bash: .bash\_profile & .bashrc

- Hidden files start with .
  - ~/.bashrc is executed for every new terminal
- ~/.bash\_profile is executed when you login
  (~/.bash\_profile calls ~/.bashrc)
- These files are useful to store aliases and modify PATH

N.B. On some systems ~/.bash\_profile is replaced by ~/.profile

# bash: .bash\_profile & .bashrc

(i) Use vi to add LLs as alias for Ls -al to .bashrc

```
$ vi ~/.bashrc
$ G
$ go to end of file
$ o edit line below
$ alias lls="ls -l" add alias
$ Esc escape to navigate mode
$ :wq
* write and quit
```

# bash: .bash\_profile & .bashrc

```
alf@linux7:~ — ssh — 115×32
  .bashrc
# EWS .bashrc Template
# Process the systems global .bashrc (DO NOT REMOVE)
# Source global definitions
if [ -f /etc/bashrc ]; then
        . /etc/bashrc
fi
# If you want to modify an environment variable, for example, the search
# path, take into account the value that the variable already has. For example
# if you wish to add the directory /local/apps1/cl to your search path,
# you would use
# export PATH=$PATH:/local/apps1/cl
# This merely appends the directory /local/apps1/cl to the already-existing
# search path.
# You can also create aliases for often-used commands. For example, if you
# would prefer to type 'dir' instead of 'ls -FC', you could use
# alias dir="ls -FC"
# so that each time you typed 'dir', it would be as though you had typed
# 'ls -FC'
# User specific aliases and functions go below
alias lls="ls -l"
                                                                                                                All
                                                                                                  1,1
```

### bash: .bash\_profile & .bashrc

(ii) Use vi to add ~/Local/bin to your PATH in .bashrc

# bash: .bash\_profile & .bashrc

```
alf@linux7:\sim — ssh — 115\times32
# .bashrc
# EWS .bashrc Template
# Process the systems global .bashrc (DO NOT REMOVE)
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if [ -f /etc/bashrc ]; then
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# If you want to modify an environment variable, for example, the search
# path, take into account the value that the variable already has. For example
# if you wish to add the directory /local/apps1/cl to your search path,
# vou would use
# export PATH=$PATH:/local/apps1/cl
# This merely appends the directory /local/apps1/cl to the already-existing
# search path.
# You can also create aliases for often-used commands. For example, if you
# would prefer to type 'dir' instead of 'ls -FC', you could use
# alias dir="ls -FC"
# so that each time you typed 'dir', it would be as though you had typed
# 'ls -FC'
# User specific aliases and functions go below
alias lls="ls -l"
export PATH=$PATH:~/local/bin
                                                                                                                 All
                                                                                                   1,1
```

# bash: installing software

Typical anatomy of an installation from source:

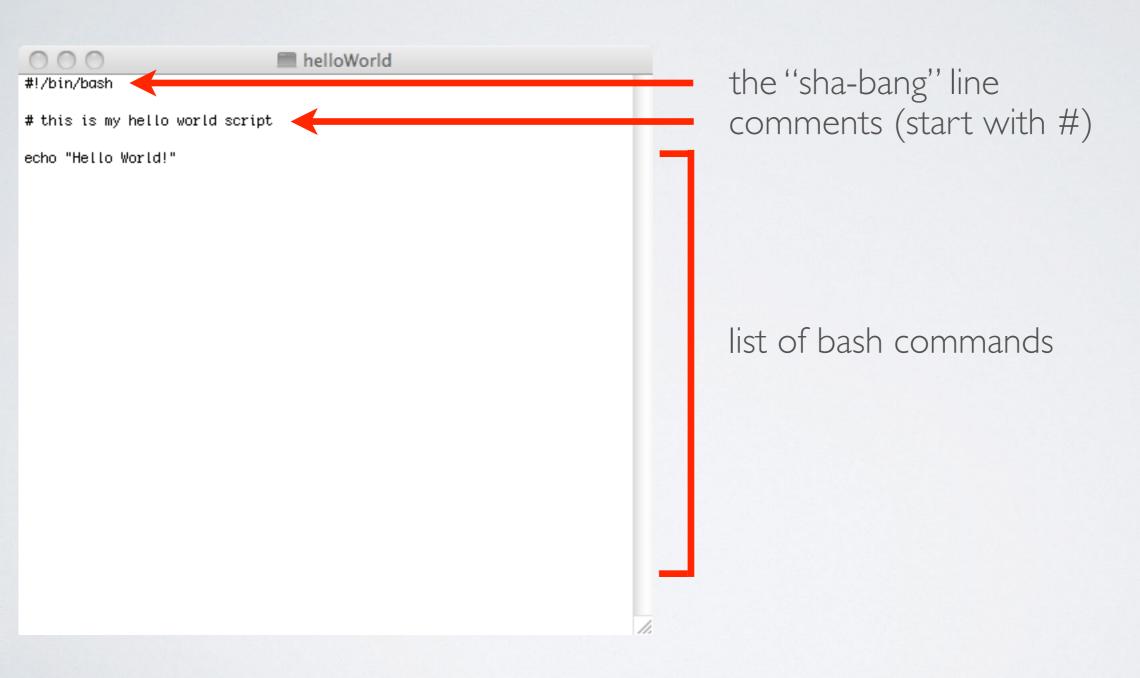
# V. bash scripting

# What is bash scripting?

- A bash script is nothing more than a list of bash commands in an executable text file
- Exactly the same behavior could be achieved by copying and pasting the script into the bash shell
- Extremely powerful way to automate system tasks
  - e.g. file downloads system backups job submission file processing

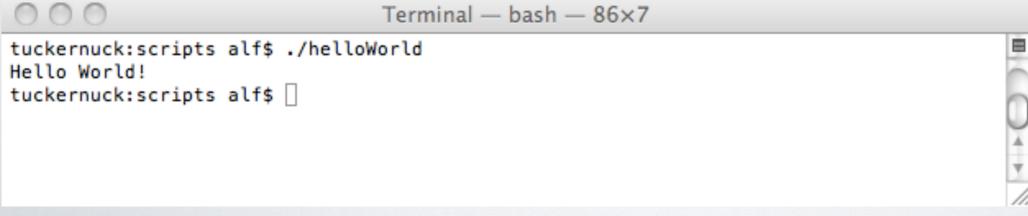
# Anatomy of a script

- A script is nothing more than a text file
  - write using vi, emacs, Notepad, or favorite text editor



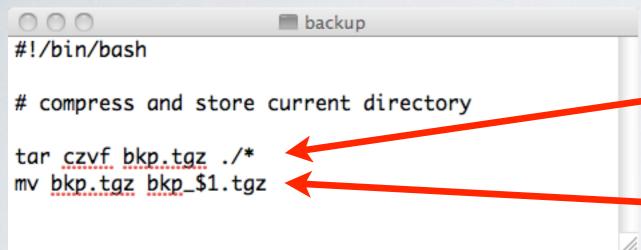
### Script I: hello world!

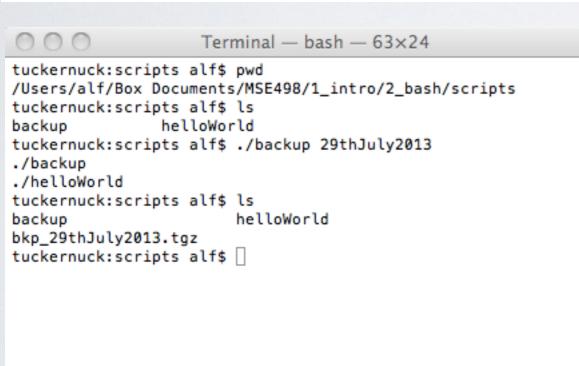
```
$ touch helloWorld
                           new script file
 chmod 755 helloWorld
                           making executable
 vi helloWorld
                           edit line below
$ i
                           enter insert mode
$ #!/bin/bash <Enter>
$ # this is my hello world script <Enter>
 echo "Hello World!"
                           escape to navigate mode
  Esc
                           write and quit
 :WQ
```



### Script 2: backup

Passing variables \$1, \$2, \$3, ...





Placing all files in current directory into a compressed tape archive bkp.tgz

Renaming bkp.tgz bkp\_<arg>.tgz where arg is the first argument in the call to the executable

### Script 3: summer

- while loop
- \$# and shift

```
#!/bin/bash

# sum all numbers passed to script

sum=0
while [ $# -gt 0 ] ; do
        echo "newNum=$1"
        sum=`expr $sum + $1`
        echo "sum=$sum"
        echo ""
        shift
done
```

```
Terminal — bash — 46×19

tuckernuck:scripts alf$ ./summer
tuckernuck:scripts alf$ ./summer 10
newNum=10

tuckernuck:scripts alf$ ./summer 10 -4 9 17
newNum=10
sum=10

newNum=-4
sum=6

newNum=9
sum=15

newNum=17
sum=32
tuckernuck:scripts alf$ [
```

arithmetic comparisons

Initializing sum to 0

while loop - run loop while the variable \$# is greater than 0

- \$# = number of parameters in exec call
- shift = kick out \$1 and shift rest down (i.e. \$1  $\leftarrow$  \$2, \$2  $\leftarrow$  \$3, \$3  $\leftarrow$  \$4, ...)
- arithmetic comparisons:

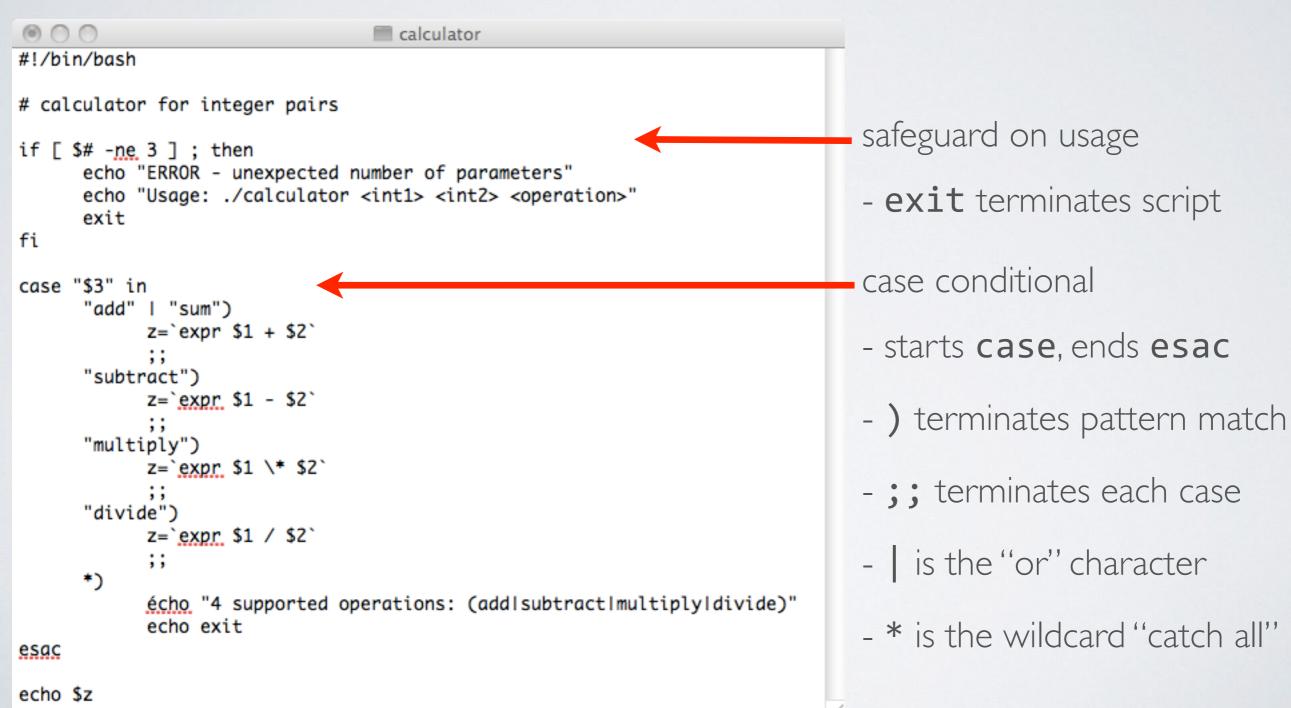
### Script 4: oracle

- if/else statement
- nesting

```
oracle
#!/bin/bash
# oracle guessing game
magicNumber=15
                                                                 if loop
if [ $1 -eq $magicNumber ]; then
      echo "You're correct!"
else
                                                                 nested if loop
     if [ $1 -gt $magicNumber ]; then
            echo "Too high!"
      else
            echo "Too low!"
                                                                 - can also use the construct:
     fi
                                                                 if []; then
fi
                                                                 elif []; then
             Terminal — bash — 53 \times 19
                                                                 elif ∏; then
tuckernuck:scripts alf$ ./oracle
./oracle: line 7: [: -eq: unary operator expected
                                                                 else
./oracle: line 10: [: -gt: unary operator expected
Too low!
tuckernuck:scripts alf$ ./oracle 26
tuckernuck:scripts alf$ ./oracle -12
tuckernuck:scripts alf$ ./oracle 15
You're correct!
tuckernuck:scripts alf$
```

#### Script 5: calculator

- case conditional
- exit
- defensive programming



### Script 5: calculator

```
Terminal — bash — 56×15

tuckernuck:scripts alf$ ./calculator

ERROR - unexpected number of parameters
Usage: ./calculator <int1> <int2> <operation>
tuckernuck:scripts alf$ ./calculator 7 3 add
10
tuckernuck:scripts alf$ ./calculator 7 3 sum
10
tuckernuck:scripts alf$ ./calculator 7 3 subtract
4
tuckernuck:scripts alf$ ./calculator 7 3 multiply
21
tuckernuck:scripts alf$ ./calculator 7 3 divide
2
tuckernuck:scripts alf$ ./calculator 7 3 divide
```

# Script 6: stringer

arrays **\$@** 

```
#!/bin/bash

# appends ".txt" to all strings other than "virus"

strArray=("$@")
echo "strArray = ${strArray[@]}"

fileArray=()
for str in ${strArray[@]} ; do
    if [ $str != "virus" ] ; then
        sz=${#fileArray[@]}
        fileArray[`expr $sz + 1`]=$str"".txt
    fi
done
echo "fileArray = ${fileArray[@]}"
```

```
Terminal — bash — 65×11

tuckernuck:scripts alf$ ./stringer good bad ugly
strArray = good bad ugly
fileArray = good.txt bad.txt ugly.txt
tuckernuck:scripts alf$ ./stringer clean1 virus clean2 clean3
strArray = clean1 virus clean2 clean3
fileArray = clean1.txt clean2.txt clean3.txt
tuckernuck:scripts alf$ []
```

Create an array strArray from parameters

- \$@ = all parameters passed to bash call
- \${ARRAY[@]} = array contents

Create empty array fileArray

For all strings except "virus" append txt and store in fileArray

- **\${#ARRAY[@]}** = array size
- "" terminates \$ dereference string
- str comparisons:

=	equal
!=	not equal
>	greater than
<	less than
-n <str></str>	not empty
-z <str></str>	empty

### Script 7: filer

infinite loop Ctrl + C

myDirectory is not a regular file in pwd

tuckernuck:scripts alf\$

Please enter a file name to test (Ctrl + C to exit):

read user input

```
filer
#!/bin/bash
# tests whether user supplied strings are files in pwd
while [ 1 -ne 0 ] ; do
      echo "Please enter a file name to test (Ctrl + C to exit):"
      read str
      if [ -f $str ]; then
             echo "$str is a regular file in pwd"
      else
             echo "$str is not a regular file in pwd"
      fi
      echo
done
                   Terminal — bash — 67×19
tuckernuck:scripts alf$ ls
backup
              filer
                           myDirectory
                                         stringer
calculator
              helloWorld
                           oracle
                                         summer
tuckernuck:scripts alf$ ./filer
Please enter a file name to test (Ctrl + C to exit):
summer is a regular file in pwd
Please enter a file name to test (Ctrl + C to exit):
winter
winter is not a regular file in pwd
Please enter a file name to test (Ctrl + C to exit):
```

Infinite loop (Ctrl + C to break)

Read user input into str

Test if str is a regular file in the present working directory

- file comparison operators
  - -e file exists (may be directory)
  - -f file exists (not directory)
  - -d directory exists
  - -r file readable
  - -w file writable
  - -x file executable

# Script 8: squarer

iterating functions

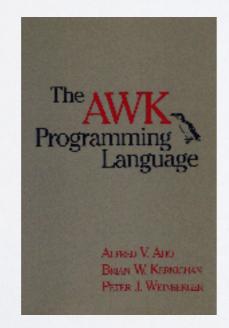
sleep

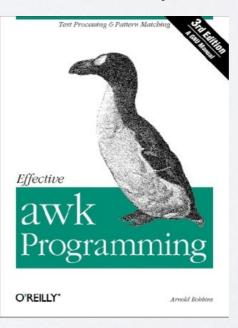
```
squarer
#!/bin/bash
                                                   Declaring a function at top of script
# function declarations
function square() {
      z='expr $1 \* $1
                                                   As for main function $1,$2,... are passed variables
      echo $z
# prints square of every eighth number between 56 and 107
                                                   Setting up the iterative loop
start=56
stop=107
step=8
i=$start
                                                   Performing square using our function
while [ $i -le $stop ] ; do
      i2=`square $i`
                                                   sleep 0.5 = 0.5 s pause between prints
      echo "i \times i = i2"
      sleep 0.5
      i='expr $i + $step'
                                                   incrementing loop variable
done
```

#### VI. awk

#### awk

- awk is a programming language in its own right
- Developed at Bell Labs in 70's by Aho, Weinberger, & Kernighan
- Powerful, simple, fast and flexible language
- Standard part of most Linux distributions, used primarily for rapid and efficient line-by-line text processing





# Why awk?

- "Forget awk, I'll just use vi / emacs / Notepad!"
- OK, good luck...
  - extract the third column of this 50,000 line file
  - divide the second field of each line by the seventh, and save results in csv format
  - extract every 15th line of this file and invert the field ordering to run from last to first
- awk can do these things (and many others!) extremely efficiently and quickly using "one liner" commands
  - integrates seamlessly into bash shell cat <file> | awk ...
  - integrates seamlessly into bash scripts
  - great power using only a handful of commands
  - is simply the "right tool" for many text processing jobs

#### awk basics

- Rudimentary awk, comprehensive beginner's tutorial at: <a href="http://www.grymoire.com/Unix/Awk.html">http://www.grymoire.com/Unix/Awk.html</a>
- Anatomy of an awk program

```
awk 'BEGIN { ... } 

Do stuff before starting [optional] 

{ ... } 

Line-by-line processing 

END { ... }' 

Do stuff after end-of-file [optional] 

inFile > outFile 

Read from inFile, write to outFile
```

- Can place within a script, or enter directly into terminal
- White space doesn't matter

#### awk basics

Alternatively, can pipe input from terminal

```
cat inFile > awk 'BEGIN { ... }
{ ... }
END { ... }'
> outFile
```

- Omit "> outFile" to output directly to terminal
- Use ">>" instead of ">" to append rather than overwrite

# What goes in the { }?

- Commands perform line-by-line text processing
- Assignment of internal awk variables
- Flow control and loops
- Pulling in of bash variables from surrounding script
- Printing to terminal or file
- Basic arithmetic

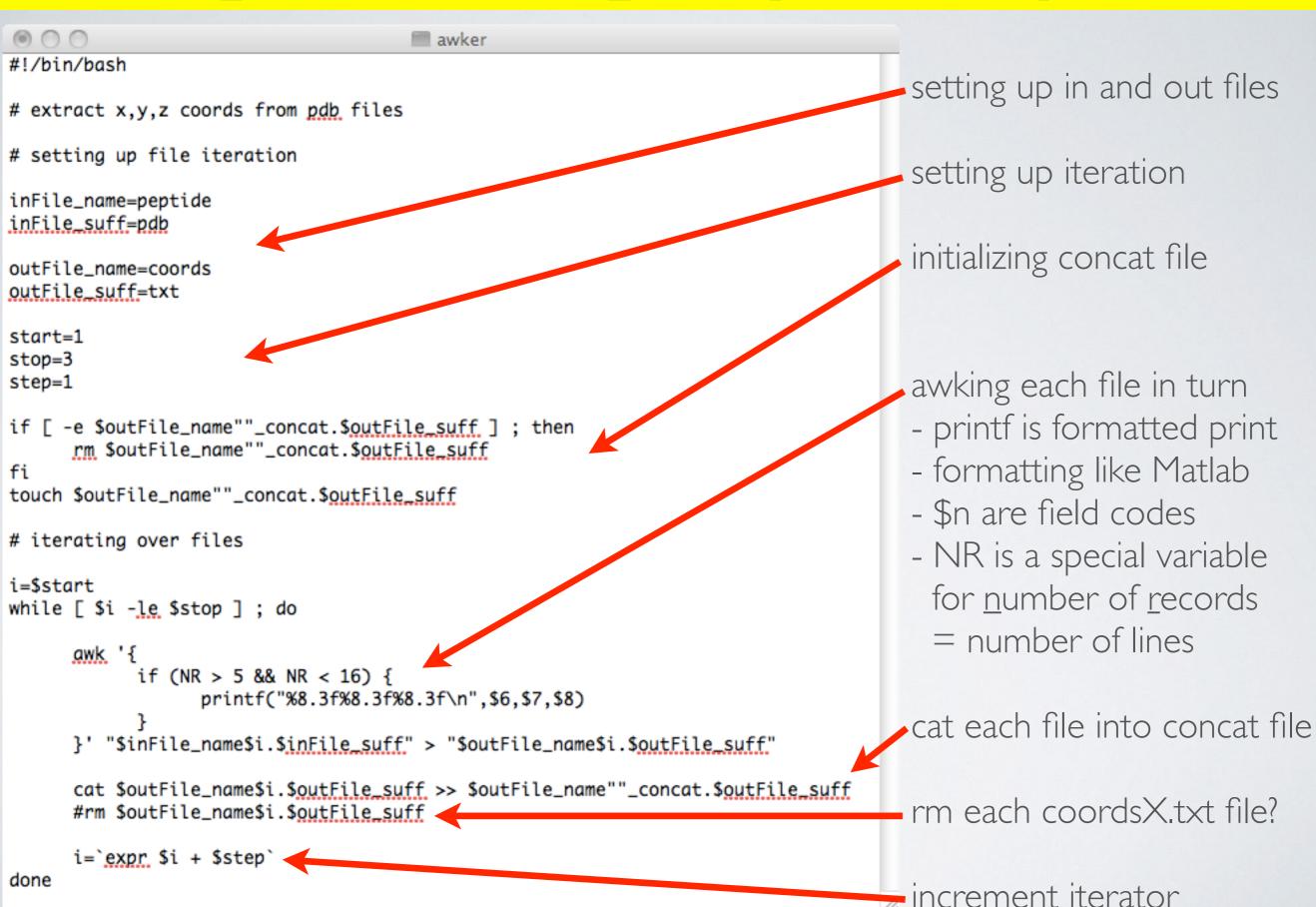
# [bash + awk] script example

- Extract the x,y,z coordinates of peptide atoms from pdb formatted files peptide[1-3].pdb into coords[1-3].txt
- Concatenate coords[1-3].txt into coords\_concat.txt
- Use bash to iterate over files
- Use awk to perform text processing

```
peptide1.pdb
REMARK
TITLE
         Protein in water t=
                              0.00000
REMARK
         THIS IS A SIMULATION BOX
CRYST1
        30.000
               30.000 30.000 90.00
MODEL
            1
ATOM
         1 CH3 ACE
                              12.710 13.550 14.060 1.00
                ACE
ATOM
                              13.940 13.780 13.200
ATOM
                              13.810 13.690 11.980 1.00
ATOM
                              15.140 14.090 13.710 1.00
ATOM
                              15.470 14.590 15.030 1.00
ATOM
                              15.820 13.370 15.880 1.00
ATOM
                              16.680 15.490 14.870 1.00
ATOM
                              17.650 15.130 14.200 1.00
ATOM
               NAC
                              16.760 16.620 15.570 1.00
        10 CH3 NAC
ATOM
                              15.700 17.290 16.300 1.00
TER
ENDMDL
```

```
12.710 13.550 14.060
13.940 13.780 13.200
13.810 13.690 11.980
15.140 14.090 13.710
15.470 14.590 15.030
15.820 13.370 15.880
16.680 15.490 14.870
17.650 15.130 14.200
16.760 16.620 15.570
15.700 17.290 16.300
```

# [bash + awk] script example



# [bash + awk] script example

```
coords_concat.txt
12.710 13.550 14.060
13.940 13.780 13.200
13.810 13.690 11.980
15.140 14.090 13.710
15.470 14.590 15.030
15.820 13.370 15.880
16.680 15.490 14.870
17.650 15.130 14.200
16.760 16.620 15.570
15.700 17.290 16.300
12.718 13.940 14.128
13.912 13.876 13.177
13.779 13.427 12.038
15.126 14.114 13.654
15.559 14.482 14.993
15.903 13.162 15.687
16.707 15.479 14.919
17.719 15.207 14.290
16.661 16.648 15.569
15.603 17.318 16.306
12.710 13.615 13.995
13.968 13.676 13.137
13.908 13.358 11.952
15.136 14.106 13.627
15.468 14.683 14.911
15.388 13.763 16.136
16.738 15.517 14.857
17.472 15.395 13.877
16.923 16.519 15.721
15.969 17.005 16.693
```

Doing this [by hand / in Excel / in Matlab] at any significant scale would be extremely tedious and error prone!