

# Lecture 9    Scaling Latency

Module 1: Bitcoin. (lectures 2-7).

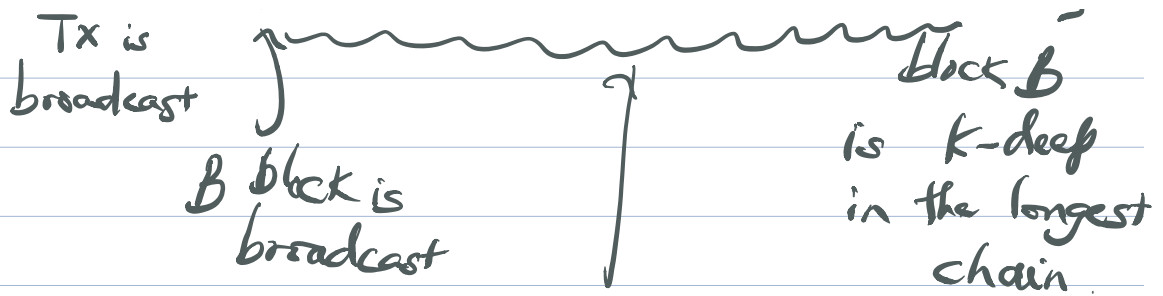
Module 2: Scaling Bitcoin (lectures 8-15)

- improving performance while still retaining longest chain protocol
  - more or less the software stack is unchanged.
- throughput (#8)  
**latency (#9)**  
storage & compute (#10)  
trust taken out externally (#10)  
energy #12

(1) Bitcoin latency.

time from when a tx was broadcast until the tx is confirmed in the ledger





- seed bottleneck
- depends on how large  $k$  is.

$$\text{Latency} \approx k \cdot \frac{1}{\lambda}$$

Rate of blocks

But due to forking, not all blocks may be on a chain.

$$\text{Latency} \approx k \cdot \frac{1}{\frac{(1-\beta)\lambda}{1+(1-\beta)\lambda\Delta}}$$

network delay

$$\Delta = \frac{D}{T} + \frac{B}{C}$$

$B \leftarrow$  block size  
 $C \leftarrow$  capacity

Speed of  
light  
Propagation  
delay

processing  
delay

$$\text{Latency} \approx k \cdot \Delta.$$

$$\frac{1}{(1-\beta)\lambda\Delta} \cdot \frac{1}{1+(1-\beta)\lambda\Delta}.$$

for low forking:  $\lambda\Delta \ll 1$ .

how about  $k$ ?

From lecture 6;  $P_e \approx e^{-ck}$

$$k \approx \frac{1}{c} \log\left(\frac{1}{P_e}\right).$$

↑  
Constant depends on  $\beta$ .

$$\text{Latency} \approx \frac{1}{c} \cdot \underbrace{\log\left(\frac{1}{P_e}\right)}_{\text{security}} \cdot \frac{1}{(1-\beta)\lambda}.$$

$$\lambda \ll \frac{1}{\Delta}$$

Bitcoin:  $\frac{1}{\lambda} \approx 10 \text{ minutes}$

$$k = 200$$

then latency = 16 hours.

Only way to improve latency is

\* reduce  $k$  ; but this reduces security

\* increase  $\lambda$  ; but this reduces security.

Ethereum:  $\frac{1}{\lambda} = 15s$   
 $k = 100$

latency = 25 minutes.

Way better than Bitcoin performance.

improvement simply by picking better

parameters.

Question: Can one make relatively small changes to the longest chain protocols of PoW mining while scaling latency?

⇒ do not want latency to depend on security level.

→ decouple security from latency.

Hybrid Consensus.

BFT Consensus algorithms provide

fast consensus among a fixed set of participating nodes.

1982 ; ← began

40 years later: Very good state of the art.

It will enter 2 such protocols in

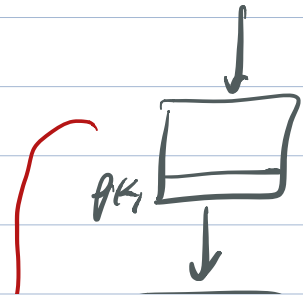
# Module 3

For now blackbox BFT consensus

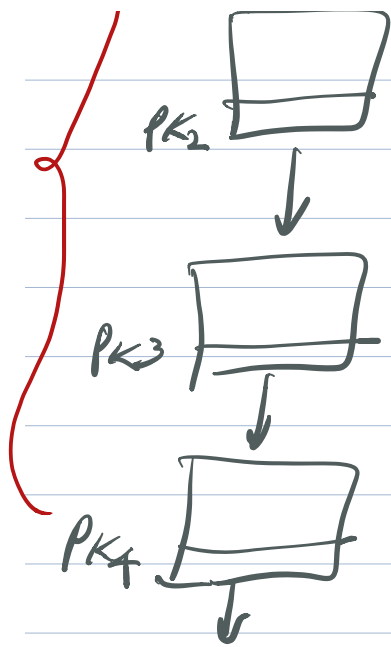
Q: How to bring this blackbox to Bitcoin to speed up latency?

challenge: to use the blackbox, one needs to have a fixed set of participants.

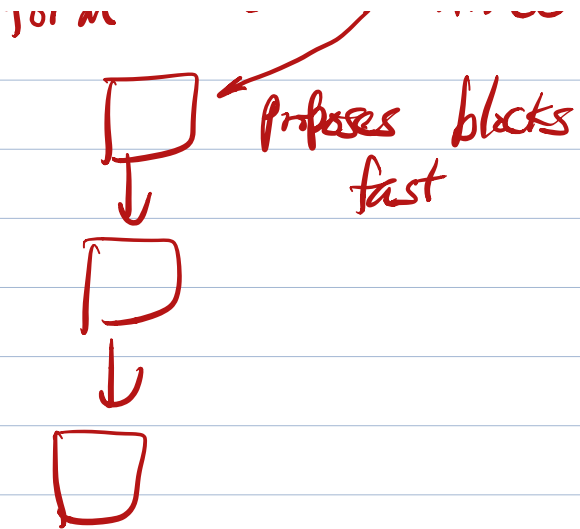
Idea: elect the BFT participants (Committee) from the longest chain itself.



(PK<sub>1</sub>, PK<sub>2</sub>, PK<sub>3</sub>, PK<sub>4</sub>)  
from a committee.



Slow  
longest chain  
protocol.



- The committee evolves over time as the longest chain progresses.
- This keeps refreshing the committee for BFT protocol.
- Vulnerable to an adaptive adversary.

Can pick which miner  
is adversarial dynamically as a  
function of blockchain state

- In practice: bribing attack.  
works because miners can have  
very small hash power but  
get lucky to be a proposer.

Prism



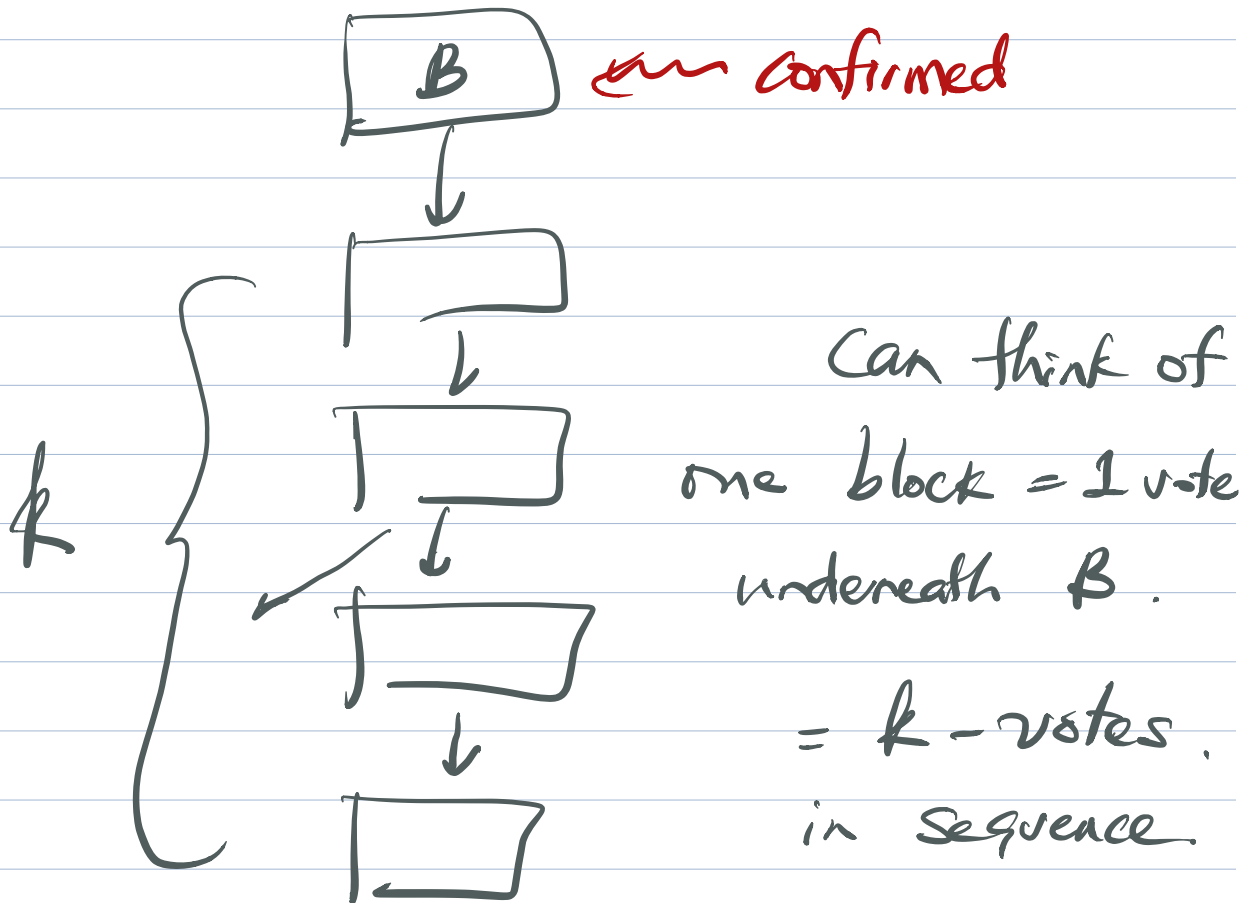
- Prism 1.0 which scaled  
throughput; last lecture.

Optimal latency.

Decoupling Principle:  
Security      Voting



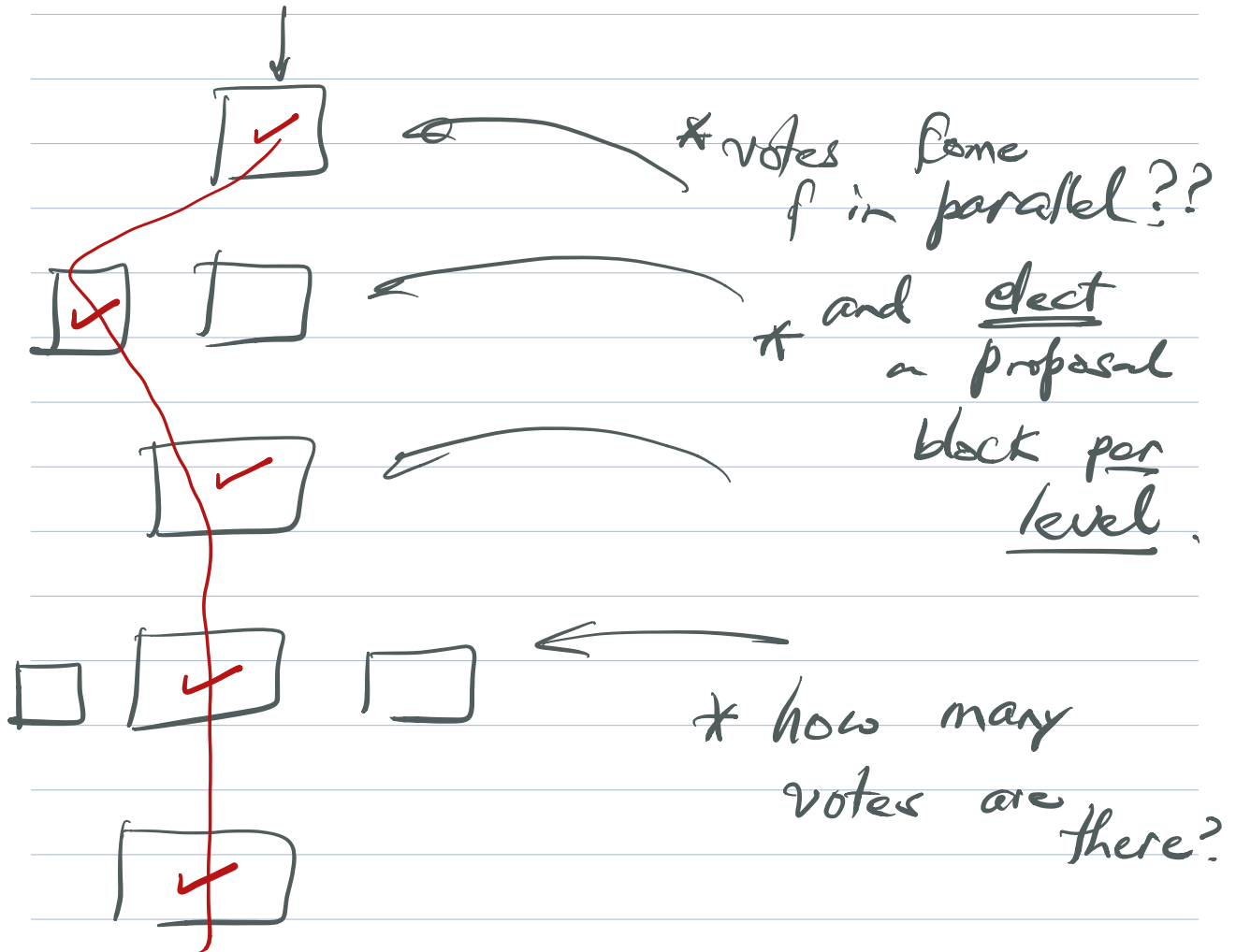
$k$ -deep Confirmation rule is a form of voting.



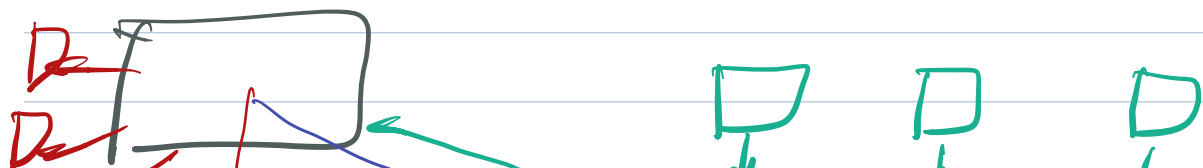
really need  $k$  large  $\sim$  sample the miners.

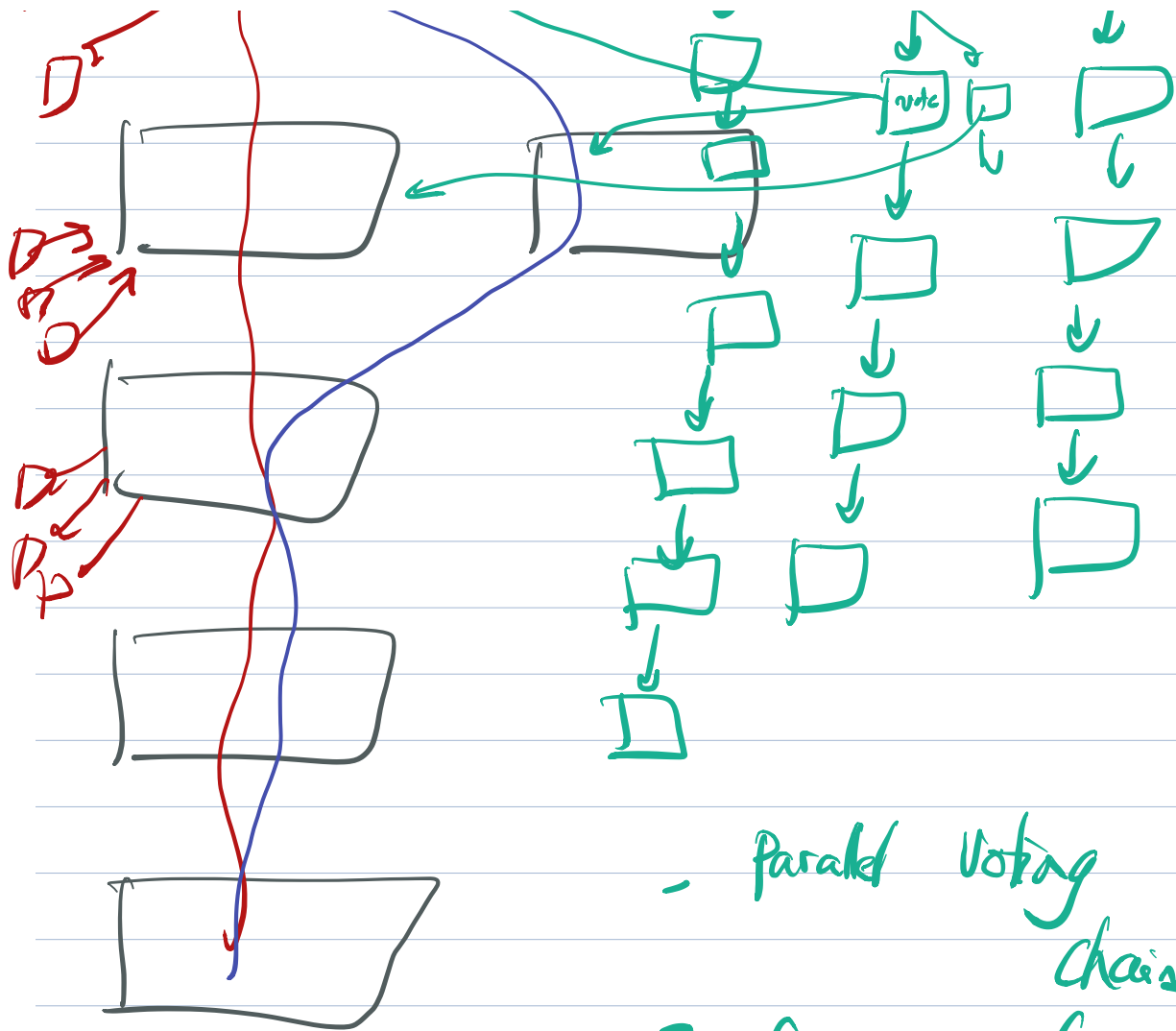
when  $k$  is small

Java: vote in parallel



Prism: many parallel  
Voting chains





Proposal rate  
Voting rate  
Mining rate

- Parallel Voting chains
- fixed # of voting chains

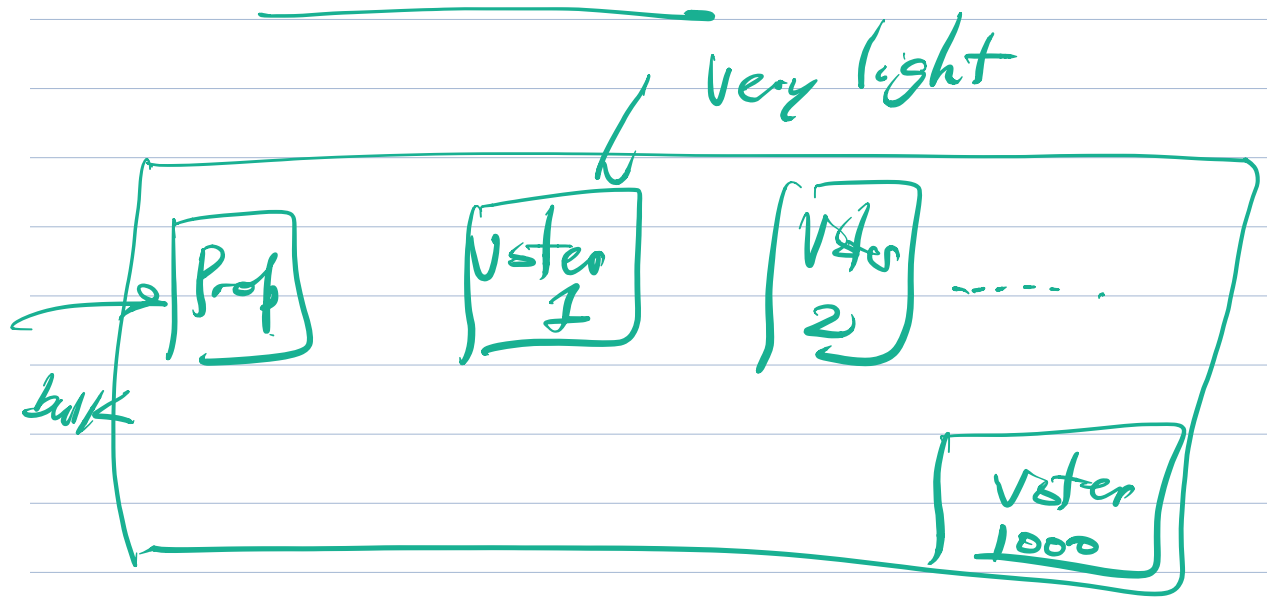
e.g. 2000.

honest miner picks to be  
 prop  
 &  
 voting  
 block  
 at random

But how do you prevent adv. from congregating?

Sortition or many-to-1 mining.

Super block:



mine superblock

hash (superblock) decides

which are the superblock  
plays.