

University of Illinois at Urbana-Champaign  
Department of Electrical and Computer Engineering

ECE 534: RANDOM PROCESSES

Spring 2005

**Information Sheet**

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| <b>Instructor:</b>         | Christoforos Hadjicostis    357CSL<br>E-mail: chadjic@uiuc.edu    Office Hours: Monday 4:00–6:00pm in 351CSL  |
| <b>Teaching Assistant:</b> | Karen Guan    119CSL<br>E-mail: kguan@uiuc.edu    Office Hours: Tuesday 3:00–5:00pm in 114CSL   |
| <b>Time and Place:</b>     | Lectures: MW 2:30–3:50pm in 1214 Siebel.<br>Quiz, Midterm Exams and makeup lectures: Wednesday 5:00–7:00pm  |
| <b>Required Textbook:</b>  | B. Hajek, <i>An Exploration of Random Processes for Engineers</i> .<br>Available for download at<br><a href="http://comm.csl.uiuc.edu/~hajek/Papers/randomprocesses.html">http://comm.csl.uiuc.edu/~hajek/Papers/randomprocesses.html</a><br>and also available at the TIS Copy Shop. |
| <b>Course Web Page:</b>    | <a href="http://courses.ece.uiuc.edu/ece534/">http://courses.ece.uiuc.edu/ece534/</a>   |

**Grading and Exams:** Homework (10%), Probability Quiz on 02/09 (10%), Midterm 1 on 03/09 (20%), Midterm 2 on 04/13 (20%) and Final Exam (scheduled for 05/12 from 1:30–4:30pm, 40%). Exams are closed book; one 8.5"x11" sheet of notes (both sides) is permitted for Midterm 1, two sheets are permitted for Midterm 2, and three for the final. The Probability Quiz and the Midterm Exams will be from 5–7pm.

**Homework Policy:** Collaboration on the homework is permitted but each student must write and submit independent solutions. Homework is due within the first five minutes of the class period on the due date. Late homework will not be accepted without prior arrangement with the instructor. The bottom homework grade will be dropped to accommodate one missed homework for every student.

**List of recommended textbooks reserved at Grainger:**

1. H. Stark and J. W. Woods, *Probability and Random Processes with Applications to Signal Processing*. Third Edition, Prentice Hall, 2001.
2. R. G. Gallager, *Discrete Stochastic Processes*. Kluwer, 1996.
3. H. Stark and J. W. Woods, *Probability and Random Processes with Applications to Signal Processing*. Second Edition, Prentice Hall, 1994.
4. W. B. Davenport, Jr. and W. L. Root, *An Introduction to the Theory of Random Signals and Noise*. McGraw Hill, 1987.
5. E. Wong and B. Hajek, *Stochastic Processes in Engineering Systems*. Springer Verlag, 1985.
6. A. Papoulis, *Probability, Random Variables and Stochastic Processes*. Second Edition, McGraw Hill, 1984.
7. E. Wong, *Introduction to Random Processes*. Springer Verlag, 1983.
8. B. D. O. Anderson and J. B. Moore, *Optimal Filtering*. Prentice Hall, 1979.
9. W. Rudin, *Principles of Mathematical Analysis*. Third Edition, McGraw-Hill, New York, 1976.
10. R. B. Ash, *Basic Probability Theory*. Academic Press, 1972.
11. L. Breiman, *Probability*. Addison-Wesley, 1968.
12. H. Cramer and M. R. Leadbetter, *Stationary and Related Stochastic Processes*. Wiley, 1967.
13. E. Parzen, *Stochastic Processes*. Holden Day, 1962.

## Course Outline

### I. Review of Probability Theory

1. Basic axioms; probability space and measure; sigma algebras
2. Conditional probability and independence
3. Random variable; probability distribution and density
4. Random vectors; conditional distributions and independence
5. Functions of random variables and random vectors
6. Expectation; conditional expectation and properties

### II. Sequences of Random Variables

1. Notions of convergence
2. Limit theorems; large deviations

### III. Random Vectors and Minimum Mean Squared Error (MMSE) Estimation

1. Linear MMSE and MMSE estimators
2. Orthogonality principle
3. Jointly Gaussian random variables and vectors
4. Kalman filtering

### IV. Random Processes

1. Continuous- and discrete-time random processes
2. Stationarity and wide-sense stationarity (WSS)
3. Second-order processes; mean and correlation function spectrum
4. Markov processes and martingales; Gaussian, Wiener, and Poisson processes

### V. Calculus for Random Processes

1. Continuity of random processes; differentiation and integration
2. Orthogonal representation of random processes (Karhunen-Loeve expansion)
3. Ergodicity

### VI. Stationary Random Processes and Spectral Analysis

1. Power spectral density and its estimation
2. Random processes through linear systems
3. Spectral representation of random processes

### VII. Minimum Mean Squared Error (MMSE) Estimation

1. MMSE estimation and linear MMSE estimation for random vectors
2. Discrete- and continuous-time Kalman filter
3. The Wiener filter; spectral factorization and applications