

## Possibly Useful Formulas

**Admissible:**  $\hat{h}(n) \leq h(n)$

**Consistent:**  $\hat{h}(n) - \hat{h}(m) \leq h(n, m)$

**Value Iteration:**  $u_i(s) = r(s) + \gamma \max_a \sum_{s'} P(s'|s, a) u_{i-1}(s)$

**Policy Evaluation:**  $u_\pi(s) = r(s) + \gamma \sum_{s'} P(s'|s, \pi(s)) u_\pi(s')$

**Policy Improvement:**  $\pi_{i+1}(s) = \operatorname{argmax}_a \sum_{s'} P(s'|s, a) u_{\pi_i}(s')$

**Alpha-Beta Max Node:**  $v = \max(v, \text{child}); \quad \alpha = \max(\alpha, \text{child})$

**Alpha-Beta Min Node:**  $v = \min(v, \text{child}); \quad \beta = \min(\beta, \text{child})$

**Expectiminimax:**  $u(s) = \begin{cases} \max_a \sum_{s'} P(s'|a, a) u(s') & s \in \text{max states} \\ \min_a \sum_{s'} P(s'|a, a) u(s') & s \in \text{min states} \end{cases}$

**Mixed Nash Equilibrium:** 
$$\begin{aligned} P(A=0)r_B(0,0) + P(A=1)r_B(1,0) &= P(A=0)r_B(0,1) + P(A=1)r_B(1,1) \\ P(B=0)r_A(0,0) + P(B=1)r_A(0,1) &= P(B=0)r_A(1,0) + P(B=1)r_A(1,1) \end{aligned}$$

**Unification:**  $S: \{\mathcal{V}_P, \mathcal{V}_Q\} \rightarrow \{\mathcal{V}_Q, \mathcal{C}\}$  such that  $S(P) = S(Q) = U$

**CBOW Generative:** 
$$\mathcal{L} = -\frac{1}{T} \sum_{t=1}^T \sum_{j=-c, j \neq 0}^c \ln \frac{\exp(\mathbf{v}_t^T \mathbf{v}_{t+j})}{\sum_{\mathbf{v} \in \mathcal{V}} \exp(\mathbf{v}^T \mathbf{v}_{t+j})}$$

**Skip-gram Contrastive:** 
$$\mathcal{L} = -\frac{1}{T} \sum_{t=1}^T \left( \sum_{\mathbf{v}' \in \mathcal{D}_+(w_t)} \ln \frac{1}{1 + e^{-\mathbf{v}'^T \mathbf{v}_t}} + \sum_{\mathbf{v}' \in \mathcal{D}_-(w_t)} \ln \frac{1}{1 + e^{\mathbf{v}'^T \mathbf{v}_t}} \right)$$

**Transformer:**  $\mathbf{c}_t = \sum_s \alpha(t, s) \mathbf{v}_s$

**Attention:**  $\alpha(t, s) = \frac{\exp(\mathbf{q}_t^T \mathbf{k}_s)}{\sum_{s'} \exp(\mathbf{q}_t^T \mathbf{k}_{s'})}$