

# Collab Worksheet 10

CS440/ECE448, Spring 2021

Week of 4/19 - 4/23, 2021

## Question 1

Consider a simultaneous game in which each player has three possible moves: A, B, or C. The payoff matrix is shown below. In each square, the first number refers to payoff for Alice (the player whose moves are shown on the row-label), the second number refers to payoff for Bob (the player shown on the column label).

Alice's Move	Bob's Move		
	A	B	C
A	0\0	25\40	5\10
B	40\25	0\0	5\15
C	10\5	15\5	10\10

- (a) Are there any dominant strategies? If so, what are they? If not, why not?
- (b) Are there any pure-strategy Nash equilibria? If so, what are they? If not, why not?
- (c) Are there any Pareto-optimal solutions? If so, what are they? If not, why not?

## Question 2

Alice and Bob are playing a game called "exes and ohs". First, Alice draws either an X or an O, without showing it to Bob. Then Bob does the same. Then they show each other their moves, and they each receive the number of points shown in the following payoff matrix. In each square, Alice's payoff is below the diagonal line, Bob's is above it:

Alice's Move	Bob's Move	
	X	O
X	6\6	4\10
O	10\4	2\2

- (a) What are the Pareto-optimal outcomes for this game?
  
- (b) Are there fixed-strategy Nash equilibria for this game? If so, what are they? If not, why not?
  
- (c) Is there a mixed-strategy Nash equilibrium for this game? If so, what is it? If not, why not?