

ECE 431

Electric Machinery

Name: Solutions

Test #2

April 5, 2019

NetID: _____

You may use one 2-sided sheet of your own hand-written notes as reference.

Please do all work on this test. Label any solutions that are written on the backs of pages or on any spare sheets.

Q1. (35 Points)

A 480V (line voltage), 4 pole, 60 Hz synchronous motor is drawing 30A from the grid at 0.95 lagging power factor. The motor is operating with a field current of 5A and a synchronous reactance of 10 ohms.

- Calculate the internal voltage and load angle.
- Draw the phasor diagram corresponding to this operating condition, and using dashed lines, overlay the phasor diagram when operating at unity power factor with constant excitation.
- Calculate the armature current, internal voltage, load angle of the synchronous motor when it is operated at unity power factor with constant excitation.

a) $\theta = -\cos^{-1} 0.95$
 $= -18.19^\circ$

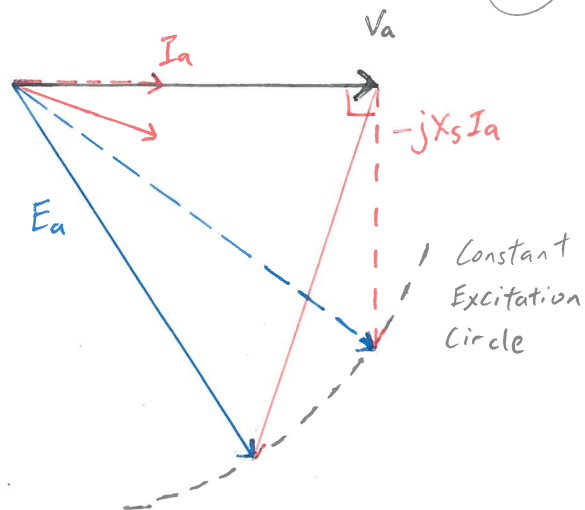
$$I_a = 30 \angle -18.19^\circ \text{ A}$$

$$V_a = \frac{480}{\sqrt{3}} = 277.13 \angle 0^\circ \text{ V}$$

$$E_a = V_a - jX_s I_a$$

$$= 338.96 \angle -57.23^\circ \text{ V}$$

b)



c) $|E_a| = 338.96 \text{ V}$

$$|V_a| = 277.13 \text{ V}$$

$$|X_s I_a| = \sqrt{|E_a|^2 - |V_a|^2}$$

$$= 195.17 \text{ V}$$

$$I_a = \frac{|X_s I_a|}{10} = 19.52 \angle 0^\circ \text{ A}$$

$$E_a = V_a - jX_s I_a$$

$$= 338.96 \angle -35.13^\circ \text{ V}$$

Q2. (30 Points)

A synchronous generator with a synchronous reactance of 0.5pu is supplying the grid at rated voltage, rated KVA and 0.85 lagging power factor. A fault occurs and reduces the generator output voltage to 0.5pu. After the fault is cleared, the output voltage is restored to rated voltage.

- Calculate the initial internal voltage(pu) and load angle.
- Draw the power curves for the generator and mark out the areas and angles that are required to evaluated generator stability using the equal area criterion.
- Write out the equations required to calculate the critical angle. DO NOT solve for the critical angle.

$$a) \theta = -\cos^{-1} 0.85$$

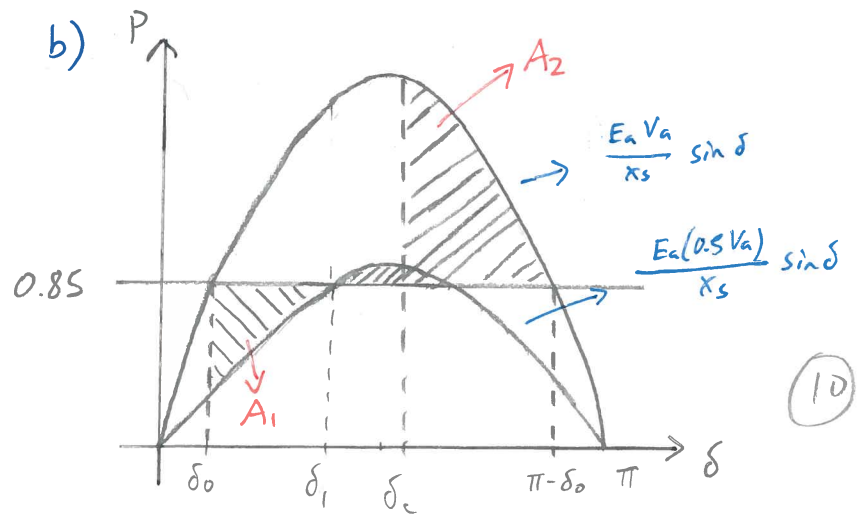
$$= -31.79^\circ$$

$$I_a = 1.0 \angle -31.79^\circ \text{ pu}$$

$$E_a = V_a + jX_s I_a$$

$$= 1.33 \angle 18.59^\circ \text{ pu}$$

$$\delta_0 = 18.59^\circ = 0.3245 \text{ rad}$$



$$c) A_1 = \int_{\delta_0}^{\delta_c} 0.85 - \frac{E_a \cdot (0.5 V_a)}{X_s} \sin \delta \, d\delta$$

$$= \int_{\delta_0}^{\delta_c} 0.85 - 1.33 \sin \delta \, d\delta$$

$$A_2 = \int_{\delta_c}^{\pi - \delta_0} \frac{E_a V_a}{X_s} \sin \delta - 0.85 \, d\delta + \int_{\delta_1}^{\delta_c} \frac{E_a (0.5 V_a)}{X_s} \sin \delta - 0.85 \, d\delta$$

$$= \int_{\delta_c}^{\pi - \delta_0} 2.66 \sin \delta - 0.85 \, d\delta + \int_{\delta_1}^{\delta_c} 1.33 \sin \delta - 0.85 \, d\delta$$

$$A_1 = A_2$$

Q3. (35 Points)

A DC shunt motor has an armature resistance of 0.05 Ohms and a field resistance of 180 Ohms. A no-load speed of 1840 rpm is obtained when the motor is connected to a 200V supply. The motor is now connected to a load at the same voltage. Assume the load torque can be approximated by the following relationship,

$$T_{\text{load}} = 36 + 0.5\omega \text{ Nm}$$

- Calculate the motor speed at load
- Calculate the speed if the supply voltage is reduced to 120V
- What is the efficiency of the DC motor when operated at the new voltage?

$$I_f = \frac{200}{180} = 1.11 \text{ A}$$

$$\text{At no-load, } I_a = 0$$

$$E_a = 200 \text{ V}, \omega = 192.68 \text{ rad/s}$$

$$E_a = K_f I_f \omega \quad K_f = 0.935 \frac{\text{V} \cdot \text{s}}{\text{A} \cdot \text{rad}}$$

$$b) I_f = \frac{120}{180} = 0.667 \text{ A}$$

$$36 + \frac{\omega}{2} = K_f I_f \frac{V_a - K_f I_f \omega}{R_a}$$

$$\omega = 176.45 \text{ rad/s}$$

(10)

$$a) T_{\text{load}} = T_{\text{motor}}$$

$$36 + \frac{\omega}{2} = K_f I_f I_a$$

$$= K_f I_f \frac{V_a - E_a}{R_a}$$

$$36 + \frac{\omega}{2} = K_f I_f \frac{V_a - K_f I_f \omega}{R_a}$$

$$\omega = 186.7 \text{ rad/s}$$

(10)

$$c) T = 36 + \frac{\omega}{2}$$

$$= 124.22 \text{ Nm}$$

$$E_a = K_f I_f \omega$$

$$= 110.04 \text{ V}$$

$$I_a = \frac{V_a - E_a}{R_a}$$

$$= 199.16 \text{ A}$$

$$\cancel{P_{in} = V_a I_a = 25899 \text{ W}} \quad P_{in} = V_a (I_a + I_f) = 23979 \text{ W}$$

$$P_{out} = T \omega = 21919 \text{ W}$$

$$\eta = \frac{P_{in}}{P_{out}} \times 100 = \cancel{96.71\%}$$

$$= 91.41\%$$

(15)