

## Exam II Solution

Spring 1997

#1,  $k\omega\sqrt{3} = \frac{480}{\sqrt{3}}$   $k\omega = 92.3 \Omega$ ,  $92.3 \times 2 = 10X_s$   $X_s = 18.46 \Omega$

$$92.3 I_f \angle \delta = 10 \angle 0^\circ \times j 18.46 + \frac{480}{\sqrt{3}} \angle 0^\circ = 277 + j 184.6 = 333 \angle 34^\circ$$

$$I_f = 3.6 \text{ A}$$

#2,  $\frac{480}{\sqrt{3}} \angle 0^\circ = j 18.46 \bar{I} + 92.3 I_f \angle \delta$   $20 \text{ HP} = 14,920 \text{ W}$

(a)  $\bar{I} = \left( \frac{\frac{1}{3} 14,920}{480/\sqrt{3}} \right) \angle 0^\circ = 17.95 \angle 0^\circ$

minimum  $|\bar{I}|$  means  
 $\text{pf} = 1.0$

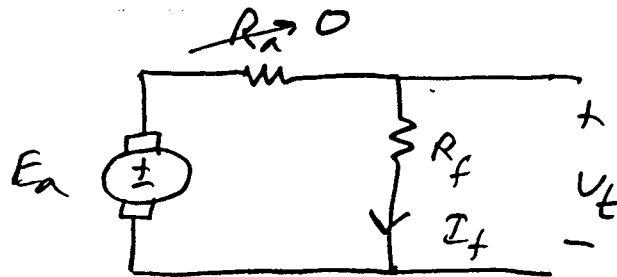
$$92.3 I_f \angle \delta = 277 \angle 0^\circ - j 18.46 \times 17.95 = 277 - j 331 = 432 \angle -50^\circ$$

$$I_f = 4.7 \text{ A}$$

(b) Minimum  $I_f$  when  $P_{in} = P_{max} = \frac{3 \times 277 \times 92.3 I_f}{18.46} = 14,920$

$$I_f = 3.6 \text{ A}$$

#3,



$$E_a = C_1 \omega + k_f^{SH} \omega I_f \approx V_t = R_f I_f$$

$$C_1 1200 + k_f^{SH} 1200 \times \frac{100}{100} = 100$$

$$C_1 1200 + k_f^{SH} 1200 \times \frac{120}{80} = 120$$

subtract

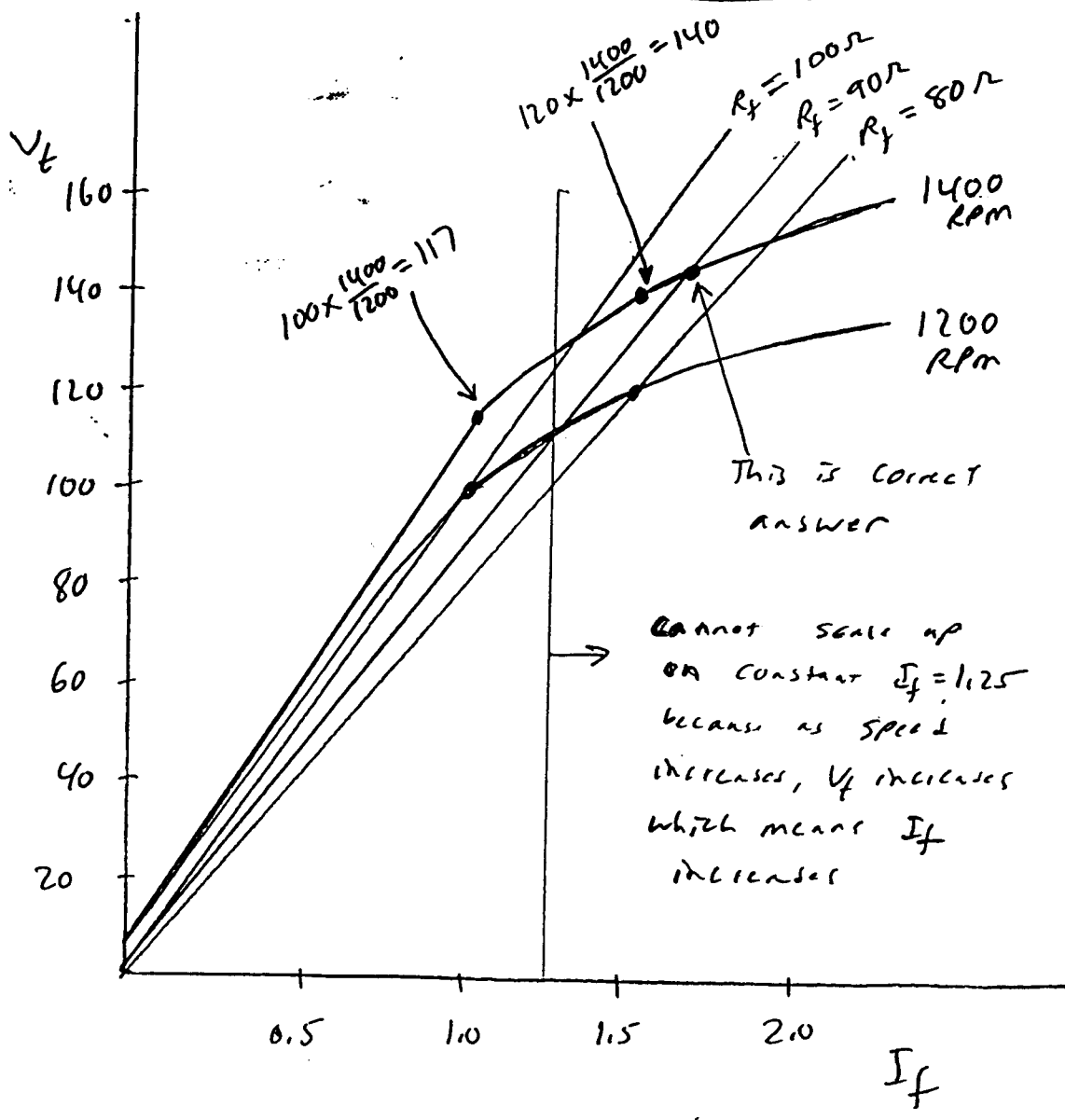
$$k_f^{SH} 1200 \times 0.5 = 20 \quad k_f^{SH} = \frac{40}{1200} \quad C_1 = \frac{60}{1200}$$

$$V_t \approx \frac{60}{1200} \times 1400 + \frac{40}{1200} \times 1400 \times \frac{V_t}{90} = V_t$$

$R_f = 90$   
 $R_{fa} = 1400$

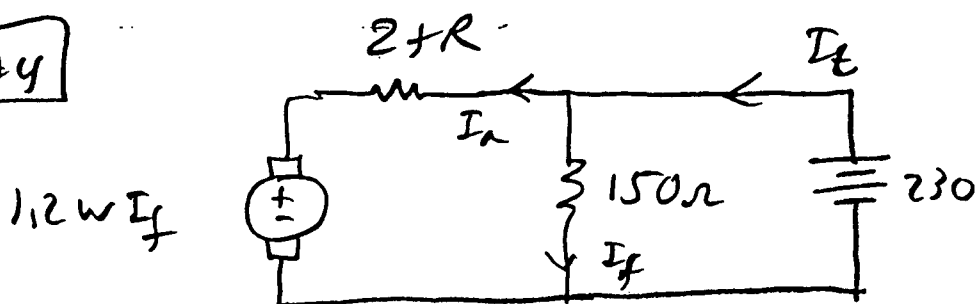
$$70 \times 90 = 43.33 V_t$$

$$V_t = 145 V$$



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#4



$$I_f = \frac{230}{150} = 1.533 \text{ A} \quad \text{want} \quad 20 = 1.533 + \frac{230}{2+R}$$

$$R = 10.45 \Omega$$

$$T_{To} = \frac{1.2\omega I_f I_a}{\omega} = 1.2 \times 1.533 I_a$$

Shaft

(A)

$$I_a = \frac{230 - 1.2 \times 1.533 \omega}{12.45}$$

$$T_{To} = 33.98 - 0.2718 \omega$$

Shaft

$$\omega(0.01) = \omega(0) + \left. \frac{d\omega}{dt} \right|_0 \cdot 0.01 = 0 + \frac{1}{0.2} (33.98 - 0) \cdot 0.01 = 1.699 \text{ r/s}$$

$$\omega(0.02) = 1.699 + \frac{1}{0.2} (33.98 - 0.2718 \times 1.699) \times 0.01 = 3.375 \text{ r/s}$$

(b) As  $t \rightarrow \infty$  (no load)  $\omega \rightarrow \frac{33.98}{0.2718} = 125 \text{ r/s}$