

Q1. (30 points):

A balanced, 3-phase, 60 HZ, 3-wire, impedance load is served by a balanced, 3-phase, 3-wire, ABC sequence source. A voltmeter between two lines reads 275 Volts. An ammeter in one line reads 13 Amps. A wattmeter connected to read the power "into" the A-B lines reads 1650 Watts.

- Find the power factor of the load.
- Find the total 3-phase real power absorbed by the load.
- A capacitor bank is used to correct the load power factor to unity. Compute the power readings in the two wattmeter method.
- Draw a schematic showing how a wattmeter can be used to 'measure' the reactive power consumed by the balanced 3-phase load, with appropriate polarity markings on the voltage and current measurements.

12 a. $V_{LL} = 275V$
 $I_L = 13A$

$$P_1 = V_{LL} I_L \cos(\theta + 30^\circ) = 1650$$

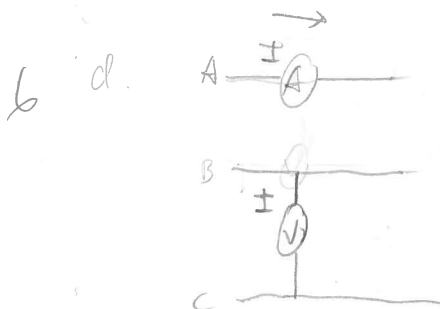
$$\cos(\theta + 30^\circ) = \frac{1650}{275 \times 13} = 0.4615 \Rightarrow \theta + 30^\circ = 62.51^\circ$$

$$\theta = 32.51^\circ$$

$$PF = \cos(\theta) = \boxed{0.8433}$$

b. $P_{3\phi} = \sqrt{3} V_{LL} I_L \cos(\theta) = \sqrt{3} \times 275 \times 13 \times 0.8433$
 $= \boxed{5222 W}$

c. $\theta = 0$. $P_1 = P_2 = V_{LL} I_L \cos(30^\circ) = \frac{P_{3\phi}}{2} = \boxed{2611 W}$



$$Q_{3\phi} = \sqrt{3} P_{wrm}$$

3/6

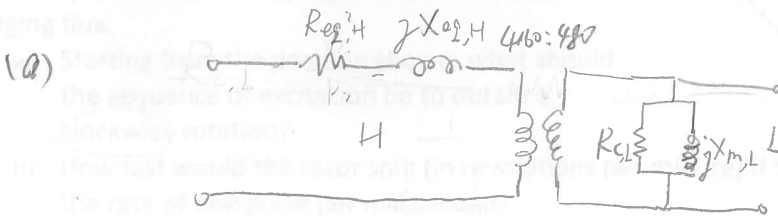
Q2. (35 points):

The following test results were found for a single-phase, 60 HZ, 30 KVA transformer with voltage ratings 4160/480 Volts:

Open-circuit test: $V_L = 480$ V, $I_L = 4$ A, $P_2 = 380$ W

Short-circuit test: $V_H = 142$ V, $I_H = 7.2$ A, $P_1 = 440$ W

- Compute all the parameters of the approximate equivalent circuit with the shunt elements moved directly across the source.
- Draw the approximate equivalent circuit and label all impedances with per unit values.
- Find the high side voltage when the transformer is delivering rated kVA at 0.87 lagging power factor to a load on the low voltage side with a 480V across the load.



$$R_{c,L} = \frac{V_L^2}{P_2} = 606.3 \Omega \quad Q_2 = \sqrt{V_L^2 I_L^2 - P_2^2} = \sqrt{(480 \times 4)^2 - 380^2} = 1882 \text{ Var} \quad X_{m,L} = \frac{V_L^2}{Q_2} = 1224 \Omega$$

$$R_{c,H} = \left(\frac{4160}{480}\right)^2 R_{c,L} = 8.667^2 R_{c,L} = 45540 \Omega \quad X_{m,H} = \left(\frac{4160}{480}\right)^2 X_{m,L} = 9193.6 \Omega$$

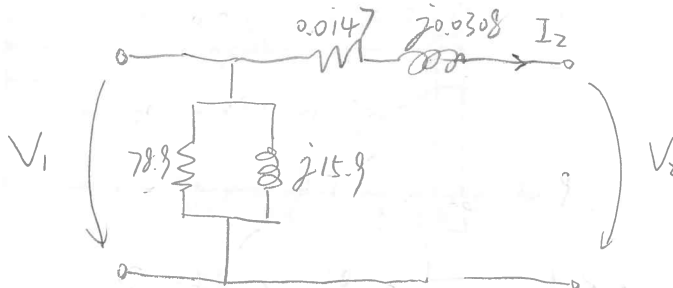
$$R_{eq,H} = \frac{P_1}{I_H^2} = 8.488 \Omega \quad Q_1 = \sqrt{(V_H I_H)^2 - P_1^2} = 922.9 \text{ Var} \quad X_{eq,H} = \frac{Q_1}{I_H^2} = 17.80 \Omega$$

(b)

$$Z_{H,base} = \frac{V_{rated,H}^2}{S_{rated}} = \frac{4160^2}{30 \times 10^3} = 576.85 \Omega$$

$$R_{c,pu} = \frac{R_{c,H}}{Z_{H,base}} = 78.9 \quad X_{m,pu} = \frac{X_{m,H}}{Z_{H,base}} = 15.9$$

$$R_{eq,pu} = \frac{R_{eq,H}}{Z_{H,base}} = 0.0147 \quad X_{eq,pu} = \frac{X_{eq,H}}{Z_{H,base}} = 0.0308$$



(c)

$$\bar{V}_{2,pu} = 1.0 \angle 0^\circ \quad \theta = \arccos(0.87) = 29.54^\circ \quad |\bar{I}_{2,pu}| = \frac{|S_{2,pu}|}{|\bar{V}_{2,pu}|} = \frac{1.0}{1.0} = 1.0$$

$$\bar{I}_{2,pu} = 1.0 \angle -\theta = 1.0 \angle -29.54^\circ = 0.87 - j0.493$$

$$\bar{V}_{1,pu} = \bar{V}_{2,pu} + (R_{eq,pu} + jX_{eq,pu}) \cdot \bar{I}_{2,pu} = 1 + (0.0147 + j0.0308)(0.87 - j0.493)$$

$$= 1.02797 + j0.01955 = 1.0282 \angle 1.089^\circ \quad |\bar{V}_1| = 1.0282 \times 4160 = 4277 \text{ V}$$

Q4. (35 points)

A reluctance machine with a 6/4 configuration has the following parameters.

Rotor outer radius = 6 cm

Air gap, $g = 1\text{ mm}$

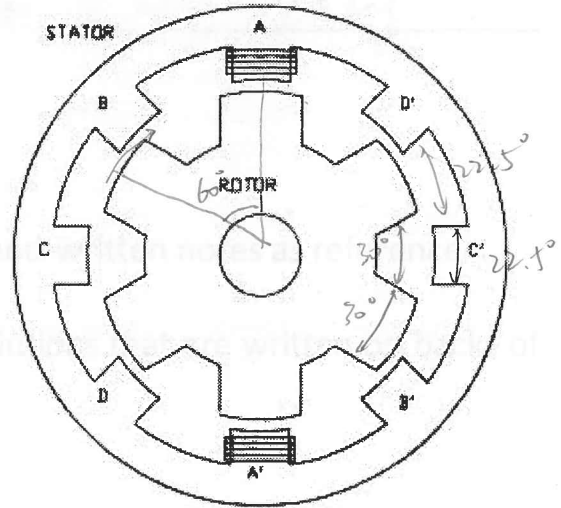
Rotor pole angle = $\pi/6$ radians

stator pole angle = $\pi/8$ radians

Axial length = 10 cm

Number of total turns per phase = 40

Assume rotor and stator cores have extremely high permeability. Assume infinite reluctance when there is no stator/rotor pole overlap. Ignore saturation and fringing flux.

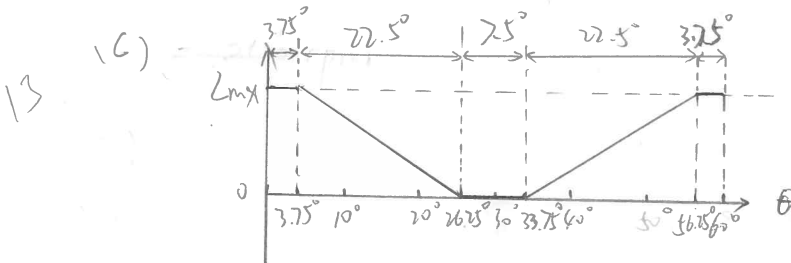


- Starting from the position shown, what should the sequence of excitation be to obtain a clockwise rotation?
- How fast would the rotor spin (in revolutions per minute) if single phase excitation is applied at the rate of one pulse per millisecond?
- Plot the phase-A inductance as a function of rotor position θ , as the rotor is rotated clockwise from $\theta=0$ to $\theta=60$ degrees.
- Plot the torque as the rotor is rotated clockwise from $\theta=0$ to $\theta=60$ degrees with Phase A current = 1A and all other currents set to zero.

(a) $A \rightarrow B \rightarrow C \rightarrow D$

(b) $1 \text{ pulse/ms} = 1 \text{ step/ms} \Rightarrow f_s = 1000 \text{ steps/sec}$
 $S = mNr = 6 \times 4 = 24 \text{ steps/rev}$

$$n = \frac{60 f_s}{S} = 2500 \text{ rpm}$$

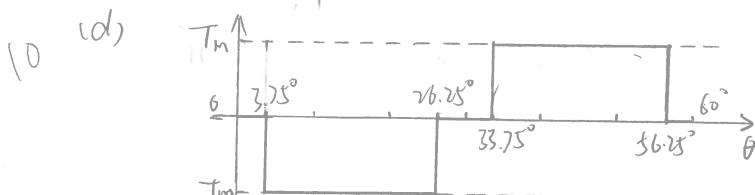


$$\frac{30 - 22.5}{2} = 3.75^\circ$$

$$R = 0.06 \text{ m}, \alpha = \frac{\pi}{8}, D = 0.10 \text{ m}, N_{ph} = 40$$

$$\text{reluctance } R_g = \frac{2g}{\mu_0 (\alpha R D)}$$

$$L_{max} = \frac{N_{ph}^2}{R_g} = \frac{\mu_0 \alpha R D N_{ph}^2}{2g} = \frac{1.2566 \times 10^{-6} \times \frac{\pi}{8} \times 0.06 \times 0.10 \times 40^2}{2 \times 1 \times 10^{-3}} = 2.369 \text{ mH}$$



$$T_m = \frac{2 W_m'}{2\theta} = \frac{1}{2} I^2 \frac{L_{max}}{\alpha} = \frac{1}{2} \times 1^2 \times \frac{2.369 \times 10^{-3}}{\frac{\pi}{8}} = 3.016 \times 10^{-3} \text{ Nm}$$