While we wait....

• A process initiates Bully algorithm after detecting the leader’s failure.

• What is the worst-case turn-around time?
  • Assuming no other node fails.
  • Assume timeout is computed using the knowledge of one-way message latency (T)
Today’s agenda

• **Wrap up leader election**
  - Chapter 15.3

• **Consensus**
Recap: Leader Election

- In a group of processes, elect a *Leader* to undertake special tasks
  - *Let everyone know* in the group about this Leader.

- Safety condition:
  - During the run of an election, a correct process has either not yet elected a leader, or has elected process with best attributes.

- Liveness condition:
  - Election run terminates and each process eventually elects someone.

- Two classical algorithms:
  - Ring-based algorithm
  - Bully algorithm

- Difficulty of ensure both safety and liveness in an asynchronous system under failures.
Recap: Leader Election

- In a group of processes, elect a Leader to undertake special tasks
  - *Let everyone know* in the group about this Leader.
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  - Election run terminates and each process eventually elects someone.
- Two classical algorithms:
  - Ring-based algorithm
  - **Bully algorithm**
- Difficulty of ensure both safety and liveness in an asynchronous system under failures.
Bully Algorithm

• When a process wants to initiate an election
  • if it knows its id is the highest
    • it elects itself as coordinator, then sends a Coordinator message to all processes with lower identifiers. Election is completed.
  • else
    • it initiates an election by sending an Election message
    • (contd.)
Bully Algorithm (2)

• **else** it initiates an election by sending an *Election* message
  • Sends it to only processes that have a higher id than itself.
  • **if** receives no answer within timeout, calls itself leader and sends *Coordinator* message to all lower id processes. Election completed.
  • **if** an answer received however, then there is some non-faulty higher process => so, wait for coordinator message. If none received after another timeout, start a new election run.

• A process that receives an *Election* message replies with *disagree* message, and starts its own leader election protocol (unless it has already done so).
Bully Algorithm (2)

• **else** it initiates an election by sending an *Election* message
  • Sends it to only processes that have a *higher id than itself*.
  • **if** receives no answer within *timeout*, calls itself leader and sends *Coordinator* message to all lower id processes. Election completed.
  • **if** an answer received however, then there is some non-faulty higher process => so, wait for coordinator message. If none received after another *timeout*, start a new election run.

• A process that receives an *Election* message replies with *disagree* message, and starts its own leader election protocol (unless it has already done so).
Timeout values

• Assume the one-way message transmission time (T) is known.

• First timeout value (when the process that has initiated election waits for the first response)
  • Must be set as accurately as possible.
    • If it is too small, a lower id process can declare itself to be the coordinator even when a higher id process is alive.
  • What should be the first timeout value be, given the above assumption?
    • $2T + \text{(processing time)} \approx 2T$

• When the second timeout happens (after ‘disagree’ message), election is re-started.
  • A very small value will lead to extra “Election” messages.
  • A suitable option is to use the worst-case turnaround time.
Performance Analysis

• Best-case
  • Second-highest id detects leader failure
    • Highest remaining id initiates election.
  • Sends (N-2) Coordinator messages
  • Turnaround time: 1 message transmission time (T)

• Worst-case: For simplicity, assume no failures after a process calls for election.
  • if any lower id process detects failure and starts election.
  • Turnaround time: 4 message transmission times (4T)
Bully Algorithm: Example

P2 initiates election after detecting P5’s failure.

1. P2 initiates election

2. P2 receives "replies"

3. P3 & P4 initiate election

4. P3 receives reply

5. P4 receives no reply

P4 waits for $T$ more time after P2 receives its "disagree" message.

5. P4 announces itself
Analysis

• Best-case
  • Second-highest id detects leader failure
    • Highest remaining id initiates election.
  • Sends \((N-2)\) Coordinator messages
  • Turnaround time: 1 message transmission time

• Worst-case: For simplicity, assume no failures after a process calls for election.
  • Turnaround time: 4 message transmission times
    • if any lower id process detects failure and starts election.
      • \(\text{Election} + (\text{disagree} \& \text{Election}) + (\text{Timeout} - T) + \text{Coordinator}\)
  • When the process with the lowest id in the system detects failure.
    • \((N-1)\) processes altogether begin elections, each sending messages to processes with higher ids.
    • \(i\)-th highest id process sends \((i-1)\) election messages
    • Number of Election messages
      \[
      = N-1 + N-2 + \ldots + 1 = (N-1) \cdot \frac{N}{2} = O(N^2)
      \]
Correctness

• In synchronous system model:
  • Set timeout accurately using known bounds on network delays and processing times.
  • Satisfies safety and liveness.

• In asynchronous system model:
  • Failure detectors cannot be both accurate and complete.
  • Either liveness and safety is violated.
Why is Election so hard?

• Because it is related to the consensus problem!

• If we could solve election, then we could solve consensus!
  • Elect a process, use its id’s last bit as the consensus decision.

• But (as we will soon see) consensus is impossible in asynchronous systems, so is election!
Today’s agenda

- Wrap up leader election
  - Chapter 15.3

- Consensus

- Goals:
  - Understand the problem of consensus
  - How to achieve consensus in a synchronous system
  - Difficulty of achieving consensus in an asynchronous system
  - Good-enough consensus algorithms for asynchronous systems
Agenda for the next 2 weeks

• Consensus
  • Consensus in synchronous systems
    • Chapter 15.4
  • Impossibility of consensus in asynchronous systems
    • We will not cover the proof in details
  • Good enough consensus algorithm for asynchronous systems:
    • Paxos made simple, Leslie Lamport, 2001
  • Other forms of consensus algorithm
    • Raft (log-based consensus)
    • Block-chains (distributed consensus)
Agenda for today

• **Consensus**
  • Consensus in synchronous systems
    • *Chapter 15.4*
  • Impossibility of consensus in asynchronous systems
    • *We will not cover the proof in details*
  • A good enough consensus algorithm for asynchronous systems:
    • *Paxos made simple, Leslie Lamport, 2001*
• Other forms of consensus
  • Blockchains
  • Raft (log-based consensus)
Consensus

• Each process proposes a value.

• All processes must agree on one of the proposed values.

• Examples:
  • The generals must agree on the time of attack.
  • An object replicated across multiple servers in a distributed data store.
    • All servers must agree on the current version of the object.
  • Transaction processing on replicated servers
    • Must agree on the order in which updates are applied to an object.
  • …
Consensus

• Each process **proposes** a value.
• All processes must **agree** on one of the proposed values.
• The final value can be decided based on any criteria:
  • Pick minimum of all proposed values.
  • Pick maximum of all proposed values.
  • Pick the majority (with some deterministic tie-breaking rule).
  • Pick the value proposed by the *leader*.
    • *All processes must agree on who the leader is.*
  • If reliable total-order can be achieved, pick the proposed value that gets delivered first.
    • *All process must agree on the total order.*
• ……
Consensus Problem

• System of N processes \((P_1, P_2, \ldots, P_n)\)

• Each process \(P_i\):
  • begins in an *undecided* state.
  • proposes value \(v_i\).
  • at some point during the run of a consensus algorithm, sets a decision variable \(d_i\) and enters the *decided* state.
Required Properties

• **Termination**: Eventually each process sets its decision variable.

• **Agreement**: The decision value of all correct processes is the same.
  - If $P_i$ and $P_j$ are correct and have entered the *decided* state, then $d_i = d_j$.

• **Integrity**: If the correct processes all proposed the same value, then any correct process in the decided state has chosen that value.
  - *Specific definition of integrity may vary across sources and systems.*
  - *Safeguard against algorithms that decide on a fixed constant value.*
Required Properties

• **Termination:** Eventually each process sets its decision variable.

• **Agreement:** The decision value of all correct processes is the same.
  - If $P_i$ and $P_j$ are correct and have entered the *decided* state, then $d_i = d_j$.

• **Integrity:** If the correct processes all proposed the same value, then any correct process in the decided state has chosen that value.

Which of these properties is liveness and which is safety?
Required Properties

• **Termination:** Eventually each process sets its decision variable.
  • *Liveness*

• **Agreement:** The decision value of all correct processes is the same.
  • If $P_i$ and $P_j$ are correct and have entered the *decided* state, then $d_i = d_j$.
  • *Safety*

• **Integrity:** If the correct processes all proposed the same value, then any correct process in the decided state has chosen that value.
How do we agree on a value?

• Ring-based leader election
  • Send proposed value along with elected message.
  • Turnaround time: 3NT worst case and 2NT best case (without failures).
    • $T$ is the time taken to transmit a message on a channel.
  • $O(Nft)$ if up to $f$ processes fail during the election run.
  • Can we do better?

• Bully algorithm
  • Send proposed value along with the coordinator message.
  • Turnaround time: $4T$ in the worst case without failures.
  • More than $2fT$ if up to $f$ processes fail during the election run.

What's the best we can do?
Consider the simplest algorithm

• Let’s assume the system is synchronous.

• Use a simple B-multicast:
  • All processes B-multicast their proposed value to all other processes.
  • Upon receiving all proposed values, pick the minimum.

• Time taken under no failures?
  • One message transmission time (T)

• What can go wrong?
  • If we consider process failures, is a simple B-multicast enough?
B-multicast is not enough for this

\[ \{v_1, v_2, v_3, v_5\} \]

\[ \{v_1, v_2, v_3, v_4, v_5\} \]

Need R-multicast
B-multicast is not enough for this

Need R-multicast
B-multicast is not enough for this

Need R-multicast
Handling failures

- P4 fails before sending $v_4$ to anyone.
- What should other processes do?
- Detect failure. **Timeout!**
- Assume proposals are sent at time ‘s’.
- Worst-case skew is $\epsilon$.
- Maximum message transfer time (including local processing) is $T$.
- What should the timeout value be?
Handling failures

- Assume proposals are sent at time ‘s’.
- Worst-case skew is $\epsilon$.
- Maximum message transfer time (including local processing) is $T$.
- What should the timeout value be?
- Option 1: $\epsilon + T$
  - Pi waits for $(\epsilon + T)$ time units after sending its proposal at time ‘s’.
  - Any other process must have sent proposed value before $s + \epsilon$.
  - The proposed value should have reached Pi by $(s + \epsilon + T)$.
- Will this work?
Handling failures

• Assume proposals are sent at time ‘s’.
• Worst-case skew is $\epsilon$.
• Maximum message transfer time (including local processing) is T.
• What should the timeout value be?
• How about $\epsilon + T$?

- Local time at a process $P_i$.
- $P_j$ must have sent proposed value before time $s + \epsilon$.
- The proposed value should have reached $P_i$ by $(s + \epsilon + T)$.
- Will this work?
Handling failures

• Assume proposals are sent at time ‘s’.
• Worst-case skew is $\epsilon$.
• Maximum message transfer time (including local processing) is $T$.
• What should the timeout value be?
• How about $\epsilon + 2T$?
  • Will this work?
Handling failures

- Assume proposals are sent at time ‘s’.
- Worst-case skew is $\epsilon$.
- Maximum message transfer time (including local processing) is $T$.
- What should the timeout value be?
- How about $\epsilon + 2*T$?
  - Will this work?
Handling failures

- Assume proposals are sent at time \('s'\).
- Worst-case skew is \(\epsilon\).
- Maximum message transfer time (including local processing) is \(T\).
- What should the timeout value be?
- How about \(\epsilon + 3*T\)?
  - Will this work?
Handling failures

- Assume proposals are sent at time ‘s’.
- Worst-case skew is $\epsilon$.
- Maximum message transfer time (including local processing) is $T$.
- What should the timeout value be?
- How about $\epsilon + 3T$?
  - Will this work?
Handling failures

• Assume proposals are sent at time ‘s’.
• Worst-case skew is $\epsilon$.
• Maximum message transfer time (including local processing) is $T$.
• What should the timeout value be?
• Timeout = $\epsilon + (f+1)T$ for up to $f$ failed process.

Also holds for R-multicast from a single sender.
Round-based algorithm

- For a system with at most f processes crashing
  - All processes are synchronized and operate in “rounds” of time.
    - One round of time is equivalent to $\epsilon + T$ units.
    - At each process, the $i^{th}$ round
      - starts at local time $s + (i - 1)(\epsilon + T)$
      - ends at local time $s + i(\epsilon + T)$
    - The start or end time of a round in two different processes differs by at most $\epsilon$.
  - The algorithm proceeds in $f+1$ rounds.
  - Assume communication channels are reliable.
Round-based algorithm

Values\(^r_i\): the set of proposed values known to \(P_i\) at the beginning of round \(r\).

Initially Values\(^1_i\) = \(\{v_i\}\)

for round = 1 to \(f+1\) do

    B-multicast (Values\(^r_i\) – Values\(^{r-1}_i\))

    // iterate through processes, send each a message

    Values\(^{r+1}_i\) \(\leftarrow\) Values\(^r_i\)

    wait until one round of time expires.

for each \(v_j\) received in this round

    Values\(^{r+1}_i\) = Values\(^{r+1}_i\) \(\cup\) \(v_j\)

end

end

d_i = \text{minimum}(\text{Values \(^{f+2}_i\)})
Why does this work?

- After \( f + 1 \) rounds, all non-faulty processes would have received the same set of values.

- *Proof by contradiction.*

- Assume that two non-faulty processes, say \( P_i \) and \( P_j \), differ in their final set of values (i.e., after \( f + 1 \) rounds)

- Assume that \( P_i \) possesses a value \( v \) that \( P_j \) does not possess.
  - \( P_i \) must have received \( v \) in the *very last* round, else \( p_i \) would have sent \( v \) to \( p_j \) in that last round
  - So, in the last round: a third process, \( P_k \), must have sent \( v \) to \( P_i \), but then crashed before sending \( v \) to \( P_j \).
  - Similarly, a fourth process sending \( v \) in the *last-but-one* round must have crashed; otherwise, both \( P_k \) and \( P_j \) should have received \( v \).
  - Implies at least one (unique) crash in each of the preceding rounds.
  - This means a total of \( f + 1 \) crashes, contradicts our assumption of up to \( f \) crashes.
Consensus in synchronous systems

Dolev and Strong proved that for a system with up to $f$ failures (or faulty processes), at least $f+1$ rounds of information exchange is required to reach an agreement.
What about asynchronous systems?

- Using time-based “rounds” or timeouts may not work.
- Cannot guarantee both completeness and accuracy for failure detection.
  - Cannot differentiate between an extremely slow process and a failed process.
- Key intuition behind the famous FLP result on the impossibility of consensus in asynchronous systems.
  - *Impossibility of Distributed Consensus with One Faulty Process, Fischer-Lynch-Paterson (FLP), 1985*
- Stopped many distributed system designers dead in their tracks.
- A lot of claims of “reliability” vanished overnight.
- *(Proof is not in your syllabus – optional self-study)*
What about asynchronous systems?

- We cannot “solve” consensus in asynchronous systems.
  - We cannot meet both safety and liveness requirements.
  - Maybe it is ok to guarantee just one requirement.

- Option 1:
  - Let’s set super conservative timeout for a terminating algorithm.
  - Safety violated if a process (or the network) is very, very slow.

- Option 2:
  - Let’s focus on guaranteeing safety under all possible scenarios.
  - If the real situation is not too dire, hopefully the algorithm will terminate.
Paxos Consensus Algorithm

- Paxos algorithm for consensus in asynchronous systems.
  - Most popular consensus-algorithm.
  - A lot of systems use it
    - Zookeeper (Yahoo!), Google Chubby, and many other companies.
  - Not guaranteed to terminate, but never violates safety.
Paxos Consensus Algorithm

• *Guess who invented it?*
  • Leslie Lamport!

• Original paper: The Part-time Parliament.
  • Used analogy of a “part-time parliament” on an ancient Greek island of Paxos.
  • No one understood it.
  • The paper was rejected.

• Published “*Paxos made simple*” 10 years later.
Paxos Algorithm

• Three types of roles:
  • **Proposers:** propose values to *acceptors*.
    • All or subset of processes.
    • Having a *single proposer* (leader) may allow faster termination.
  • **Acceptors:** accept proposed values (under certain conditions).
    • All or subset of processes.
  • **Learners:** learns the value that has been accepted by *majority* of acceptors.
    • All processes.
Paxos Algorithm: Try 1: Single Phase

- A proposer multicasts its proposed value to a large enough set (larger than majority) of acceptors.
- An acceptor accepts the first proposed value it receives.
- If majority of acceptors have accepted the same value v, then v is the decided value.
- *What can go wrong here?*
Paxos Algorithm: Try 1: Single phase

No decision reached!
Paxos Algorithm: Proposal numbers

• Allow an acceptor to accept multiple proposals.
  • Accepting is different from deciding.

• Distinguish proposals by assigning unique ids (a proposal number) to each proposal.
  • Configure a disjoint set of possible proposal numbers for different processes.
  • Proposal number is different from proposed value!

• A higher number proposal overwrites and pre-empts a lower number proposal.
Paxos Algorithm: Try 2: Proposal #s

What can go wrong here?
Paxos Algorithm: Try 2: Proposal #'s

When do we stop and decide on a value?

Proposers

Acceptors

Proposal #1
Value = 10

Proposal #2
Value = 20

Proposal #3
Value = 30

Accepts proposal #3

Accepts proposal #2

Accepts proposal #1

Accepts proposal #1
Paxos Algorithm

• Key condition:
  • When majority of acceptors accept a single proposal with a value \( v \), then that value \( v \) becomes the decided value.
    • This is an implicit decision. Learners may not know about it right-away.
  • Any higher-numbered proposal that gets accepted by majority of acceptors after the implicit decision must propose the same decided value.
Paxos Algorithm

Point of no return!
Any proposal accepted by majority of acceptors after this must propose the same value as proposal #1 (i.e. 10).
Paxos Algorithm: Two phases

• Phase 1:
  • A proposer selects a proposal number \( n \) and sends a prepare request with \( n \) to majority of acceptors, requesting:
    • Promise me you will not reply to any other proposal with a lower number.
    • Promise me you will not accept any other proposal with a lower number.
  • If an acceptor receives a prepare request for proposal \( \#n \), and it has not responded to a prepare request with a higher number, it replies back saying:
    • **OK!** I will make that promise for any request I receive in the future.
    • (If applicable) I have already accepted a value \( v \) from a proposal with lower number \( m < n \). The proposal has the highest number among the ones I accepted so far.
Paxos Algorithm: Two phases

• Phase 2:
  • If a proposer receives an OK response for its prepare request #n from a majority of acceptors, then it sends an accept request with a proposed value. What is the proposed value?
    • The value $v$ of the highest numbered proposal among the received responses.
    • Any value if no previously accepted value in the received responses.
  • If an acceptor receives an accept request for proposal #n, and it has not responded a prepare request with a higher number, it accepts the proposal.
Next Class

• Wrap up discussion on Paxos algorithm
  • Why it guarantees safety?
  • How do processes learn about the decided value.

• Raft: Log-based consensus
Summary

- Consensus is a fundamental problem in distributed systems.

- Possible to solve consensus in synchronous systems.
  - Algorithm based on time-synchronized rounds.
  - Need at least \((f+1)\) rounds to handle up to \(f\) failures.

- Impossible to solve consensus in asynchronous systems.
  - Cannot distinguish between a timeout and a very very slow process.
  - Paxos algorithm:
    - Guarantees safety but not liveness.
    - Hopes to terminate if under good enough conditions.