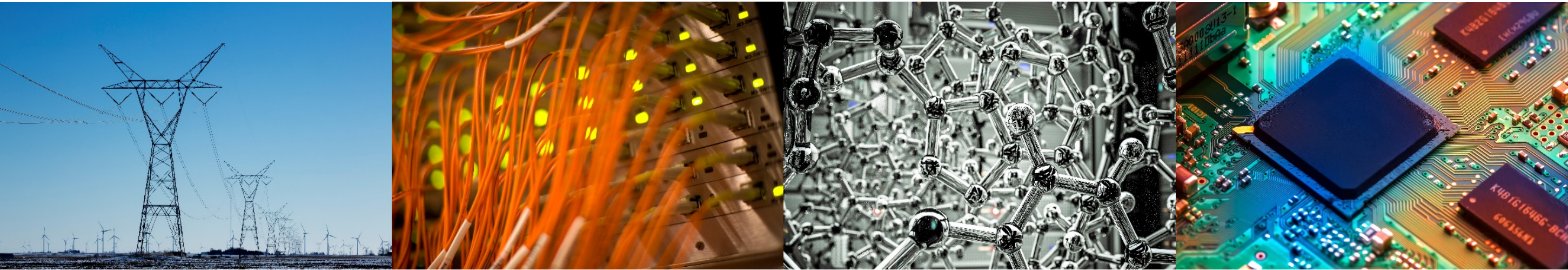


# FMCW Radar? Never Heard of it

Spencer Markowitz

The TA for most of you



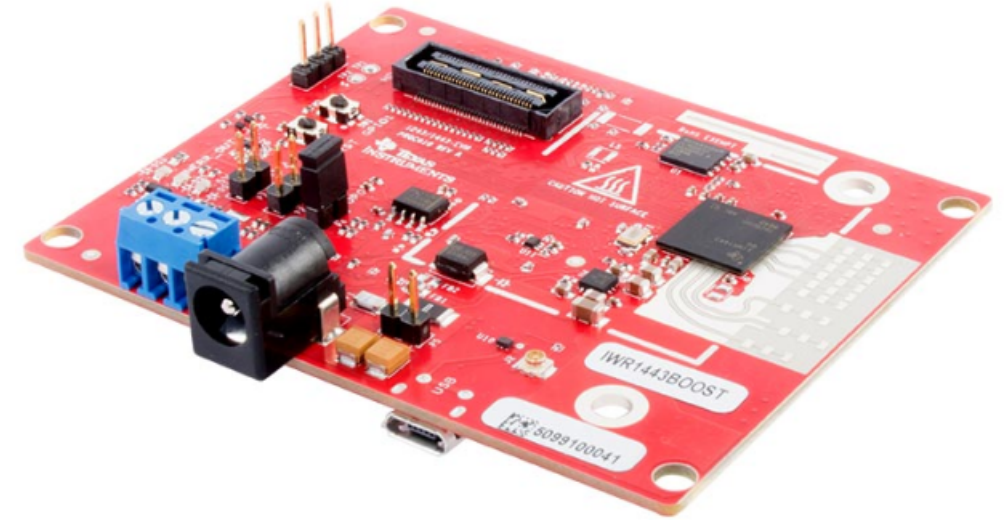
**I** ILLINOIS

Electrical & Computer Engineering

GRAINGER COLLEGE OF ENGINEERING

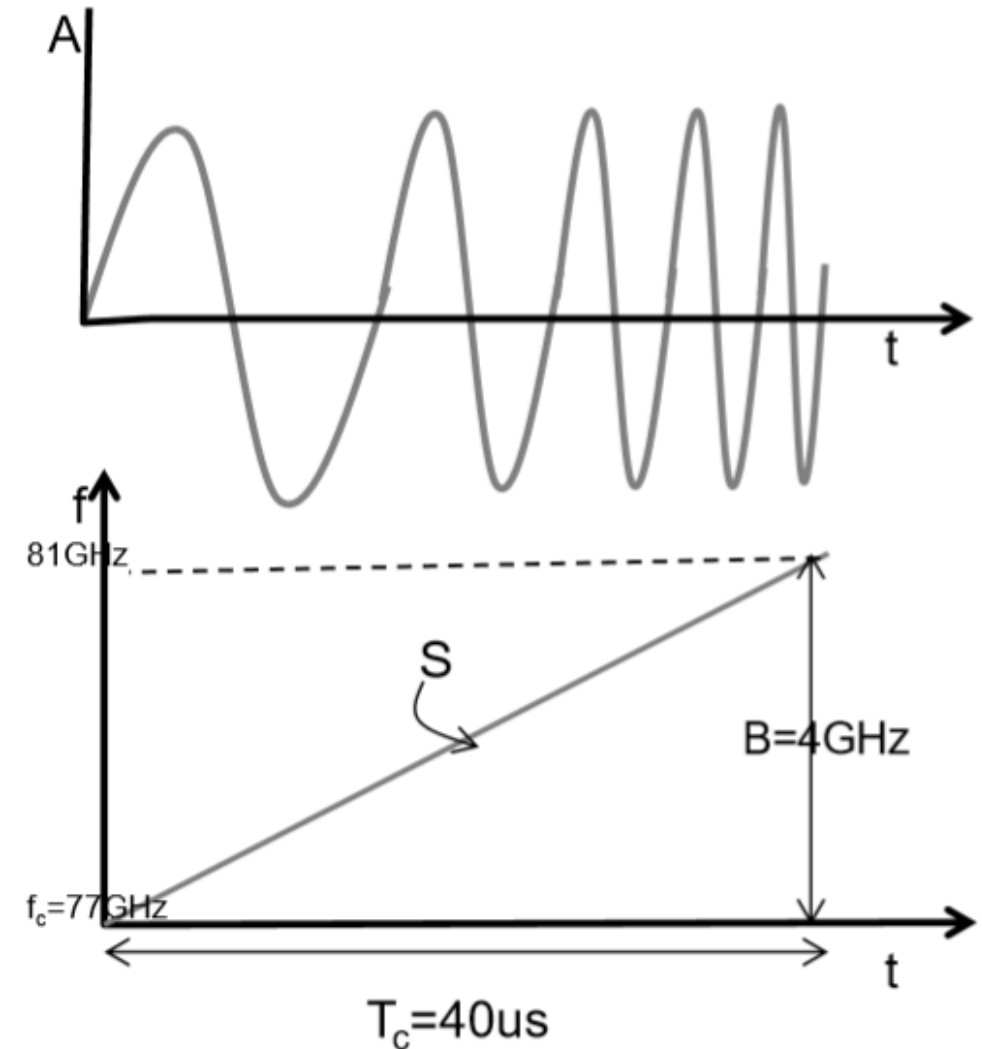
# Why aren't cameras enough?

- Low light conditions
- Occlusion
- Accurate velocity measurements
- Privacy



# Radars send chirps and listen for reflections.

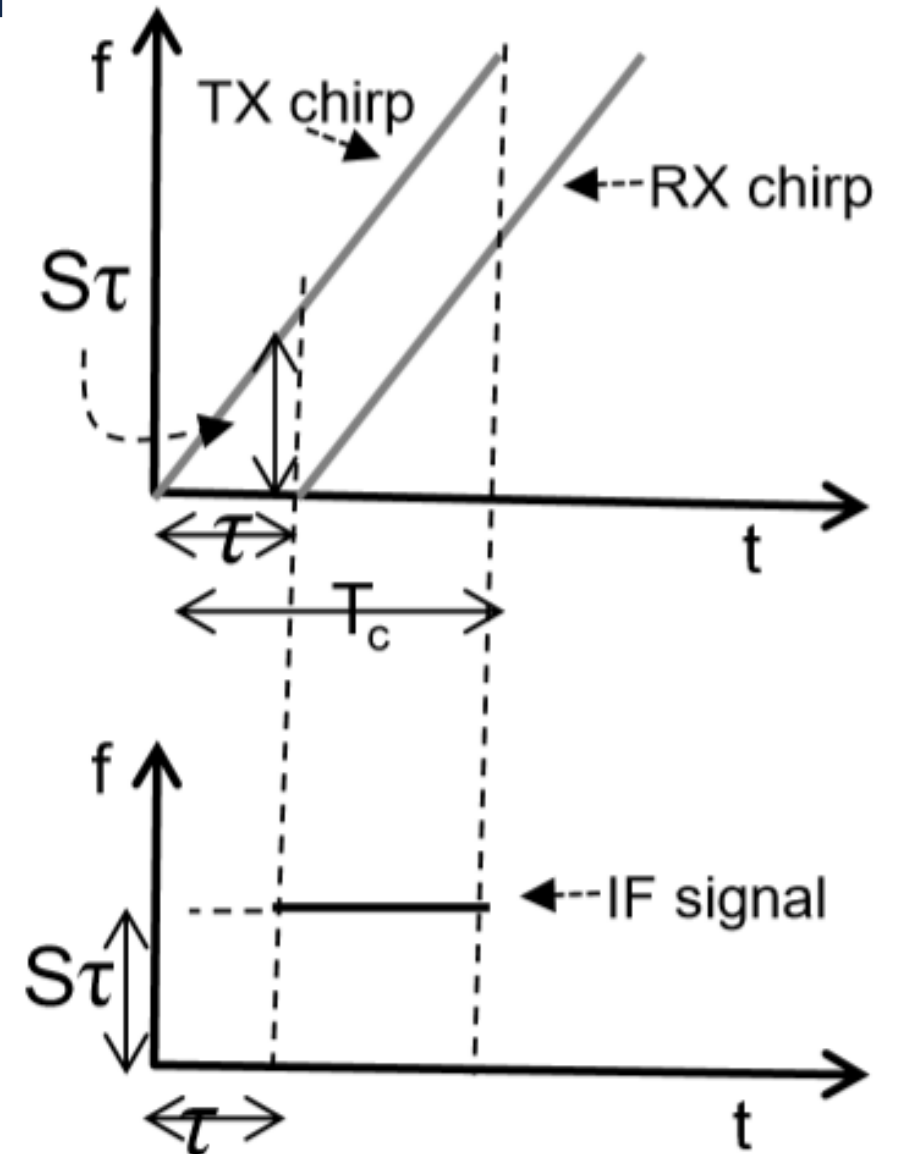
- The chirp's frequency increases linearly (our particular radar).
- That's where the "FM" comes from.
  1.  $S$  = slope
  2.  $B$  = bandwidth
  3.  $T_c$  = chirp period



# Getting the range from a reflection

- The reflected signal is just a time delayed ( $\tau$ ) version of the transmitted one.
- The difference in frequency is constant and a function of  $\tau$ .
- The frequency difference is

$$S\tau = \frac{S(2d)}{c}$$



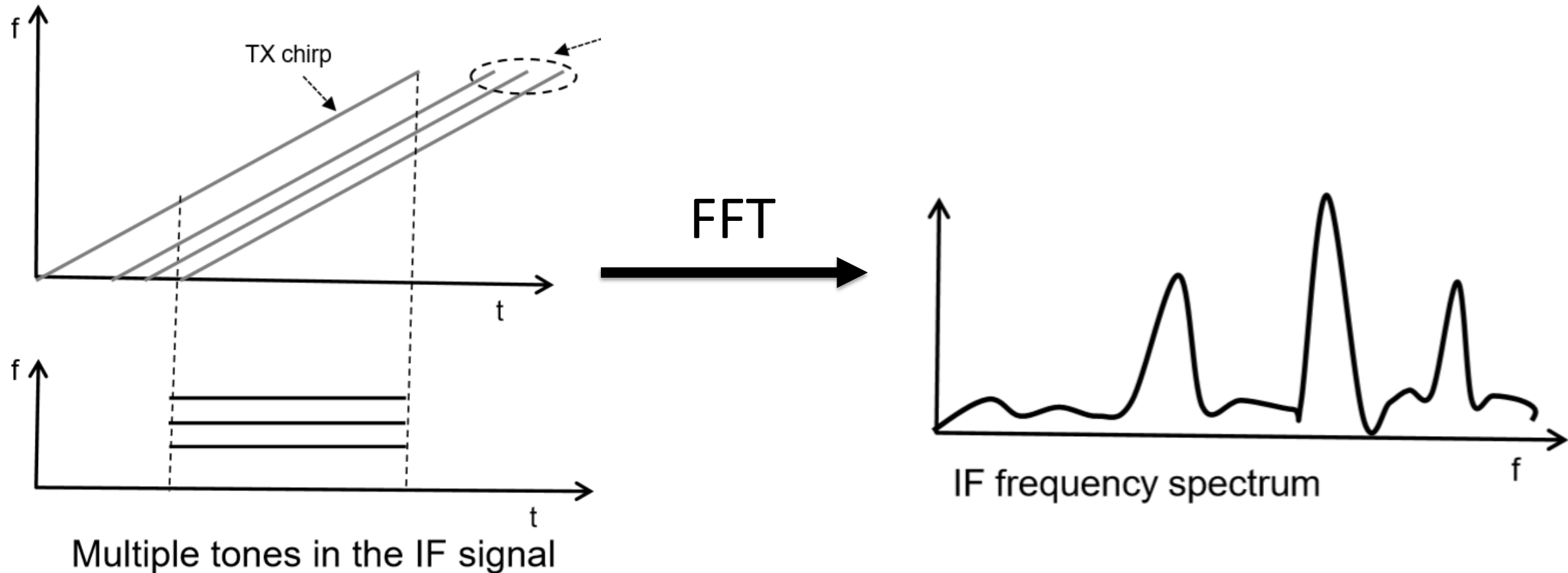
# How do we subtract frequencies again?

- Mixing signals outputs the sum/difference of the two frequencies.
- The difference is what we care about here.



Sir Mix-A-Lot


# Multiple objects gets us multiple reflections



# Remember Frequency resolution in audio?

For two objects separated by a distance  $\Delta d$ , the difference in their IF frequencies is given by  $\Delta f = \frac{S2\Delta d}{c}$

Since the observation interval is  $T_c$ , this means that

$$\Delta f > \frac{1}{T_c} \Rightarrow \frac{S2\Delta d}{c} > \frac{1}{T_c} \Rightarrow \Delta d > \frac{c}{2ST_c} \Rightarrow \frac{c}{2B} \quad (\text{since } B=ST_c)$$


The lowest detectable frequency must have one full period in the duration of a signal.

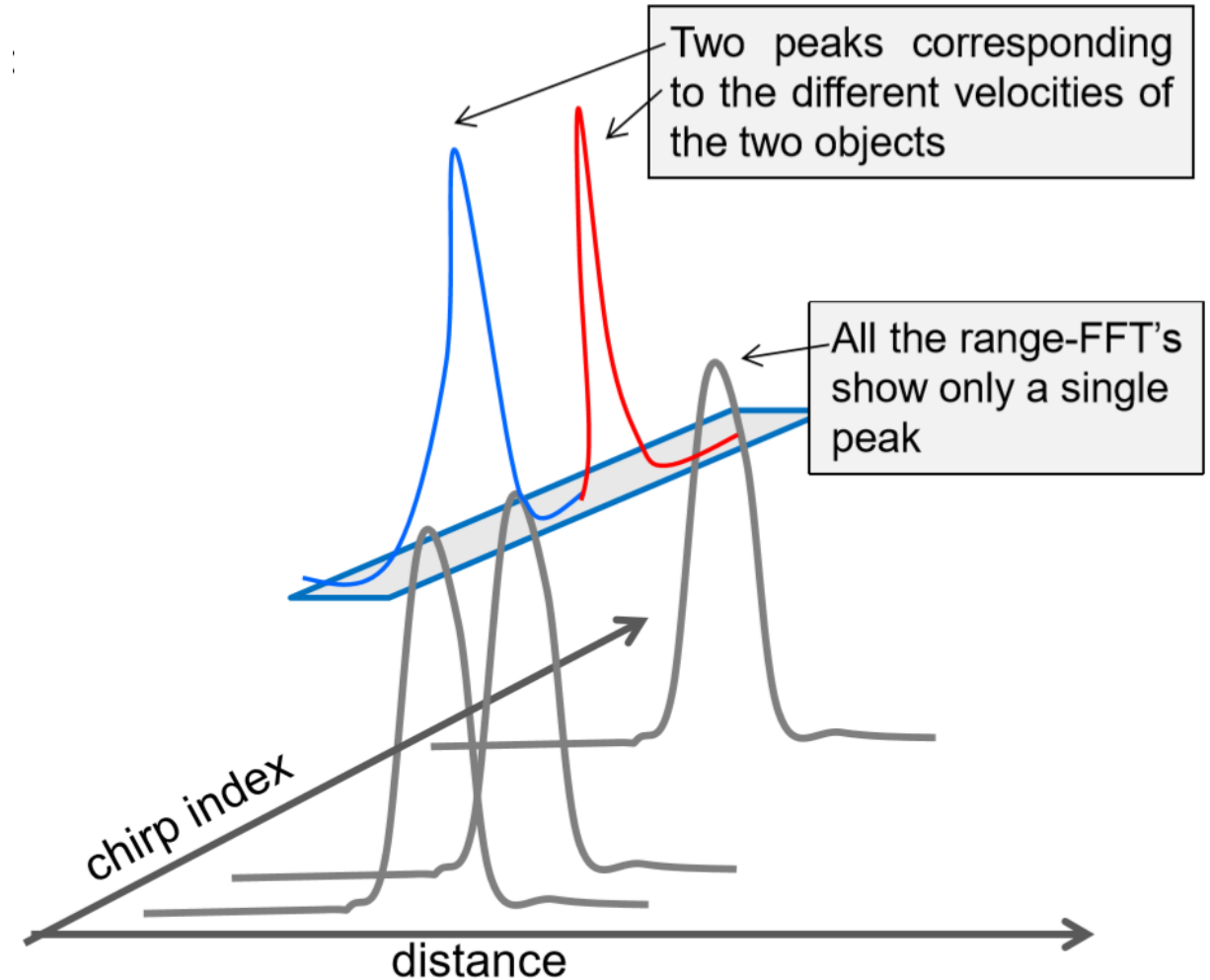
# Difference in range too small? Use the phase!

- Phase is much more responsive than the frequency to small changes in range.
- Let's say we want to measure velocity.
  - We send chirps at a very fast rate
  - Between each chirp, the magnitude peak will hardly move.
  - But the phase will!

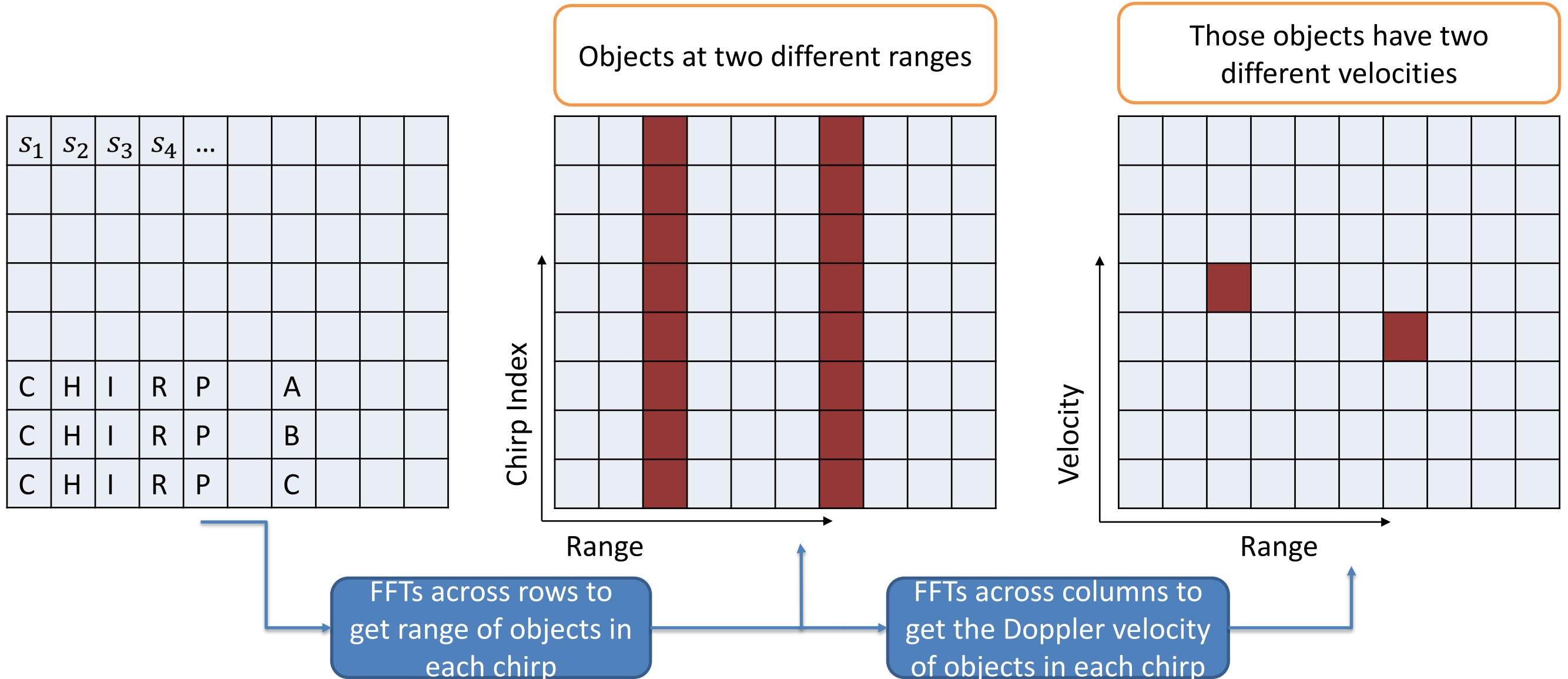


# Measuring velocity (Doppler)

- Send consecutive chirps (this includes time for sampling)
- Take the FFT across multiple chirps

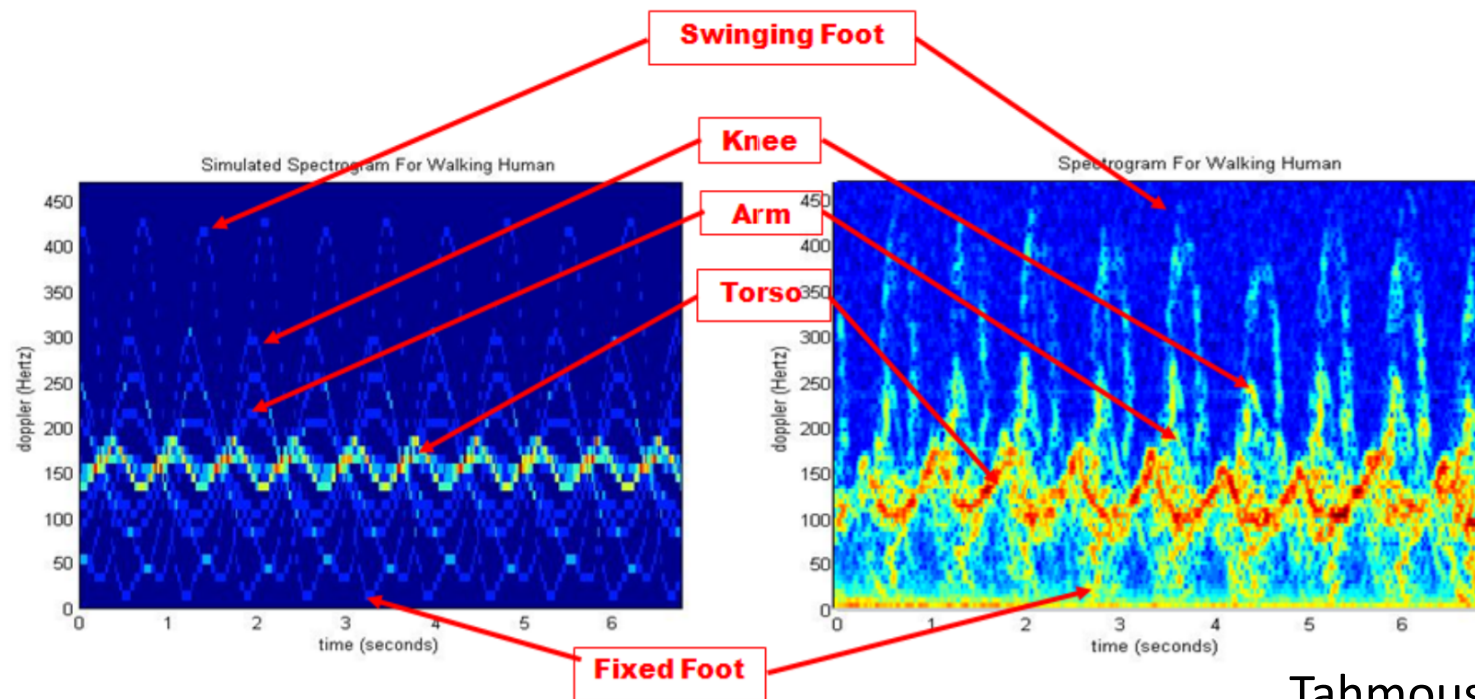


# Making this clearer with frames



# Doppler velocity for non-rigid objects

- A moving ball will have one velocity measurement
  - “That pitch was 98 mph and 5 mph and 72 mph and ...”
- Will a human have just one velocity measurement?

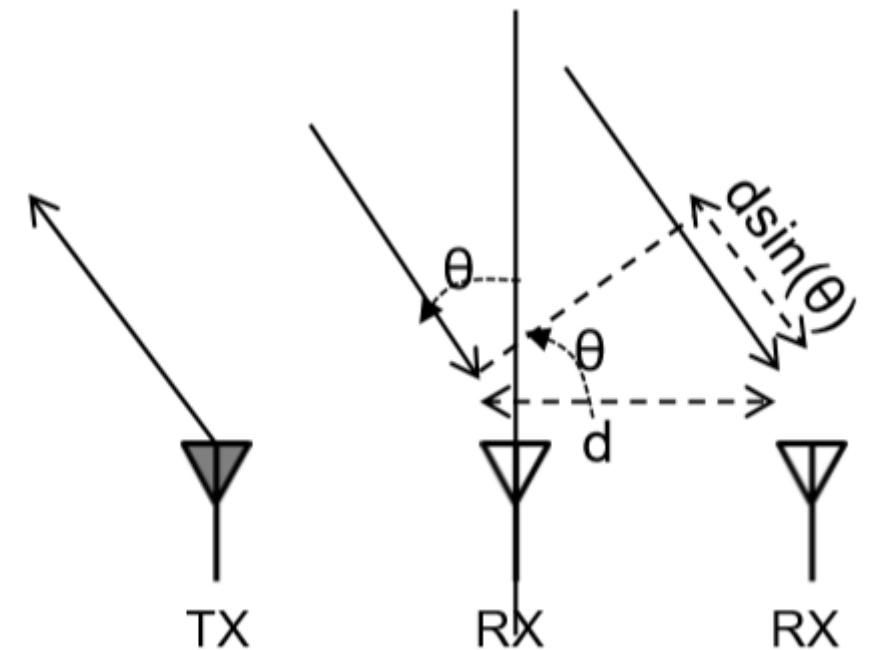
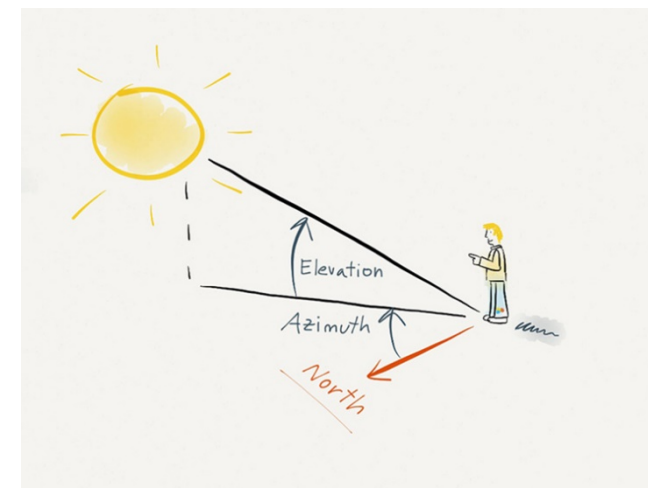


## Micro-Doppler

Tahmoush et al.

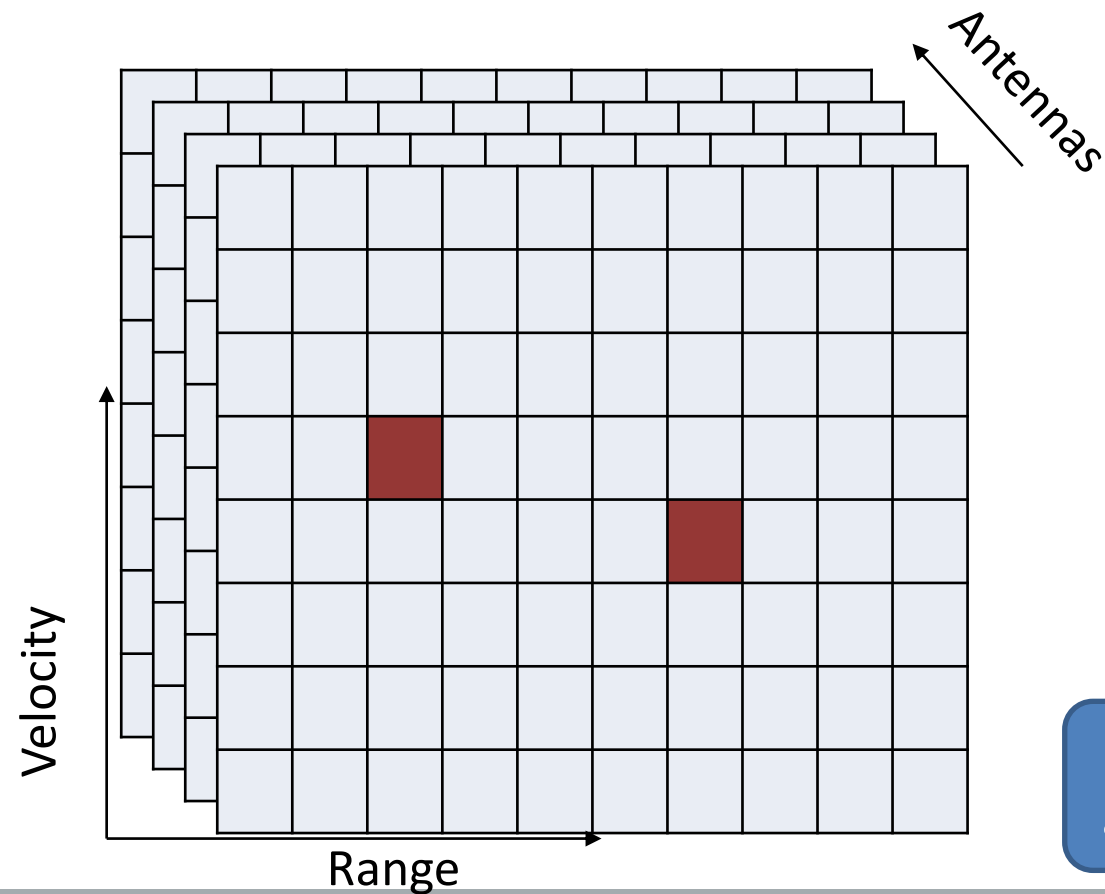
# Finding the angle of the target

- To get to the farther antenna, the signal travels more.
- This causes the phase to increase with each additional antenna.
- Take the FFT to find the rate of this change to get the angle.

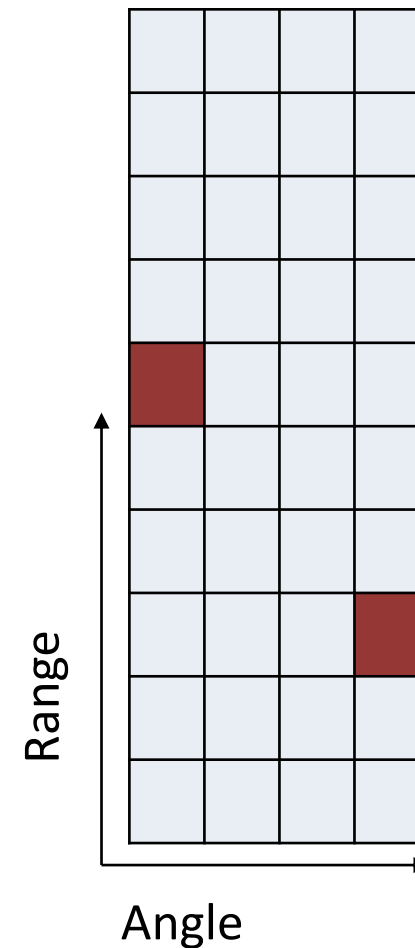


# Finding the angle

- Now assume we have a frame for each antenna
  - Last example was for one antenna

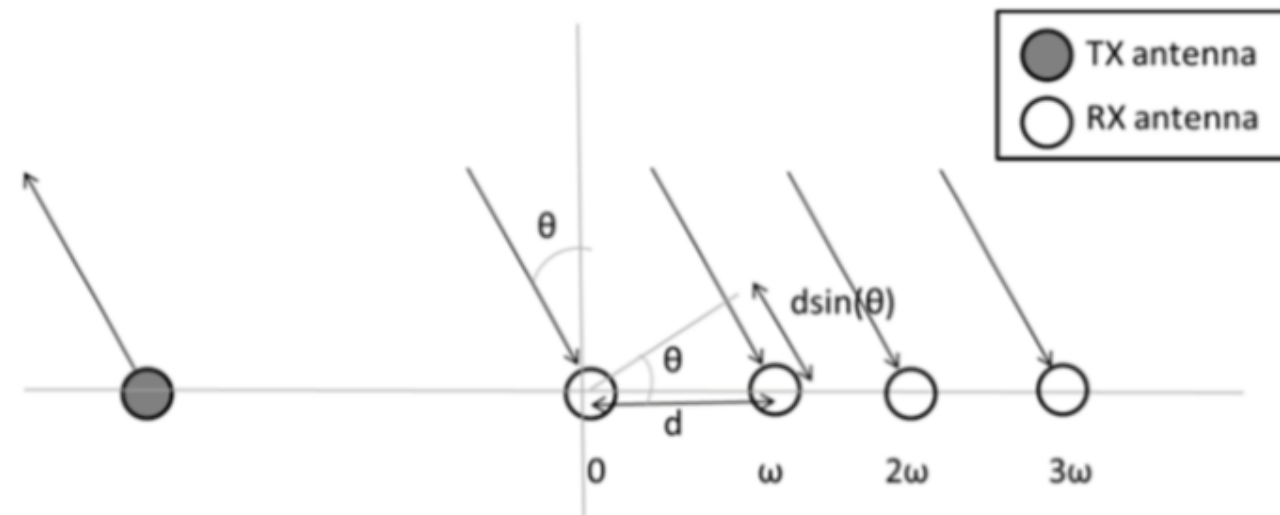


FFTs across the antennas to get angle



# More than one antenna

- More distance traveled => more phase accumulated



# 2x4 = 1x8? Obviously\*

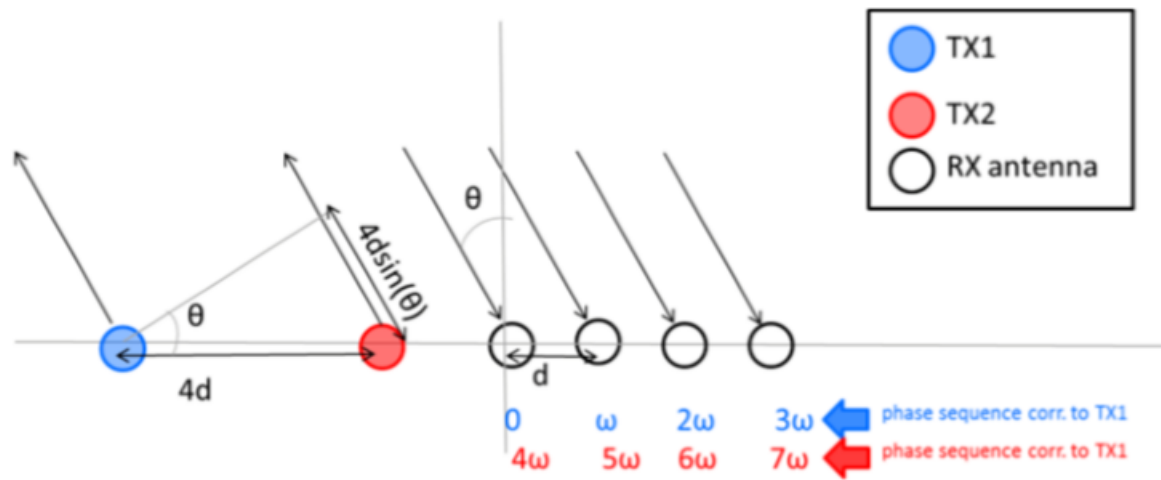
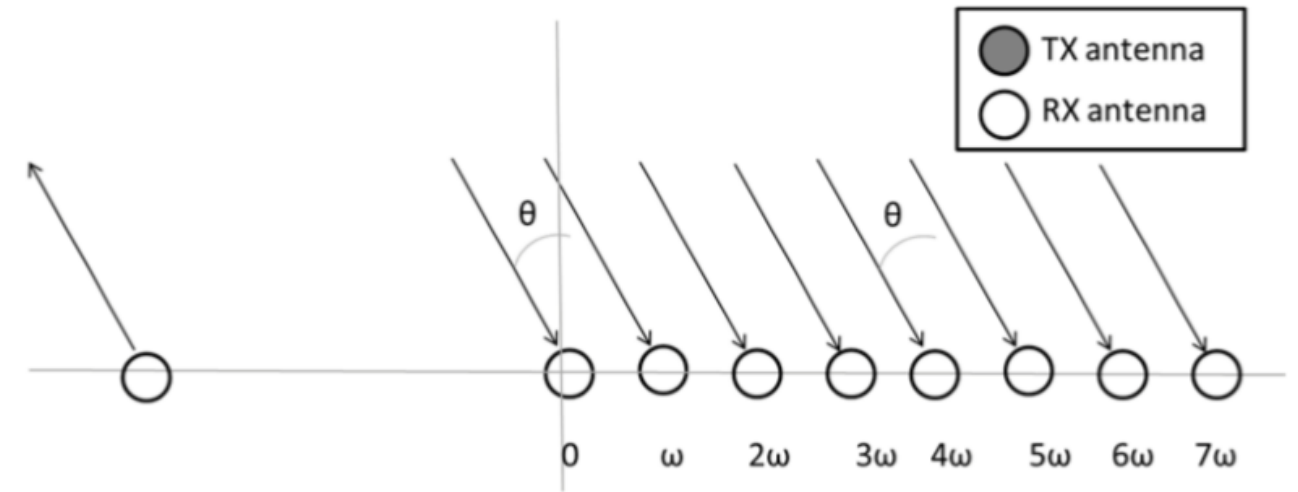
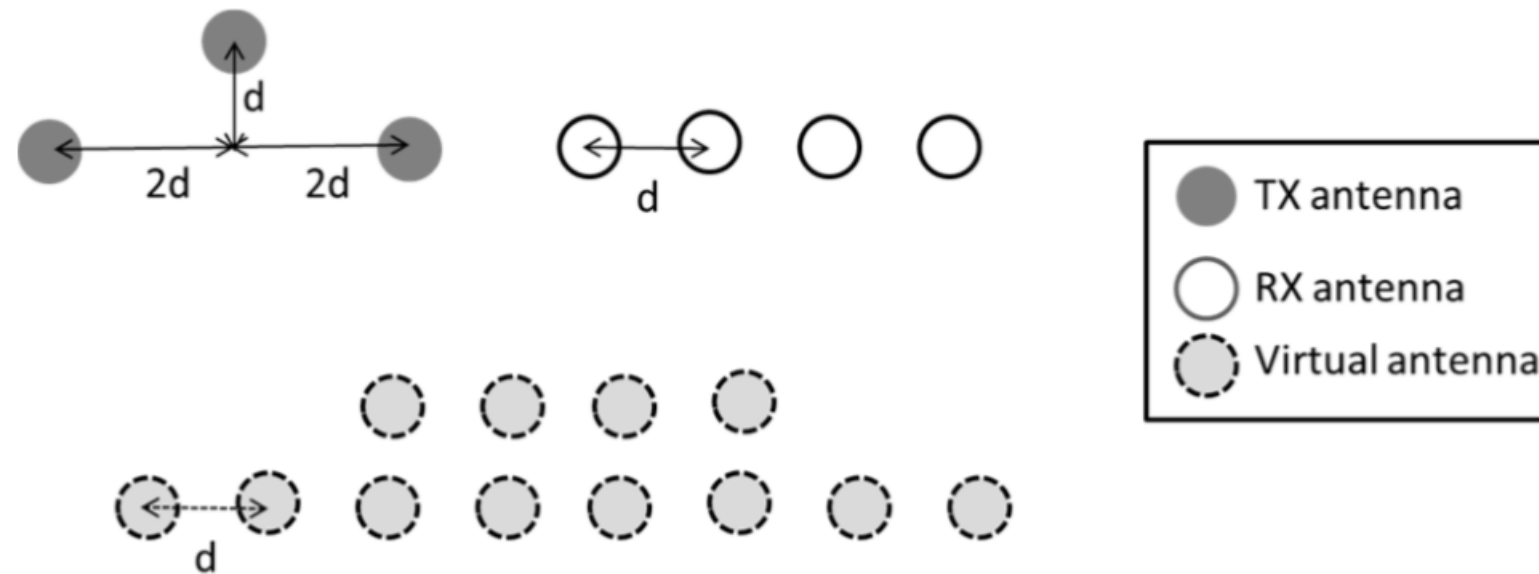


Figure 5. Principle of MIMO Radar



# 2D virtual antennas

- Angular resolution in 2 dimensions





# What to tell your friends

- Radars send chirps and sample the responses
- If you stack chirps vertically and stack multiple antenna frames...
  - FFT of samples in each chirp => ranges
  - FFT across chirps => velocities
  - FFT across antennas => angles
- Micro doppler provides features for object or action identification

# References

- Many diagrams were from TI's [introduction](#) to FMCW radar
- D. Tahmoush and J. Silvius, "Visualizing and displaying radar micro-doppler data," Proceedings of SPIE - The International Society for Optical Engineering, vol. 8021, 05 2011
- TI MIMO Radar Application Report