

UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN  
Department of Electrical and Computer Engineering

ECE 498DLJ PRINCIPLES OF SIGNAL ANALYSIS  
Fall 2011

**MIDTERM EXAM**

Friday, October 21, 2011

- This is a **CLOSED BOOK** exam.
- There are a total of 100 points in the exam. Each problem specifies its point total. Plan your work accordingly.
- You must **SHOW YOUR WORK** to get full credit.

Problem	Score
1	
2	
3	
4	
5	
Total	

Name: \_\_\_\_\_

**Problem 1 (20 points)**

Calculate the Fourier series coefficients  $a_0$ ,  $a_k$ ,  $b_k$ ,  $k = 1, 2, \dots$ , for the periodic signal  $x(t) = x(t + 8)$ :

$$x(t) = \begin{cases} 1, & 0 \leq t < 1 \\ -1, & 1 \leq t \leq 3 \\ 0, & 3 < t < 8 \end{cases}$$

**Problem 2 (20 points)**

Compute the Fourier transform of  $y(t)$ . Write your answer in the form  $Y(\Omega) = jA(\Omega)$ , for some real-valued function  $A(\Omega)$ . The function  $A(\Omega)$  should have no complex exponentials in it, and no imaginary parts.

$$y(t) = \begin{cases} 0.25, & -1 \leq t < 0 \\ -0.25, & 0 \leq t < 1 \\ 0, & \text{elsewhere} \end{cases}$$

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**Problem 3 (20 points)**

Start with the signal  $x[n] = \delta[n] + \delta[n - 1]$ . Find the 4-point DFT,  $X[k]$ , for  $0 \leq k \leq 3$ . Simplify, so that there are no complex exponentials left in your answer.

**Problem 4 (20 points)**

Suppose that we have a signal bandlimited to 5kHz. We want to digitally bandpass filter it to pass all signal components in the range  $1000 \leq f \leq 2000\text{Hz}$ , where  $\Omega = 2\pi f$ , and to eliminate all other frequencies.

- (a) What is the minimum  $F_s$  necessary to avoid aliasing?
- (b) For the sampling rate  $F_s$  that you chose in part (a), what are the corresponding bandpass edges,  $\omega_l$  and  $\omega_u$ , of the discrete-time filter  $H_d(\omega)$ ?
- (c) Sketch the frequency response  $H_d(\omega)$  of the desired filter, for  $0 \leq \omega \leq 2\pi$  (note the non-standard frequency range over which I have asked you to sketch the frequency response!!)

**Problem 5 (20 points)**

Assume that  $x[n] = x_c(nT)$ , where  $1/T = 10,000$  samples/second. For each of the following signals, find  $x[n]$  and  $X_d(\omega)$ .

(a)  $x_c(t) = 0.2\text{sinc}(2000\pi t)$  (sinc, not sin!)

(b)  $y_c(t) = \cos(7000\pi t)$ .