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# **ECE 398GG – ELECTRICAL VEHICLES**

## **12a. Power Converter Basics**

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**A. Stillwell**

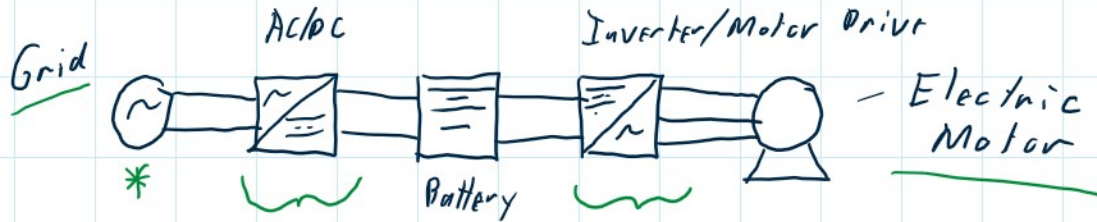
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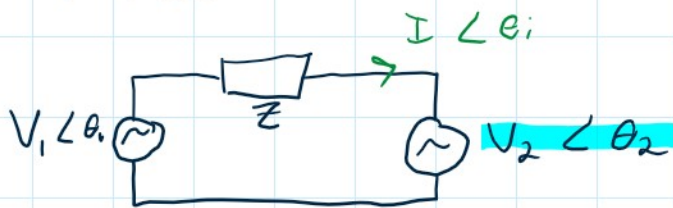
Today:

↳ Switching Power Converters - Basics

High Level System:



Review



Grid

EV charger

Power into the EV charger,  $P_2$

$$P_2 = \frac{V_1 \cdot V_2}{|Z|} \cdot \sin(\theta_2 - \theta_1)$$

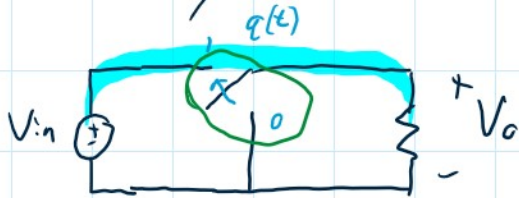
↳ EV charger regulates Voltage + Phase

the grid "sees" to control power flow

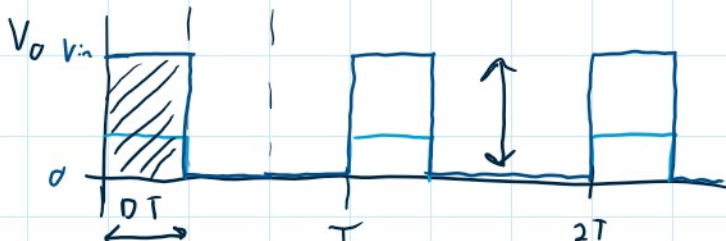
How? Power Electronics [ECE 464/469]

Goal: want to regulate  $V_{out}$ , from  $V_{in}$

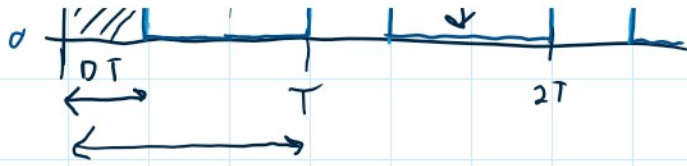
Switching Converter (DC-DC)



$D = \text{duty cycle}$   
 $0 \leq D \leq 1$



i.e.  $D = 33\% = \frac{1}{3}$



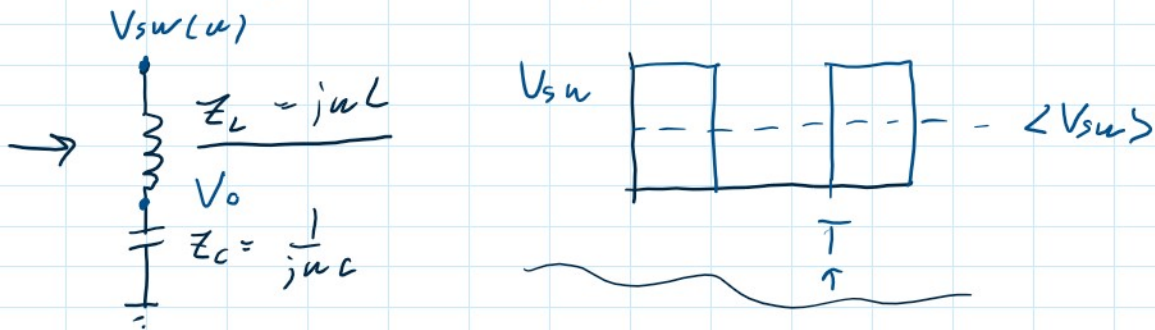
i.e.  $p = 33\% = 1/3$

$$\langle V_o \rangle = \frac{V_{in} \cdot DT}{T} = p V_{in} = \langle V_o \rangle$$

↳ We can generate the right average value by switching

↳ add a filter (LPF) to extract Avg

↳ all elements of filter (LC) are lossless  
↳ high efficiency possible



$$V_o = \frac{Z_C}{Z_L + Z_C} \cdot V_{sw}$$

$$V_o(\omega_k) = \frac{Z_C(\omega_k)}{Z_L(\omega_k) + Z_C(\omega_k)} \cdot V_{sw}(\omega_k)$$

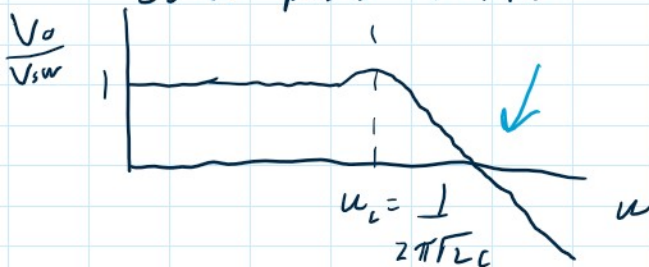
$$\omega \Rightarrow 0 \quad Z_L(\omega) \Rightarrow 0, \quad Z_C \Rightarrow \infty$$

$$V_o(\omega_0) = V_{sw}(\omega_0) \quad [\text{inductor is short at DC}]$$

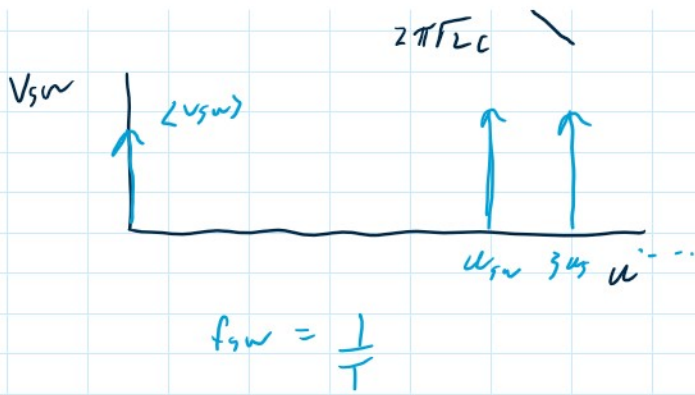
$$\omega \Rightarrow \infty \quad Z_L \Rightarrow \infty, \quad Z_C \Rightarrow 0$$

$$V_o(\omega_{\infty}) \Rightarrow 0$$

Low pass filter

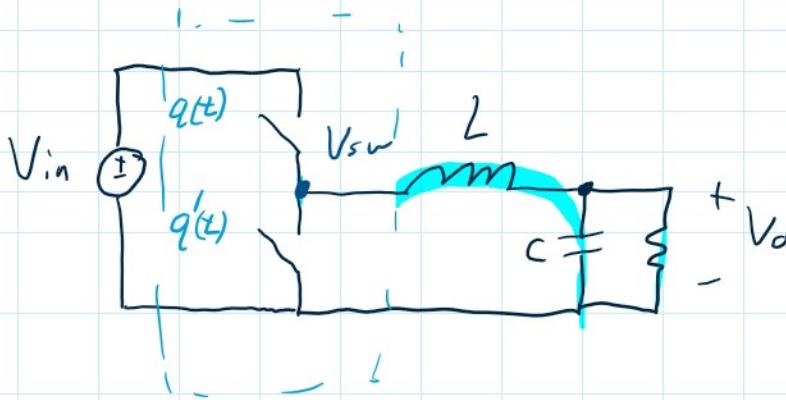


$V_{sw} | \dots$



Low frequency DC component passes through  
 $\rightarrow$  High frequency switching are filtered out

### Buck converter



$$\langle V_{sw} \rangle = D \cdot V_{in} \quad V_o = \langle V_{sw} \rangle = D V_{in}$$

observation:  $\langle V_L \rangle$  ?

$$\langle V_{sw} \rangle = \langle V_L \rangle + \langle V_o \rangle$$

$$\Rightarrow \langle V_L \rangle = 0$$

This makes sense from an energy perspective

$\rightarrow$  for an ideal power converter in steady state,  $\langle P_{out} \rangle = \langle P_{in} \rangle$

$\langle \text{energy} \rangle$  in  $L, C$  should be constant

$$\langle E_L \rangle = \frac{1}{2} L \langle i_L^2 \rangle \quad \langle E_C \rangle = \frac{1}{2} C \langle V_C^2 \rangle$$

$$\langle E, L \rangle = \left\langle \frac{1}{2} L i_L^2 \right\rangle \quad \langle E, C \rangle = \left\langle \frac{1}{2} C V_C^2 \right\rangle$$

$$\left\langle \frac{dE, L}{dt} \right\rangle = 0 \quad \left\langle \frac{dE, C}{dt} \right\rangle = 0$$

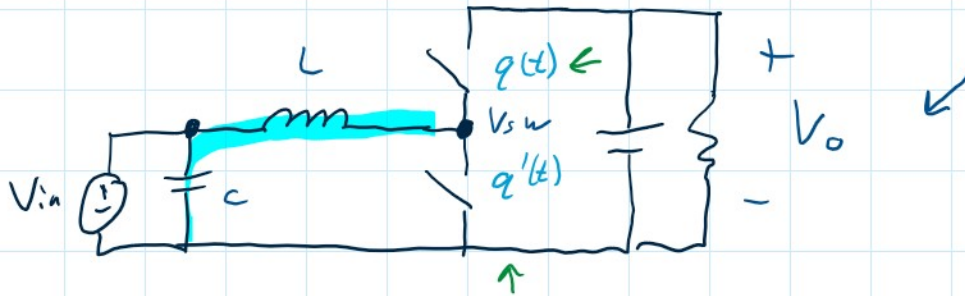
$$\langle V_L \rangle = \left\langle L \frac{di_L}{dt} \right\rangle = 0 \quad \langle i_C \rangle = \left\langle C \frac{dV_C}{dt} \right\rangle = 0$$

In Periodic Steady state

$$\boxed{\langle V_L \rangle = 0, \quad \langle i_C \rangle = 0}$$

$$\langle P_{in} \rangle = \langle P_{out} \rangle$$

Example: Boost Converter



$$\langle V_{sw} \rangle = D \cdot V_o = V_{in}$$

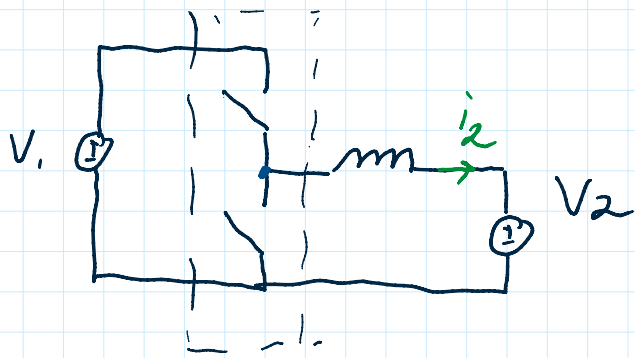
$$\frac{V_o}{V_{in}} = \frac{1}{D} \quad \text{— reverse of Buck}$$

$$V_{out} = \frac{1}{D} \cdot V_{in}$$

Note: common convention in Boost is the low side switch is active switch

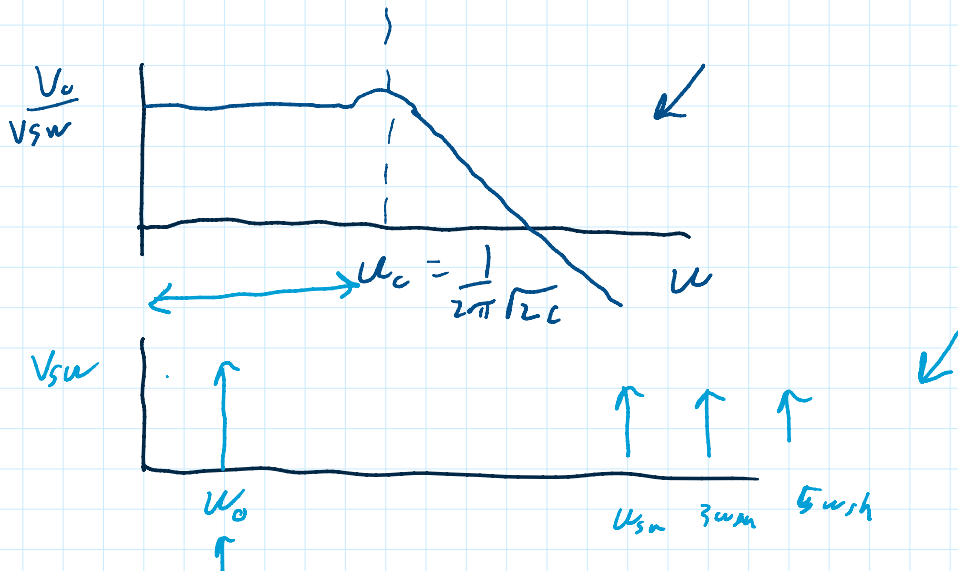
$$\frac{V_o}{V_{in}} = \frac{1}{1-D}$$

↳ we can abstract this



AC/DC + DC/AC conversion

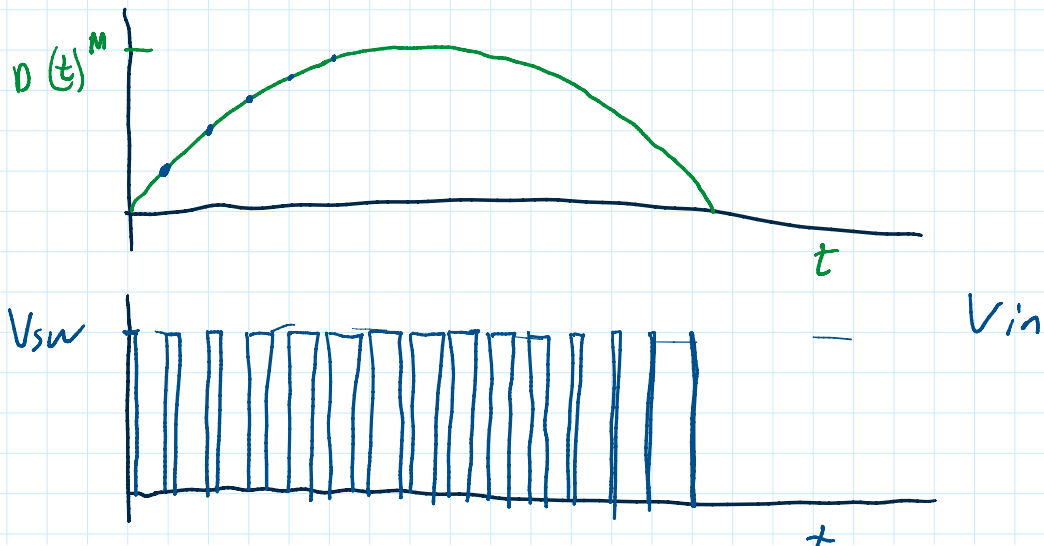
recall Buck LC Filter

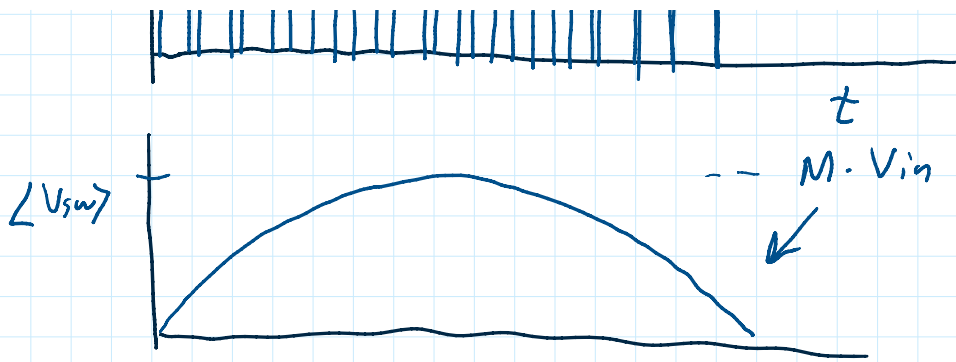


$f = 60 \text{ MHz} \quad \omega_0 = 2\pi f = 377 \text{ rad/s}$

instead of  $D$ , we have  $D(t)$

$p(t) = M \cdot \sin(\omega_0 t)$

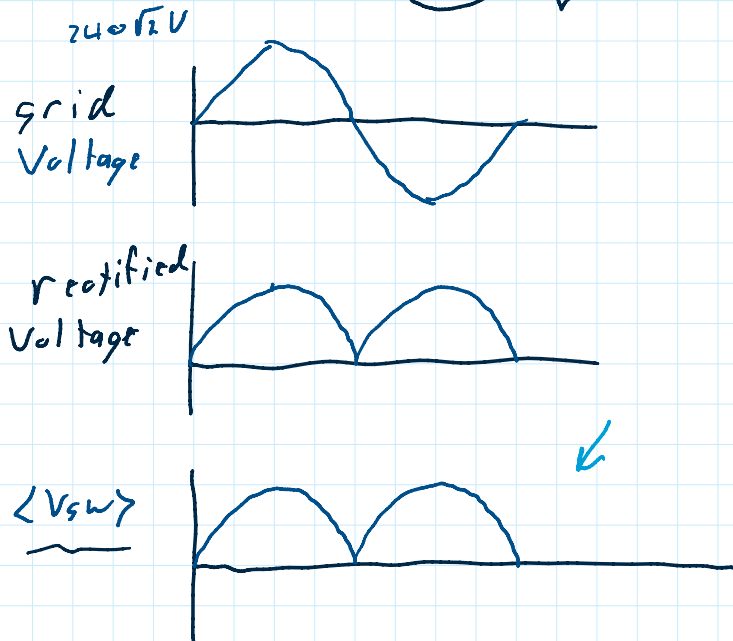
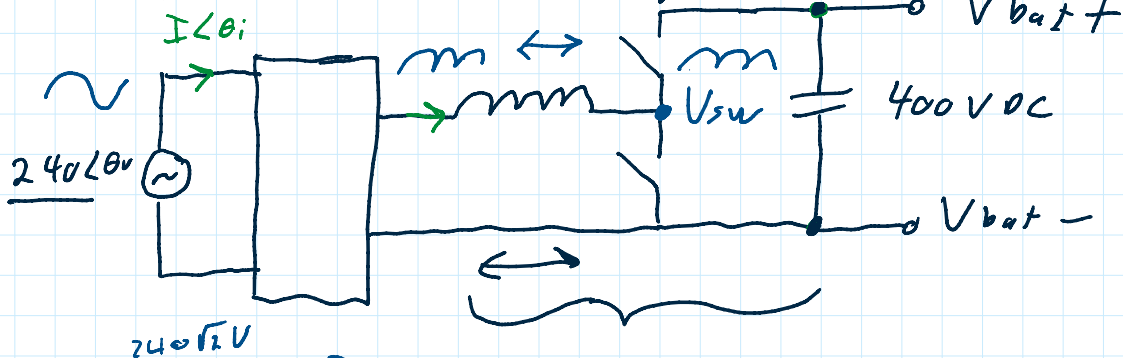




↳ Note: add unfoldeen, or use bipolar source to get negative half cycle

↳ this can be in buck (step down) or Boost operation (step up)

### Simple Boost EV charger



### EV charger controls <math>\langle V\_{sw} \rangle</math>

↳ control Power flow into/out of EV (Battery)

↳ control Power flow into/out of EV (Battery)

↳ also controls current phase  $\Rightarrow \phi$

↳ also control  $P + Q$