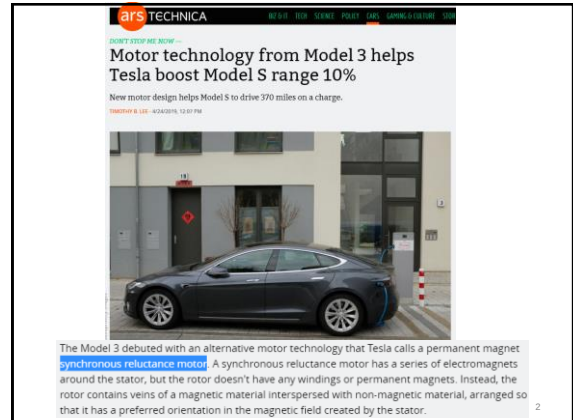


ECE330: Power Circuits & Electromechanics Lecture 17. Energy conversion cycles

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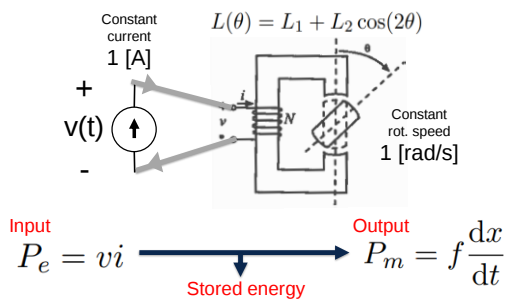


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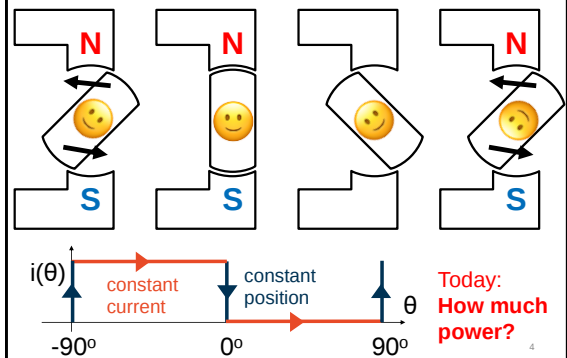
2

Last time: Rotating reluctance machine



3

Last time: Switched reluctance system



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Line integral definition of energy

$$\text{Energy}(\lambda_1, x_1) - \text{Energy}(\lambda_0, x_0) = \int_C \underline{F}(r) \cdot d\underline{r} = \int_C i(\lambda, x) d\lambda + \int_C -f(\lambda, x) dx$$

Path independent (via conservation)

Energy from Electrical

Energy from Mechanical

Path dependent

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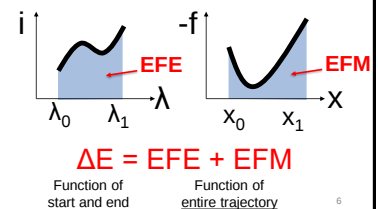
Trajectories and force diagrams

$$\text{Energy}(\lambda_1, x_1) - \text{Energy}(\lambda_0, x_0) = \int_C \underline{F}(r) \cdot d\underline{r} = \int_C i(\lambda, x) d\lambda + \int_C -f(\lambda, x) dx$$

Monday:

1. Draw trajectory from description
2. Draw force diagrams from trajectory

Friday: Analyze electrical machines as a sequence of trajectories



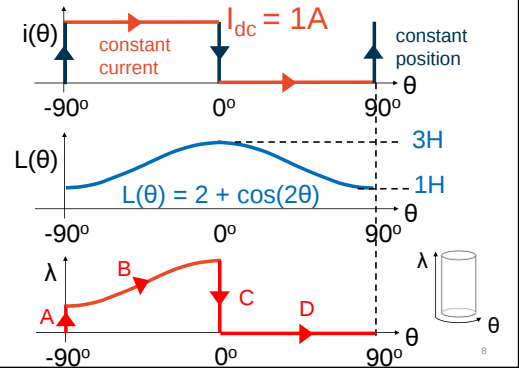
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Today

- Example: Switched reluctance machine
- Example: Linear actuator

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Reluctance machine conversion cycle

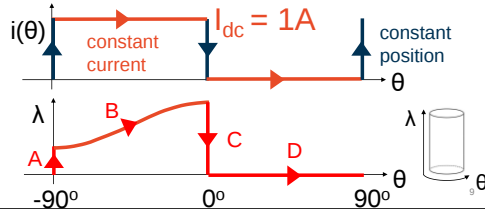


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Reduction to EFE / EFM problem

$L(\theta) = 2 + \cos(2\theta)$. Find the EFE / EFM:

- A. Constant $\theta = -90^\circ$, current $0 \rightarrow 1A$.
- B. Constant $i = 1A$, position $-90^\circ \rightarrow 0^\circ$.
- C. Constant $\theta = 0^\circ$, current $1A \rightarrow 0A$.
- D. Constant $i = 0A$, position $0^\circ \rightarrow 90^\circ$.



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Reduction to EFE / EFM problem

$L(\theta) = 2 + \cos(2\theta)$. Find the EFE / EFM:

- A. Constant $\theta = -90^\circ$, current $0 \rightarrow 1A$.

$$L'(\theta) = \frac{\partial L}{\partial \theta} = -2\sin(2\theta).$$

$$\tau^e = \frac{\partial}{\partial \theta} \left\{ \frac{1}{2} L(\theta) i^2 \right\} = -i^2 \sin(2\theta).$$

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Reduction to EFE / EFM problem

$L(\theta) = 2 + \cos(2\theta)$. Find the EFE / EFM:

- B. Constant $i = 1A$, position $-90^\circ \rightarrow 0^\circ$.

$$L'(\theta) = \frac{\partial L}{\partial \theta} = -2\sin(2\theta).$$

$$\tau^e = \frac{\partial}{\partial \theta} \left\{ \frac{1}{2} L(\theta) i^2 \right\} = -i^2 \sin(2\theta).$$

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Reduction to EFE / EFM problem

$L(\theta) = 2 + \cos(2\theta)$. Find the EFE / EFM:

- C. Constant $\theta = 0^\circ$, current $1A \rightarrow 0A$.

$$L'(\theta) = \frac{\partial L}{\partial \theta} = -2\sin(2\theta).$$

$$\tau^e = \frac{\partial}{\partial \theta} \left\{ \frac{1}{2} L(\theta) i^2 \right\} = -i^2 \sin(2\theta).$$

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Reduction to EFE / EFM problem

$L(\theta) = 2 + \cos(2\theta)$. Find the EFE / EFM:

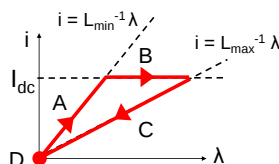
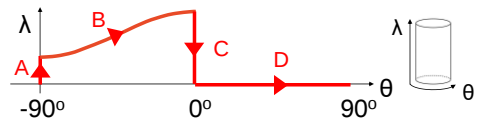
D. Constant $i = 0A$, position $0^\circ \rightarrow 90^\circ$.

$$L'(\theta) = \frac{\partial L}{\partial \theta} = -2\sin(2\theta).$$

$$\tau^e = \frac{\partial}{\partial \theta} \left\{ \frac{1}{2} L(\theta) i^2 \right\} = -i^2 \sin(2\theta).$$

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Reduction to EFE / EFM problem



$$L(\theta) = 2 + \cos(2\theta) \text{ H}$$

$$I_{dc} = 1 \text{ A}$$

$$\text{EFE}_A = +0.5 \text{ J}$$

$$\text{EFE}_B = +2.0 \text{ J}$$

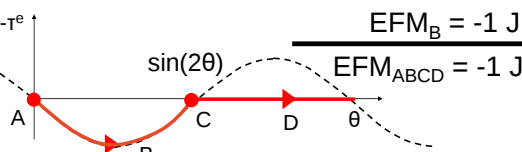
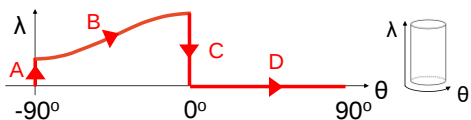
$$\text{EFE}_C = -1.5 \text{ J}$$

$$\text{EFE}_D = 0 \text{ J}$$

$$\text{EFE}_{ABCD} = +1 \text{ J}$$

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Reduction to EFE / EFM problem



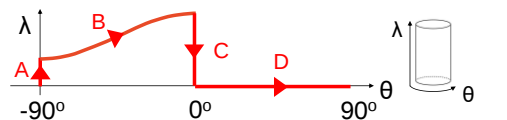
$$\tau^e = -i^2 \sin(2\theta) \text{ Nm}$$

$$I_{dc} = 1 \text{ A}$$

$$\text{EFE}_{\text{cycle}} + \text{EFM}_{\text{cycle}} = 0$$

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High-level view: "Four-stroke engine"



$$\text{Input } P_e = v i \xrightarrow{\text{Stored energy}} \text{Output } P_m = f \frac{dx}{dt}$$

	A	B	C	D
EFE [J]	+1/2 J	+2 J	-3/2 J	0
EFM [J]	0	-1 J	0	0

$$\text{Av. power out} = 1 \text{ J / half-cycle} = \mathbf{120 \text{ W @ 60 Hz}}$$

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Summary: Energy over a closed loop

$$\begin{aligned} & \text{Energy}(\lambda_1, x_1) - \text{Energy}(\lambda_1, x_1) \\ &= \oint_C \underline{F}(\underline{r}) \cdot d\underline{r} = \oint_C i(\lambda, x) d\lambda + \oint_C -f(\lambda, x) dx \\ &= 0 \end{aligned}$$

$$\begin{aligned} & \text{Motor} \\ & \text{elec} \rightarrow \text{mech} \\ & \text{EFE}|_{\text{cycle}} > 0, \quad \text{EFM}|_{\text{cycle}} < 0 \end{aligned}$$

$$\begin{aligned} & \text{Generator} \\ & \text{mech} \rightarrow \text{elec} \\ & \text{EFE}|_{\text{cycle}} < 0, \quad \text{EFM}|_{\text{cycle}} > 0 \end{aligned}$$

▲ Positive = power input, negative = power output

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Today

- Example: Switched reluctance machine
- Example: Linear actuator

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Linear actuator

$\lambda(i, x) = 5i/x$.

Find EFE_{cycle} , EFM_{cycle} .

Motor or generator?

Game plan

- Get formula for energy
- Evaluate energy at each node
- For each path
 - $\Delta E = EFE + EFM$
 - $EFE = \int i \, d\lambda$

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Linear actuator

$\lambda(i, x) = 5i/x$.

Find EFE_{cycle} , EFM_{cycle} .

Motor or generator?

Game plan

- Get formula for energy
- Evaluate energy at each node
- For each path
 - $\Delta E = EFE + EFM$
 - $EFE = \int i \, d\lambda$

$E_a = 5J, E_b = 2J, E_c = 3J, E_d = 6J$

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Linear actuator

$\lambda(i, x) = 5i/x$.

Find EFE_{cycle} , EFM_{cycle} .

Motor or generator?

Game plan

- Get formula for energy
- Evaluate energy at each node
- For each path
 - $\Delta E = EFE + EFM$
 - $EFE = \int i \, d\lambda$

$E_a = 5J, E_b = 2J, E_c = 3J, E_d = 6J$

$EFE_{a \rightarrow b} = -1.5J,$
 $EFM_{a \rightarrow b} = -1.5J,$

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Linear actuator

$\lambda(i, x) = 5i/x$.

Find EFE_{cycle} , EFM_{cycle} .

Motor or generator?

Game plan

- Get formula for energy
- Evaluate energy at each node
- For each path
 - $\Delta E = EFE + EFM$
 - $EFE = \int i \, d\lambda$

$E_a = 5J, E_b = 2J, E_c = 3J, E_d = 6J$

$EFE_{a \rightarrow b} = -1.5J, EFE_{b \rightarrow c} = -1.5J,$
 $EFM_{a \rightarrow b} = -1.5J, EFM_{b \rightarrow c} = +2.5J,$

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Linear actuator

$\lambda(i, x) = 5i/x$.

Find EFE_{cycle} , EFM_{cycle} .

Motor or generator?

Game plan

- Get formula for energy
- Evaluate energy at each node
- For each path
 - $\Delta E = EFE + EFM$
 - $EFE = \int i \, d\lambda$

$E_a = 5J, E_b = 2J, E_c = 3J, E_d = 6J$

$EFE_{a \rightarrow b} = -1.5J, EFE_{b \rightarrow c} = -1.5J, EFE_{c \rightarrow d} = +2.5J,$
 $EFM_{a \rightarrow b} = -1.5J, EFM_{b \rightarrow c} = +2.5J, EFM_{c \rightarrow d} = +0.5J,$

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Linear actuator

$\lambda(i, x) = 5i/x$.

Find EFE_{cycle} , EFM_{cycle} .

Motor or generator?

Game plan

- Get formula for energy
- Evaluate energy at each node
- For each path
 - $\Delta E = EFE + EFM$
 - $EFE = \int i \, d\lambda$

$EFE_{cycle} = -1.5 - 1.5 + 2.5 + 2.5 = +2J$

$EFM_{cycle} = -1.5 + 2.5 + 0.5 - 3.5 = -2J$

$EFE_{d \rightarrow a} = +2.5J, EFM_{d \rightarrow a} = -3.5J,$
 $EFE_{a \rightarrow b} = -1.5J, EFE_{b \rightarrow c} = -1.5J, EFE_{c \rightarrow d} = +2.5J,$
 $EFM_{a \rightarrow b} = -1.5J, EFM_{b \rightarrow c} = +2.5J, EFM_{c \rightarrow d} = +0.5J,$

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