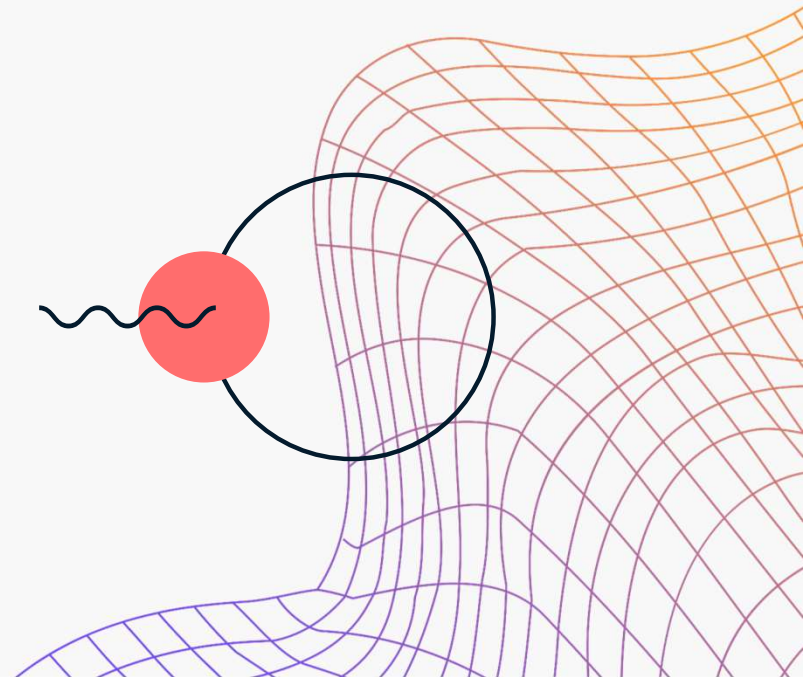


ECE329: Tutorial Session 11

November 12th, 2024



$$\Gamma = \frac{\eta_2 - \eta_1}{\eta_2 + \eta_1} \quad \tau = \frac{2\eta_2}{\eta_2 + \eta_1} = 1 + \Gamma$$

Normal incidence: GENERAL

$$\tilde{E}_i(y) = -E_0 e^{-\alpha_1 y} e^{-j\beta_1 y} \hat{x}$$

$$\tilde{H}_i(y) = -\frac{E_0}{\eta_1} e^{-\alpha_1 y} e^{-j\beta_1 y} \hat{z}$$

$$\tilde{E}_r(y) = -E_0 \Gamma e^{\alpha_1 y} e^{j\beta_1 y} \hat{x}$$

$$\tilde{H}_r(y) = \frac{E_0}{\eta_1} \Gamma e^{\alpha_1 y} e^{j\beta_1 y} \hat{z}$$

$$\sigma_1, \mu_1, \epsilon_1 \\ y < 0$$

$$y = 0$$

$$\tilde{E}_t(y) = -E_0 \tau e^{-\alpha_2 y} e^{-j\beta_2 y} \hat{x}$$

$$\tilde{H}_t(y) = -\frac{E_0}{\eta_2} \tau e^{-\alpha_2 y} e^{-j\beta_2 y} \hat{z}$$

$$\sigma_2, \mu_2, \epsilon_2 \\ y > 0$$

$$\Gamma = \frac{\eta_2 - \eta_1}{\eta_2 + \eta_1} \quad \tau = \frac{2\eta_2}{\eta_2 + \eta_1} = 1 + \Gamma$$

Normal incidence: PEC

$$\tilde{E}_i(y) = -E_0 e^{-j\beta_1 y} \hat{x}$$

$$\tilde{H}_i(y) = -\frac{E_0}{\eta_1} e^{-j\beta_1 y} \hat{z}$$

$$\tilde{E}_r(y) = -E_0 \Gamma e^{j\beta_1 y} \hat{x}$$

$$\tilde{H}_r(y) = \frac{E_0}{\eta_1} \Gamma e^{j\beta_1 y} \hat{z}$$

$$\sigma_1, \mu_1, \epsilon_1 \\ y < 0$$

$$y = 0$$

$$\tilde{E}_t(y) = \vec{0} = -E_0 \tau e^{-j\beta_2 y} \hat{x}$$

$$\tilde{H}_t(y) = \vec{0} = -\frac{E_0}{\eta_2} \tau e^{-j\beta_2 y} \hat{z}$$

$$\sigma_2 = \infty \\ y > 0$$

Oblique incidence: PEC (HW11 P2 Hint)

$$\tilde{E}_i(y, z) = -E_0 e^{-jk_y y} e^{-jk_z z} \hat{x}$$

$$\tilde{E}_r(y, z) = ?$$

$$\sigma_1 = 0, \mu_1, \epsilon_1 \\ y < 0$$

$$y = 0$$

$$\sigma_2 = \infty \\ y > 0$$

$$\tilde{E}_t(y, z) = \vec{0}$$

Oblique incidence: PEC (HW11 P2 Hint)

$$\tilde{E}_i(y, z) = -E_0 e^{-jk_y y} e^{-jk_z z} \hat{x}$$

$$\tilde{E}_r(y, z) = -\Gamma E_0 e^{jk_y y} e^{-jk_z z} \hat{x}$$

$$\tilde{E}_t(y, z) = \vec{0}$$

$$\sigma_1 = 0, \mu_1, \epsilon_1 \\ y < 0$$

$$y = 0$$

$$\sigma_2 = \infty \\ y > 0$$

Standing Waves (dielectric to PEC)

$$\tilde{E}_i(y) = -E_0 e^{-j\beta_1 y} \hat{x}$$

$$\tilde{E}_r(y) = E_0 e^{j\beta_1 y} \hat{x}$$

Problem 1: Standing Waves

A wave propagates through an imperfect dielectric and is normally incident upon a perfect electrical conductor. Is a standing wave created in the imperfect dielectric?

$$\tilde{E}_i(y) = -E_0 e^{-\alpha_1 y} e^{-j\beta_1 y} \hat{x}$$

$$\tilde{E}_r(y) = -E_0 \Gamma e^{\alpha_1 y} e^{j\beta_1 y} \hat{x}$$

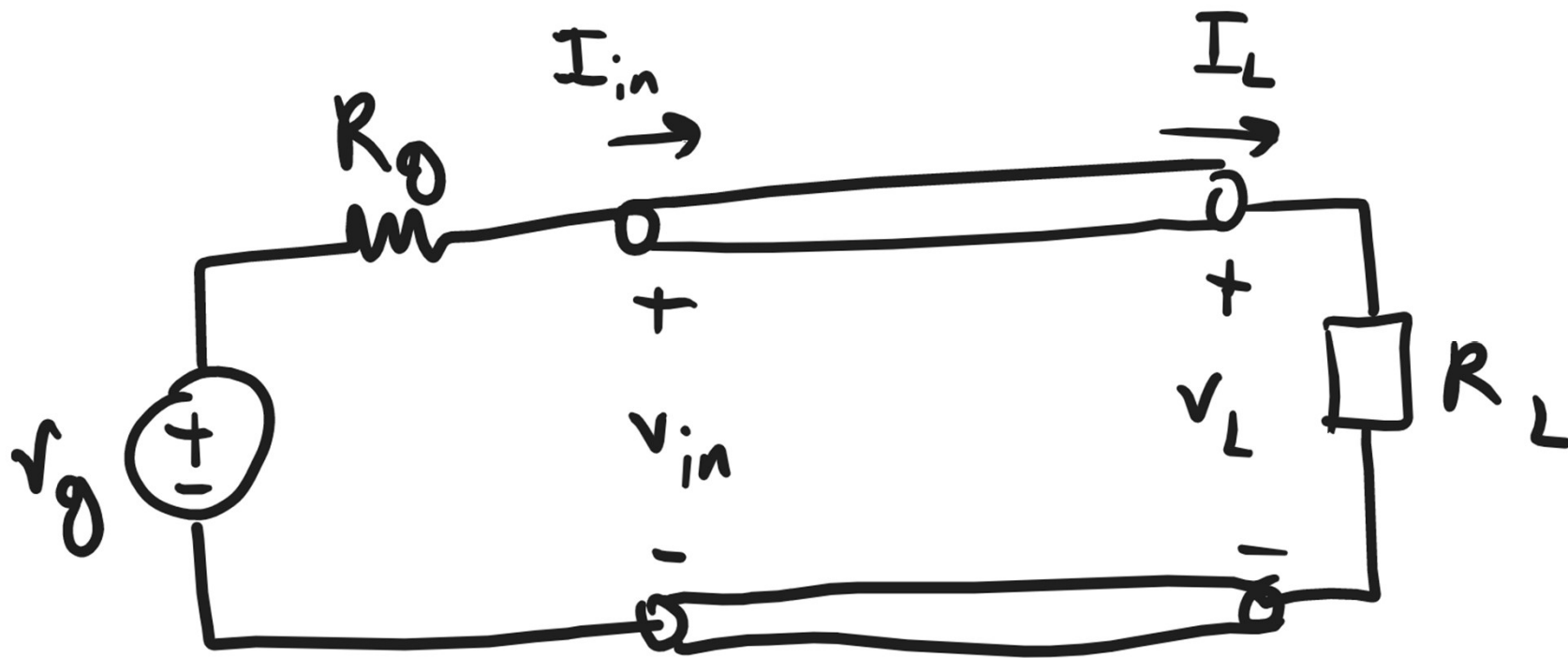


Transmission Lines!

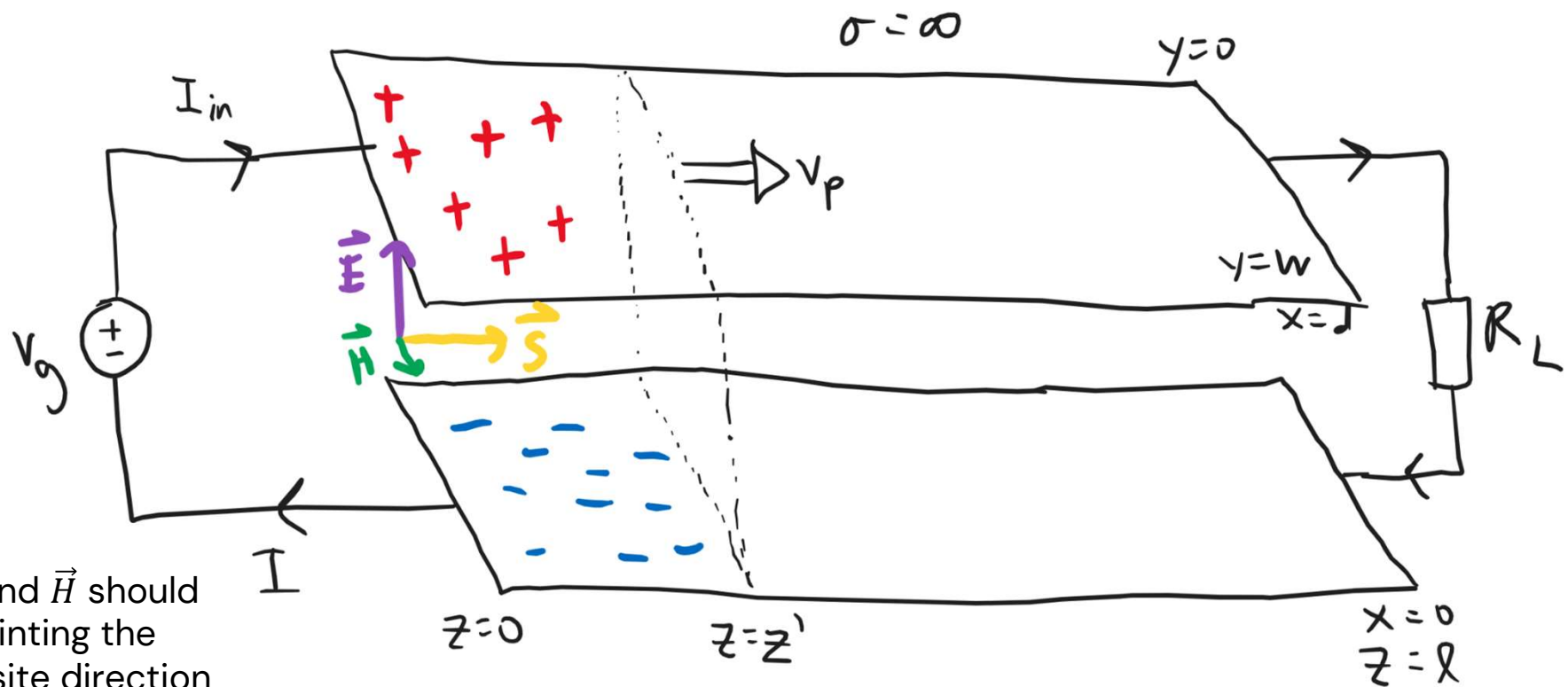
Why do we care?



Transmission Line

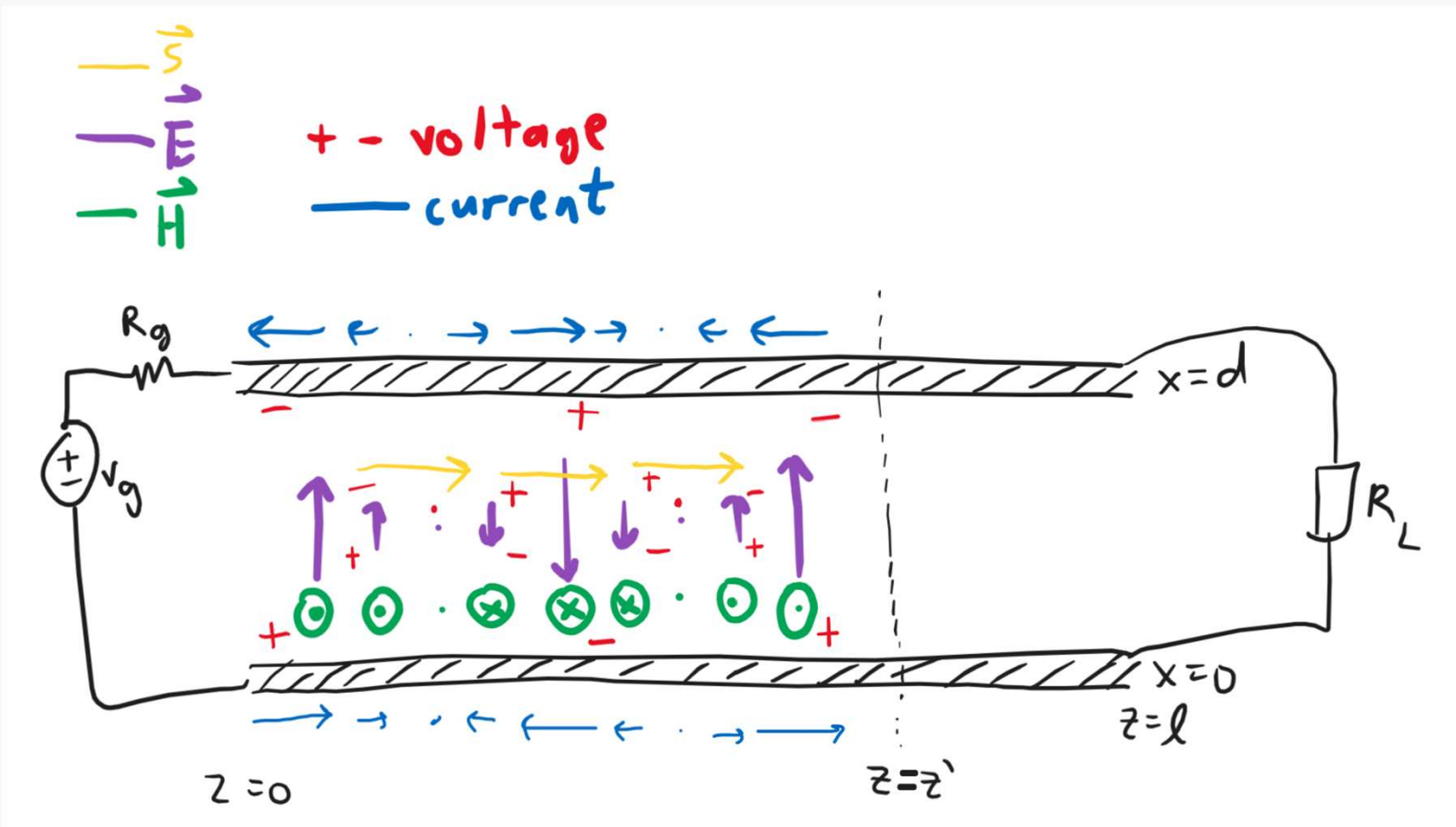


Transmission Line: Parallel Plate Version

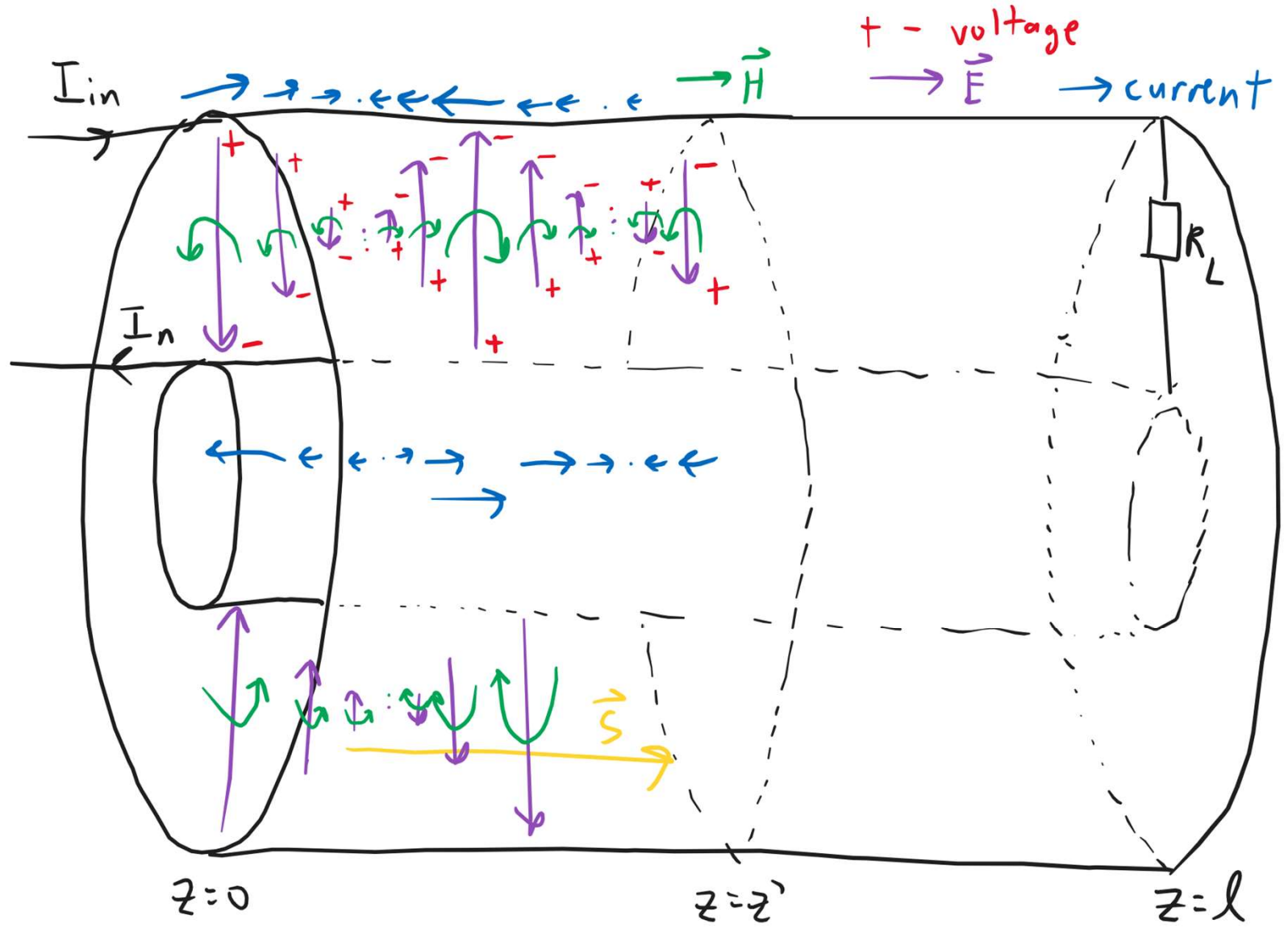


*** \vec{E} and \vec{H} should be pointing the opposite direction oops

Transmission Line: Parallel Plate Version



Coax
Version:





That's... kinda it?

The remainder of HW11 gives you the equation to use to solve for what you want.

We'll start dealing with TLs fully in HW12.



Midterm 1 equations, in one place

$$\vec{F} = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} \hat{r}$$

$$\vec{F} = q_1 \vec{E} + q_1 (\vec{v}_1 \times \vec{B})$$

$$\vec{E} = \frac{q_2}{4\pi\epsilon_0 r^2} \hat{r}$$

$$\hat{n} \cdot (\vec{D}_1 - \vec{D}_2) = \rho_s$$

$$\hat{n} \times (\vec{E}_1 - \vec{E}_2) = 0$$

$$\hat{n} \cdot (\vec{P}_1 - \vec{P}_2) = -\rho_{b,s}$$

$$\epsilon \oint \vec{E} \cdot d\vec{S} = Q_{\text{enclosed}}$$

$$\oint \vec{D} \cdot d\vec{S} = Q_{\text{enclosed}}$$

$$\iiint \rho dV = Q_{\text{enclosed}}$$

$$\oint \vec{B} \cdot d\vec{S} = 0$$

$$I = \oint \vec{j} \cdot d\vec{S} = -\frac{\partial Q_{\text{enclosed}}}{\partial t}$$

$$\epsilon = \epsilon_0 (1 + \chi_e)$$

$$\vec{P} = \epsilon_0 \chi_e \vec{E}$$

$$\vec{D} = \epsilon_0 \vec{E} + \vec{P} = \epsilon \vec{E}$$

$$\vec{j} = \sigma \vec{E}$$

$$\rho_b = -\nabla \cdot \vec{P}$$

$$\nabla \cdot \epsilon_0 \vec{E} = \rho_f + \rho_b$$

$$\nabla \cdot \vec{D} = \rho$$

$$\nabla \cdot \vec{j} = -\frac{\partial \rho}{\partial t}$$

$$-\nabla^2 V = \frac{\rho}{\epsilon}$$

$$\nabla \times \vec{E} = 0$$

$$\vec{E} = -\nabla V$$

$$\oint \vec{E} \cdot d\vec{l} = 0$$

$$V_{ab} = V(b) - V(a) = -\int_a^b \vec{E} \cdot d\vec{l}$$

$$\oint \vec{D} \cdot d\vec{S} = \iiint \nabla \cdot \vec{D} dV$$

$$\oint \vec{E} \cdot d\vec{l} = \iint (\nabla \times \vec{E}) \cdot d\vec{S}$$

$$\int_a^b \nabla V \cdot d\vec{l} = V(b) - V(a)$$



Midterm 2 equations, in one place

$$\vec{B} = \frac{\mu I}{2\pi r} \hat{\phi}$$

$$d\vec{B} = \frac{\mu I d\vec{\ell} \times \hat{r}}{4\pi r^2}$$

$$\oint_C \vec{H} \cdot d\vec{\ell} = \iint_S \vec{J} \cdot d\vec{S}$$

$$\oint_C \vec{B} \cdot d\vec{\ell} = \mu I_{\text{encl}}$$

$$\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\nabla \cdot \vec{B} = 0$$

$$\Psi = \iint_S \vec{B} \cdot d\vec{S}$$

$$-\frac{d}{dt} \iint_S \vec{B} \cdot d\vec{S} = \oint_C \vec{E} \cdot d\vec{\ell}$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\oint_C \vec{E} \cdot d\vec{\ell} = \varepsilon$$

$$\varepsilon = \frac{W}{q} = \oint_C \frac{\vec{F}}{q} \cdot d\vec{\ell}$$

$$\Psi = LI$$

$$\varepsilon = IR$$

$$v = \frac{\omega}{\beta} = \lambda f = \frac{1}{\sqrt{\mu\varepsilon}}$$

$$\omega = 2\pi f = \frac{2\pi}{T}$$

$$\eta = \frac{\sqrt{\mu}}{\sqrt{\varepsilon}}$$

$$\beta = \omega\sqrt{\mu\varepsilon}$$

$$\nabla^2 \vec{E} = \mu\varepsilon \frac{\partial^2 \vec{E}}{\partial t^2}$$

$$\vec{S} = \vec{E} \times \vec{H}$$

$$\vec{\tilde{S}} = \vec{\tilde{E}} \times \vec{\tilde{H}}^*$$

$$\langle \vec{S} \rangle = \frac{1}{2} \text{Re}\{\vec{\tilde{E}} \times \vec{\tilde{H}}^*\}$$

$$\frac{\partial}{\partial t} \left(\frac{1}{2} \varepsilon \vec{E} \cdot \vec{E} + \frac{1}{2} \mu \vec{H} \cdot \vec{H} \right) + \nabla \cdot \vec{S} + \vec{J} \cdot \vec{E} = 0$$

$$Q = CV$$

$$G = \frac{\sigma}{\varepsilon} C \quad R = \frac{1}{G}$$

$$\vec{J}_b = \frac{\partial \vec{P}}{\partial t} + \nabla \times \vec{M}$$

$$\vec{H} = \frac{\vec{B}}{\mu_0} - \vec{M}$$

$$\vec{M} = \chi_m \vec{H}$$

$$\vec{B} = \mu_0 \mu_r \vec{H} = \mu \vec{H}$$

$$A \cos(\omega t - \beta x) \hat{z} \leftrightarrow A e^{-j\beta x} \hat{z}$$

$$\hat{n} \cdot (\vec{B}_1 - \vec{B}_2) = 0$$

$$\hat{n} \times (\vec{H}_1 - \vec{H}_2) = \vec{J}_s$$

$$\hat{n} \times (\vec{M}_1 - \vec{M}_2) = \vec{J}_{b,s}$$

Midterm 3 equations, in one place

	Condition	β	α	$ \eta $	τ	$\lambda = \frac{2\pi}{\beta}$	$\delta = \frac{1}{\alpha}$
Perfect dielectric	$\sigma = 0$	$\omega\sqrt{\epsilon\mu}$	0	$\sqrt{\frac{\mu}{\epsilon}}$	0	$\frac{2\pi}{\omega\sqrt{\epsilon\mu}}$	∞
Imperfect dielectric	$\frac{\sigma}{\omega\epsilon} \ll 1$	$\sim \omega\sqrt{\epsilon\mu}$	$\beta\frac{1}{2}\frac{\sigma}{\omega\epsilon} = \frac{\sigma}{2}\sqrt{\frac{\mu}{\epsilon}}$	$\sim \sqrt{\frac{\mu}{\epsilon}}$	$\sim \frac{\sigma}{2\omega\epsilon}$	$\sim \frac{2\pi}{\omega\sqrt{\epsilon\mu}}$	$\frac{2}{\sigma}\sqrt{\frac{\epsilon}{\mu}}$
Good conductor	$\frac{\sigma}{\omega\epsilon} \gg 1$	$\sim \sqrt{\pi f\mu\sigma}$	$\sim \sqrt{\pi f\mu\sigma}$	$\sqrt{\frac{\omega\mu}{\sigma}}$	45°	$\sim \frac{2\pi}{\sqrt{\pi f\mu\sigma}}$	$\sim \frac{1}{\sqrt{\pi f\mu\sigma}}$
Perfect conductor	$\sigma = \infty$	∞	∞	0	-	0	0

$$v = \frac{\omega}{\beta} = \lambda f$$

$$\nabla^2 \tilde{E} = (j\omega\mu)(\sigma + j\omega\epsilon)\tilde{E}$$

$$\Gamma = \frac{\eta_2 - \eta_1}{\eta_2 + \eta_1}$$

$$\tau = \frac{2\eta_2}{\eta_2 + \eta_1} = 1 + \Gamma$$



Units

Charge Q : C

Current I : A

Electric field strength \vec{E} : N/C or V/m

Electric flux density \vec{D} : C/m²

Polarization field \vec{P} : C/m²

Electric potential V : V

Capacitance C : F

Magnetic flux density \vec{B} : T or Wb/m²

Magnetic field strength \vec{H} : A/m

Magnetic flux Ψ : Wb

Electromotive force ε : V

Inductance L : H

Electric permittivity ϵ : F/m

Magnetic permeability μ : H/m

Conductivity σ : Si/m

Charge density ρ : C/m³

Surface charge density ρ_s : C/m²

Current density \vec{j} : A/m²

Intrinsic impedance η : Ohm

Wave number β : rad/m



Office Hours

Any questions?

