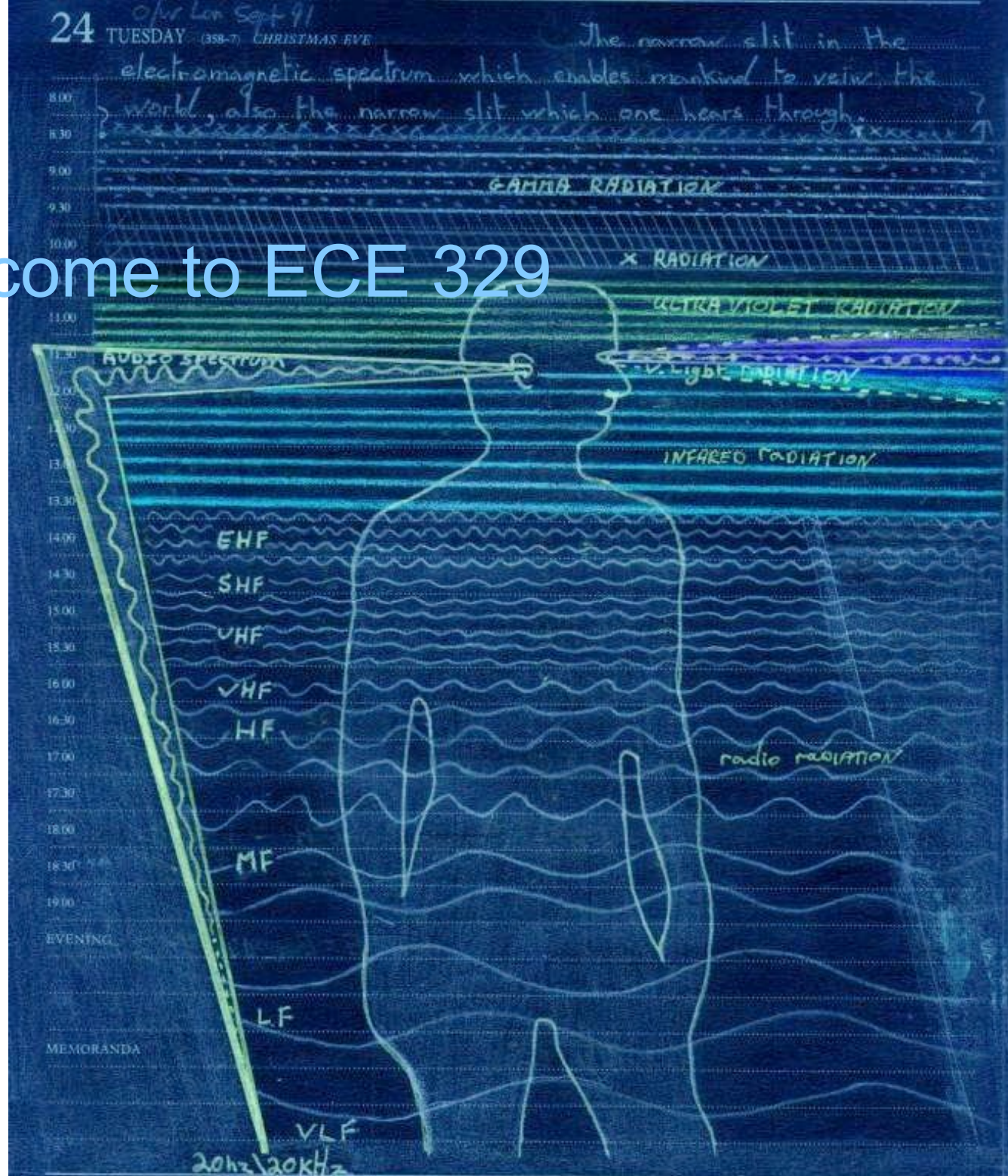


Welcome to ECE 329



Electrostatics – static electricity was known as an interesting but mystifying phenomenon of no practical use.

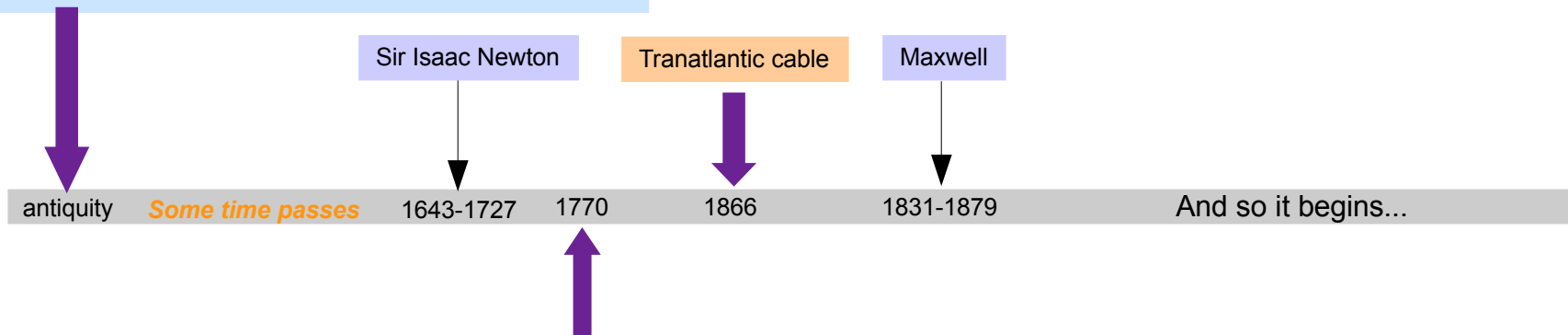
- Lightning
- Amber when rubbed attracted light objects to itself.
- Electrified fish and eels.

Magnetostatics – the existence of magnetic fields was known only through the behavior of naturally magnetized stones – lodestones. Certainly the Chinese, and perhaps the Central Americans figured out how to utilize the properties to make lodestone.

Light – of all the phenomena, light and its behavior were probably the most understood – lenses have been found that suggest that in the very early years AD the concepts of reflection and refraction were understood and exploited

History of Electromagnetics

the Reader's Digest version



State-of-the-art: 1770.

- There are two types of electricity (or maybe one that can be added to some materials and taken away from others)
- Electricity is conserved.
- There are insulators in which charge cannot move.
- There are conductors in which it can move freely.
- Equal charges repel each other.
- Opposite charges attract.
- Light reflection and refraction were understood and Sir Isaac Newton had put forth the notion that light was made of very small particles.

THE ELECTROMAGNETIC SPECTRUM

THESE WAVES TRAVEL THROUGH THE ELECTROMAGNETIC FIELD. THEY WERE FORMERLY CARRIED BY THE AETHER, WHICH WAS DECOMMISSIONED IN 1897 DUE TO BUDGET CUTS.

ABSORPTION SPECTRA:

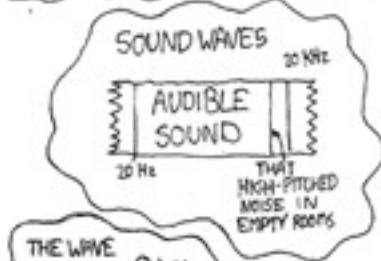
HYDROGEN:



HELIUM:



OTHER WAVES:



SHOUTING CAR DEALERSHIP COMMERCIALS

CIA (SECRET)

HAM RADIO

KOSHER RADIO

SPACE RAYS CONTROLLING STEVE BALLMER

99.3 "THE FOX"

101.5 "THE BADGER"

104.3 "THE FRIGHTENED SQUIREL"

24/7 NPR PRIDE DRIVES

CELL PHONE

CANCER RAYS

ALIENS SETI

GRAVITY

WIFI

BRAIN WAVES

SOLANESI

SUPERMAN'S HEAT VISION

JACK BLACK'S HEAT VISION

SUNLIGHT

MAIN DEATH STAR LASER

POTATO

BLOGORAYS

MAIL-ORDER X-RAY GLASSES

SINISTER GOOGLE PROJECTS

POWER & TELEPHONE

RADIO & TV

MICROWAVES

TOASTERS

IR

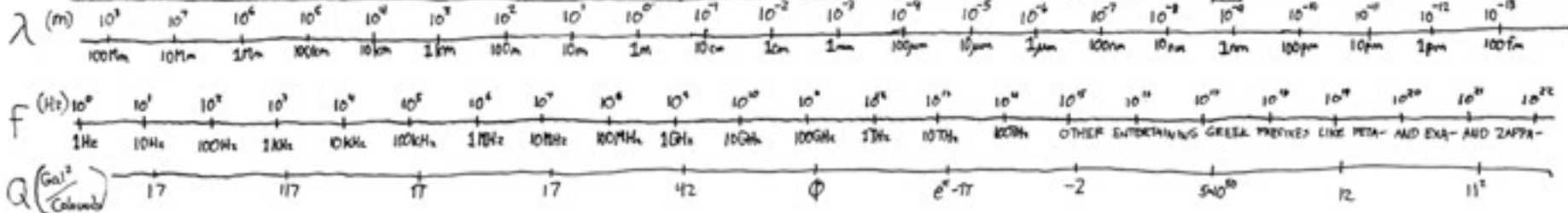
VISIBLE LIGHT

UV

MILLER LIGHT

X-RAYS

GAMMA/COSMIC RAYS



QUESTION: How do we even know that electricity exists – or anything else really?

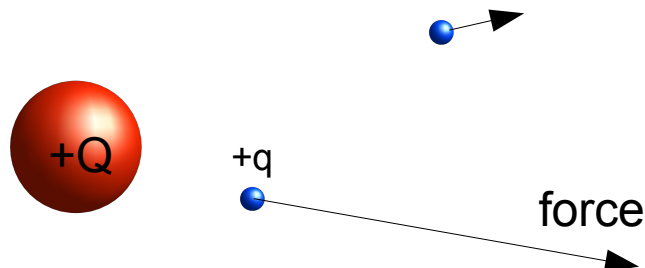
The answer to this question is at the heart of understanding electromagnetism and all of physics really.

Answer: We know about our world because we can observe the effects of the existence of – say other matter or charged particles. From direct experience we know that gravity exists because everything that we drop is always pulled downward. In the case of electric phenomena we know how charged particles affect each other through experimentation. The simple law that we will learn is one of 2 fundamental pieces of evidence that constitutes all of electromagnetism.

INTERACTION between CHARGES

Charges exert a force on one another according to these observations:

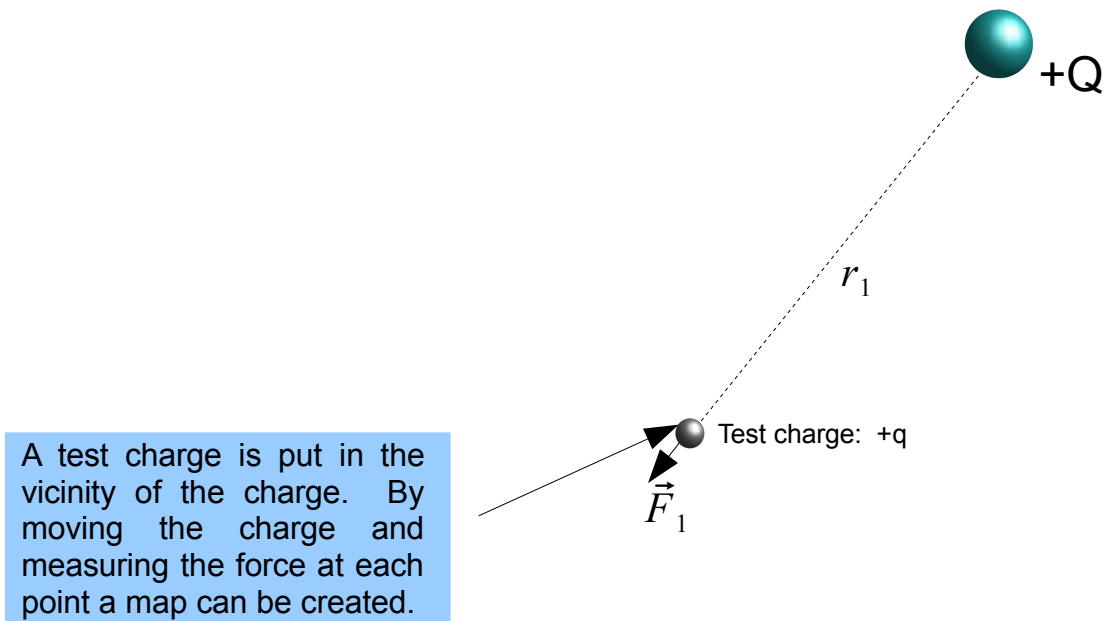
- *magnitude of the force is proportional to the magnitude of both charges*
- *magnitude of the force is inversely proportional to the square of the distance between them*
- *direction of the force lies along the direction of a line connecting the charges. Like charges repel, unlike attract.*



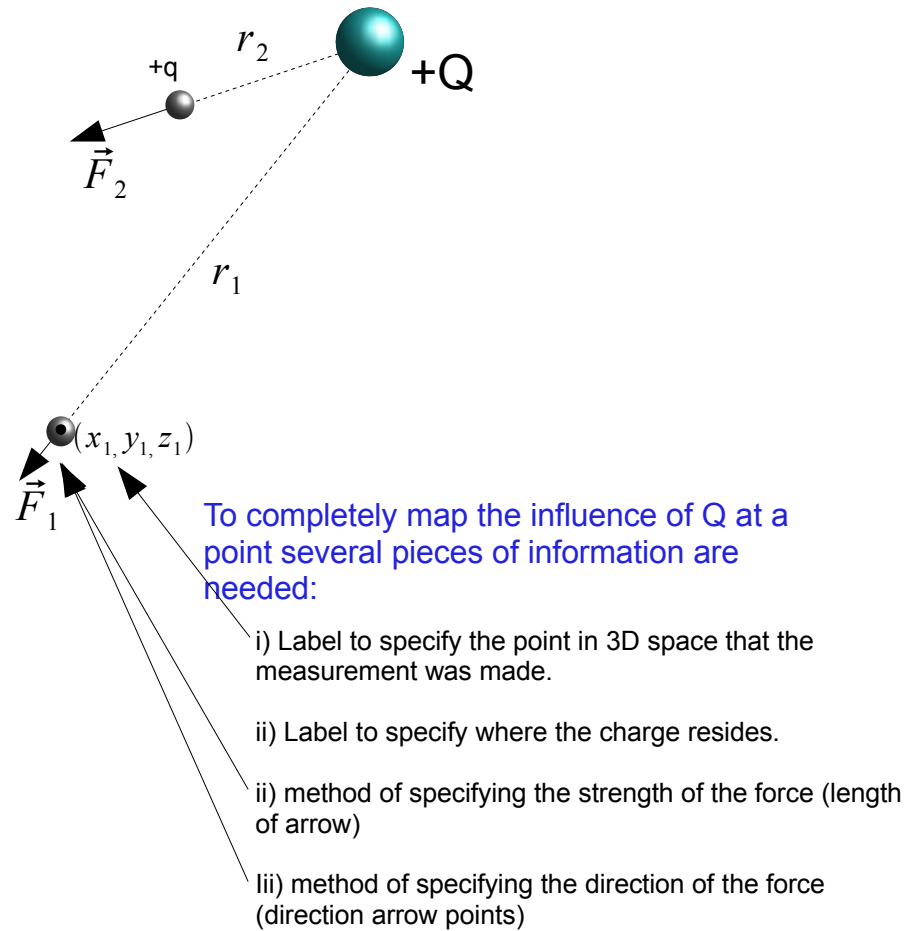
MATH Concepts -

- coordinate systems
- vector notation
- fields

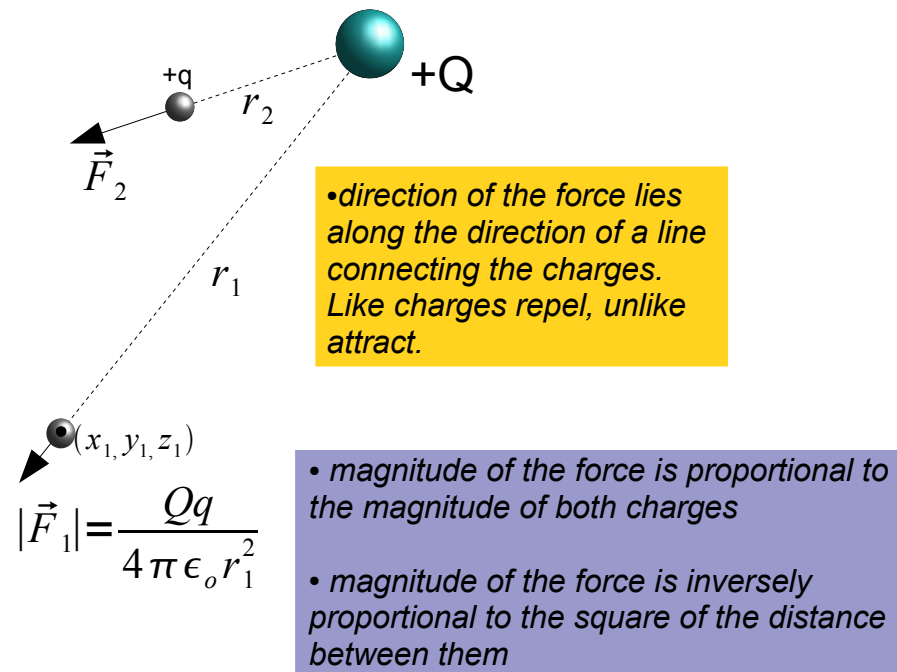
Mapping the influence of a charged particle:



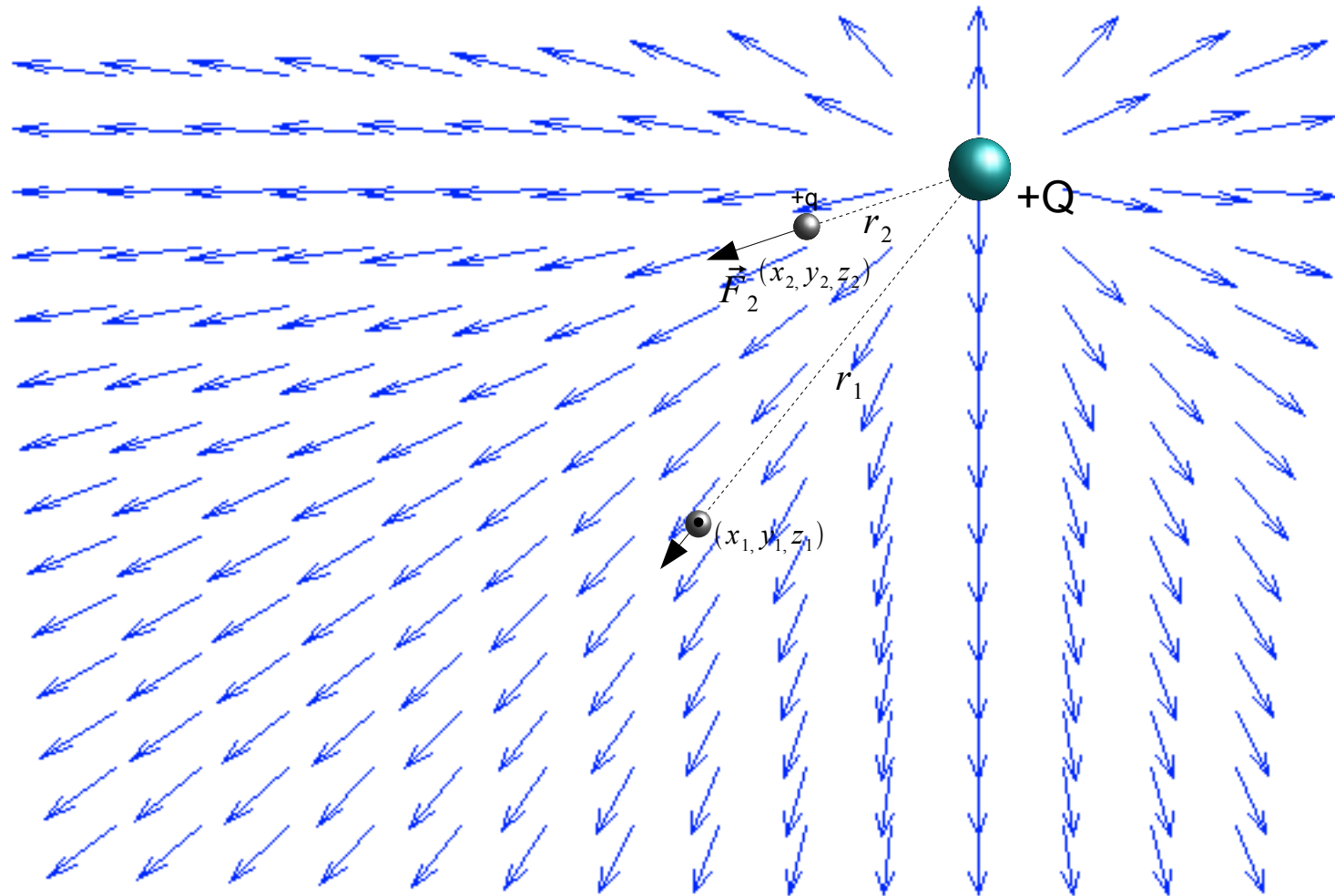
Mapping the influence of a charged particle:



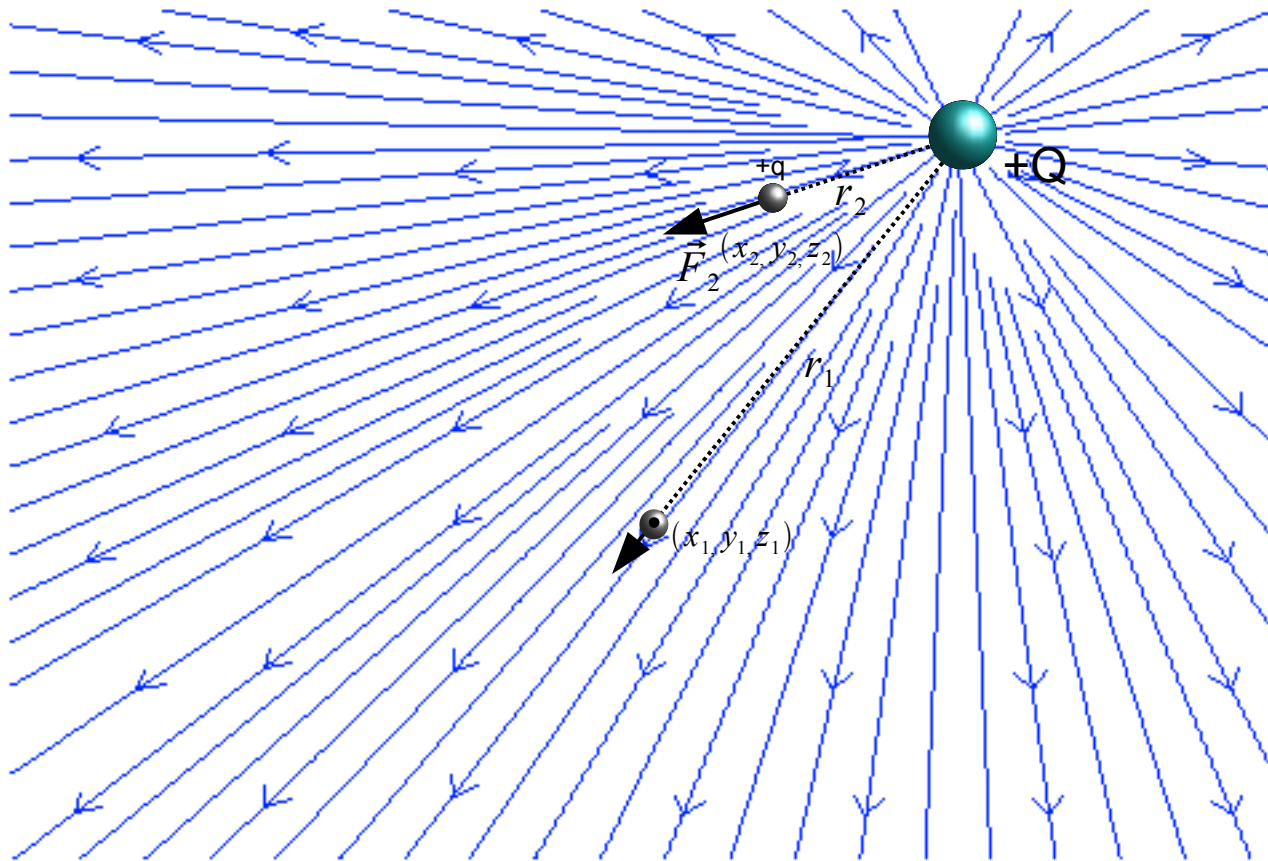
Mapping the influence of a charged particle:



Map of the force that a test charge feels in the vicinity of charge +Q



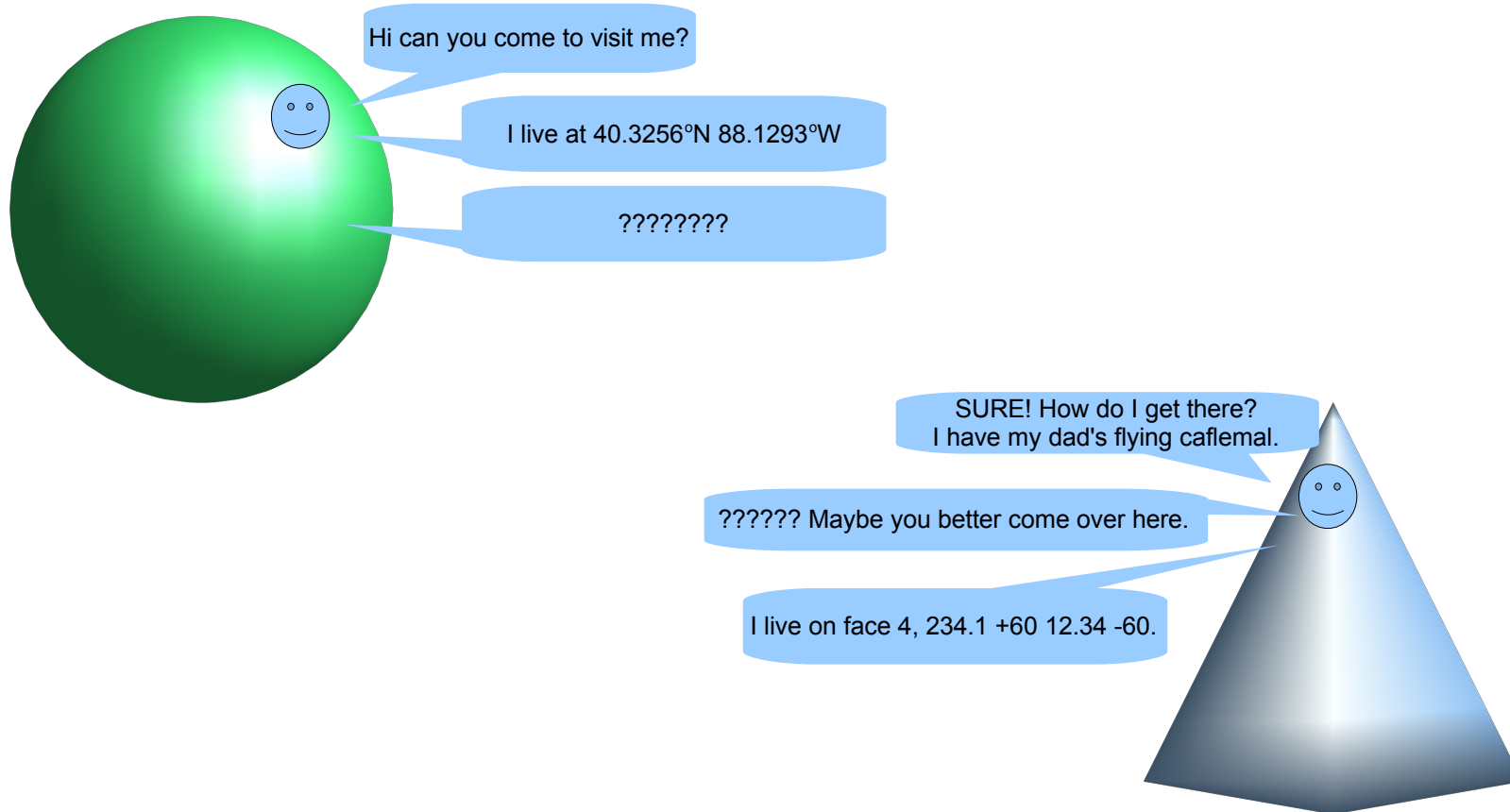
Map of the force that a test charge feels in the vicinity of charge $+Q$
FIELD LINES



To description of how $+Q$ influences the test charge q at all points in space mathematically we need to find suitable operators and a geometry that fits our problems.

STEP 1: DEFINE A COORDINATE SYSTEM

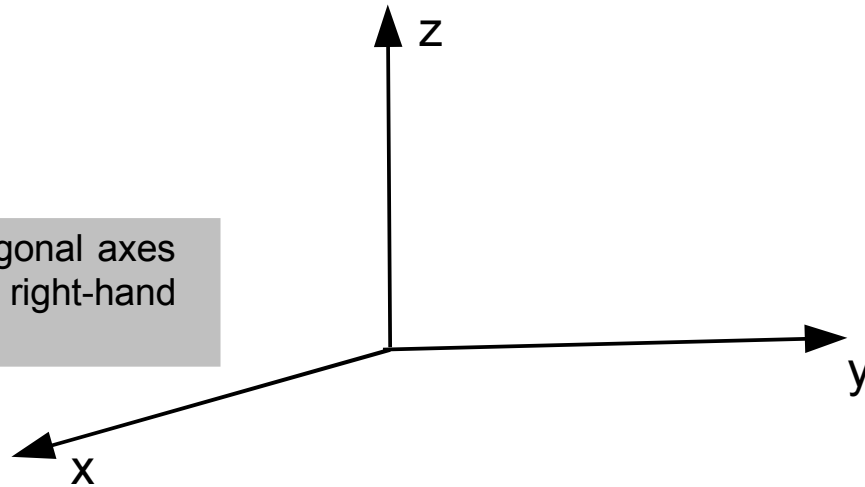
- specify origin
- define method of specifying a point
- define a method of specifying a vector



COORDINATE SYSTEMS

- specify origin
- define method of specifying a point
- define a method of specifying a vector

3 mutually orthogonal axes
following the right-hand
convention

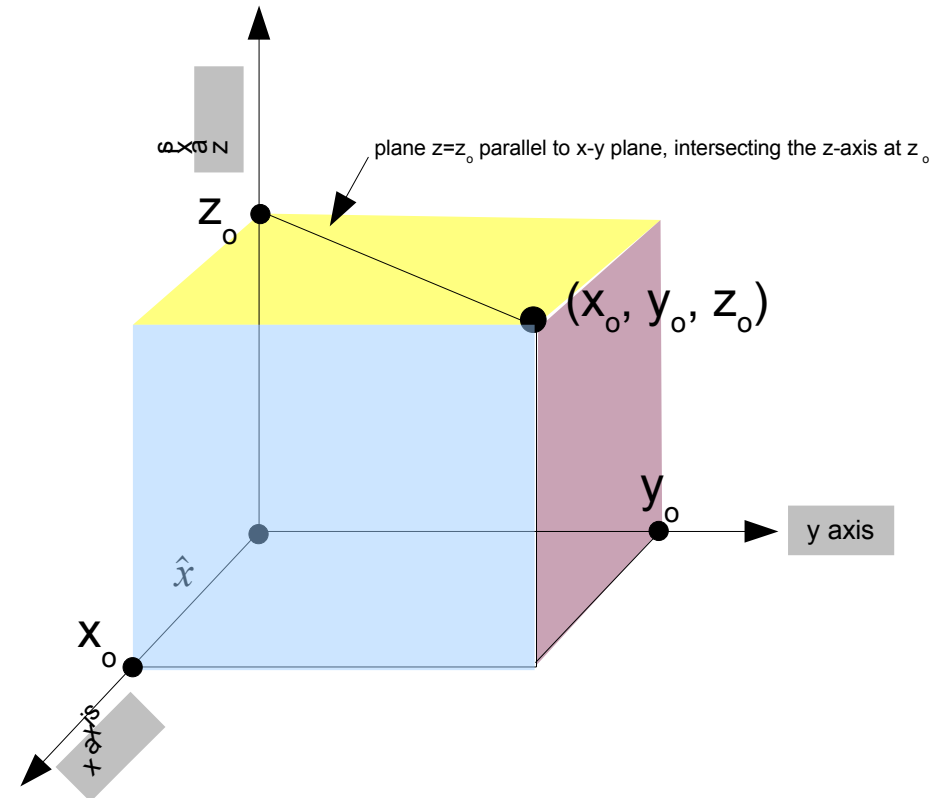
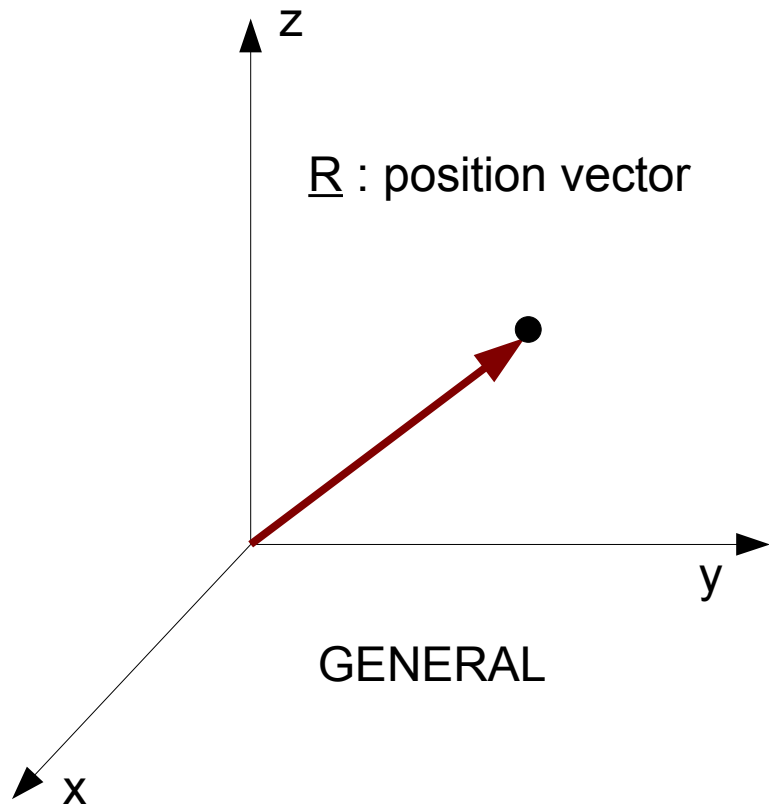


Rene Descarte invented what is now called the Cartesian Coordinate system, named in his honor. This achievement happened around 1637...

Without this innovation, the complex mathematics needed to quantify physical concepts would be impossibly difficult. Consider trying to describe quantitatively, using only words and some hand drawn figure how light behaves when going through a lens, for example.

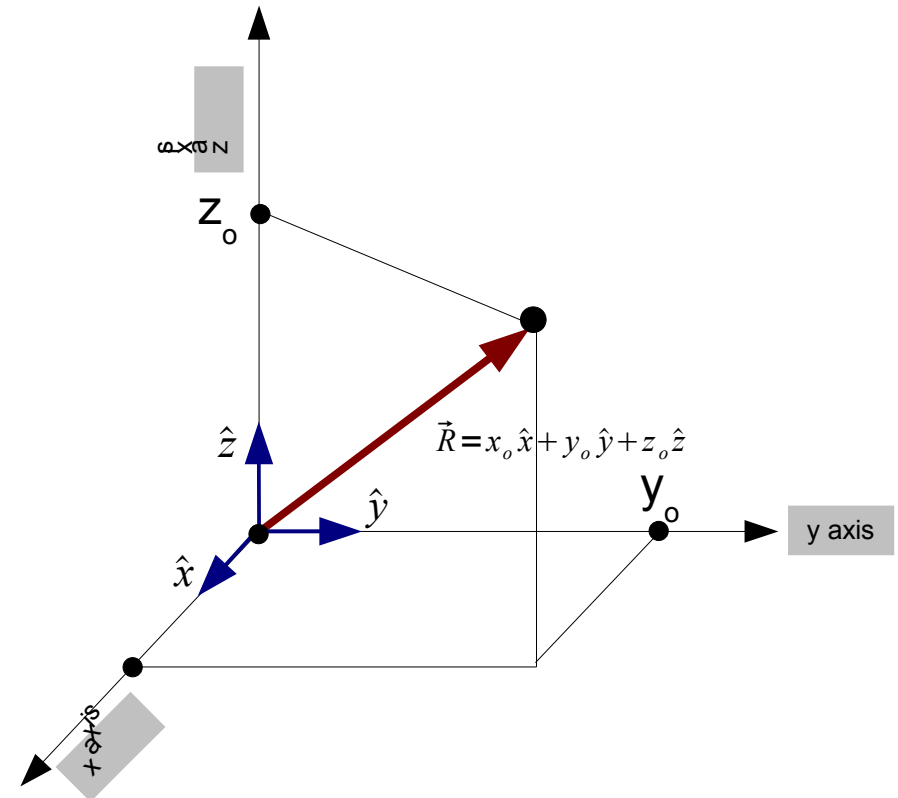
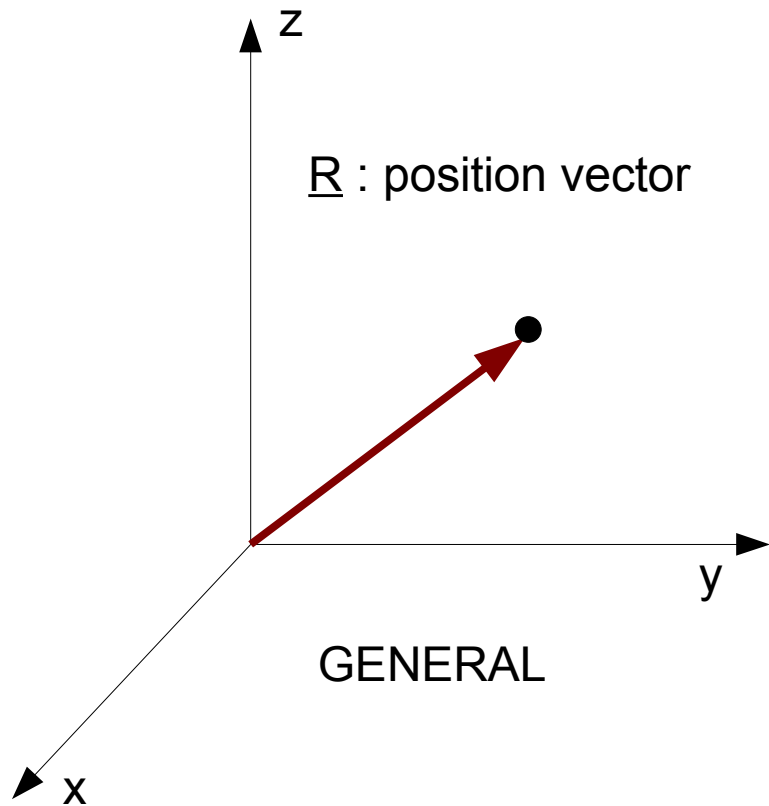
COORDINATE SYSTEMS

- specify origin
- **define method of specifying a point**
- define a method of specifying a vector



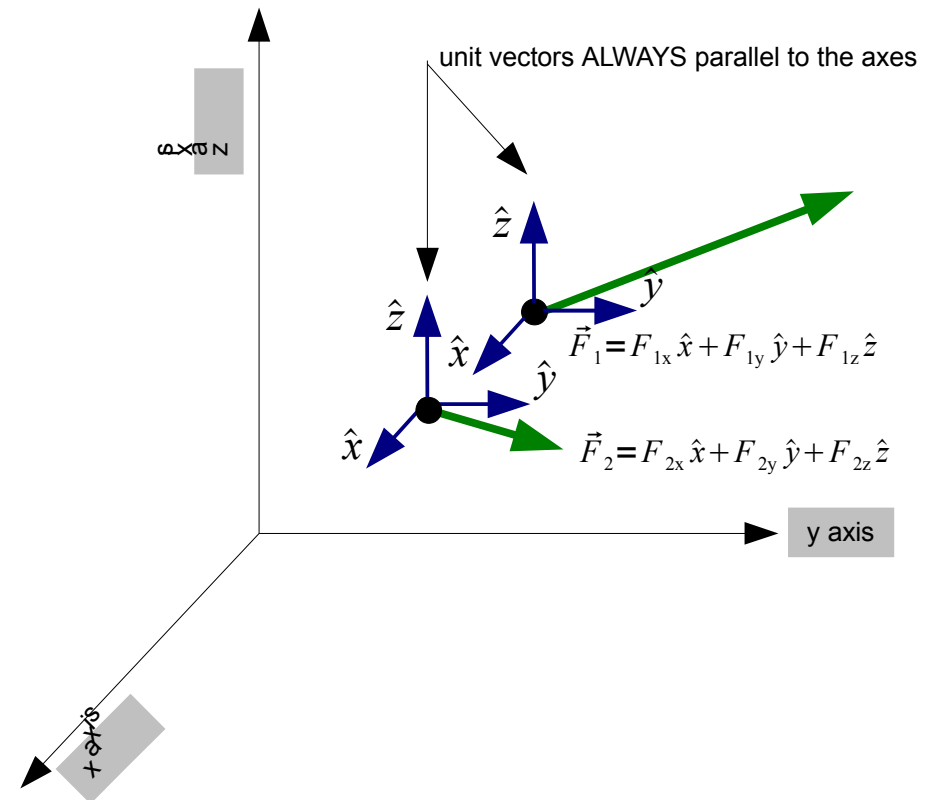
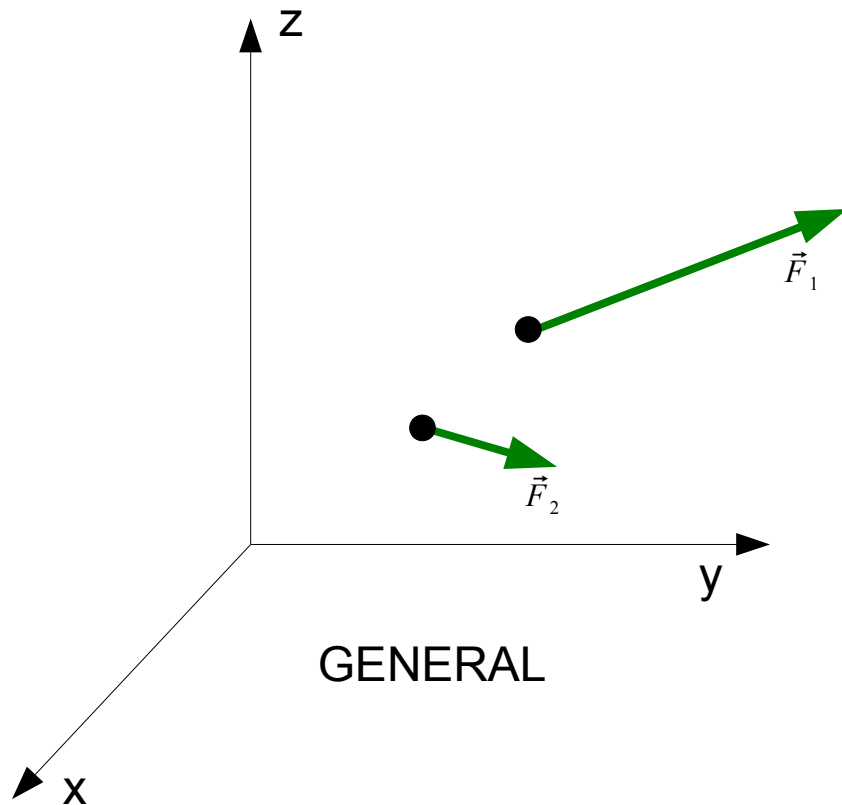
COORDINATE SYSTEMS

- specify origin
- **define method of specifying a point**
- define a method of specifying a vector



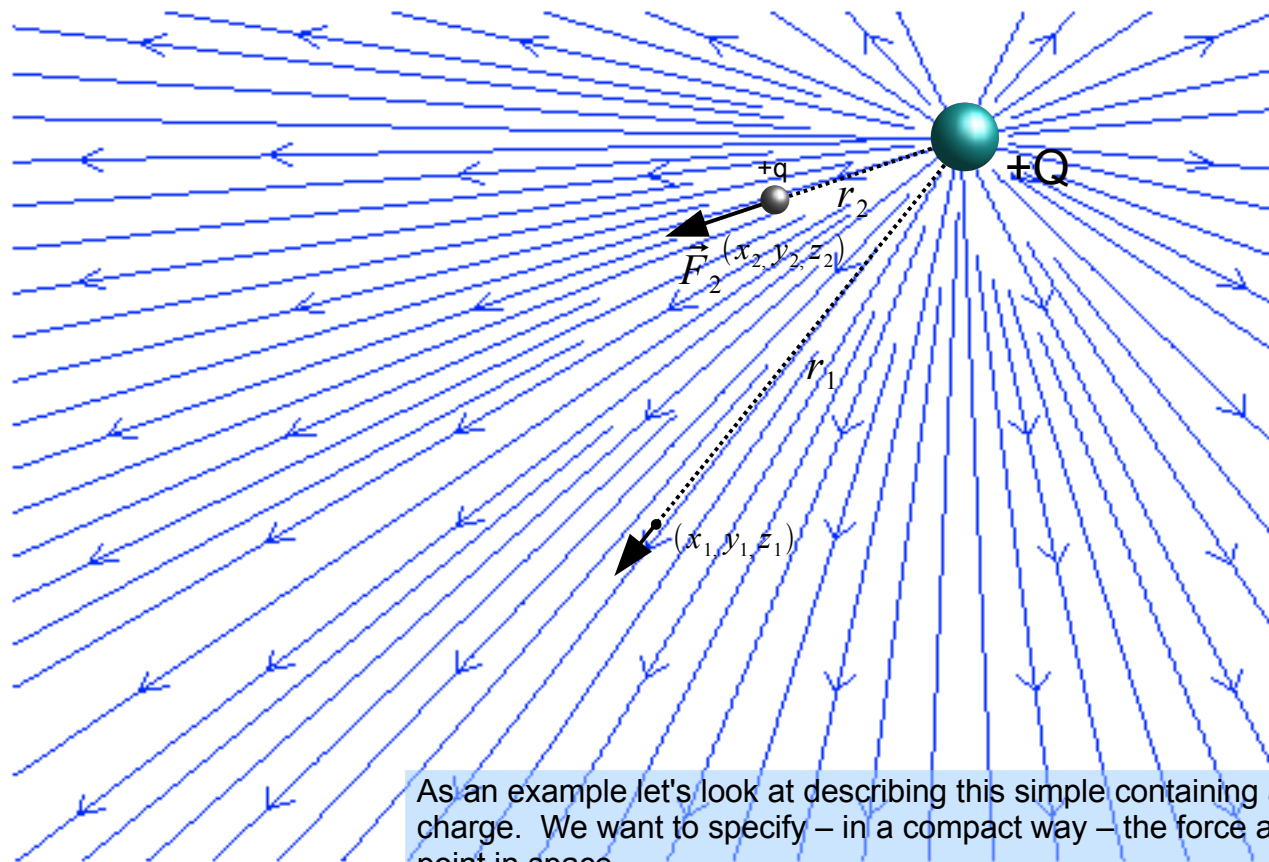
COORDINATE SYSTEMS

- specify origin
- define method of specifying a point
- **define a method of specifying a vector**



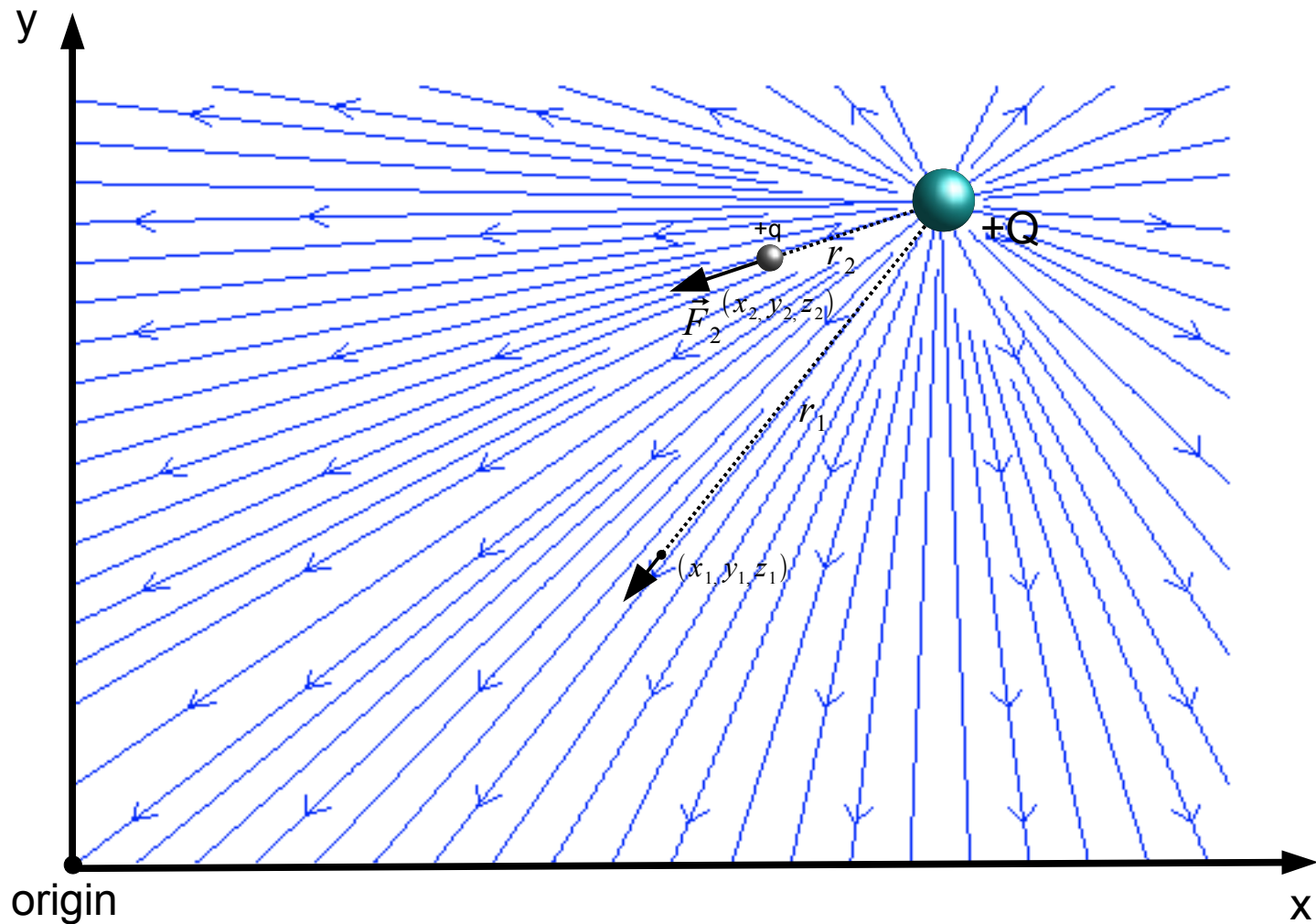
COORDINATE SYSTEMS

- specify origin
- define method of specifying a point
- define a method of specifying a vector



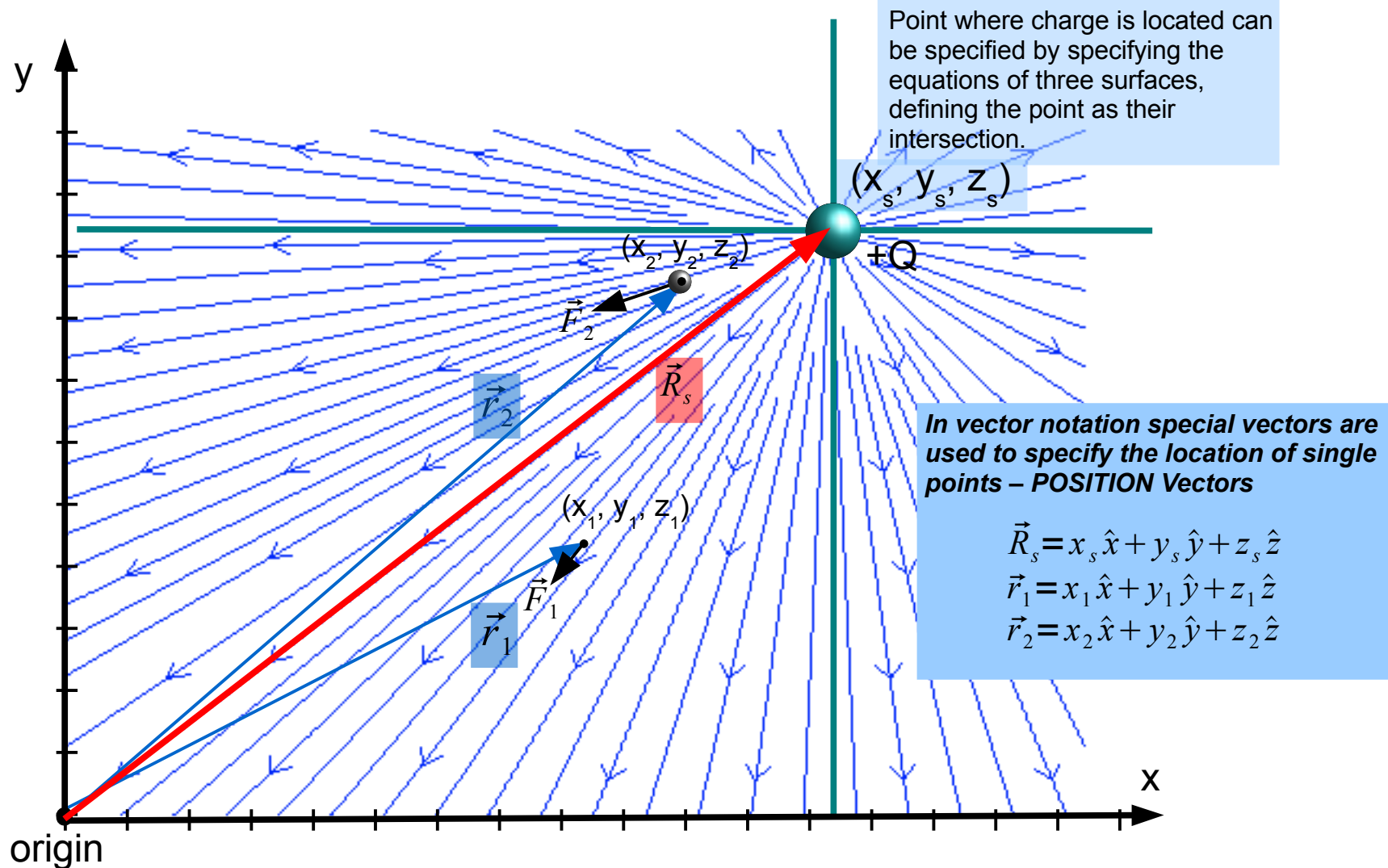
COORDINATE SYSTEMS

- specify origin
- define method of specifying a point
- define a method of specifying a vector



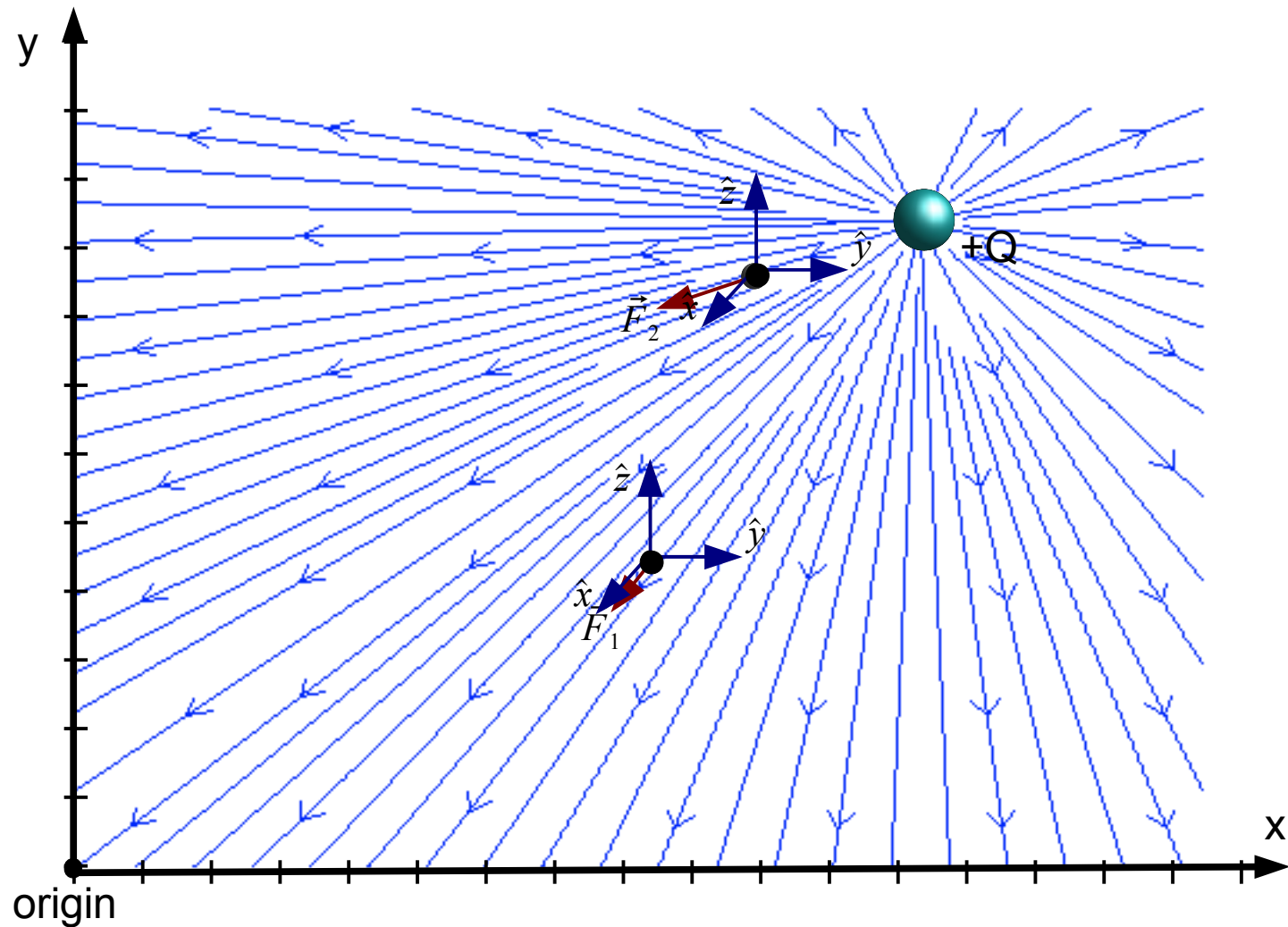
COORDINATE SYSTEMS

- specify origin
- define method of specifying a point
- define a method of specifying a vector



COORDINATE SYSTEMS

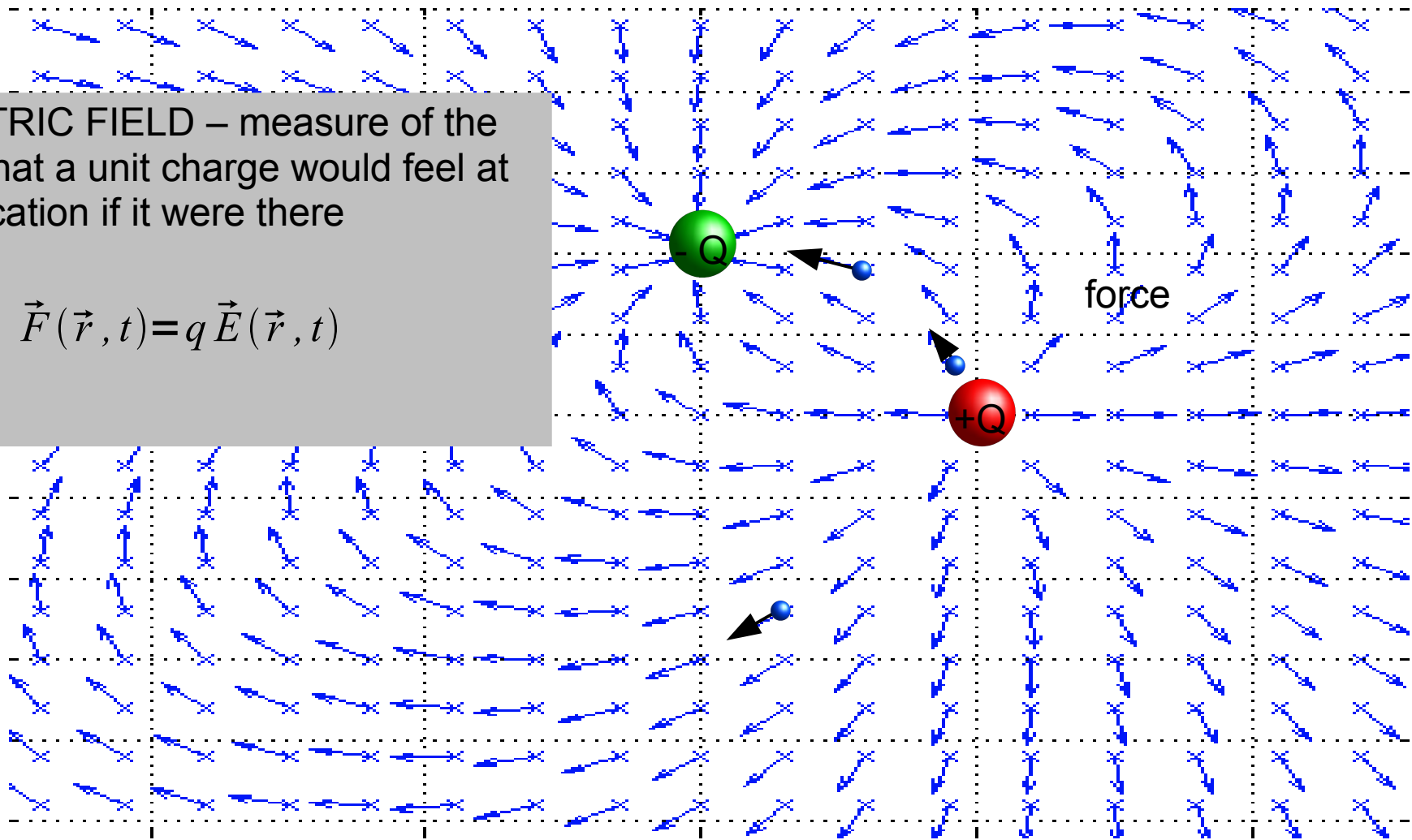
- specify origin
- define method of specifying a point
- define a method of specifying a vector



FIELDS

ELECTRIC FIELD – measure of the force that a unit charge would feel at any location if it were there

$$\vec{F}(\vec{r}, t) = q\vec{E}(\vec{r}, t)$$

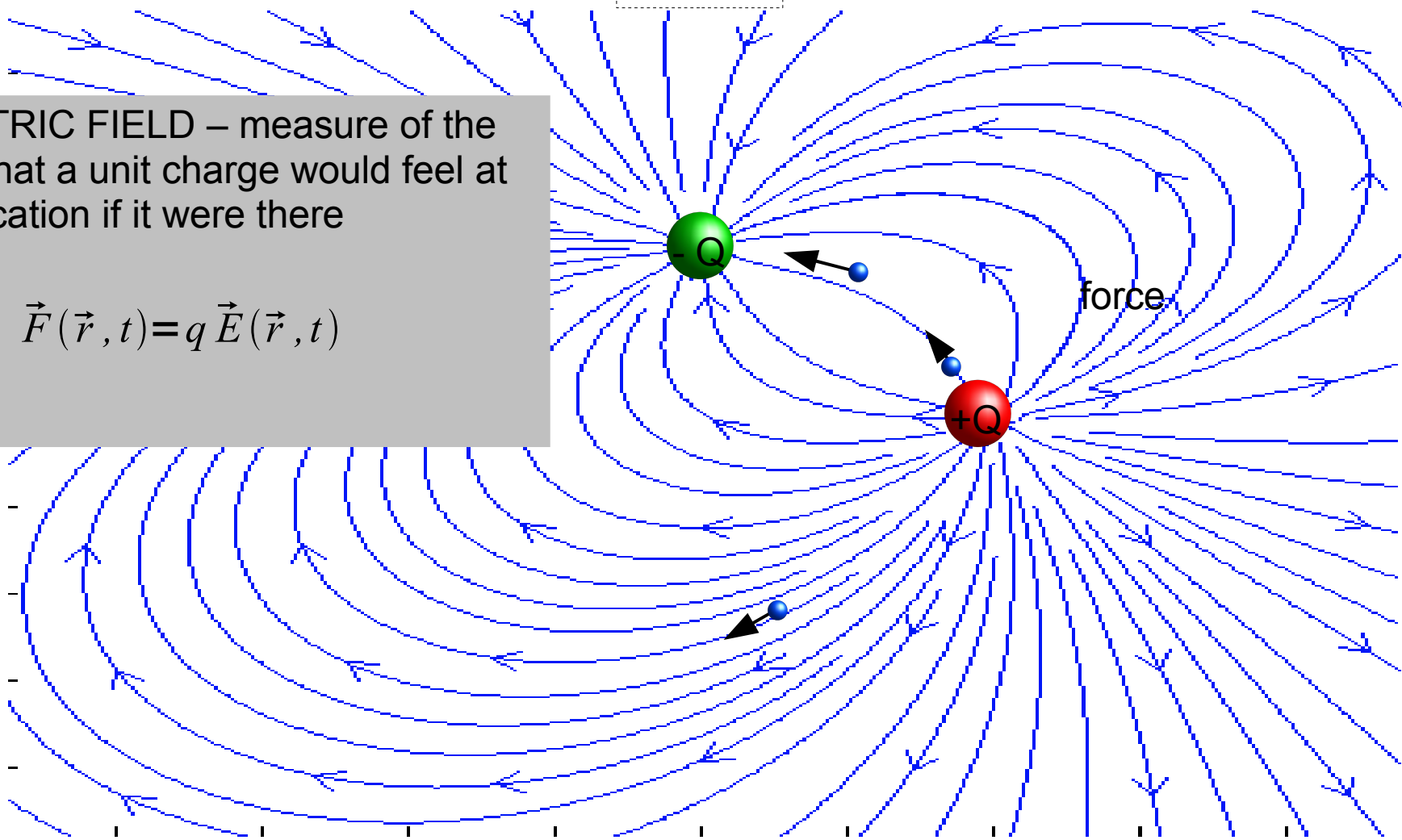


FIELDS

ELECTRIC FIELD – measure of the force that a unit charge would feel at any location if it were there

$$\vec{F}(\vec{r}, t) = q \vec{E}(\vec{r}, t)$$

force



Maxwell equations in integral and differential form

Name	Differential form	Integral form
Gauss's law	$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$	$\oiint_{\partial V} \mathbf{E} \cdot d\mathbf{A} = \frac{Q(V)}{\epsilon_0}$
Gauss's law for magnetism	$\nabla \cdot \mathbf{B} = 0$	$\oiint_{\partial V} \mathbf{B} \cdot d\mathbf{A} = 0$
Maxwell–Faraday equation (Faraday's law of induction)	$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$	$\oint_{\partial S} \mathbf{E} \cdot d\mathbf{l} = -\frac{\partial \Phi_{B,S}}{\partial t}$
Ampère's circuital law (with Maxwell's correction)	$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}$	$\oint_{\partial S} \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_S + \mu_0 \epsilon_0 \frac{\partial \Phi_{E,S}}{\partial t}$

MATH Concepts -

• vector products

\mathbf{E} – electric field

\mathbf{B} – magnetic field (well not exactly)

the basis for these equations and all of the interesting phenomena are based on 2 very simple concepts:

- i) simple interaction between charged particles
- ii) delayed response to change

LORENTZ FORCE

Now that we have some notation and the concept of the definition of a field we can investigate how these 2 simple concepts lead to the equation set that is the basis for electromagnetic analysis.

i) simple interaction between charged particles

LORENTZ FORCE – if a charge particle moves in a space where electric and magnetic fields exist it will feel a force generated by both fields in accordance with the following formula:

$$\vec{F} = q \vec{E} + q \vec{v} \times \vec{B}$$

it is clear that, depending on one's frame of reference q , the charge particle experiencing the force may or may not be moving. Forces and charge are both quantities that are invariant under changes in reference frame.

WHAT DOES THIS IMPLY ABOUT E and B ?

Units in mksA system:

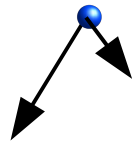
- $q [=] \text{C} = \text{sA}$,
- $E [=] \text{N/C} = \text{V/m}$,
- $B [=] \text{V.s/m}^2 = \text{Wb/m}^2 = \text{T}$,
- $\rho [=] \text{C/m}^3$,
- $J [=] \text{A/m}^2$,

where
 C , N , V , Wb , and T
are abbreviations for
Coulombs, *Newtons*, *Volts*, *Webers*, and ,
respectively.

Charge q is quantized in units of
 $e = 1.602 \times 10^{-19} \text{ C}$, a relativistic
invariant.

LORENTZ FORCE

i) delayed response to change – this is the property that has allowed electromagnetic theory to remain in tact despite upheavals in the approach to physics brought on by the advent of relativity and quantum mechanics.



What happens to the force that this charge feels?



from $t = -\infty$ to t_0
the green
charge is
stationary

moves with velocity v for $dt = 5s$



from $t = t_0 + v \cdot dt$ to
 ∞ the green
charge is again
stationary

REVIEW Problems

Coordinate systems/vector notation

Find the distance between two points in space.

- adding and subtracting vectors

Find the amount of work needed to move charges in electric and magnetic fields.

- adding and subtracting vectors
- dot (or scalar, or inner) product

Calculate the angular momentum of a rotating charge.

- adding and subtracting vectors
- cross (or vector, or outer) product

REVIEW Problems

Coordinate systems/vector notation

Find the distance between two points in space.

- adding and subtracting vectors

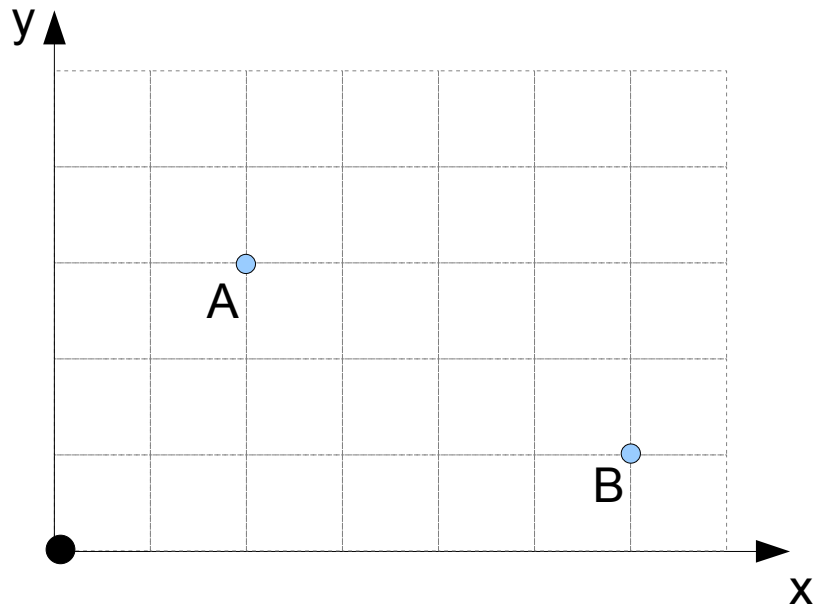


REVIEW Problems

Coordinate systems/vector notation

Find the distance between two points in space.

- adding and subtracting vectors



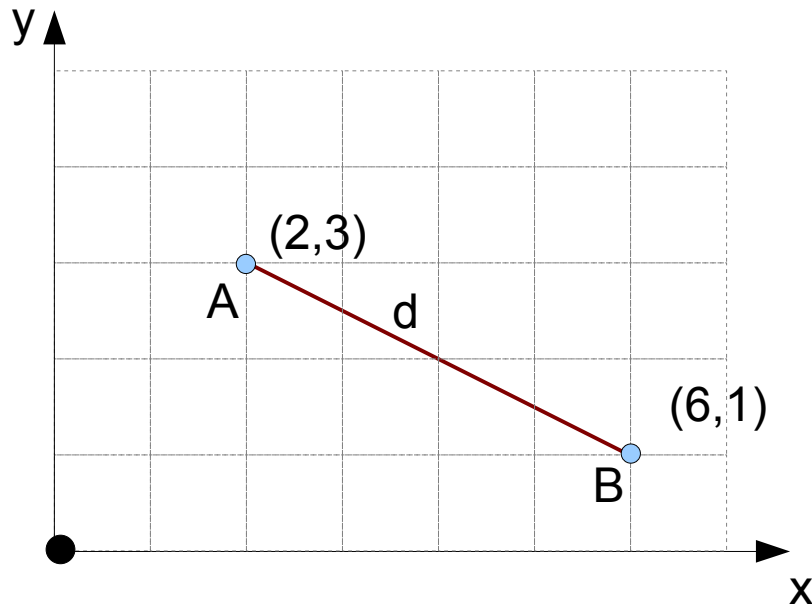
establish coordinate system and units

REVIEW Problems

Coordinate systems/vector notation

Find the distance between two points in space.

- adding and subtracting vectors



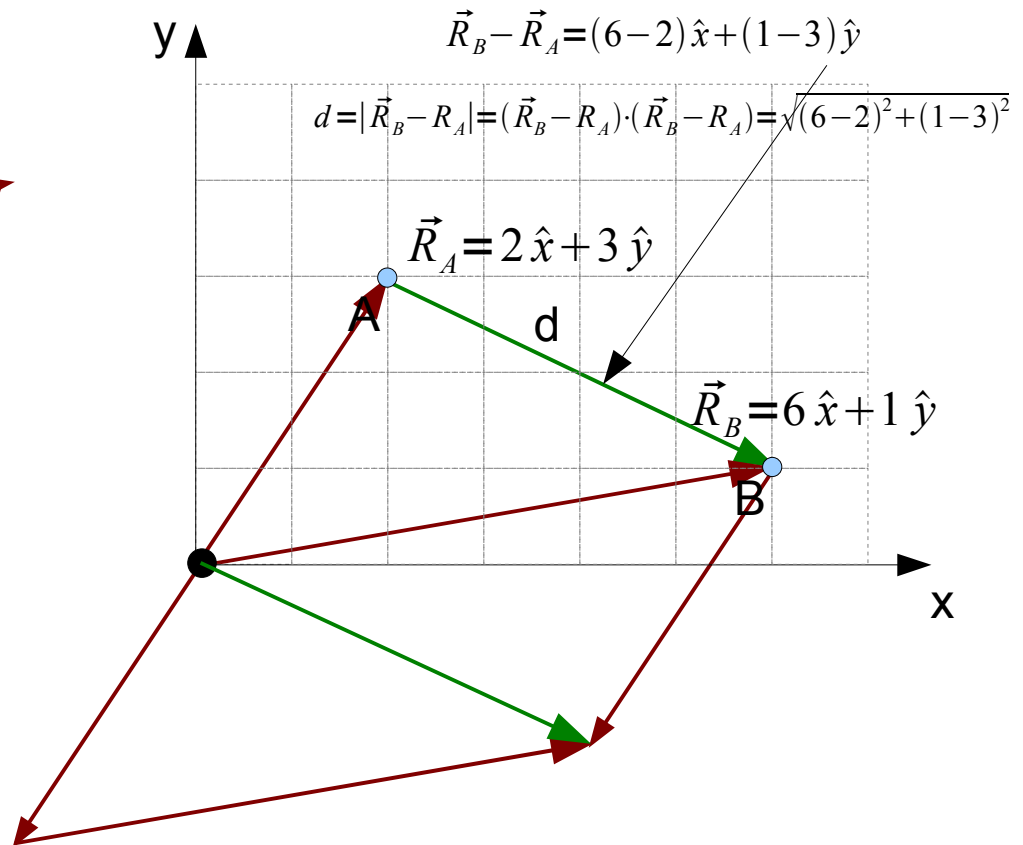
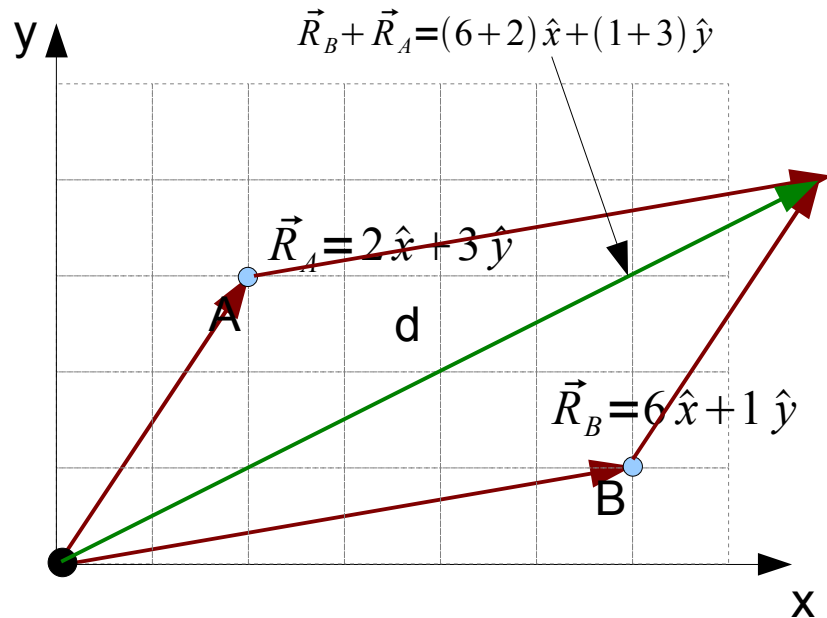
$$d = \sqrt{(2-6)^2 + (3-1)^2}$$

REVIEW Problems

Coordinate systems/vector notation

Find the distance between two points in space.

- adding and subtracting vectors

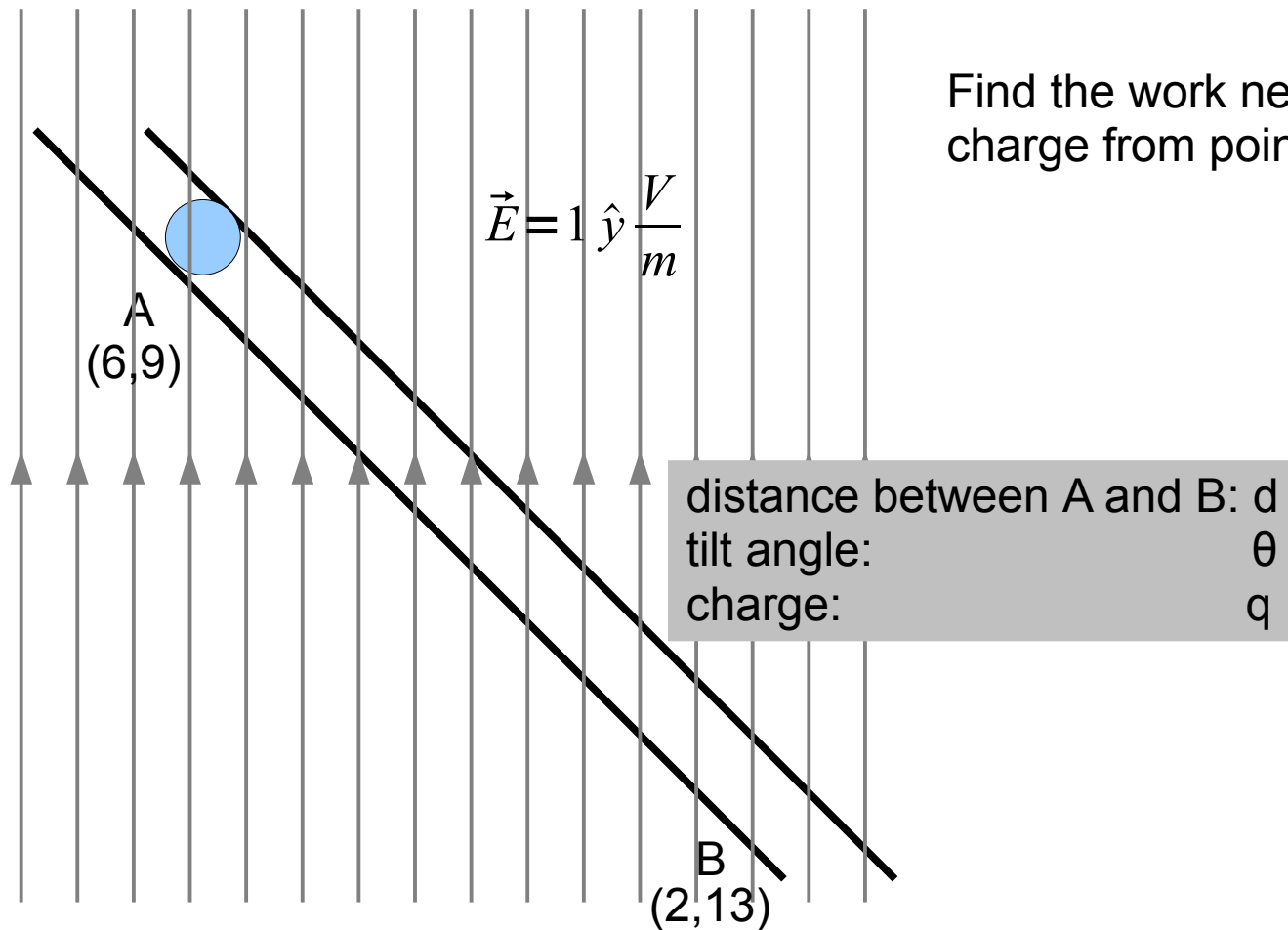


REVIEW Problems

Coordinate systems/vector notation

Find the amount of work needed to move charges in electric and magnetic fields.

- adding and subtracting vectors
- dot (or scalar, or inner) product



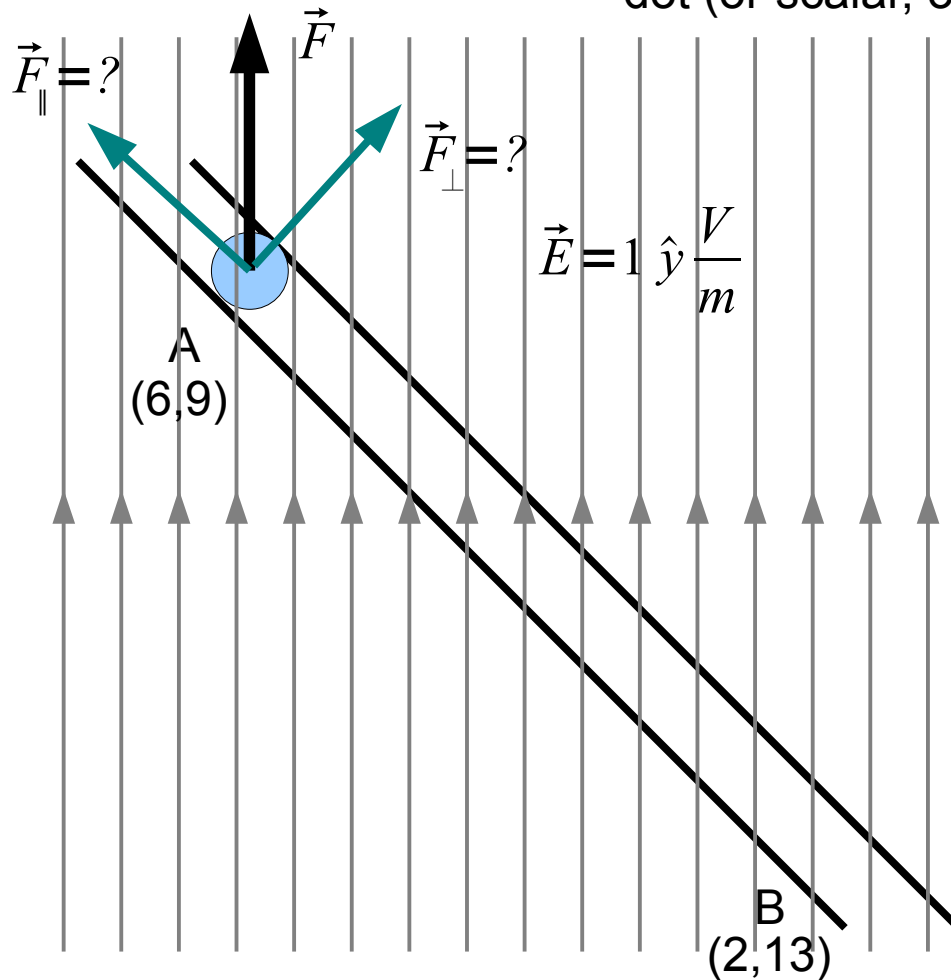
Find the work needed to move the charge from point A to point B

REVIEW Problems

Coordinate systems/vector notation

Find the amount of work needed to move charges in electric and magnetic fields.

- adding and subtracting vectors
- dot (or scalar, or inner) product



$$|\vec{F}_{\parallel}| d = \text{work}$$

REVIEW Problems

Lorentz Force

calculate the position and velocity of a particle in an electric and/or magnetic field

calculate the electric and magnetic fields present by the motion of charged particles

REVIEW Problems

Lorentz Force

calculate the position and velocity of a particle in an electric and/or magnetic field

$$\vec{F} = m \vec{a} = q \vec{E}$$

$$ma_x = qE_x$$

$$ma_y = qE_y$$

$$ma_z = qE_z$$

REVIEW Problems

Lorentz Force

calculate the position and velocity of a particle in an electric and/or magnetic field

Suppose $E_x = E_o$ and $E_y = E_o$

What do we expect to happen?

$$ma_x = m \frac{dv_x}{dt} = qE_o \quad \text{or} \quad \frac{dv_x}{dt} = \frac{q}{m} E_o$$

this is a simple differential equation that can be solved by simply integrating in time to get -

$$v_x = \frac{q}{m} E_o t + v_o$$

REVIEW Problems

Lorentz Force

$$v_x = \frac{q}{m} F_o t + v_o$$

$$x = \frac{q}{2m} E_o t^2 + v_{ot} + x_o$$

The velocity is shown to increase linearly in time going faster and faster with no limit in the direction of the field – IS THIS CORRECT?

REVIEW Problems

Lorentz Force

calculate the position and velocity of a particle in an electric and/or magnetic field

$$\vec{F} = m \vec{a} = q \vec{E}$$

$$ma_x = qE_x$$

$$ma_y = qE_y$$

$$ma_z = qE_z$$

REVIEW Problems

Lorentz Force

calculate the position and velocity of a particle in an electric and/or magnetic field

Suppose $B_z = B_0$

What do we expect to happen?

$$m \frac{dv_x}{dt} = q B_0 v_y$$
$$m \frac{dv_y}{dt} = -q B_0 v_x$$

$$\vec{F} = q \vec{v} \times \vec{B}$$

this is a simple differential equation set of second order with constant coefficients whose solutions are of the form $v_x = A e^{st}$

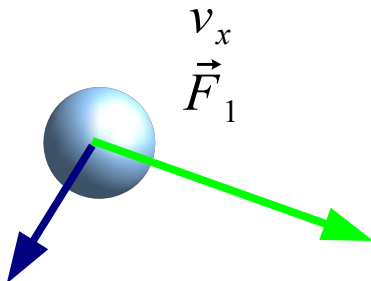
$$\frac{d^2 v_x}{dt^2} + \frac{q^2 B_0^2}{m^2} v_x = 0$$

REVIEW Problems

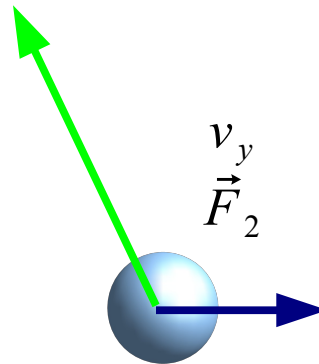
Lorentz Force

calculate the electric and magnetic fields present by the motion of charged particles

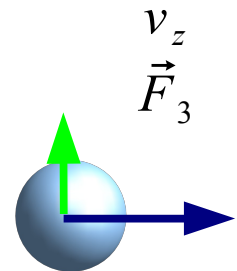
A constant electric field and a constant magnetic field MAY exist – either or both can be present. Suppose you want to know the magnitude and direction of the fields and all you have is a single test charge. What experiment would you perform?



move charge a little bit
in the x-direction and
measure the force



move charge a little bit
in the y-direction and
measure the force

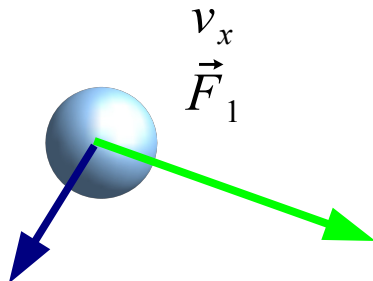


move charge a little bit
in the z-direction and
measure the force

REVIEW Problems

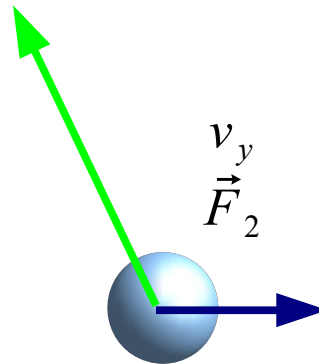
Lorentz Force

$$\begin{aligned} F_{1x} &= qE_x \\ F_{1y} &= qE_y - q(v_x B_z) \\ F_{1z} &= qE_z + q(v_x B_y) \end{aligned}$$



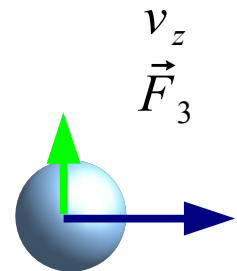
move charge a little bit
in the x-direction and
measure the force

$$\begin{aligned} F_{2x} &= qE_x + q(v_y B_z) \\ F_{2y} &= qE_y \\ F_{2z} &= qE_z - q(v_y B_x) \end{aligned}$$



move charge a little bit
in the y-direction and
measure the force

$$\begin{aligned} F_{3x} &= qE_x - q(v_z B_y) \\ F_{3y} &= qE_y + q(v_z B_x) \\ F_{3z} &= qE_z \end{aligned}$$



move charge a little bit
in the z-direction and
measure the force

measured quantities

known experiment parameters

desired quantities

REVIEW Problems

Lorentz Force

calculate the electric and magnetic fields present by the motion of charged particles

A constant electric field and a constant magnetic field MAY exist – either or both can be present. Suppose you want to know the magnitude and direction of the fields and all you have is a single test charge. What experiment would you perform?

$$\vec{F}_1 = 0 \quad V_x = 0$$

$$\vec{F}_2 = 0 \quad V_y = 0$$

$$\vec{F}_3 = A \hat{z} \quad V_z = 1$$

no information
about the magnetic
field

$$\vec{F}_1 = 0 \quad V_x = 0$$

$$\vec{F}_2 = 0 \quad V_y = 1$$

$$\vec{F}_3 = A \hat{z} \quad V_z = 1$$

$$\vec{F}_1 = 0 \quad V_x = 0$$

$$\vec{F}_2 = 0 \quad V_y = 0$$

$$\vec{F}_3 = A \hat{z} \quad V_z = 1$$

some examples – charged particles moving in an antenna

what we know as propagating electromagnetic radiation could be computed this way, but it is completely impossible analytically using these two fundamental properties. It is almost impossible to compute the field of a single moving charge this way, but with perseverance... It was Faraday's and Maxwell's genius – particularly Maxwell to realize that the fields themselves have some very simple properties at a more abstract level which are more amenable to analysis. The sources and fields can be simply connected and – the fields can be substituted for the sources in many cases – radiation is a good example.

