

## HOUR EXAMINATION #1

**1) Write your official:**

Last Name (use capital letters): \_\_\_\_\_

First Name (use capital letters): \_\_\_\_\_

NetId & UIN: \_\_\_\_\_

**2) Write your name and section at the back of the test.**

**DO NOT TURN THIS PAGE UNTIL YOU ARE TOLD**

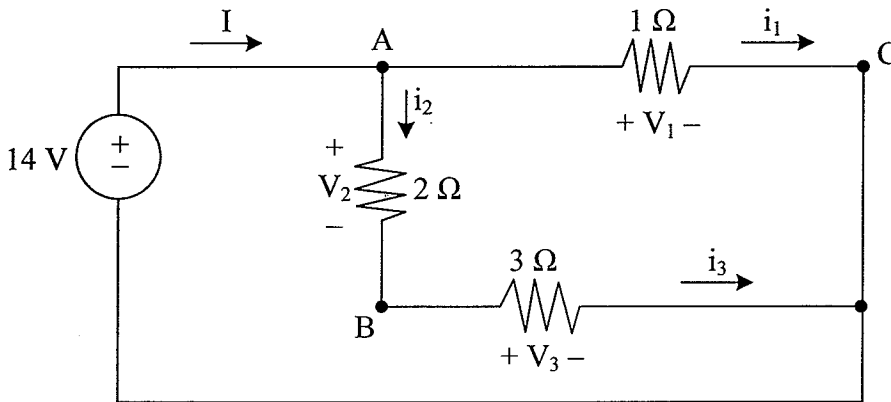
**Make sure to write your name AGAIN at the top of every page of your exam.**

A. Write or print clearly. Answer each problem on the exam itself. If you need extra paper, there is an extra sheet at the end of this exam. Clearly identify the problem number on any additional pages.

B. In order to receive **partial or full credit**, you must **show all your work**, e.g., your solution process, the equation(s) that you use, the values of the variables used in the equation(s), etc. You must also **include the unit of measurement** in each answer.

**Students caught cheating on this exam will earn a grade of F for the entire course. Other penalties may include suspension and/or dismissal from the university.**

**Problem 1 (40 points)**



- a) [6 pts.] Write two KVL equations (use only voltage parameters). Clearly indicate on the circuit which loop you are using.

① ..... ② .....

- b) [6 pts.] Write two KCL equations (use only current parameters). Clearly indicate which node you are using.

③ ..... ④ .....

- c) [6 pts.] Write three Ohm Law equations.

⑤ ..... ⑥ ..... ⑦ .....

- d) [6 pts.] Using equations above, solve the circuit. Clearly show all steps you are using.

(write answers on next page)

**Problem 1** (*continued*)

$i_1 =$

$i_2 =$

$i_3 =$

$V_1 =$

$V_2 =$

$V_3 =$

$I =$

**e)** [8 pts.] Compute the SRS power for each component. **Show work.**

$P(14\text{ V}) =$

$P(2\ \Omega) =$

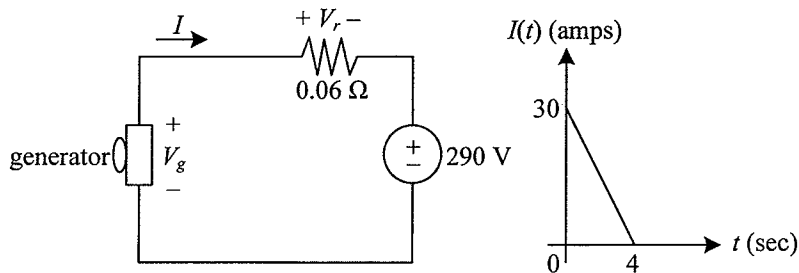
$P(1\ \Omega) =$

$P(3\ \Omega) =$

**f)** [8 pts.] Compute  $i_3$  using the Current Divider Rule. **Clearly show work** (showing a formula is not enough — explain what you do).

$i_3 =$

**Problem 2** (20 points) The kinetic energy of a Toyota Prius car is 53 kilojoules (kJ) when it travels at 20 miles per hour (mph). The car's regenerative braking system has a generator that converts the kinetic energy into electricity, which recharges the battery. We model the battery as a 290 V ideal voltage source and a  $0.06\ \Omega$  resistor. Starting from a speed of 20 mph, the brakes are applied at time  $t = 0$ , and the current  $I(t)$  from the generator decreases linearly from 30 A to 0 A at time  $t = 4$  seconds (sec).



- a) [2 pts.] Write a KVL equation that relates  $V_r$  and  $V_g$ .
- b) [4 pts.] Determine the value of  $V_g$  when  $I$  reaches 0. Explain your reasoning.

$$V_g = \boxed{\phantom{000000}}$$

- c) [8 pts.] Determine the average SRS power  $P_{avg}$  for the 290 V voltage source between 0 and 4 seconds. Show your work.

$$P_{avg} = \boxed{\phantom{000000}}$$

- d) [6 pts.] Determine the total amount of energy returned to the voltage source and the efficiency of the regenerating system in this case.

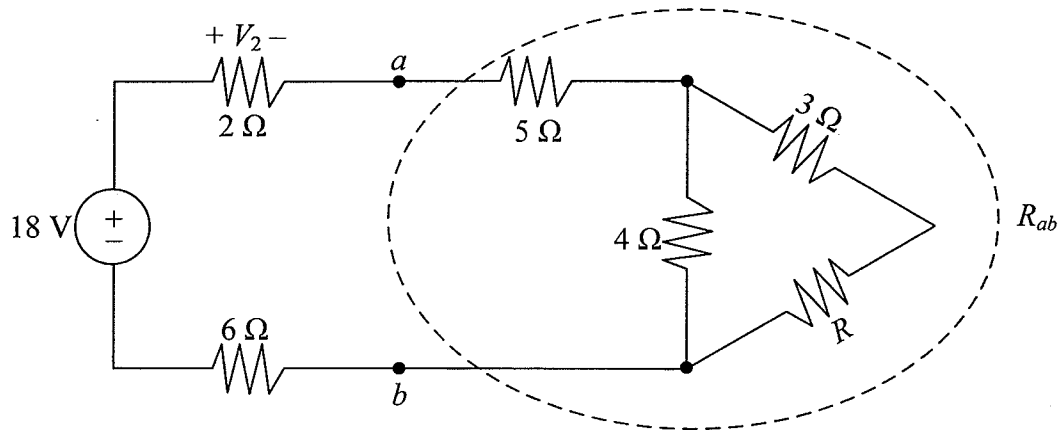
$$\text{Energy} = \boxed{\phantom{000000}}$$

$$\text{Efficiency} = \boxed{\phantom{000000}}$$

**Problem 3** (20 points)

- a) [10 pts.] Show that the equivalent resistance  $R_{ab}$  between node  $a$  and node  $b$  is  $\frac{9R + 47}{R + 7} \Omega$ .

Explain your reasoning using diagrams, formulas, and words.

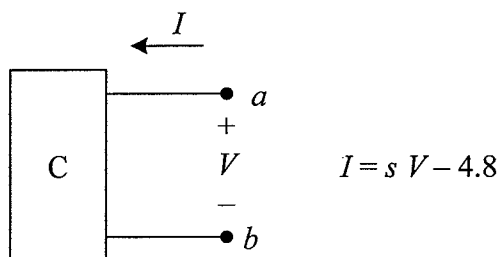


- b) [5 pts.] Using part a), explain why it is impossible to choose  $R$  so that  $R_{ab} < 6 \Omega$ .

- c) [5 pts.] Using the Voltage Divider Rule, determine the value of  $V_2$  when  $R_{ab} = 7 \Omega$ .

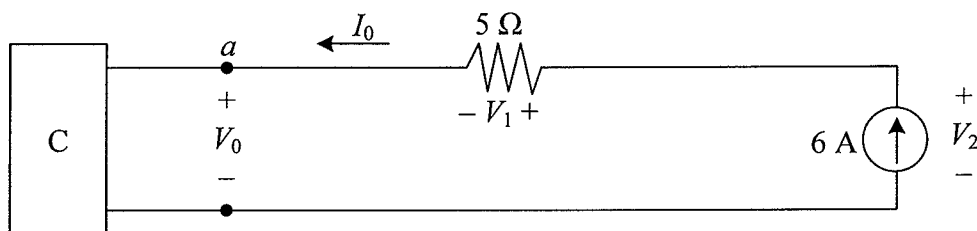
$$V_2 = \boxed{\phantom{000000}}$$

**Problem 4** (20 points) The component C below has the I-V characteristic shown, with an unknown constant  $s$ . The units are amps and volts.



a) [5 pts.] Can C be a single resistor (with no other components)? Answer *yes* or *no* or *insufficient information*, and **justify your answer**.

b) When C is connected to the resistor and ideal current source shown below, the operating voltage  $V_0$  is 9 V.



(i) [5 pts.] Determine the value of  $s$  (in amps/volts). **Show work.**

$s =$

(ii) [6 pts.] Determine the values of  $V_1$  and  $V_2$ . **Show work.**

$V_1 =$

$V_2 =$

(iii) [4 pts.] Does the 6 A current source generate or dissipate electrical power? **Justify your answer**. [HINT:  $V_2 > 0$ ]