

Attribute-Based Cryptography

Lecture 21
And Pairing-Based Cryptography

Identity-Based Encryption

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 - In IBE, **receiver has to obtain its SK** from the authority

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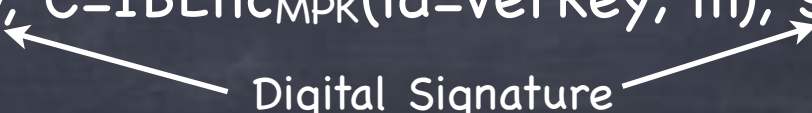
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- Without pairing: Using QR, Lattices, ...

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- Required to be not degenerate: $e(g, g) \neq 1$

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- **Decisional Bilinear DH assumption:** (g^a, g^b, g^c, g^{abc}) is indistinguishable from (g^a, g^b, g^c, g^z) . (a, b, c, z random)

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- CPA security based on Decisional-BDH

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- Ciphertexts can be created (by anyone) by incorporating attributes/policies

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- Application: End-to-End privacy in Attribute-Based Messaging

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 - Audit log inspection: grant auditor authority to read only messages with certain attributes

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 - Linear algebra over some finite field (e.g. $GF(p)$)
- For efficiency need a small matrix

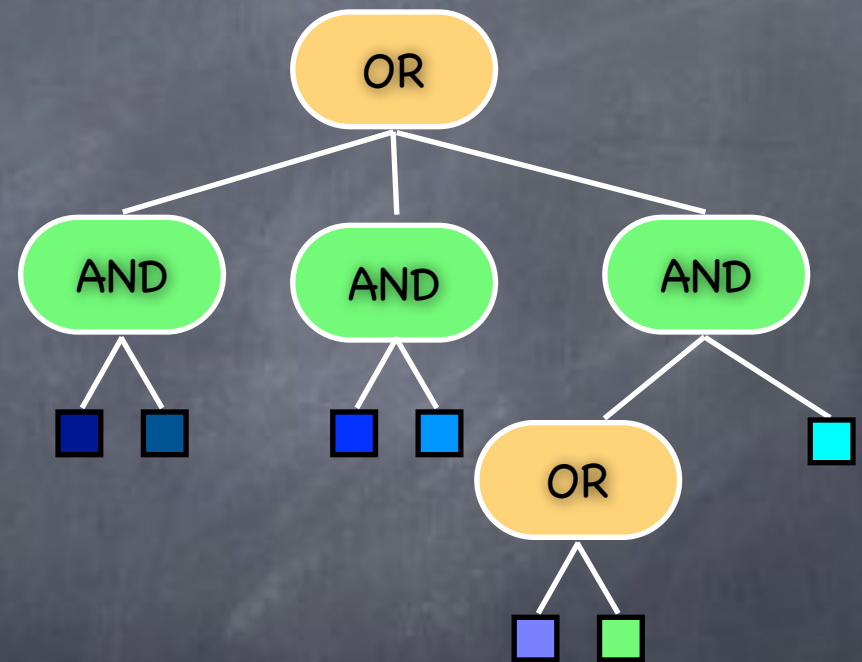
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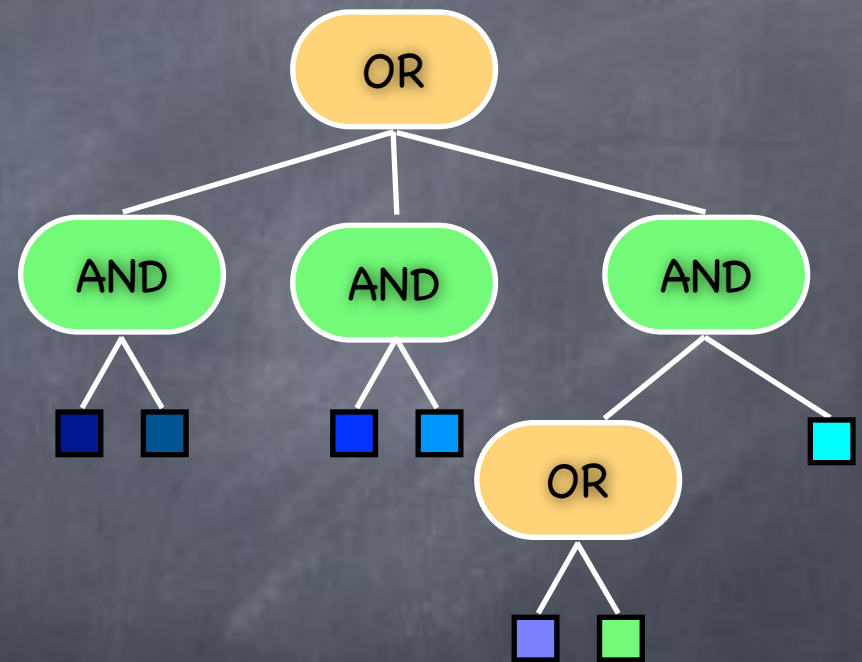
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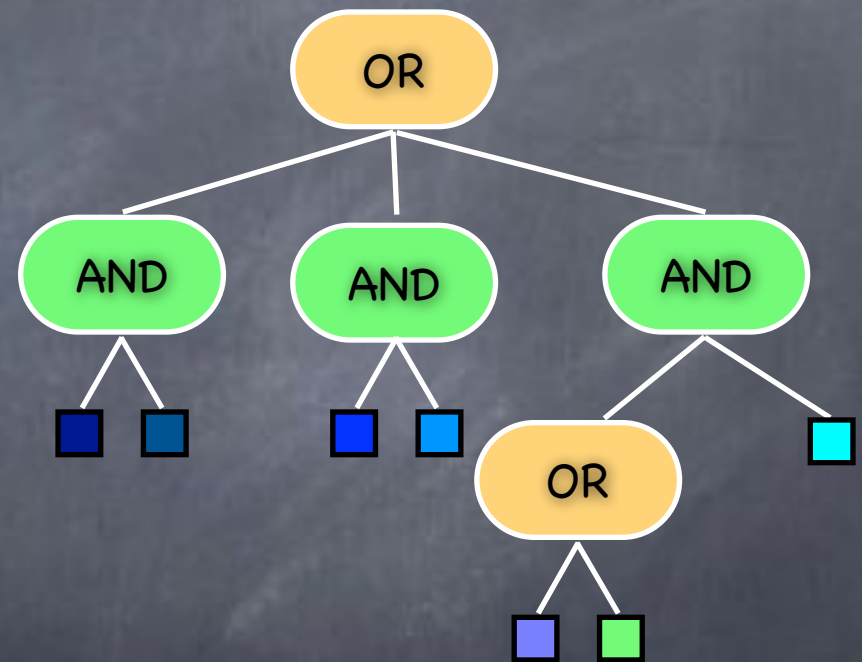


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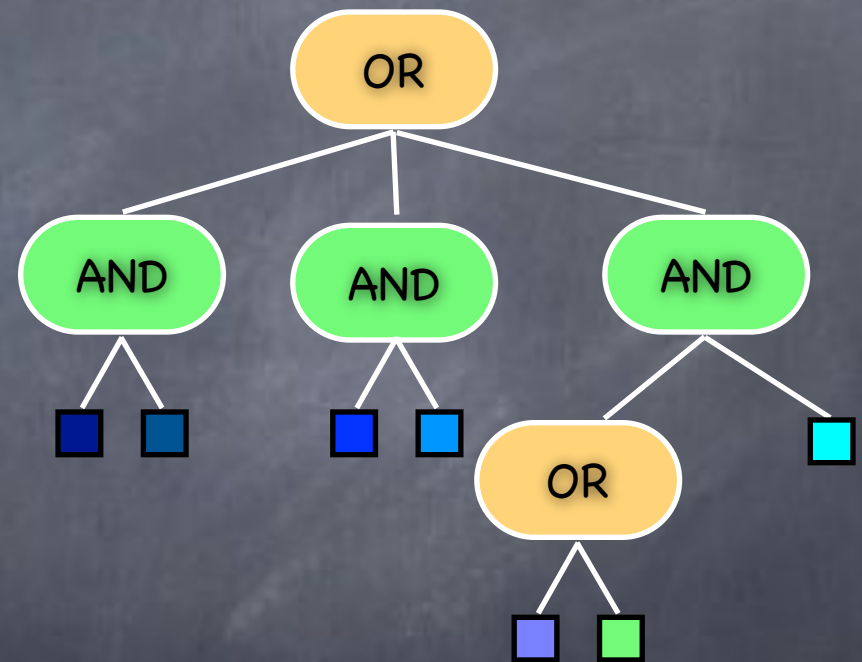


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- Can allow threshold gates too

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where $v = [v_1 \dots v_d]$ s.t. $v_i=0$ if $\text{label}(i) \notin A$, and $v_L=[1 \dots 1]$

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A KP-ABE Scheme

- MPK: $g, Y=e(g,g)^y, T = (g^{t^1}, \dots, g^{t^n})$ (n attributes)
- MSK: y and t_a for each attribute a
- $\text{Enc}(m, A; s) = (A, \{T_a^s\}_{a \in A}, M.Y^s)$
- SK for policy L (with d rows): Let $u=(u_1 \dots u_d)$ s.t. $\sum_i u_i = y$.
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 - Choosing a random vector u for each key helps in preventing collusion

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- Constructions based on the Decision Linear assumption
 - $(f, g, h, f^x, g^y, h^{x+y})$ and (f, g, h, f^x, g^y, h^z) indistinguishable for random f, g, h, x, y, z .

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- Using conventional tools. More efficiently using bilinear pairings.

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