

MAC. SKE in Practice.

Lecture 5

RECALL

Message Authentication Codes

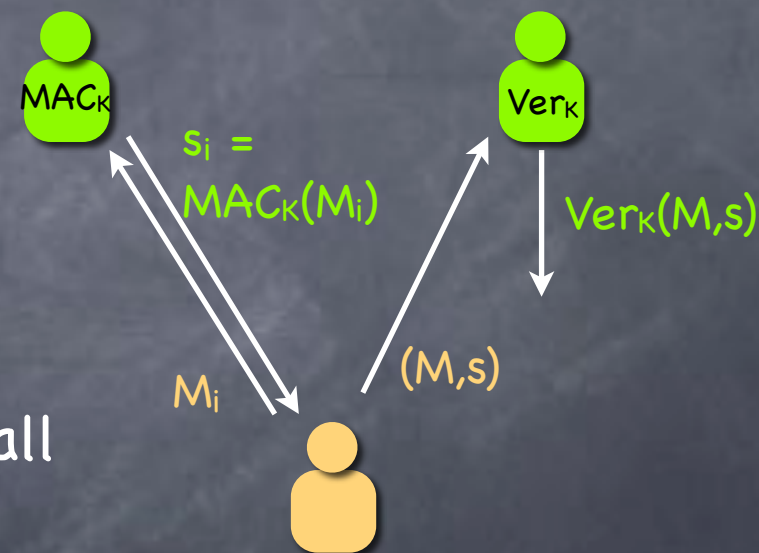
- A single short key shared by Alice and Bob

- Can sign any (polynomial) number of messages

- A triple (KeyGen, MAC, Verify)

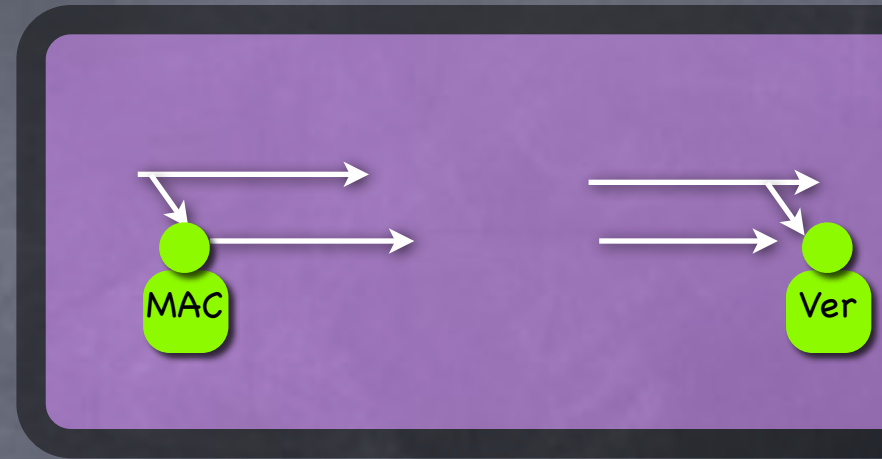
- Correctness: For all K from KeyGen, and all messages M , $\text{Verify}_K(M, \text{MAC}_K(M))=1$

- Security: probability that an adversary can produce (M,s) s.t. $\text{Verify}_K(M,s)=1$ is negligible unless Alice had computed and output $s=\text{MAC}_K(M)$



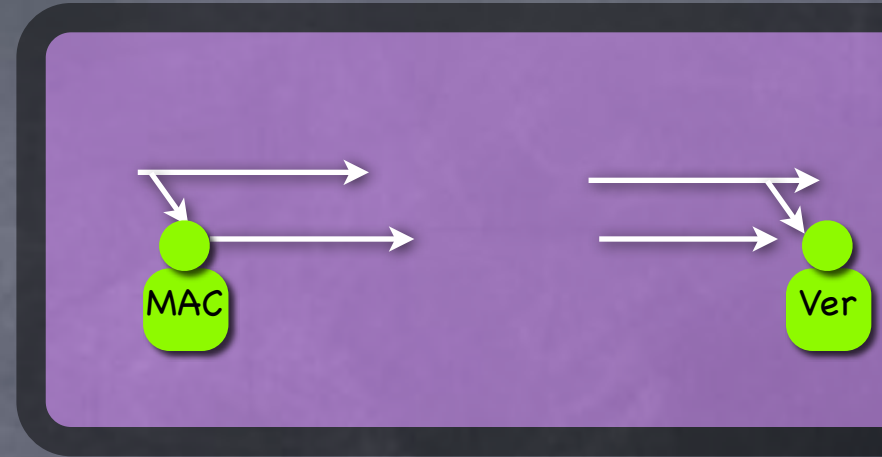
$$\text{Advantage} = \Pr[\text{Ver}_K(M,s)=1 \text{ and } (M,s) \notin \{(M_i,s_i)\}]$$

One-time MAC



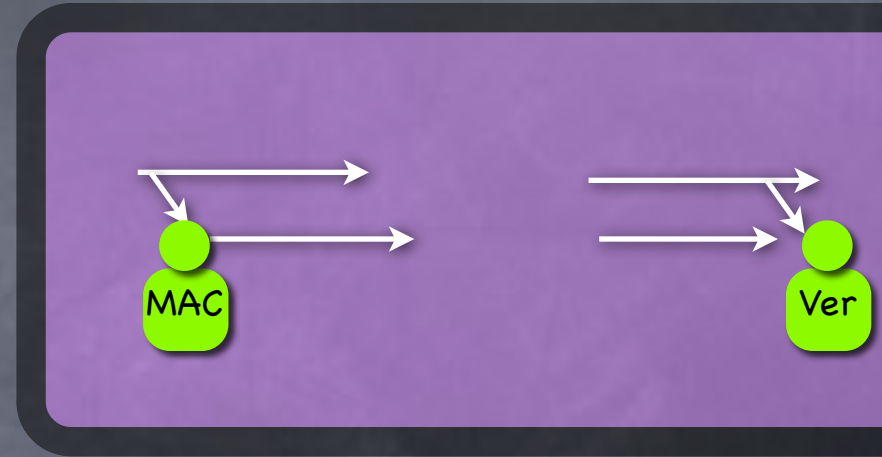
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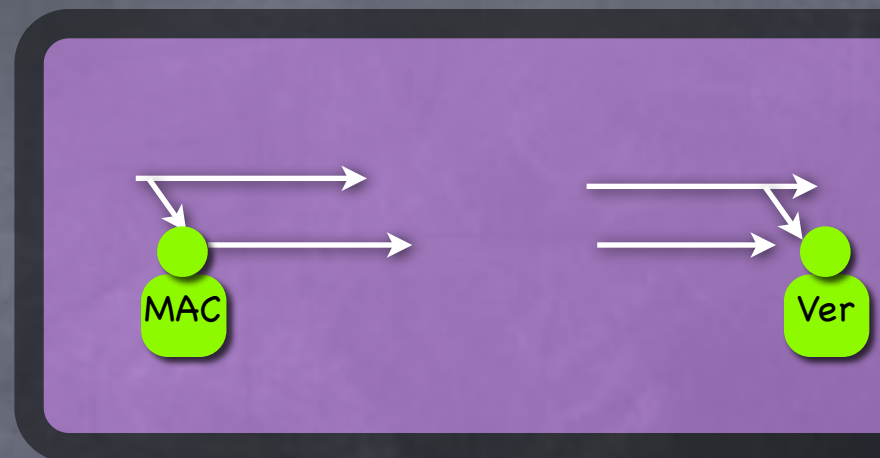
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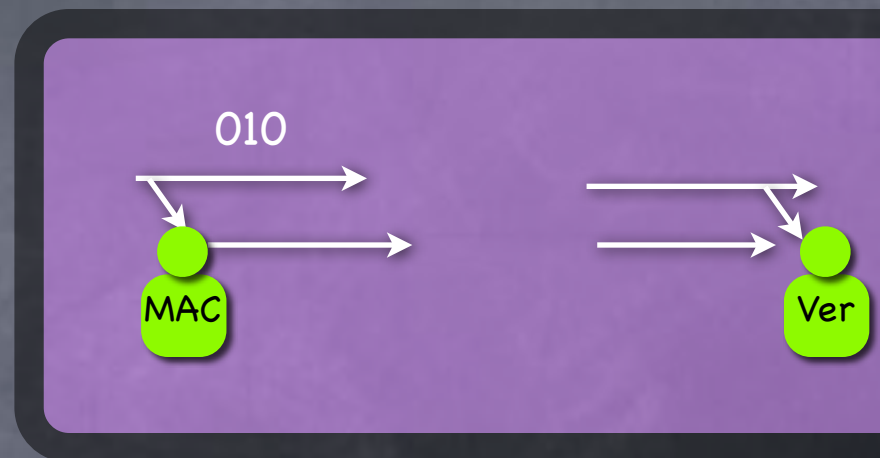
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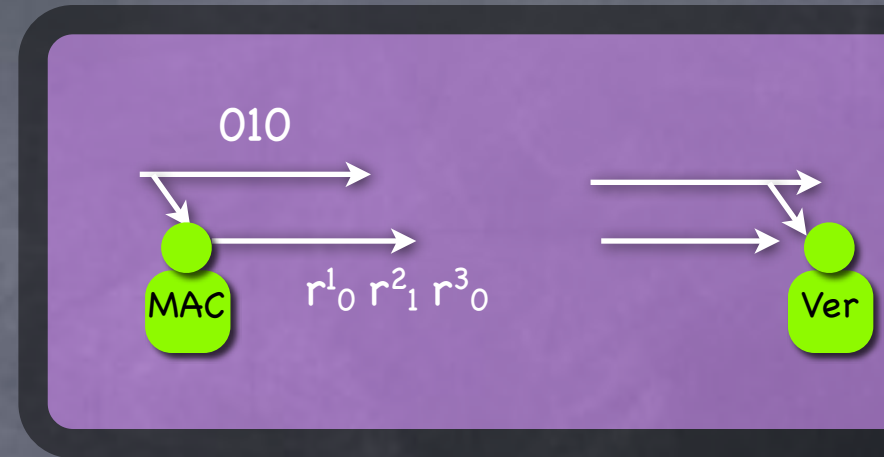
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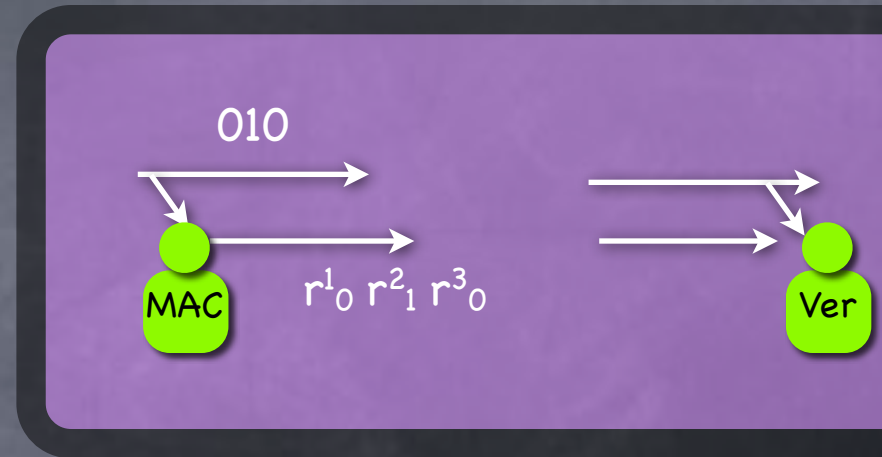
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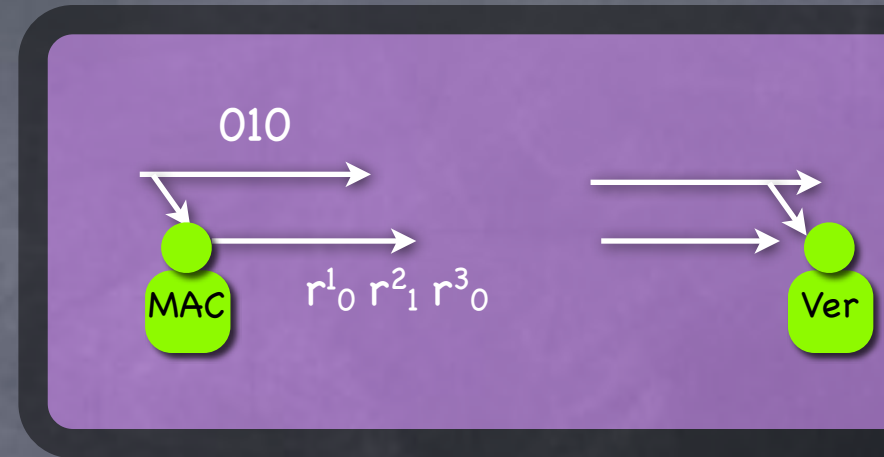
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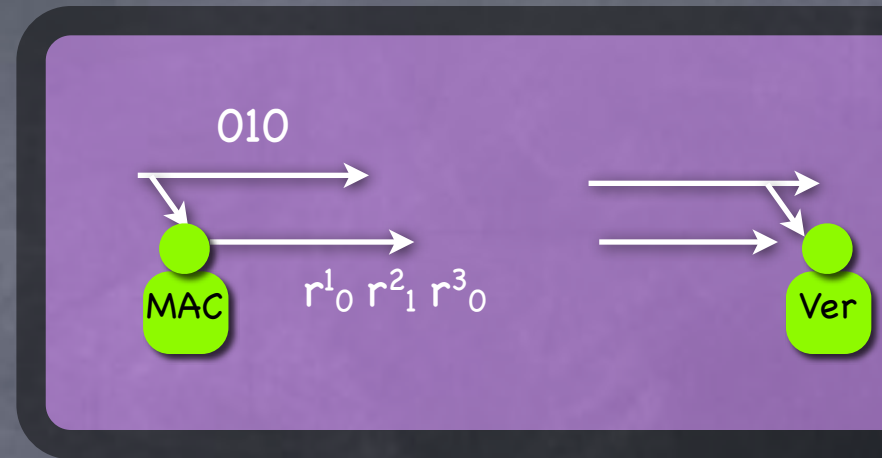
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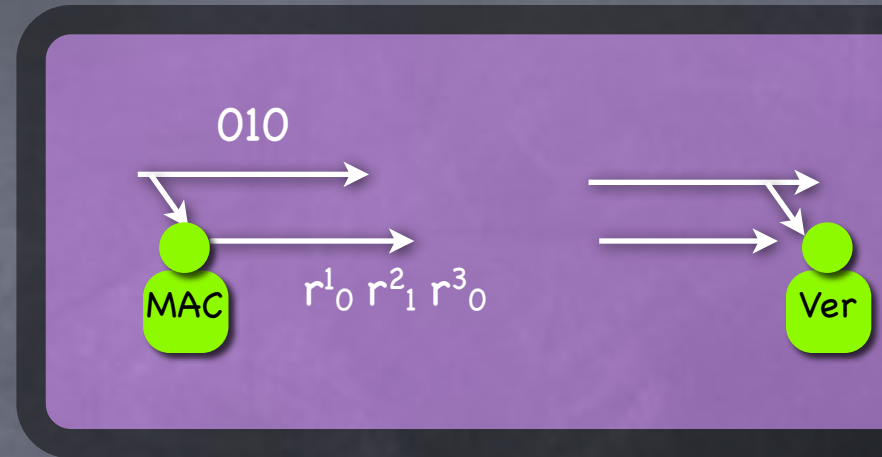
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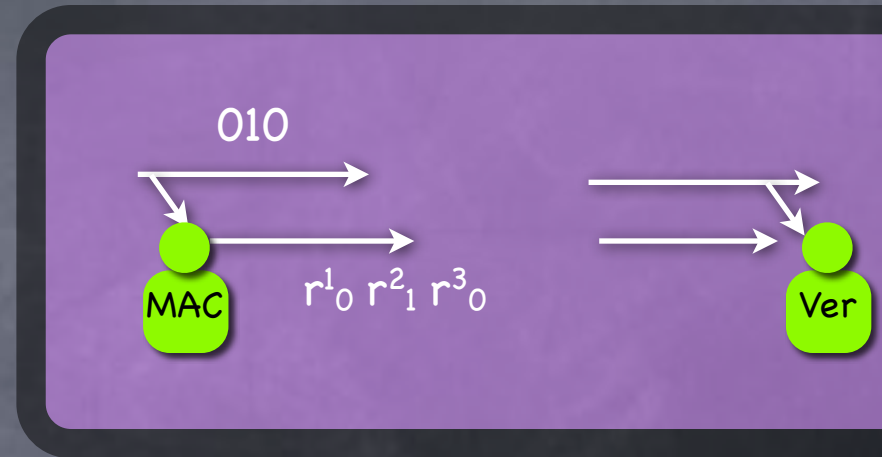
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 - No computational restriction on adversary



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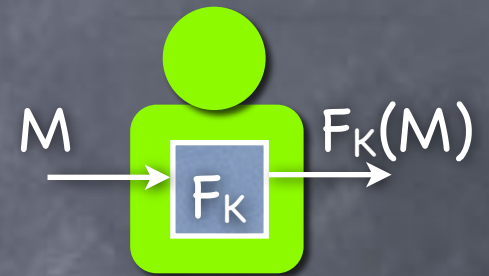
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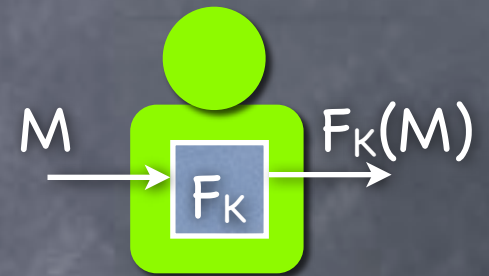
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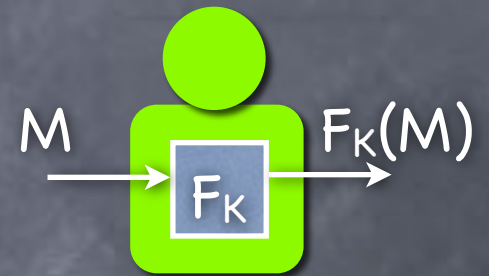
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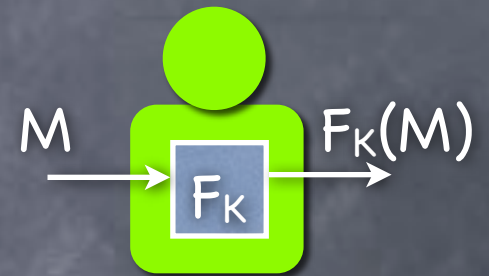
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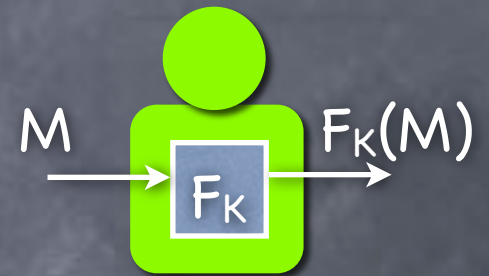
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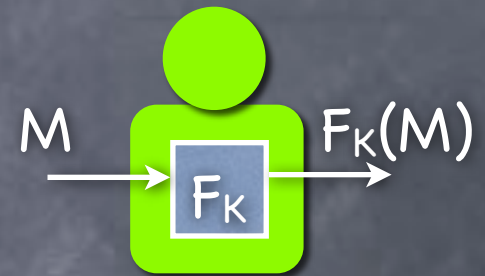
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Recall: advantage in breaking a PRF F is the diff in prob a test has of outputting 1, when given F vs. truly random R

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- Can we use a PRF with a fixed block-length (i.e., a block cipher)?

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- Inefficient! Tag length increases with message length

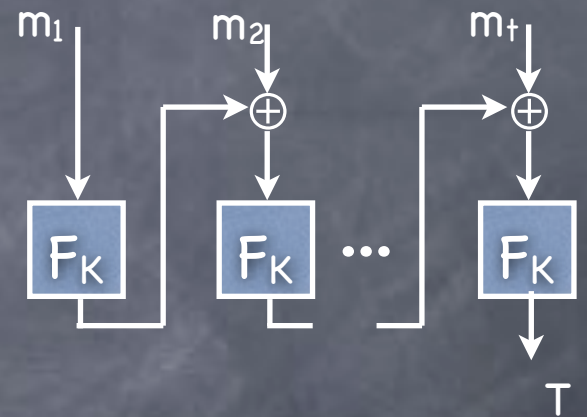
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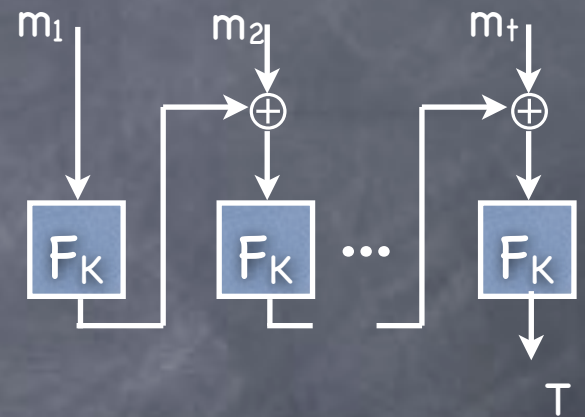
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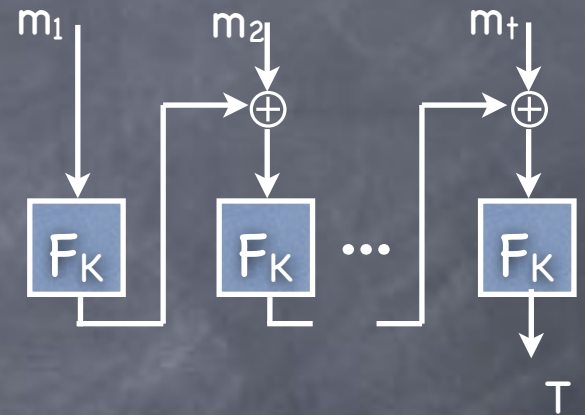
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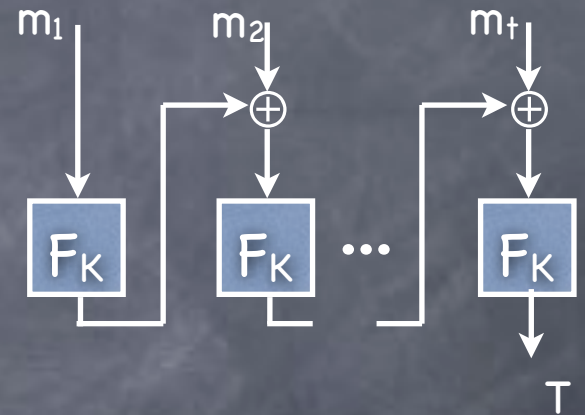
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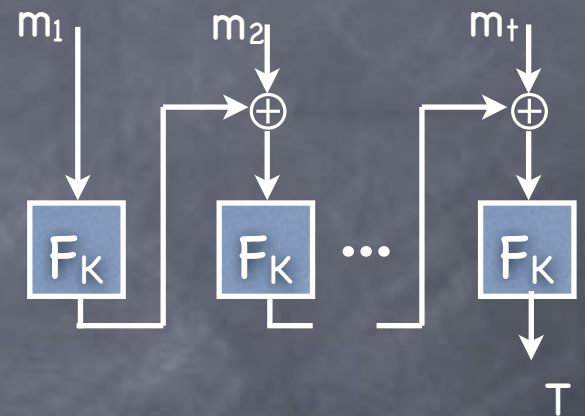
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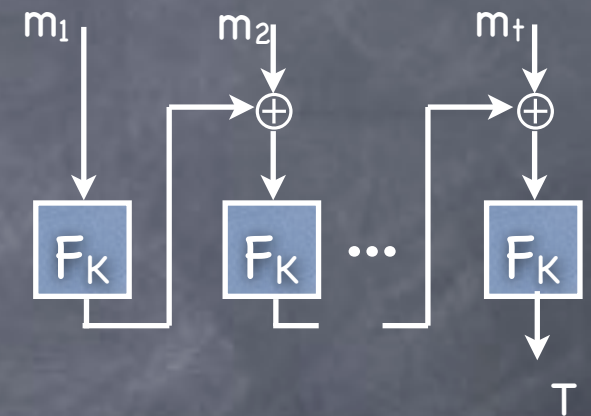
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- Later: Hash-based HMAC used in TLS and IPSec IETF Standard. 1997

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- NIST Standard: For multi-message encryption, use a block-cipher in CTR mode

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 - As a PRP (or at least, against key recovery)

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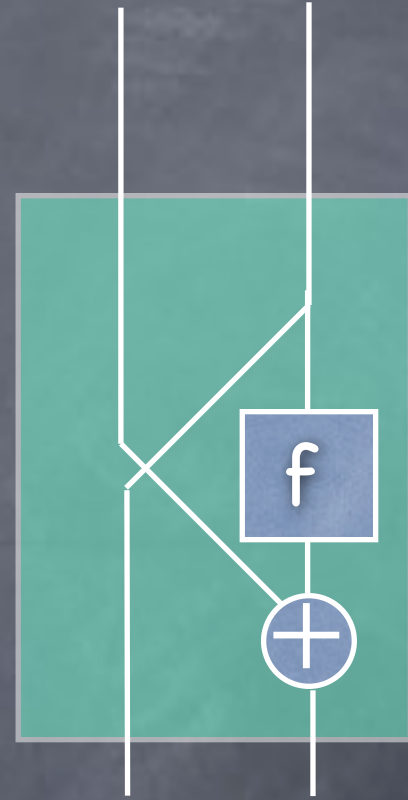
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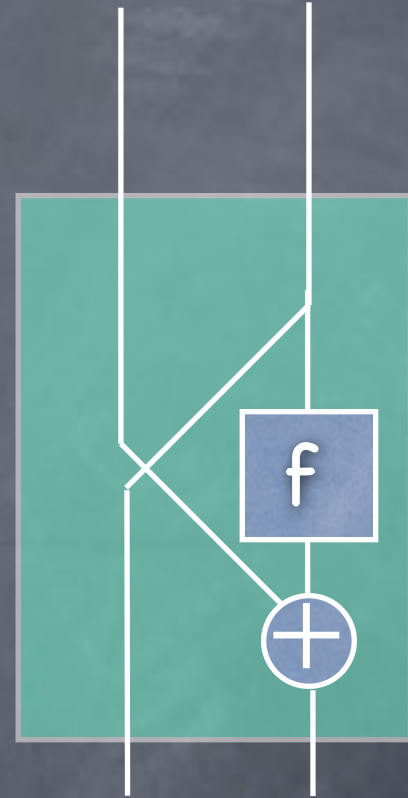
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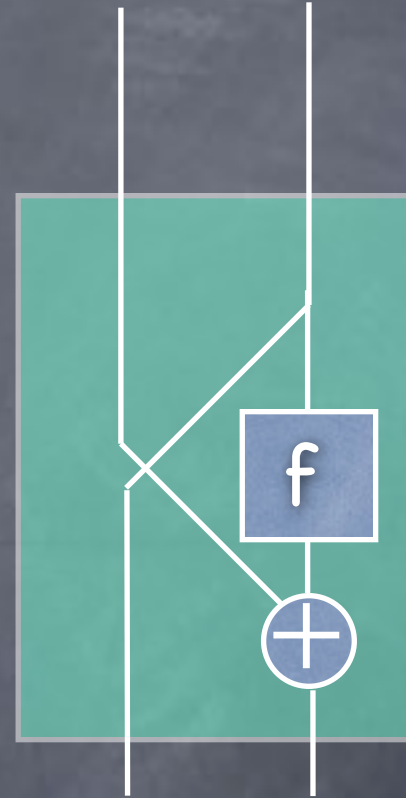
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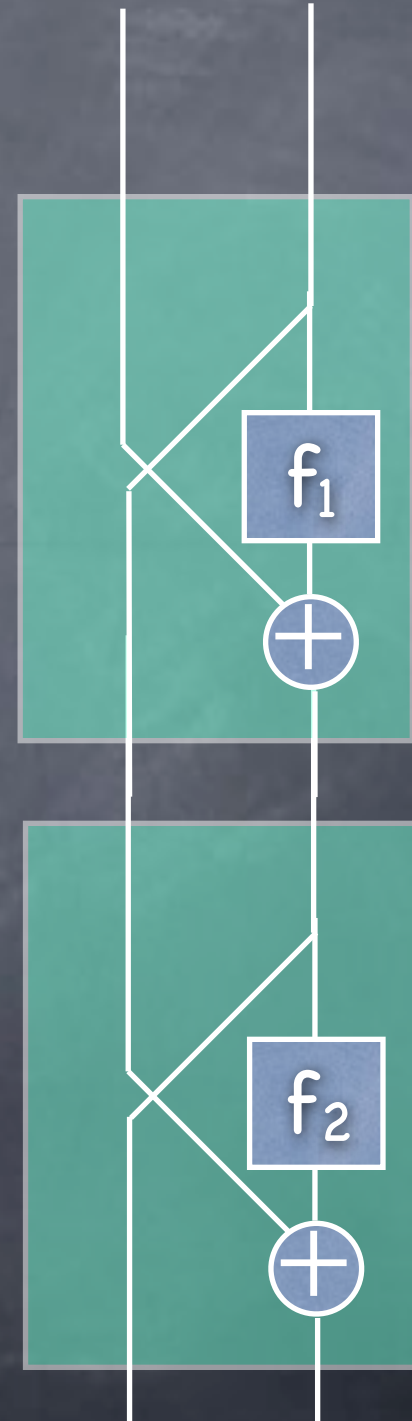
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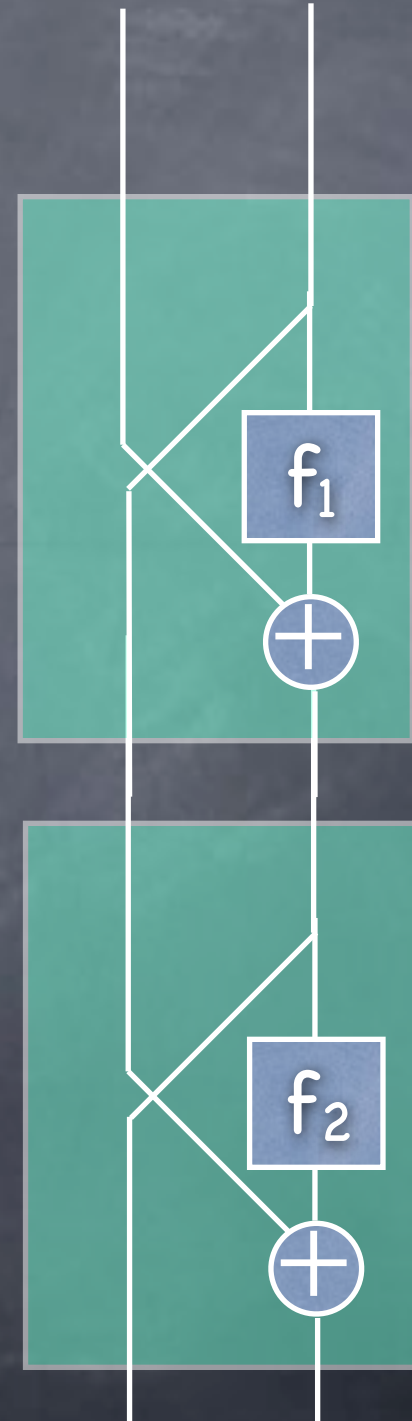
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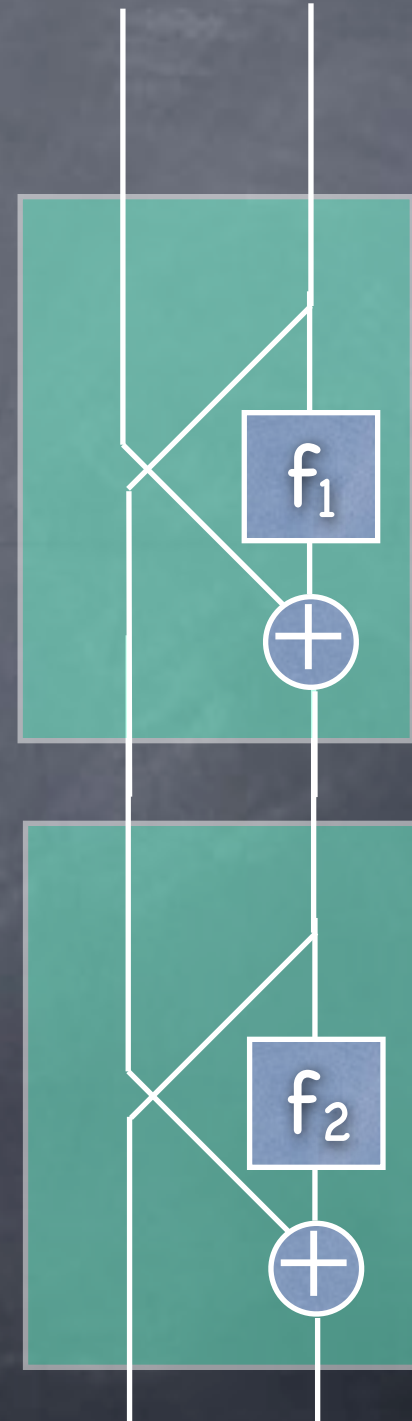
Feistel Network

- Building a permutation from a (block) function
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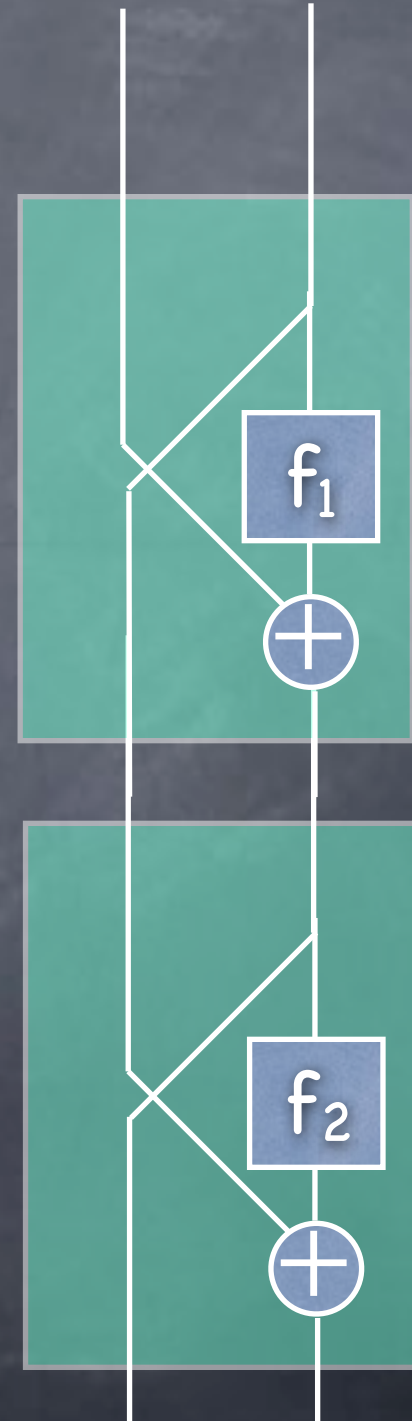
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- Fewer layers do not suffice! [Exercise]



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- Triple DES: 3 successive applications of DES (or DES^{-1}) with 3 keys

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 - No “simple” hardness assumption known to imply any sort of security for AES



General Math

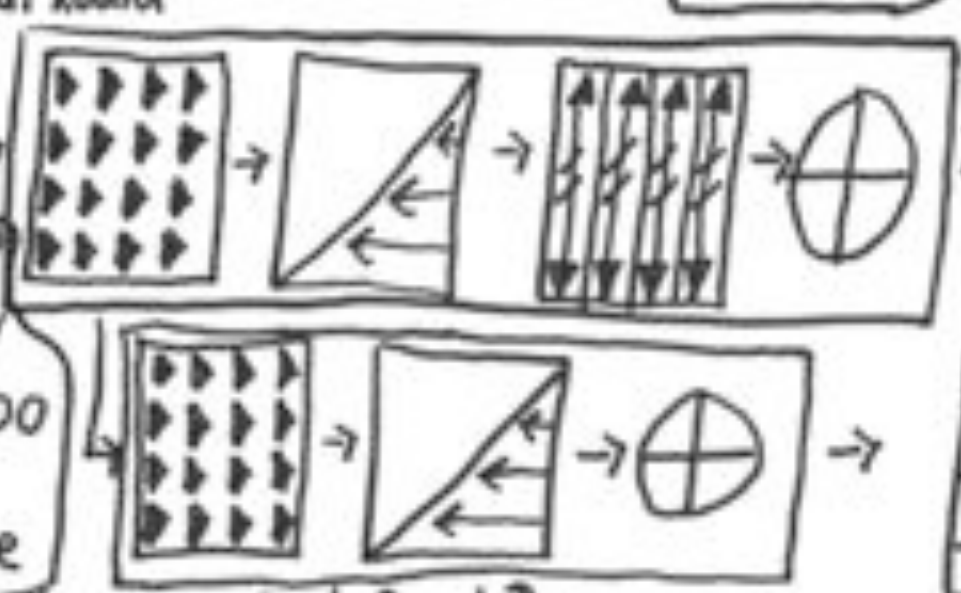
11B = AES Polynomial = $x^8 + x^4 + x^3 + x + 1$

Fast Multiply

$x \cdot a(x) = (a \ll 1) \oplus (a_7 = 1) ? 1B : 00$

$\log(x \cdot y) = \log(x) + \log(y)$

Use $(x+1) = 03$ for log base



Intermediate Rounds

#	Key
9	128
11	192
13	256

Ciphertext

?	?	?	?
?	?	?	?
?	?	?	?
?	?	?	?

S-Box (SRD)

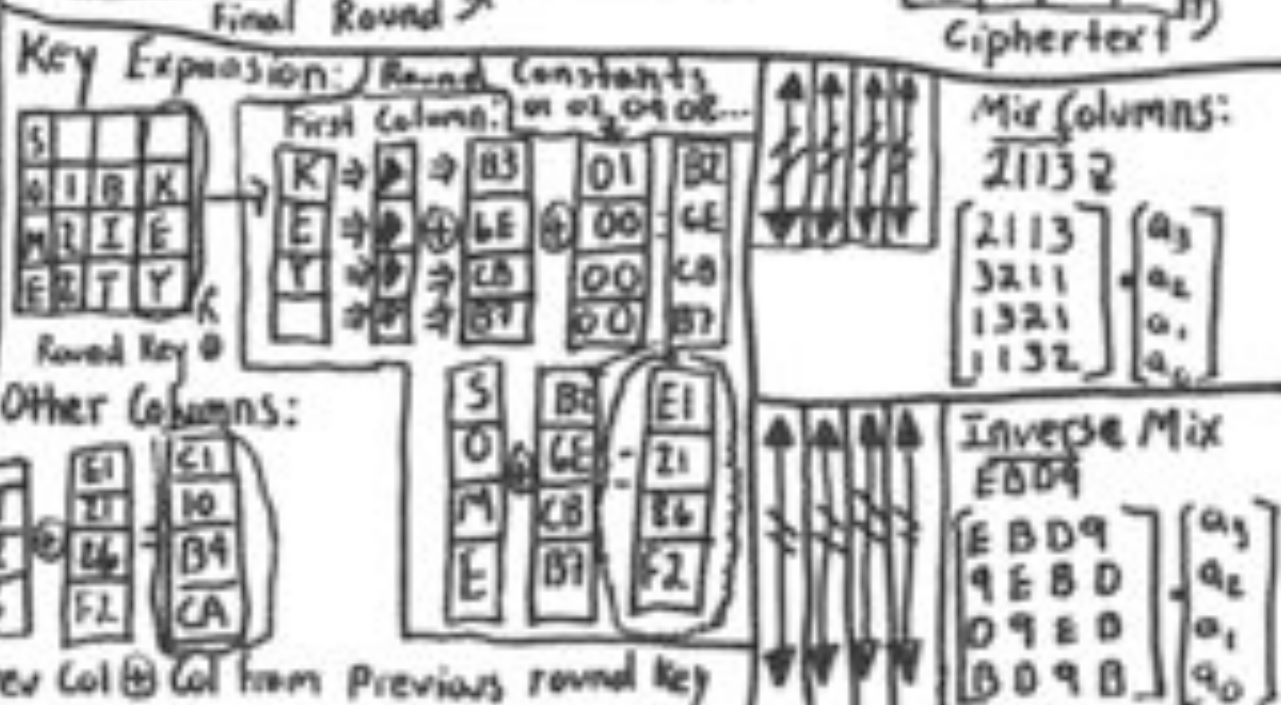
$SRD[a] = f(g(a))$

$g(a) = a^{-1} \text{ mod } m(x)$

See Think $53 \oplus 63$

5 is and 3 is $(0110 \ 0011)^T$

11111000	a_7	\oplus	00001
01111100	a_6		
00111110	a_5		
00011111	a_4		
10001111	a_3		
11000111	a_2		
11100011	a_1		
11110001	a_0		



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 - Meet-in-the-middle, linear cryptanalysis, differential cryptanalysis, impossible differential cryptanalysis, boomerang attack, integral cryptanalysis, cube attack, ...

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 - AE with Associated Data: Allows unencrypted (but authenticated) parts of the plaintext, for headers etc.

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 - e.g. RC4 in BitTorrent, Skype, PDF