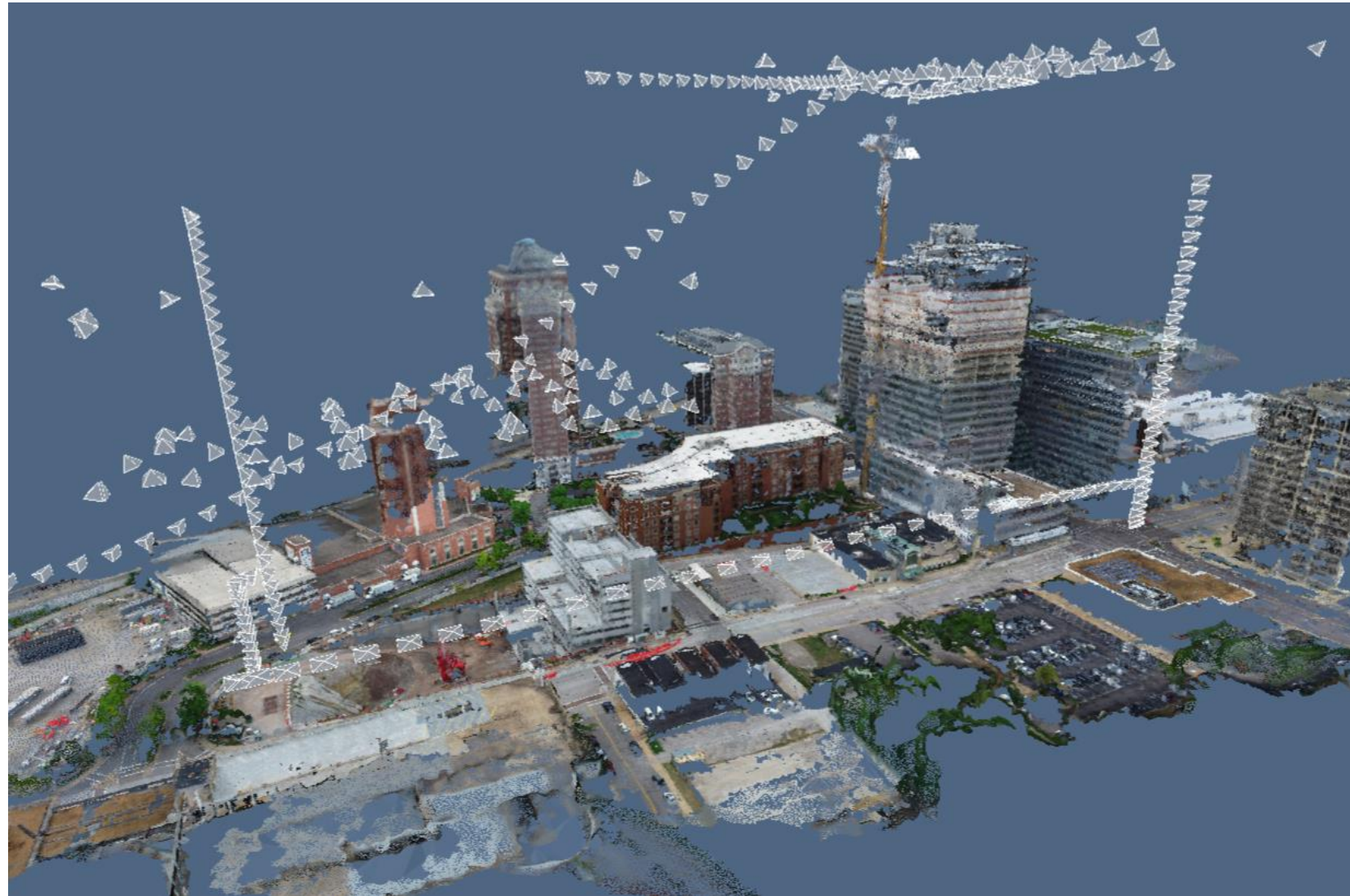


# 3D Vision

Derek Hoiem  
University of Illinois

Fall 2021



# Today's class

- A little about me
- Intro to 3D vision
- Course logistics
- 2D-3D Basics

# About me

Raised in “upstate” NY



# About me



**1998-2002**  
**Undergrad at SUNY Buffalo**  
B.S., EE and CSE



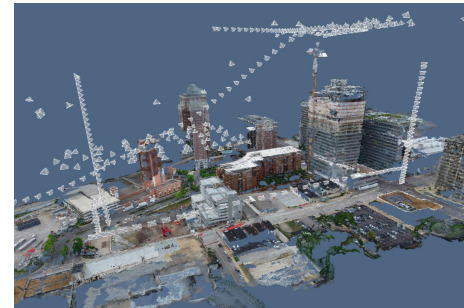
**2002-2007**  
**Grad at Carnegie Mellon**  
Ph.D. in Robotics



**2007-2008**  
**Postdoc at Beckman Institute**



**2009-**  
**Prof in CS at UIUC**



**2016-**  
**CTO / Chief  
Scientist  
Reconstruct**



# Computer vision provides situational awareness

What



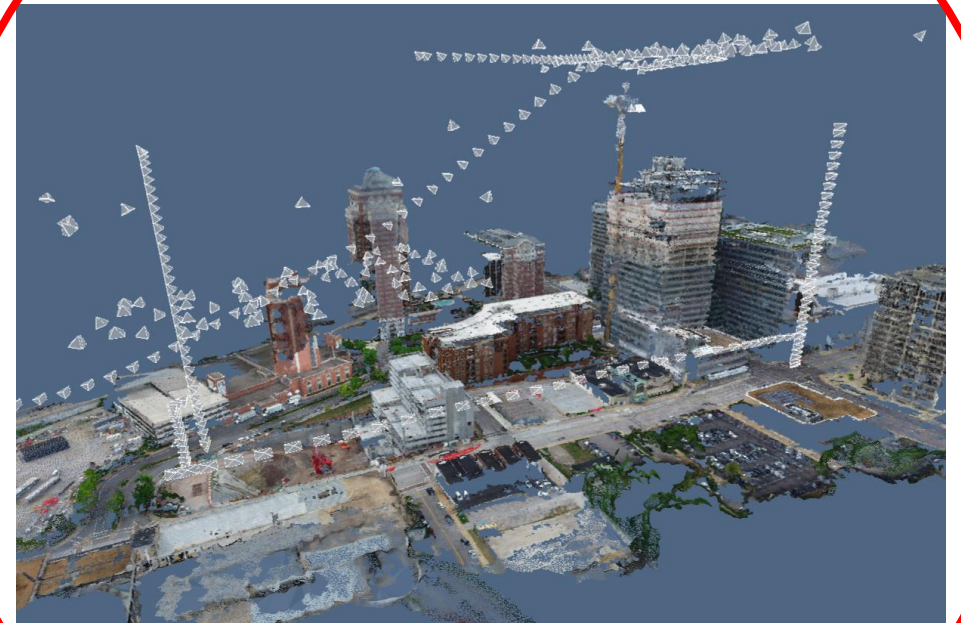
[Kirillov et al 2019]

Who



[Sun et al 2019]

Where

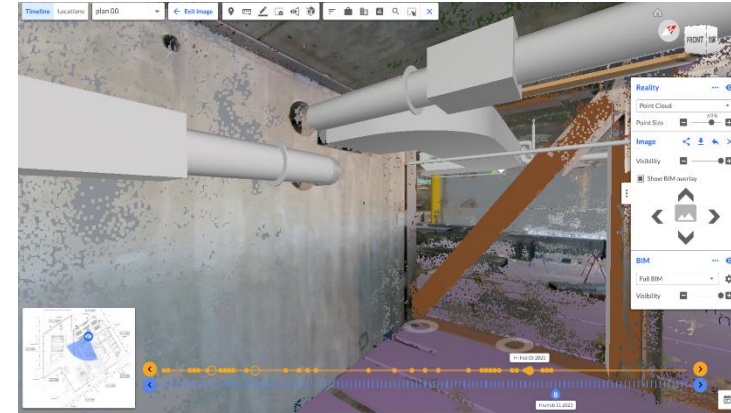


Reconstruct

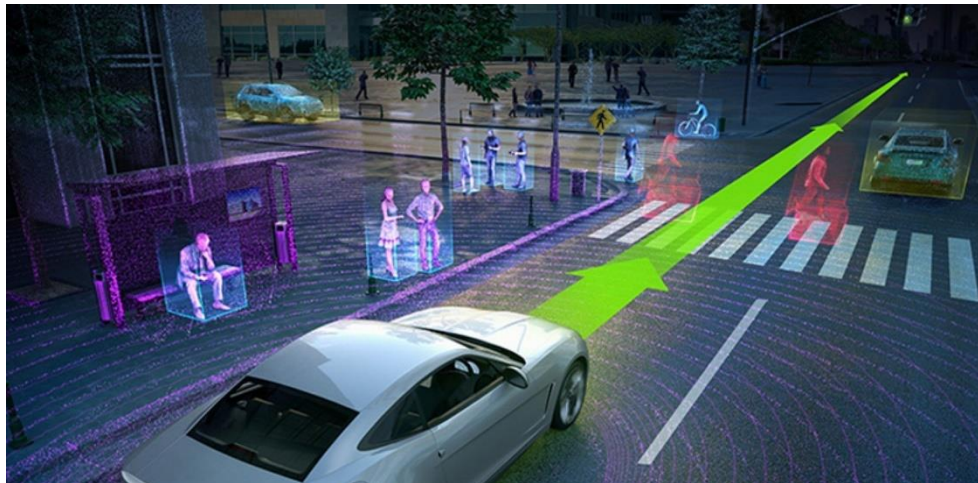
# 3D Vision Matters



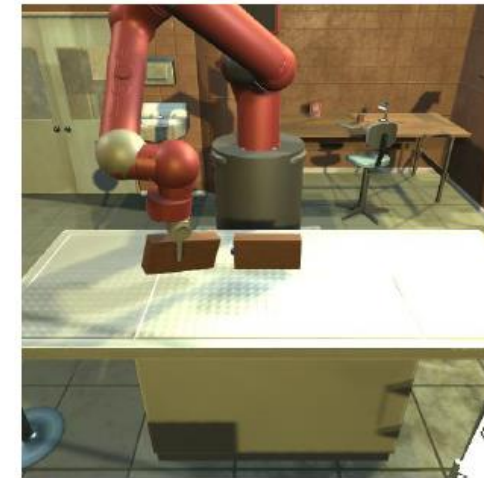
Inspection: Reduce cost and time of inspection to enable frequent inspection and reduce disasters



Construction: Reduce schedule cost, risk, and plan deviation to benefit builders, owners, and dwellers



Driving: Fewer accidents, less stress



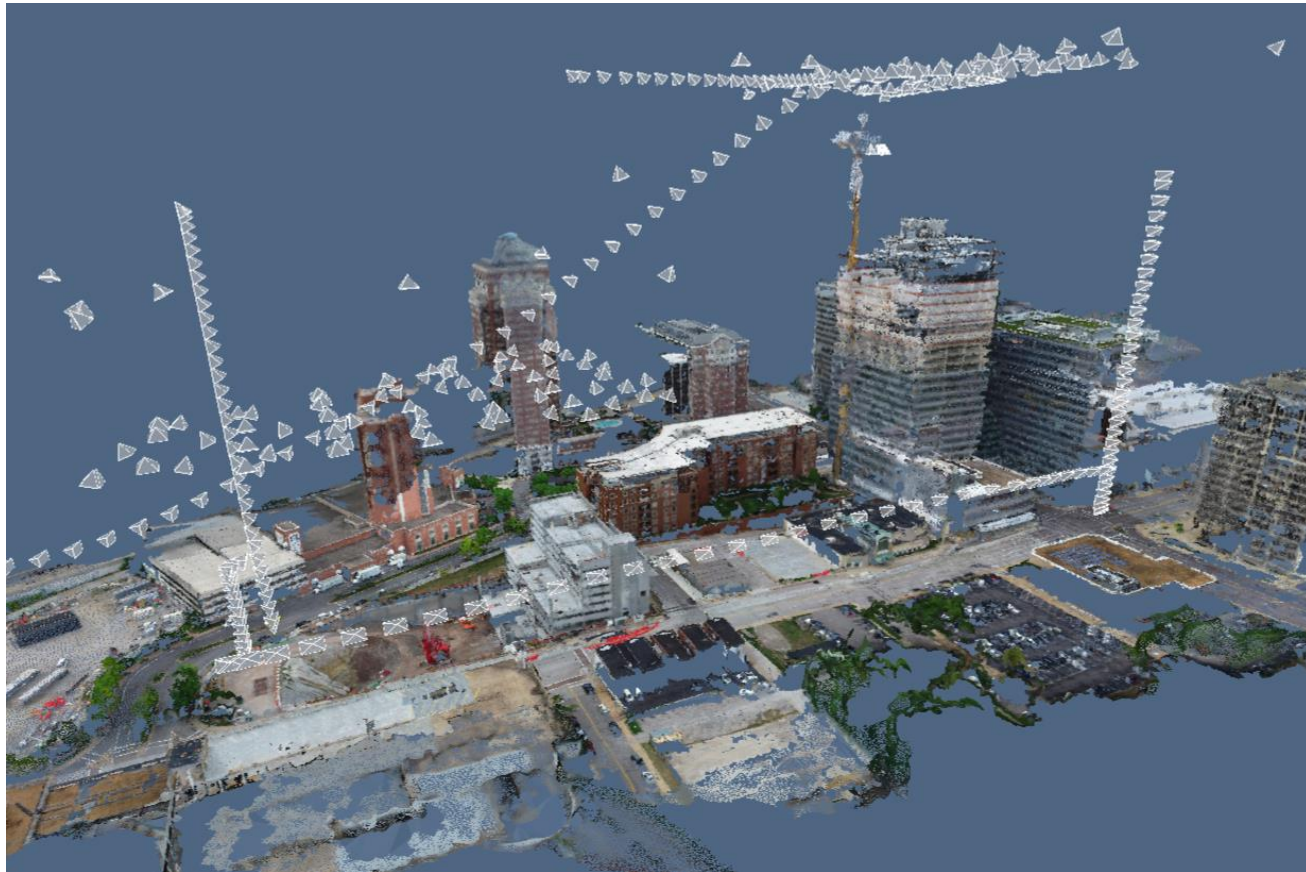
Robotics: Do repetitive jobs fast, dangerous jobs safely

Image: Hu et al. 2019



# What is the layout of the environment?

**Multiview Reconstruction**



[Reconstruct]

**Single-view Reconstruction**



[Zou et al. 2018]



# What does the scene look like from new views?

**Mesh-based**



[Riegler Kolton 2020]

**NeRF**



[Mildenhall et al. 2020]



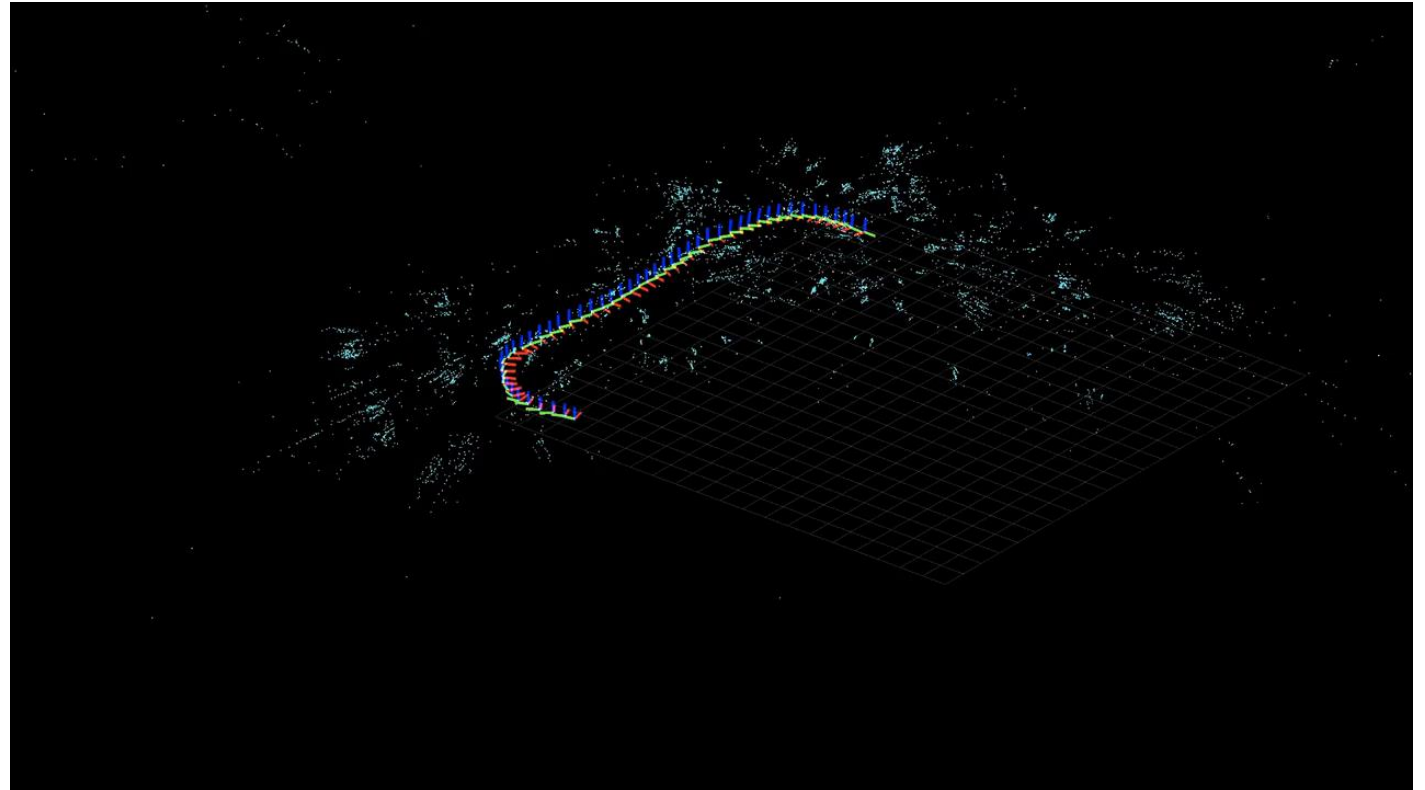
# Where were the photos taken from?

**Structure from Motion (SfM)**



[Reconstruct]

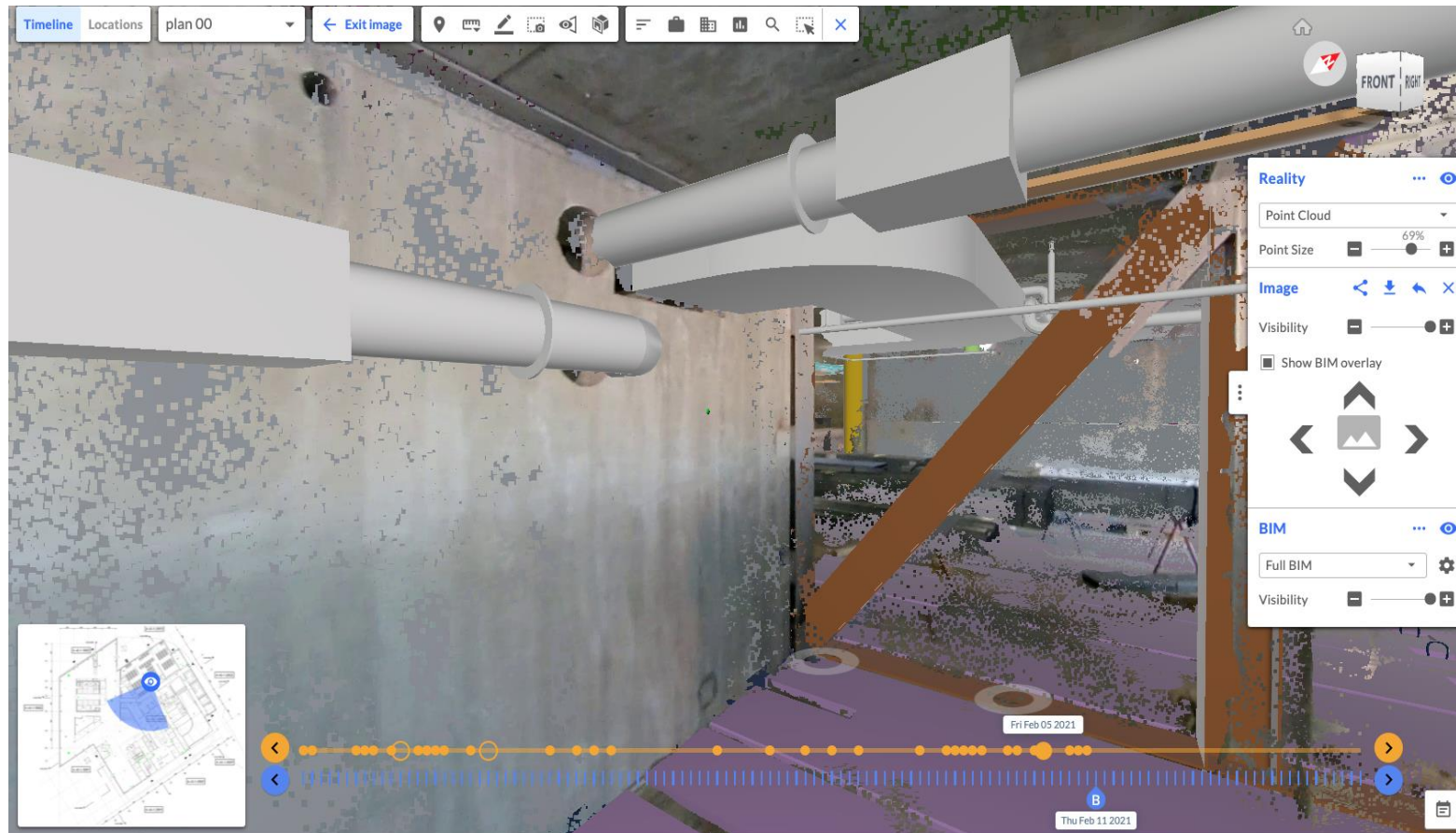
**Simultaneous Localization and Mapping (SLAM)**



[OpenSpace.ai]

# How does reality compare to expected?

## Alignment, Shape Fitting

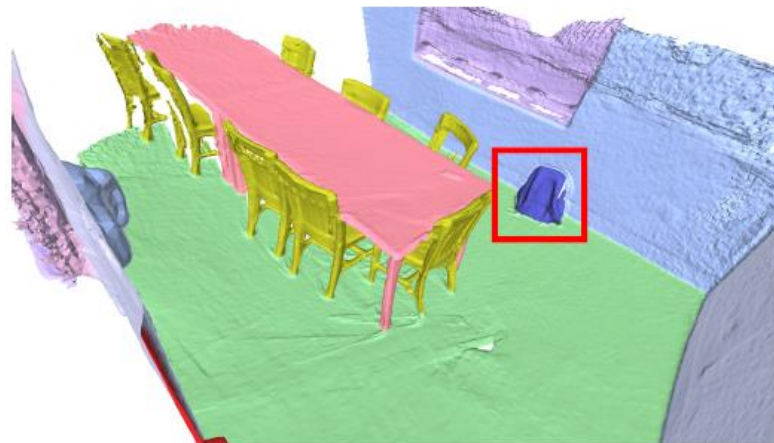


[Reconstruct]



# What objects are there? What are their poses/shapes?

## Semantic Segmentation

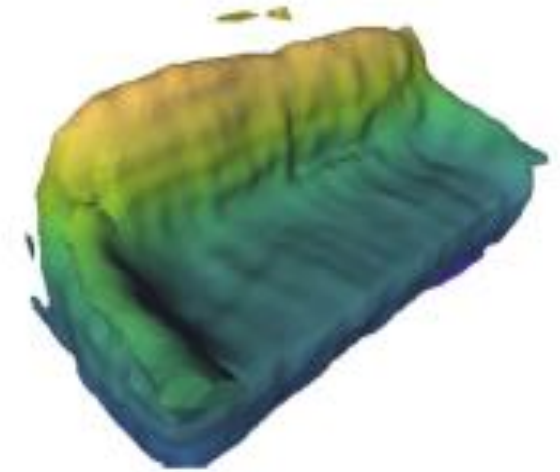


[Hu et al. 2021]

## Single-view Shape



RGB Image



Predicted Mesh

[Shin et al. 2018]

# My first main research project: single-view 3D reconstruction

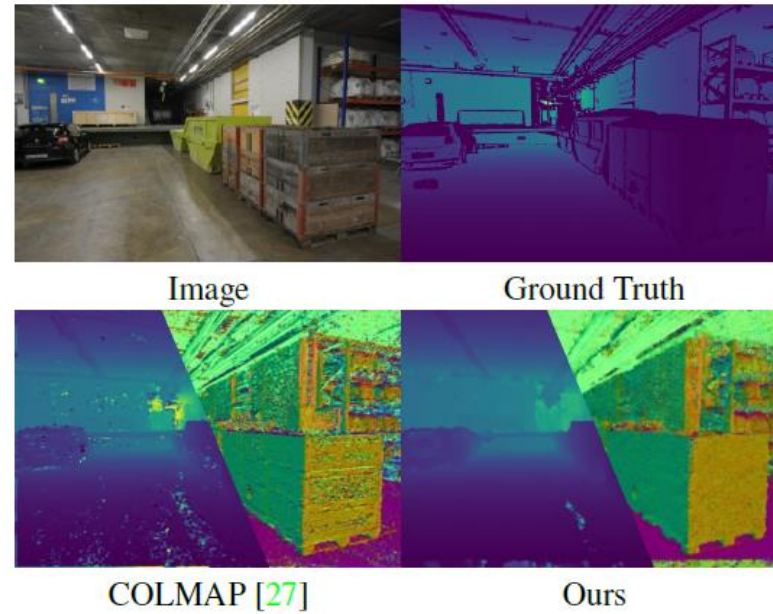


with Efros, Hebert



# Most recent: multi-view 3D Reconstruction

PatchMatch-RL (Lee et al. 2021)



# Everything in between

## Research

- Single-view layout and novel view synthesis [SG 2005, ICCV 2005, IJCV 2007, ICCV 2009, CVPR 2012, CVPR 2018]
- Robot path planning [IROS 2006]
- Objects in 3D context [CVPR 2006, IJCV 2008, CVPR 2008]
- 3D Object Recognition [CVPR 2007, ECCV 2010, CVPR 2018]
- 3D Photo Manipulation [SG 2007, SGA 2011]
- Occlusion Boundaries [ICCV 2007, IJCV 2011]
- RGBD Scene Analysis [ECCV 2012, IJCV 2019]
- Object 3D shape estimation [CVPR 2013, CVPR 2015, ICCV 2017]
- 3D material recognition [CVPR 2016]
- Structure-from-motion [3DV 2018, ECCV 2018, 3DV 2020]

## Commercial Application

- Reconstruct: SfM, SLAM, MVS, meshing, recognition, registration

**But I still  
have a lot to  
learn!**



# This Class

- Learn fundamentals of 3D vision
  - Lectures on Thursdays
- Learn state-of-the-art
  - Discuss papers you select and read on Tuesdays
- Improve research skills
  - Identify potential directions: survey, paper reports
  - Design proof-of-concept: research proposal
  - Perform PoC, re-assess: research paper

# Prerequisites

- Graduate-level computer vision (CS 543 or equivalent)
- Engaged or interested in 3D Vision research

# Materials

- Website: <https://courses.engr.illinois.edu/cs598dwh/fa2021/>
  - Syllabus
  - Schedule
  - Paper selection/reports



# Paper Readings

## For each topic

[Before Thursday class]

1. **Group assignment.** Groups are (randomly) assigned by the professor and listed in [Paper Selection](#). One tab for each topic, one row per group.

[ Before Tuesday class]

2. **Scribe.** Group selects a scribe. Whoever has been scribe fewest times should be scribe next. In case of tie, can choose by interest.
3. **Paper selection.** The scribe chooses a topical paper in consultation with the other group members by **end of day Thursday** and puts title/link next to group in [Paper Selection](#). No two groups can choose the same paper! First to claim the paper gets it.
4. **Paper reading and review.** By **10:45am Tuesday**, each group member (including scribe) submits their reviews using the [Review Form](#).

[In class Tuesday]

5. **Discussion.** In class, students split into groups and discuss the ideas of the paper and ideas for future work or other applications.
6. **Summary.** During discussion period, scribe consolidates discussion in [one summary slide](#). Copy-paste the template under the topic and fill in the slide. Can include figures from paper. Put slides in group order.
7. **Report out.** Scribe presents summary to class.

# Course Project

## 1. [Survey](#)

- Assigned group
- Choose different topic for each group
- 4-6 page report: overview, taxonomy, evaluation, analysis, research ideas

## 2. Research Proposal

- You form group
- Choose research proposal idea
- 2-3 page report: motivation, related work, proposed approach, contributions, significance, planned experiments including proof-of-concept

## 3. Project Report

- Same group as proposal
- Perform proof-of-concept experiments
- 4 page report: intro, approach, PoC results, recommendations

Reviews: everyone reviews one survey and one proposal

# Grading

- Paper reviews and discussion: 50%
  - Must do at least 10 for full points
  - ½ credit if review is unsatisfactory or discussion is missed
- Course project: 50%
  - Survey 15%
  - Proposal 15%
  - Report 15%
  - Reviews 5%
  - Grading is “satisfactory” (full credit), “needs improvement” (3/4 credit), “unsatisfactory” (1/2 credit); can be resubmitted once if necessary
- Late policy
  - no credit for late reviews
  - project component penalty is 1% of course total per day



# Academic Integrity

- All work you submit should be your own – do not copy any text from any online reviews or papers
  - Cite sources diligently
- If your research project builds on prior/ongoing work, discuss with professor first
- Violations will be penalized through official channels

# COVID-19 Policy

- Students who feel ill must not come to class. In addition, students who test positive for COVID-19 or have had an exposure that requires testing and/or quarantine must not attend class.
  - You will not lose review/discussion points for this
- All students, faculty, staff, and visitors are required to wear face coverings in classrooms and university spaces.

# Getting help outside of class

## Office hours

- For help with projects or papers or other complex questions, see professor after class or another arranged time

## Slack:

- For discussion within student groups or logistical questions

[https://join.slack.com/t/3dvision-fa21/shared\\_invite/zt-u1yy4vk1-8oEBalkCVT15GhQeoLaF7g](https://join.slack.com/t/3dvision-fa21/shared_invite/zt-u1yy4vk1-8oEBalkCVT15GhQeoLaF7g)

## Readings/Textbook

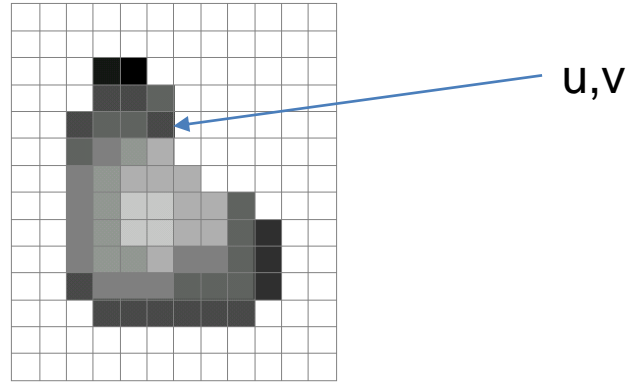
- See webpage



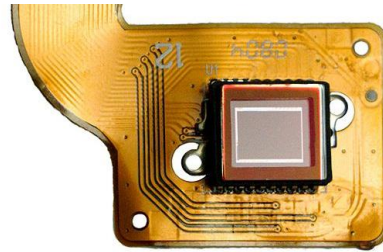
Questions about class structure/content?

# Basics of Cameras: What is a pixel?

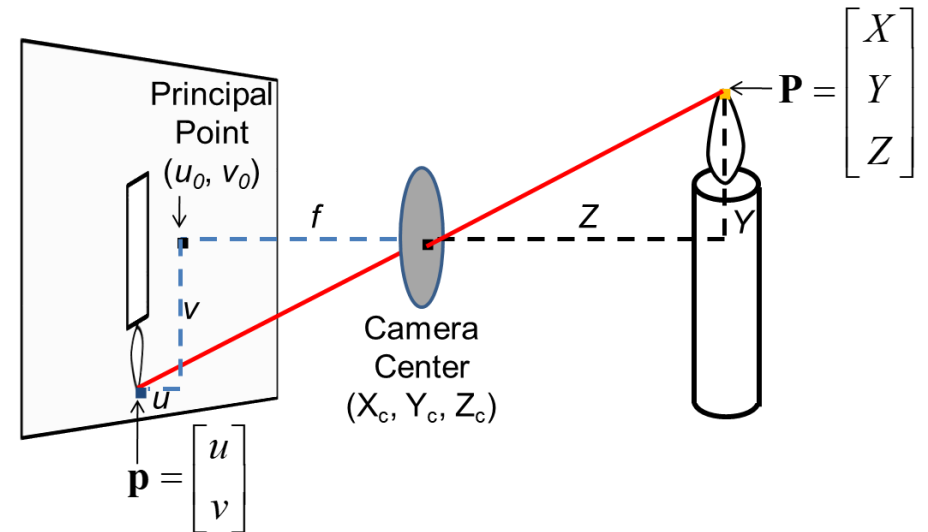
Image coordinate



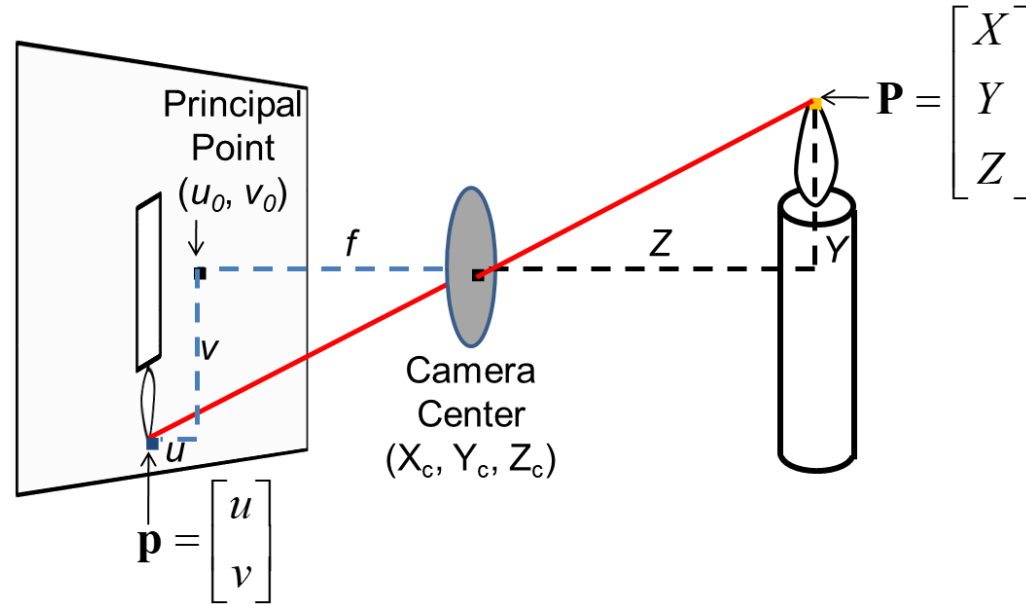
CCD cell



3D ray



# How do we map from 3D to 2D?



$$\mathbf{p} = \mathbf{K} \mathbf{P} \quad \rightarrow \quad w \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f & 0 & u_0 \\ 0 & f & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

# Homogeneous coordinates

Homogeneous  
Coordinates

$$w \begin{bmatrix} x \\ y \\ k \end{bmatrix} = \begin{bmatrix} wx \\ wy \\ wk \end{bmatrix}$$

= a Ray

Cartesian  
Coordinates

$$\Rightarrow \begin{bmatrix} \frac{wx}{wk} \\ \frac{wy}{wk} \end{bmatrix} = \begin{bmatrix} \frac{x}{k} \\ \frac{y}{k} \end{bmatrix}$$

= a Point



# Basic geometry in homogeneous coordinates

- Line equation:  $ax + by + c = 0$

$$line_i = \begin{bmatrix} a_i \\ b_i \\ c_i \end{bmatrix}$$

- Append 1 to pixel coordinate to get homogeneous coordinate

$$p_i = \begin{bmatrix} u_i \\ v_i \\ 1 \end{bmatrix}$$

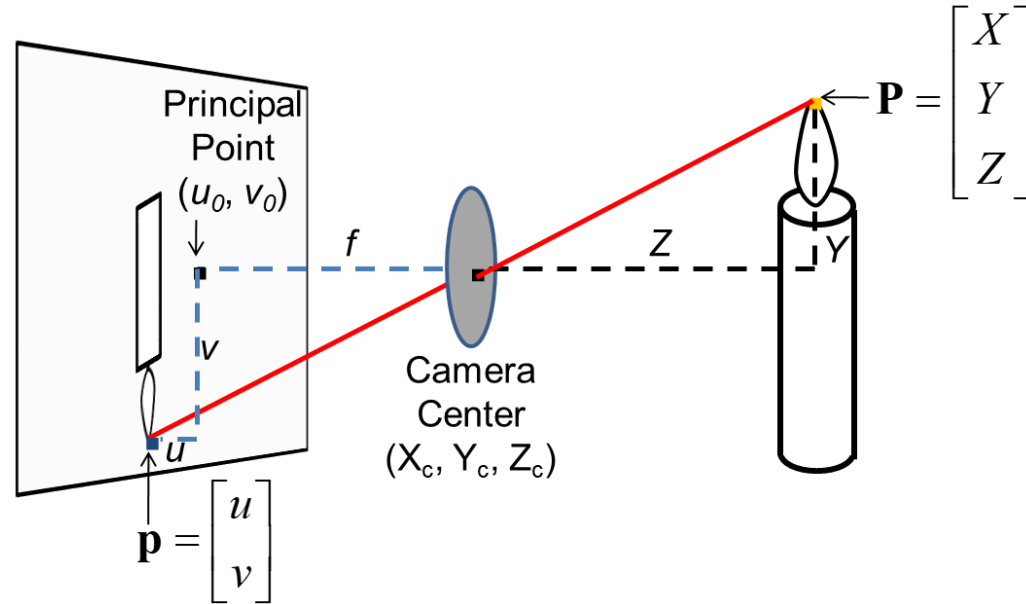
- Line given by cross product of two points

$$line_{ij} = p_i \times p_j$$

- Intersection of two lines given by cross product of the lines

$$q_{ij} = line_i \times line_j$$

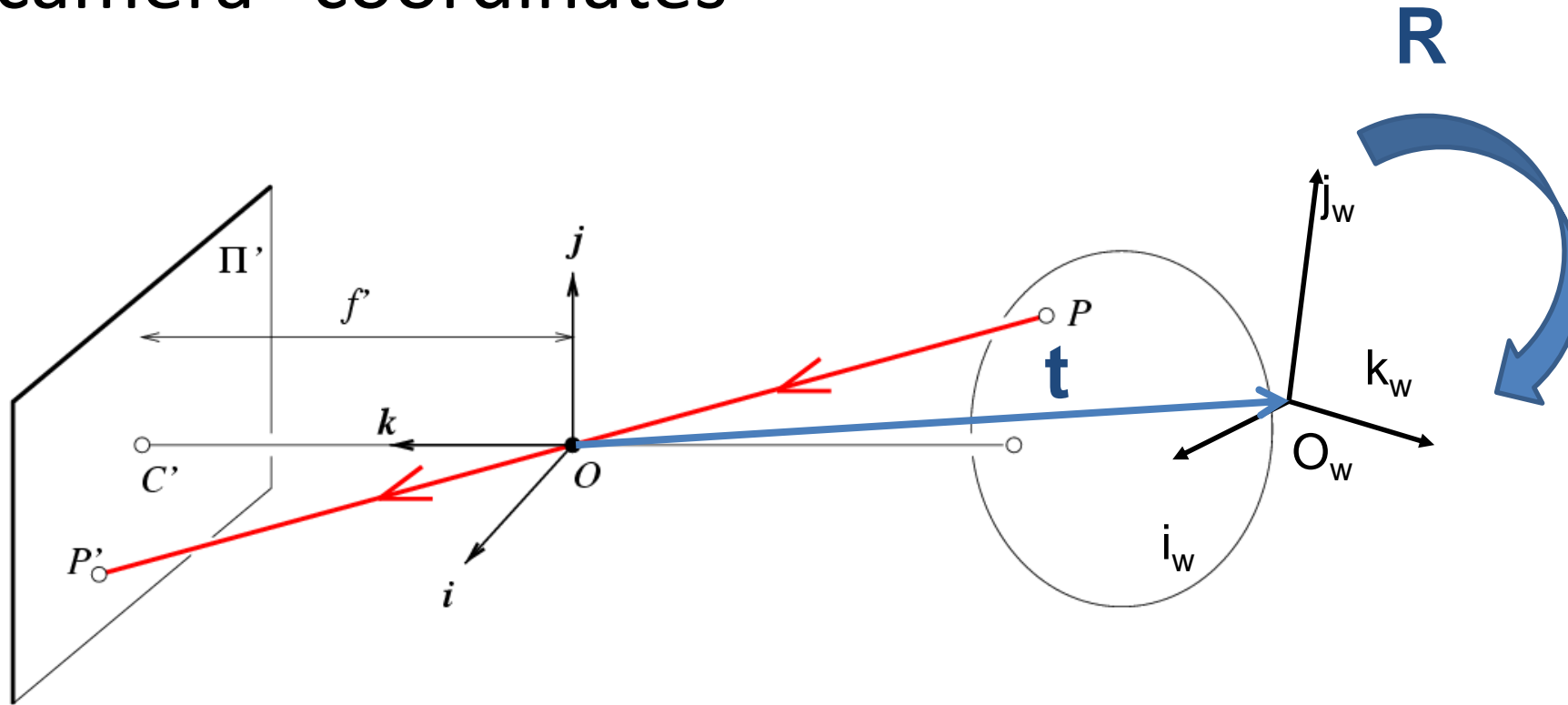
# How do we map from 2D to 3D?



Sometimes called a “bearing”

$$\mathbf{K}^{-1} \mathbf{p} = w \mathbf{P} \Rightarrow \begin{bmatrix} \frac{1}{f} & 0 & \frac{-u_0}{f} \\ 0 & \frac{1}{f} & \frac{-v_0}{f} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = w \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

# Rotation and translation map from “world” coordinates to “camera” coordinates



$$\mathbf{X}_c = [\mathbf{R} \quad \mathbf{t}] \mathbf{X}_w$$

$$\mathbf{x} = \mathbf{K} [\mathbf{R} \quad \mathbf{t}] \mathbf{X}_w$$

$\mathbf{x}$ : Image Coordinates:  $(u, v, 1)$

$\mathbf{K}$ : Intrinsic Matrix  $(3 \times 3)$

$\mathbf{R}$ : Rotation  $(3 \times 3)$

$\mathbf{t}$ : Translation  $(3 \times 1)$

$\mathbf{X}_w$ : World Coordinates:  $(X, Y, Z, 1)$

# Properties of 3D rotation matrix

$$\mathbf{R} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix}$$

$$\mathbf{R}^{-1} = \mathbf{R}^T$$

$\mathbf{R}$  is orthonormal:

$$\mathbf{R} = [\mathbf{r}_1 \quad \mathbf{r}_2 \quad \mathbf{r}_3] \longrightarrow \begin{array}{l} \|\mathbf{r}_i\| = 1 \\ \mathbf{r}_i^T \mathbf{r}_j = 0 \end{array} \quad \|\mathbf{R}\mathbf{X}\| = \|\mathbf{X}\|$$



# Rotation matrix sudoku

- Solve for missing  $r$  values (up to sign ambiguity)

$$\mathbf{R} = \begin{bmatrix} r_{11} & r_{12} & ? \\ r_{21} & r_{22} & ? \\ r_{31} & ? & ? \end{bmatrix}$$

$$\mathbf{R} = \begin{bmatrix} ? & r_{12} & ? \\ r_{21} & r_{22} & ? \\ ? & ? & ? \end{bmatrix}$$

# Questions to consider

1. What is the camera's position in world coordinates, given  $\mathbf{R}$  and  $\mathbf{t}$ ?
2. What additional information can enable recovering a 3D geometry coordinate from a 2D pixel coordinate?
3. Suppose a camera images a star (~infinite distance point). If the camera translates without rotating, what is the effect on the pixel position of the star?

# Final comments

- To do
  - Review web page and syllabus
  - Start planning with your group which paper to do for next Tuesday
- Next class: two-view stereo
- Questions?