

## LECTURE - 18

ZERO - KNOWLEDGE FAQ.

### Proofs of Knowledge

GGM, AGM. : Generic Group / Algebraic Group Models.

### Zero - Knowledge

\* Rewinding - based

\* NI Proofs in ROM

\* FHE - based / NBB Zero - Knowledge

WHAT IS ZK USEFUL FOR?

SECURE COMPUTATION.

Alice

$f$

Bob

$a$

$b$

$(pk, sk)$

$\boxed{pk}$   $\xrightarrow{pk}$  FHE.Enc( $a$ )

$\boxed{y}$   $\xleftarrow{pk}$  FHE.Enc( $f(a, b)$ )

$\boxed{Z}$   $\xrightarrow{sk}$  FHE.Dec( $y$ )

$\boxed{f(a, b)}$

$\boxed{f(a, b)}$

$\exists(r, sk)$  s.t. FHE.Dec<sub>sk</sub>( $y$ ) =  $Z$

AND KeyGen( $I, r$ )  $\rightarrow$  sk, pk

ZK compiles honest-but-curious to malicious protocols

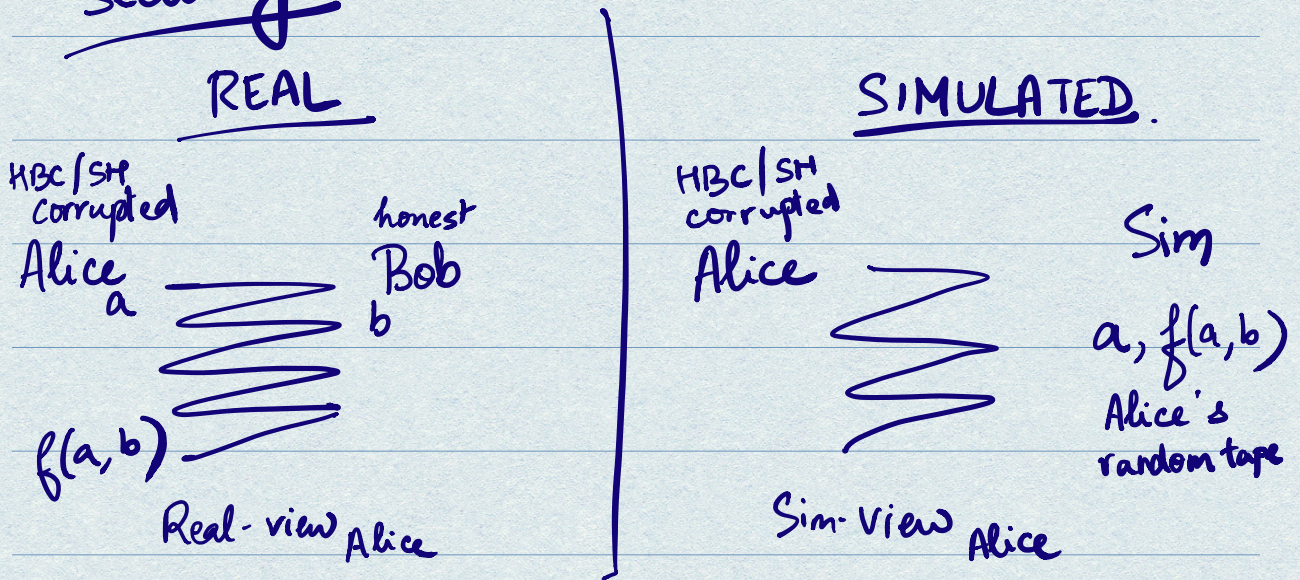
# HONEST - BUT - CURIOUS / SEMI-HONEST SECURE COMPUTATION.

A protocol  $\Pi$  is a HBC/SH secure comp. protocol if:

Correctness:

$$\forall a, b, f, \text{out}_{\Pi}(Alice(a), Bob(b)) = f(a, b)$$

Security:

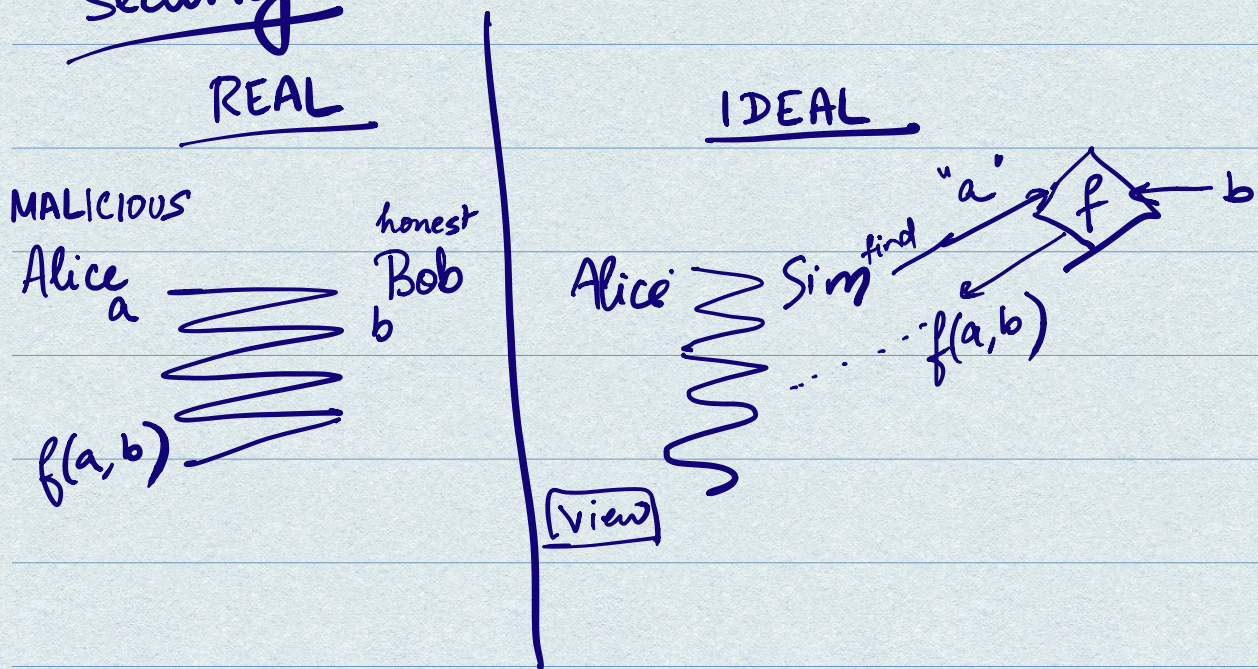


$$\text{Real-view}_{Alice} \approx \text{Sim-view}_{Alice}$$

# MALICIOUSLY SECURE COMPUTATION

Correctness: Same as before.

Security:



$$\text{Real-view}_{\text{Alice}} \approx \text{Sim-view}_{\text{Alice}}$$

(Anybody can run Sim on themselves)

$$f_1(a, b), f_2(f_1(a, b), a, b, \dots)$$

# SEMI-HONEST SECURITY OF FHE-BASED PROTOCOL.

Alice

Bob

$(pk, sk)$

$$\xrightarrow{ct_1 = \text{FHE.Enc}(a)}$$

$$\xleftarrow{ct_2}$$

$$\xrightarrow{z = \text{FHE.Dec}(ct_2)}$$

$f, b$

$$ct_2 = \text{FHE.Eval}(ct_1, f, b) + \text{noise}$$

Alice

Sim

$(pk, sk)$

$$\xrightarrow{ct_1 = \text{FHE.Enc}(a)}$$

$$\xleftarrow{ct_2'}$$

$$\xrightarrow{z = \text{FHE.Dec}(ct_2')}$$

$a$ , DOES NOT KNOW  $b$ .

$a, f(a, b)$

$$ct_2' = \text{FHE.Enc}(f(a, b))$$

+ noise

FHE with "circuit privacy" / rerandomization.

Alice

$pk, sk$

$pk,$   
 $ct_1 = \text{FHE.Enc}(a)$

$ct_2 = \text{FHE.Eval}(ct_1, f, b)$

$z = \text{Dec}(ct_2)$   
 $sk$

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Semi-honest corrupted  
Bob

Sim

$b, f(a, b)$

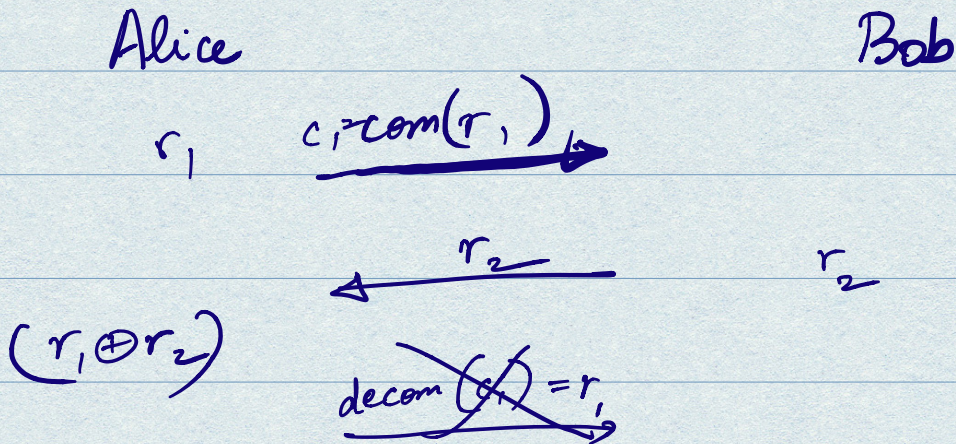
$pk,$   
 $ct_1 = \text{FHE.Enc}(0)$

$ct_2$

$z = f(a, b)$

Semi-honest  
corrupted  
Bob

# COIN-TOSSING



# MALICIOUSLY SECURE FHE. [GMW Compiler]

