

CS576 Topics in Automated Deduction

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Records in Isabelle/HOL

- Records in HOL are basically tuples, but...

```
record ('a)graph_sig =  
  Vertices :: "'a set"  
  Edges :: "('a × 'a) set"
```

```
definition one :: "(unit) graph_sig" where  
  "one ≡ ⟨ Vertices = {()}, Edges = {(((), ()))} ⟩"
```

- Components accessed by field

```
lemma "() ∈ Vertices one"  
by (simp add: one_def)
```

- Unlike functional programming languages, position of fields matters

```
⟨ Edges = {(((), ()))}, Vertices = {()} ⟩
```

causes an **"Error in record input"**

Record Field Update

- Records support field update

```
definition no_edge :: "(unit) graph_sig" where  
  "no_edge = one⟦ Edges := {} ⟧"
```

```
lemma "no_edge = ⟦ Vertices = {()}, Edges = {} ⟧"  
by (simp add: no_edge_def one_def)
```

Record Field Update

- Record update is functional

```
definition no_edge :: "(unit) graph_sig" where  
  "no_edge = one⟦Edges := {}⟧"
```

```
lemma "no_edge = ⟦Vertices = {()}, Edges = {}⟧"  
by (simp add: no_edge_def one_def)
```

```
lemma "no_edge ≠ one"  
by (simp add: no_edge_def one_def)
```

```
lemma "(Vertices no_edge = Vertices one) ∧  
      (Edges no_edge = {})"  
by (simp add: no_edge_def one_def)
```

record type representations

- Every record type may be given by field syntax:

```
lemma "(one::unit graph_sig) =  
      (one::(|Vertices::unit set, Edges::(unit × unit) set))"  
by (rule refl)
```

- Every record is extensible
 - Every record `rec_ty` defines a polymorphic type
 `('a) rec_ty_scheme`;
 type `rec_ty` same as `(unit) rec_ty_scheme`

```
term "one::(unit,unit) graph_sig_scheme"
```

- Every record type has a “hidden field” `more`

New Record Types From Old

- New record types may be created by extending existing record types with additional fields:

```
record ('a,'b) labeled_graph_sig = "'a graph_sig" +  
Label :: "('a × 'a) ⇒ ('b) option"
```

```
definition two :: "(Vertices :: nat set,  
                  Edges :: (nat × nat) set,  
                  Label :: nat × nat ⇒ bool option)" where
```

```
"two ≡
```

```
  (| Vertices = {1,2}, Edges = {(1,2)},  
    Label = (λ (m,n). (if (m,n) = (1,2) then Some True else No
```

```
constants
```

```
two :: "(nat, bool) labeled_graph_sig"
```

Record Polymorphism

- The `_scheme` types allow for (weak) record polymorphism
- Also referred to as record subtyping
- Generally, input to functions should use `_scheme` type instead of strict record type

```
definition is_graph :: "('a,'b) graph_scheme  $\Rightarrow$  bool" where  
"is_graph G  $\equiv$  ( $\forall$  e  $\in$  Edges G. {fst e, snd e}  $\subseteq$  Vertices G)"
```

```
lemma shows "is_graph one"  
by (simp add: one_def is_graph_def)
```

```
lemma shows "is_graph two"  
by (simp add: two_def is_graph_def)
```