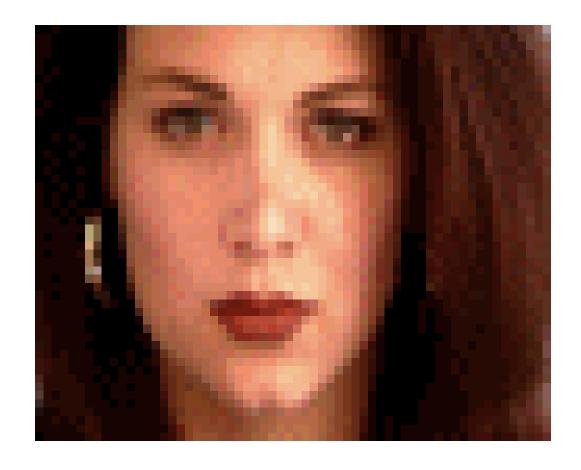
# Image Morphing



Computational Photography
Derek Hoiem, University of Illinois

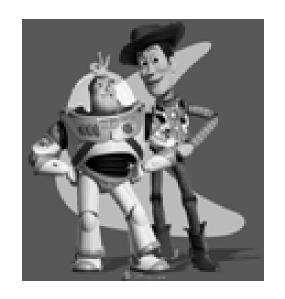
# **Project 3: Gradient Domain Editing**

General concept: Solve for pixels of new image that satisfy constraints on the gradient and the intensity

 Constraints can be from one image (for filtering) or more (for blending)

### Project 3: Reconstruction from Gradients

- 1. Preserve x-y gradients
- 2. Preserve intensity of one pixel



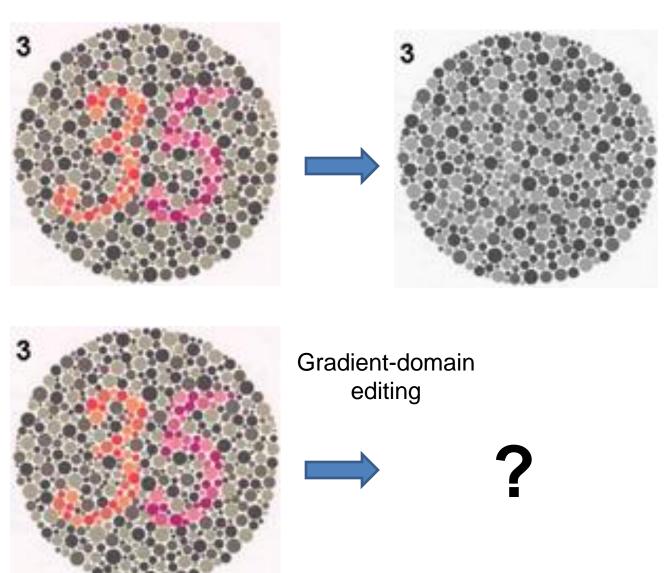
Source pixels: s

Variable pixels: v

- 1. minimize  $(v(x+1,y)-v(x,y) (s(x+1,y)-s(x,y))^2$
- 2. minimize  $(v(x,y+1)-v(x,y) (s(x,y+1)-s(x,y))^2$
- 3. minimize  $(v(1,1)-s(1,1))^2$

# Project 3 (extra): Color2Gray

rgb2gray



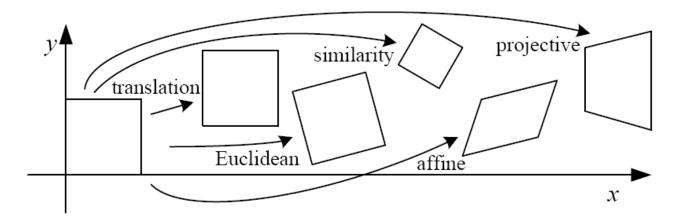
# Project 3 (extra): NPR

- Preserve gradients on edges
  - e.g., get canny edges with edge(im, 'canny')
- Reduce gradients not on edges
- Preserve original intensity





### 2D image transformations



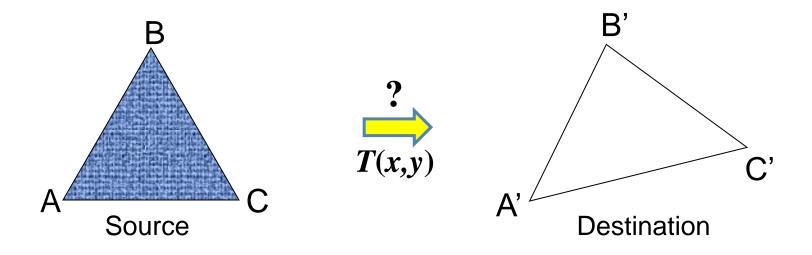
Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$egin{array}{ c c c c c c c c c c c c c c c c c c c$	2	orientation $+ \cdots$	
rigid (Euclidean)	$igg[egin{array}{c c} R & t \end{bmatrix}_{2 imes 3}$	3	lengths + · · ·	$\Diamond$
similarity	$\left  \left[ sR \mid t \right]_{2\times 3} \right $	4	angles $+\cdots$	$\Diamond$
affine	$\left[egin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	parallelism $+\cdots$	
projective	$\left[egin{array}{c}  ilde{m{H}} \end{array} ight]_{3 imes 3}$	8	straight lines	

These transformations are a nested set of groups

• Closed under composition and inverse is a member

### Take-home Question

Suppose we have two triangles: ABC and A'B'C'. What transformation will map A to A', B to B', and C to C'? How can we get the parameters?



## Today: Morphing

#### Women in art



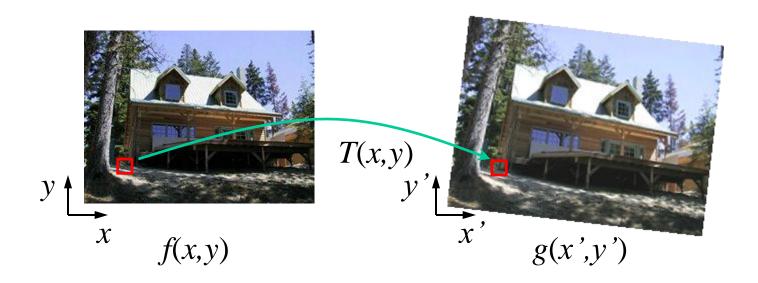
http://youtube.com/watch?v=nUDIoN-\_Hxs

Aging



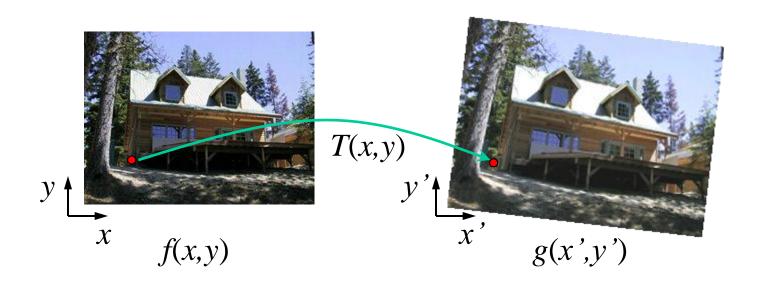
http://www.youtube.com/watch?v=L0GKp-uvjO0

### Image warping



Given a coordinate transform (x',y') = T(x,y) and a source image f(x,y), how do we compute a transformed image g(x',y') = f(T(x,y))?

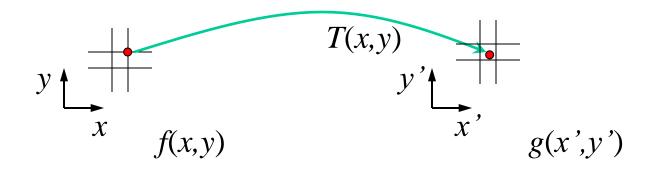
### Forward warping



Send each pixel f(x,y) to its corresponding location (x',y') = T(x,y) in the second image

### Forward warping

What is the problem with this approach?



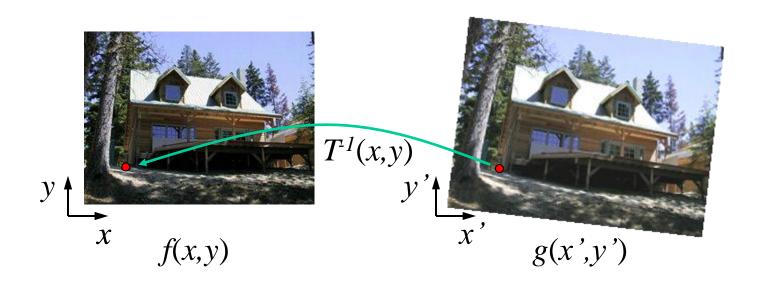
Send each pixel f(x,y) to its corresponding location (x',y') = T(x,y) in the second image

Q: what if pixel lands "between" two pixels?

A: distribute color among neighboring pixels (x',y')

Known as "splatting"

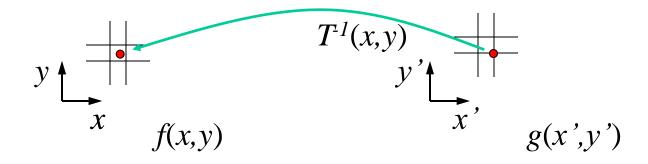
### Inverse warping



Get each pixel g(x',y') from its corresponding location  $(x,y) = T^{-1}(x',y')$  in the first image

Q: what if pixel comes from "between" two pixels?

## Inverse warping



Get each pixel g(x',y') from its corresponding location  $(x,y) = T^{-1}(x',y')$  in the first image

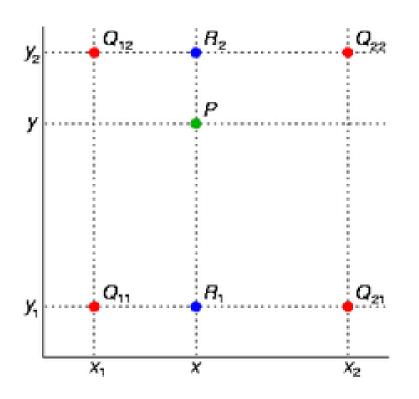
Q: what if pixel comes from "between" two pixels?

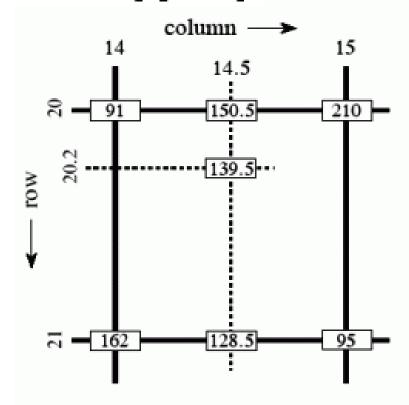
A: Interpolate color value from neighbors

- nearest neighbor, bilinear, Gaussian, bicubic
- Check out interp2 in Matlab

### Bilinear Interpolation

$$f(x,y) \approx \begin{bmatrix} 1-x & x \end{bmatrix} \begin{bmatrix} f(0,0) & f(0,1) \\ f(1,0) & f(1,1) \end{bmatrix} \begin{bmatrix} 1-y \\ y \end{bmatrix}.$$





# Forward vs. inverse warping

Q: which is better?

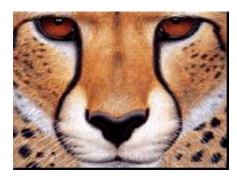
A: Usually inverse—eliminates holes

however, it requires an invertible warp function

# Morphing = Object Averaging







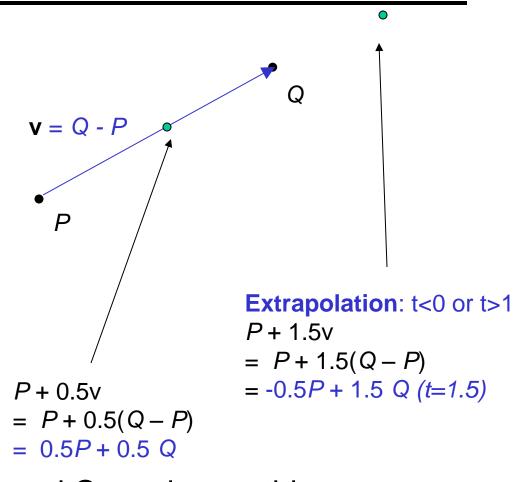
#### The aim is to find "an average" between two objects

- Not an average of two <u>images of objects</u>...
- ...but an image of the <u>average object!</u>
- How can we make a smooth transition in time?
  - Do a "weighted average" over time t

### **Averaging Points**

What's the average of P and Q?

**Linear Interpolation** New point: (1-t)P + tQ0 < t < 1



#### P and Q can be anything:

- points on a plane (2D) or in space (3D)
- Colors in RGB (3D)
- Whole images (m-by-n D)... etc.

#### Idea #1: Cross-Dissolve







Interpolate whole images:

 $Image_{halfway} = (1-t)*Image_1 + t*image_2$ 

This is called **cross-dissolve** in film industry

But what if the images are not aligned?

### Idea #2: Align, then cross-disolve



#### Align first, then cross-dissolve

Alignment using global warp – picture still valid

### Dog Averaging



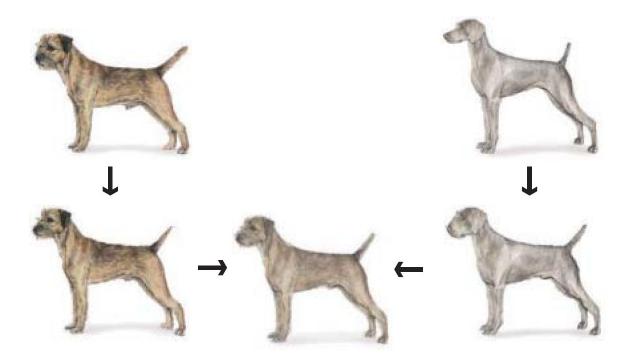
#### What to do?

- Cross-dissolve doesn't work
- Global alignment doesn't work
  - Cannot be done with a global transformation (e.g. affine)
- Any ideas?

#### Feature matching!

- Nose to nose, tail to tail, etc.
- This is a local (non-parametric) warp

### Idea #3: Local warp, then cross-dissolve



#### Morphing procedure

For every frame t,

- 1. Find the average shape (the "mean dog" ©)
  - local warping
- 2. Find the average color
  - Cross-dissolve the warped images

## Local (non-parametric) Image Warping



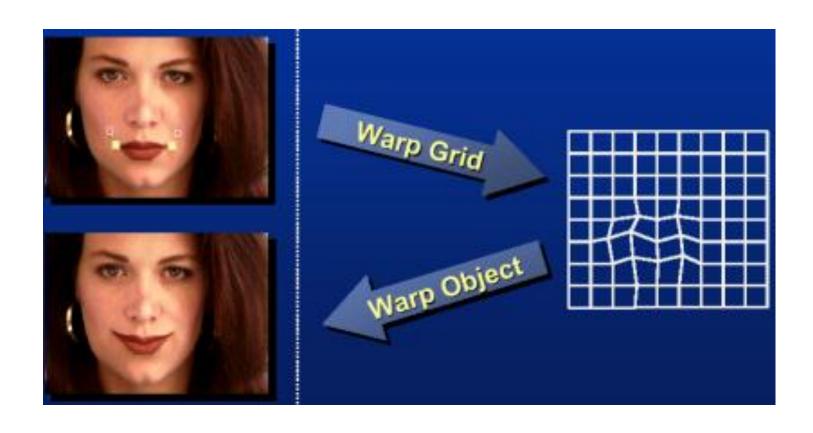


#### Need to specify a more detailed warp function

- Global warps were functions of a few (2,4,8) parameters
- Non-parametric warps u(x,y) and v(x,y) can be defined independently for every single location x,y!
- Once we know vector field u,v we can easily warp each pixel (use backward warping with interpolation)

# Image Warping – non-parametric

Move control points to specify a spline warp Spline produces a smooth vector field



### Warp specification - dense

How can we specify the warp?

Specify corresponding *spline control points* 

interpolate to a complete warping function



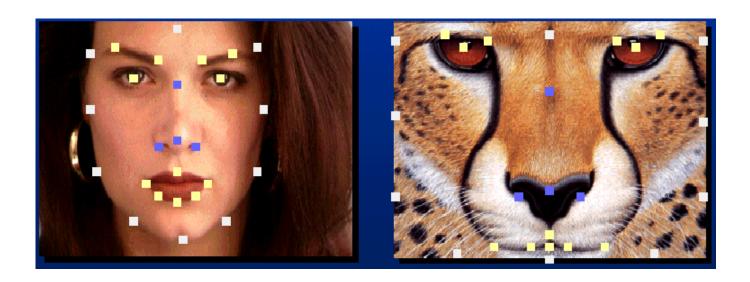
But we want to specify only a few points, not a grid

### Warp specification - sparse

#### How can we specify the warp?

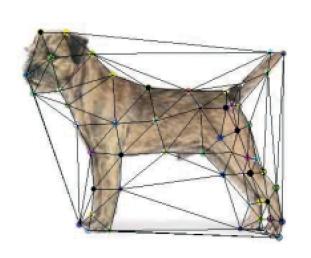
Specify corresponding points

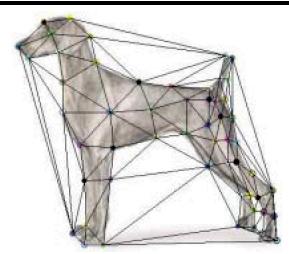
- interpolate to a complete warping function
- How do we do it?



How do we go from feature points to pixels?

### Triangular Mesh



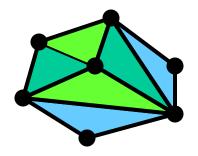


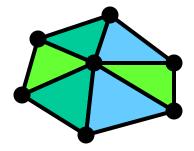
- 1. Input correspondences at key feature points
- 2. Define a triangular mesh over the points
  - Same mesh (triangulation) in both images!
  - Now we have triangle-to-triangle correspondences
- 3. Warp each triangle separately from source to destination
  - Affine warp with three corresponding points (just like takehome question)

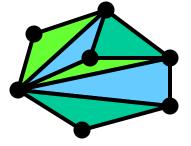
### Triangulations

A *triangulation* of set of points in the plane is a *partition* of the convex hull to triangles whose vertices are the points, and do not contain other points.

There are an exponential number of triangulations of a point set.



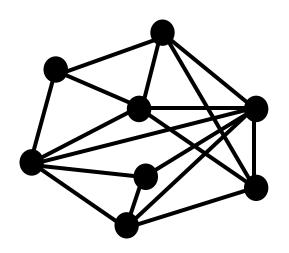




# An $O(n^3)$ Triangulation Algorithm

#### Repeat until impossible:

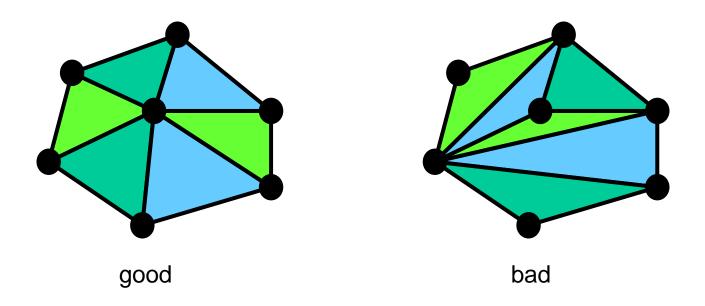
- Select two sites.
- If the edge connecting them does not intersect previous edges, keep it.



## "Quality" Triangulations

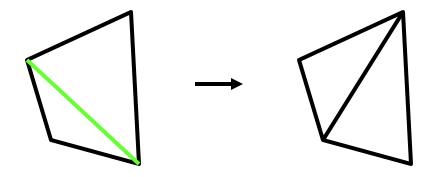
Let  $\alpha(T_i) = (\alpha_{i1}, \alpha_{i2}, ..., \alpha_{i3})$  be the vector of angles in the triangulation T in increasing order:

- A triangulation  $T_1$  is "better" than  $T_2$  if the smallest angle of  $T_1$  is larger than the smallest angle of  $T_2$
- Delaunay triangulation is the "best" (maximizes the smallest angles)



### Improving a Triangulation

In any convex quadrangle, an *edge flip* is possible. If this flip *improves* the triangulation locally, it also improves the global triangulation.

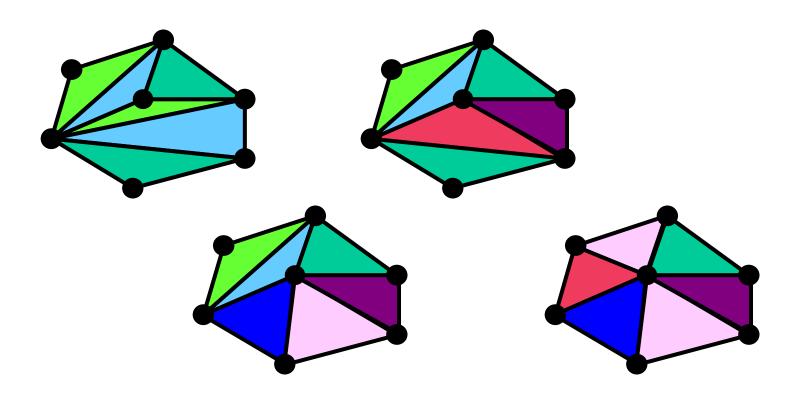


If an edge flip improves the triangulation, the first edge is called "illegal".

### Naïve Delaunay Algorithm

Start with an arbitrary triangulation. Flip any illegal edge until no more exist.

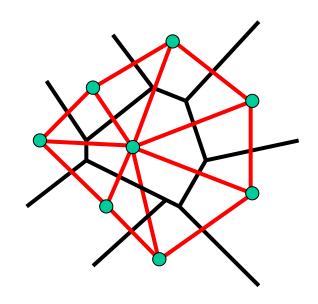
Could take a long time to terminate.



### Delaunay Triangulation by Duality

Draw the dual to the Voronoi diagram by connecting each two neighboring sites in the Voronoi diagram.

- The DT may be constructed in O(nlogn) time
- This is what Matlab's delaunay function uses

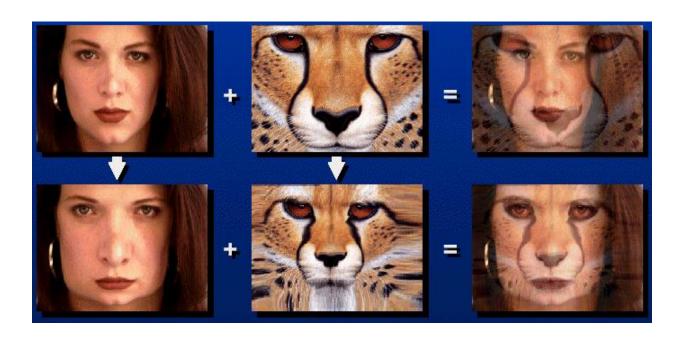


Demo: <a href="http://www.cs.cornell.edu/home/chew/Delaunay.html">http://www.cs.cornell.edu/home/chew/Delaunay.html</a>

### Image Morphing

#### How do we create a morphing sequence?

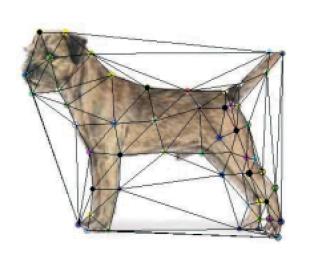
- 1. Create an intermediate shape (by interpolation)
- 2. Warp both images towards it
- 3. Cross-dissolve the colors in the newly warped images

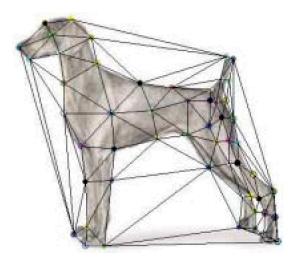


# Warp interpolation

How do we create an intermediate shape at time t?

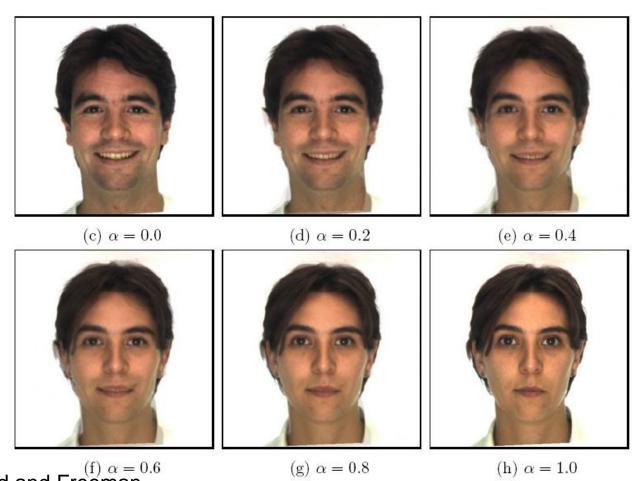
- Assume t = [0,1]
- Simple linear interpolation of each feature pair
  - (1-t)\*p1+t\*p0 for corresponding features p0 and p1





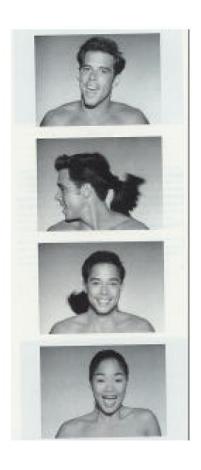
### Morphing & matting

# Extract foreground first to avoid artifacts in the background



Slide by Durand and Freeman

### Dynamic Scene



Black or White (MJ): <a href="http://www.youtube.com/watch?v=R4kLKv5gtxc">http://www.youtube.com/watch?v=R4kLKv5gtxc</a>

Willow morph: <a href="http://www.youtube.com/watch?v=uLUyuWo3pG0">http://www.youtube.com/watch?v=uLUyuWo3pG0</a>

# Summary of morphing

- 1. Define corresponding points
- 2. Define triangulation on points
  - Use same triangulation for both images
- 3. For each t = 0:step:1
  - a. Compute the average shape (weighted average of points)
  - b. For each triangle in the average shape
    - Get the affine projection to the corresponding triangles in each image
    - For each pixel in the triangle, find the corresponding points in each image and set value to weighted average (optionally use interpolation)
  - c. Save the image as the next frame of the sequence

### Next classes

- Thursday
  - Pinhole camera: start of perspective geometry

- Tuesday
  - Single-view metrology: measuring 3D distances from an image