Single-view 3D Reconstruction

Computational Photography

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Some slides from Alyosha Efros, Steve Seitz

Project 3

- Class favorites: vote please
  - “Favorites” will be presented next Thurs

Next Tuesday

- I’m out of town
- Kevin Karsch is talking about physically grounded image editing, including inserting 3D objects into photographs

Take-home question

Suppose we have two 3D cubes on the ground facing the viewer, one near, one far.

1. What would they look like in perspective?
2. What would they look like in weak perspective?

Photo credit: GazetteLive.co.uk

Take-home question

Suppose you have estimated three vanishing points corresponding to orthogonal directions. How can you recover the rotation matrix that is aligned with the 3D axes defined by these points?

- Assume that intrinsic matrix K has three parameters
- Remember, in homogeneous coordinates, we can write a 3d point at infinity as (X, Y, Z, 0)

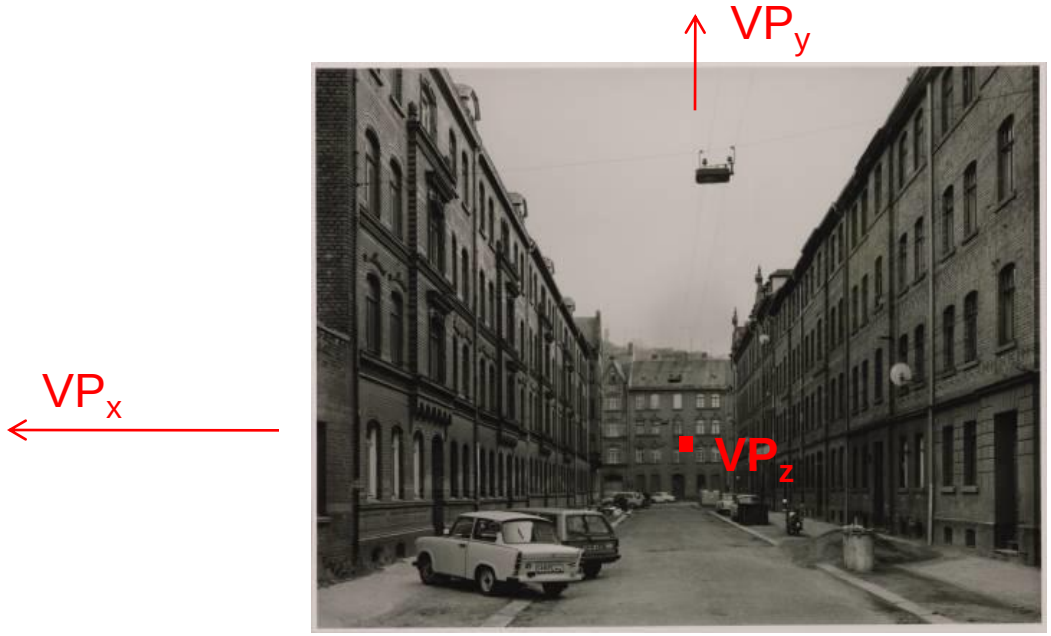
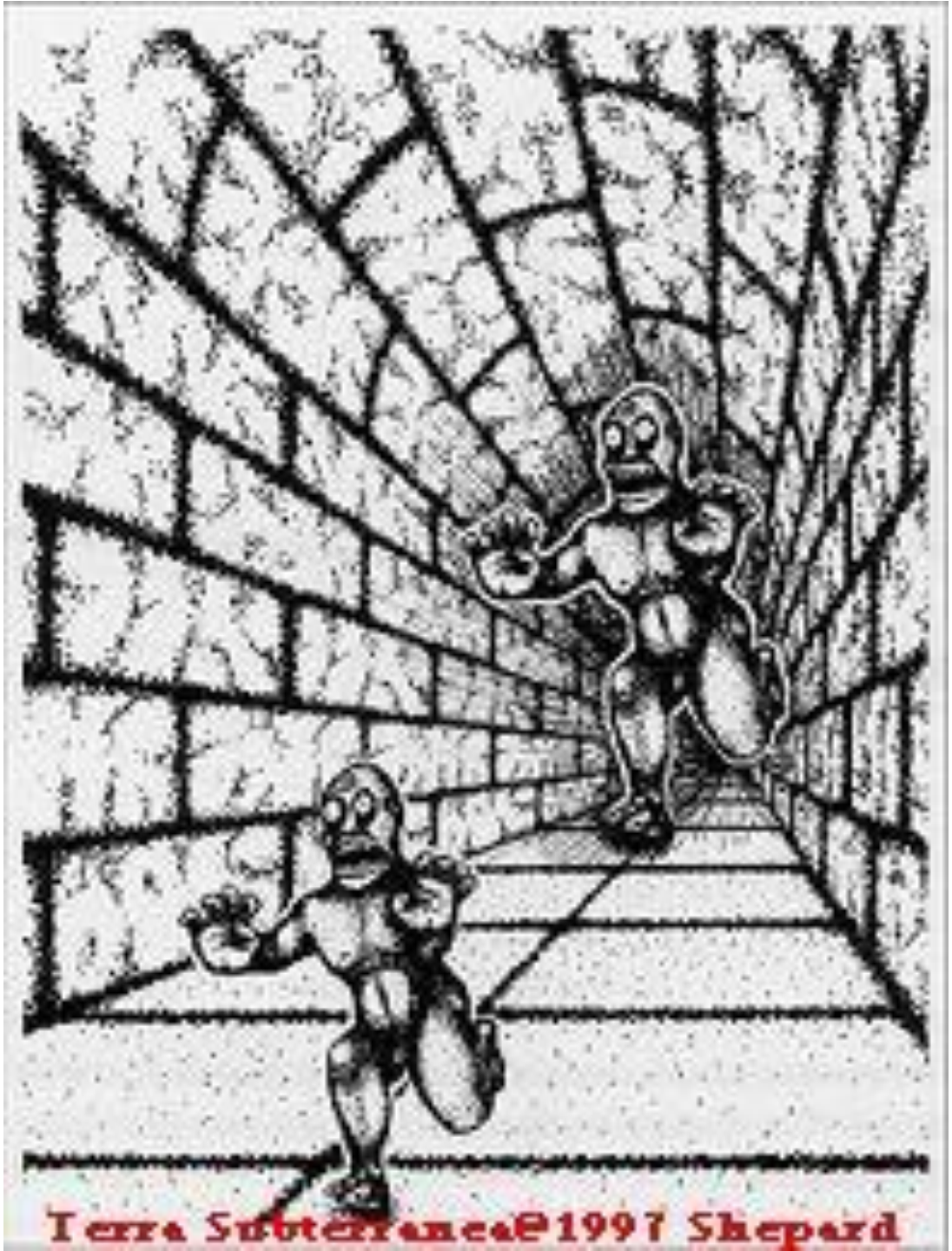


Photo from online Tate collection

Take-home question

Assume that the camera height is 5 ft.

- What is the height of the man?
- What is the height of the building?


Terra Subterranea©1997 Shepard

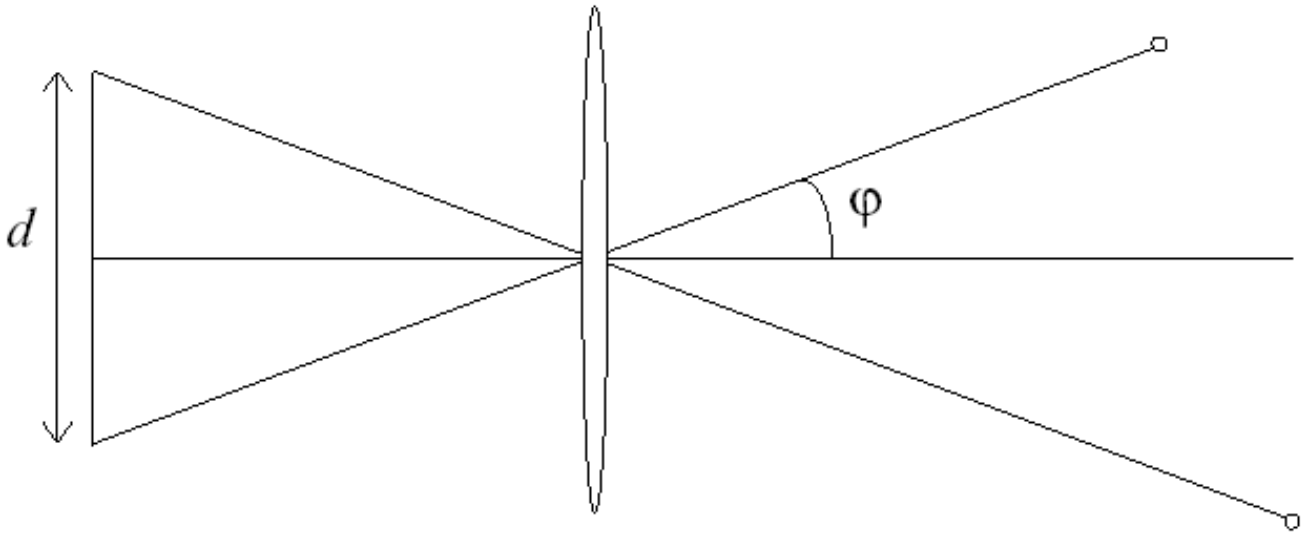
Relation between field of view and focal length

Field of view (angle width)

Film/Sensor Width

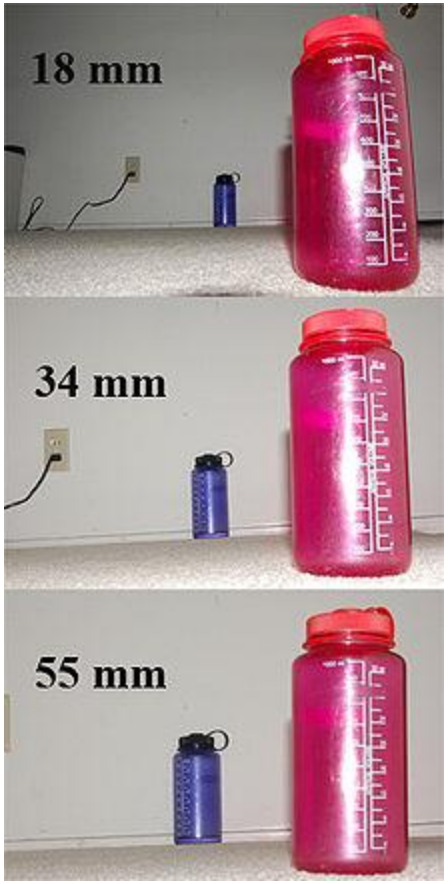
$$fov = 2\tan^{-1}\frac{d}{2f}$$

Focal length



Dolly Zoom or “Vertigo Effect”

http://www.youtube.com/watch?v=nAhGM2Fyl8Q



How is this done?

Zoom in while moving away

http://en.wikipedia.org/wiki/Focal_length

Dolly zoom (or “Vertigo effect”)

Field of view (angle width)

Film/Sensor Width

$$fov = 2\tan^{-1}\frac{d}{2f}$$

Focal length

width of object

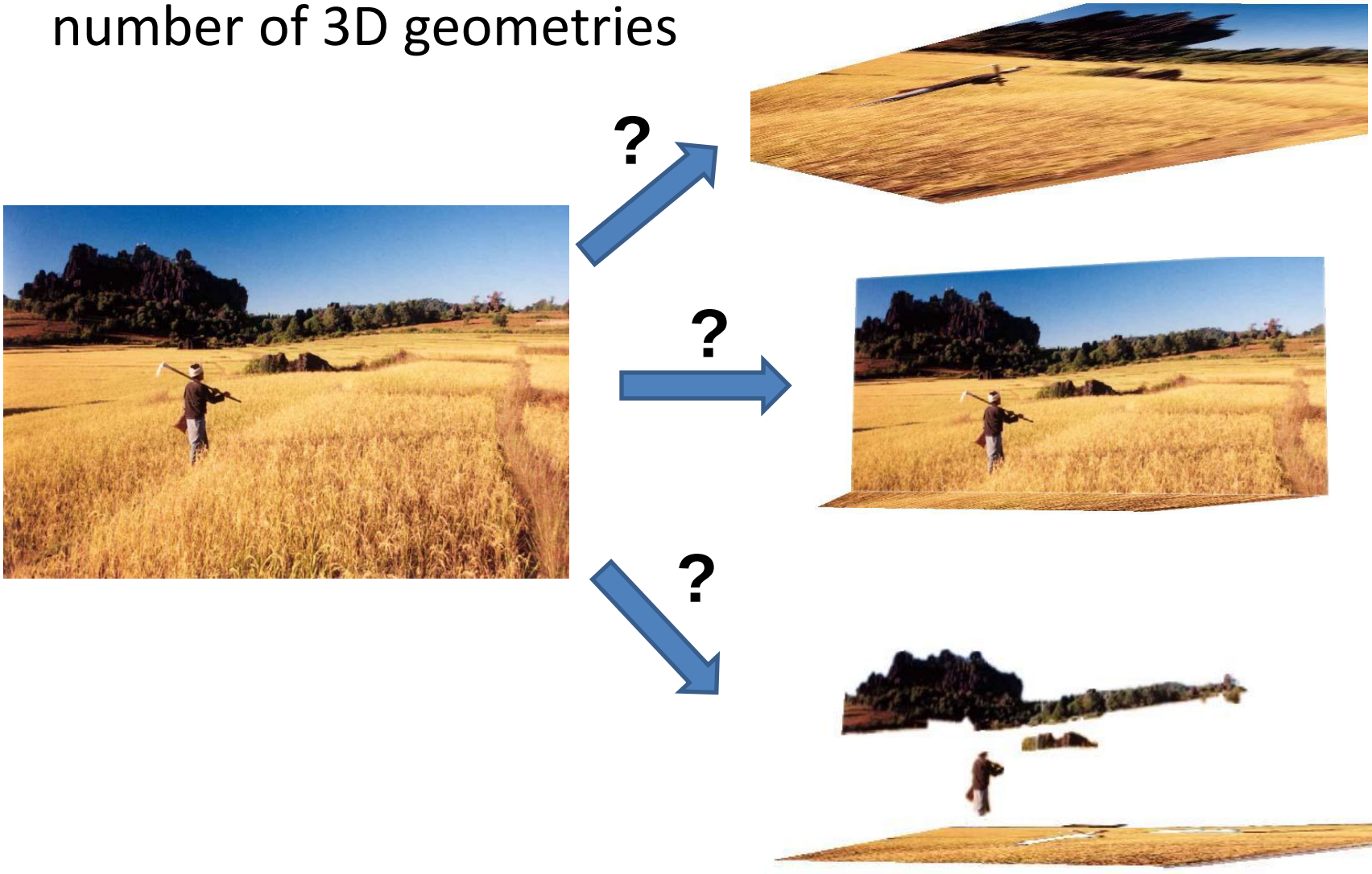
$$2\tan\frac{fov}{2} = \frac{width}{distance}$$

Distance between object and camera

Today's class: 3D Reconstruction

The challenge

One 2D image could be generated by an infinite number of 3D geometries



The solution

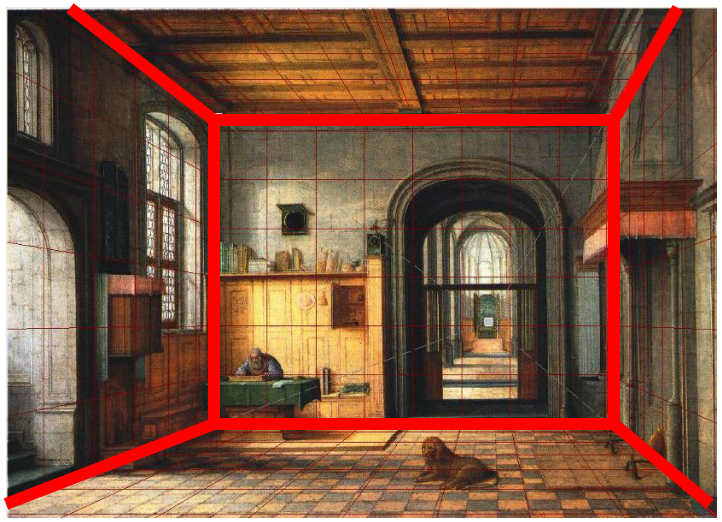
Make simplifying assumptions about 3D geometry

Unlikely

Likely

Today's class: Two Models

- Box + frontal billboards



- Ground plane + non-frontal billboards

“Tour into the Picture” (Horry et al. SIGGRAPH ’97)

Create a 3D “theatre stage” of five billboards

Specify foreground objects through bounding polygons

Use camera transformations to navigate through the scene

Following slides modified from Efros

The idea

Many scenes (especially paintings), can be represented as an axis-aligned box volume (i.e. a stage)

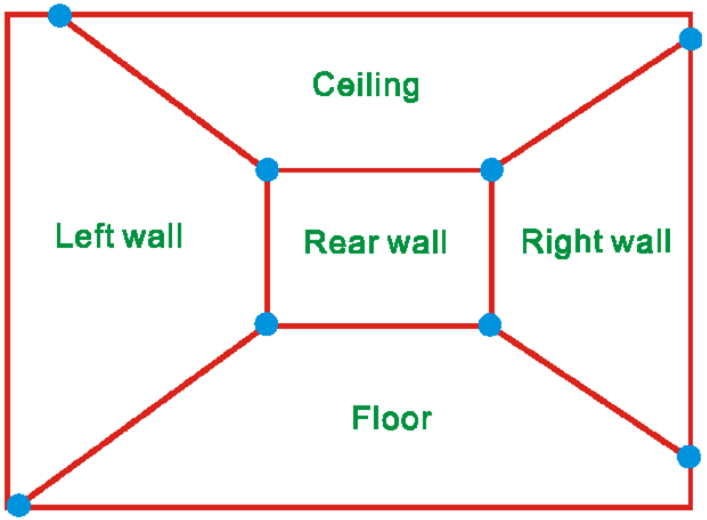
Key assumptions

- All walls are orthogonal
- Camera view plane is parallel to back of volume

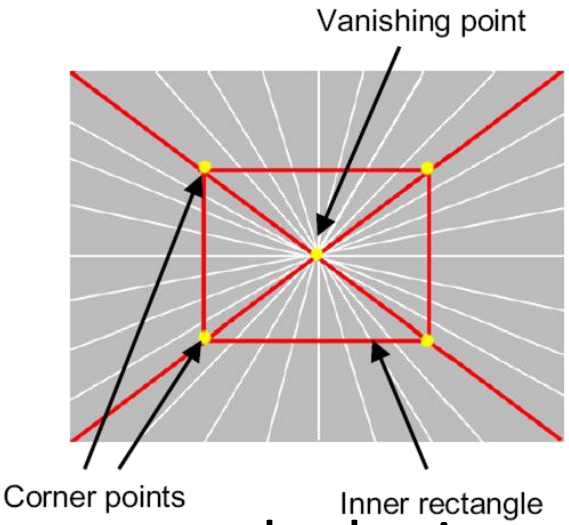
How many vanishing points does the box have?

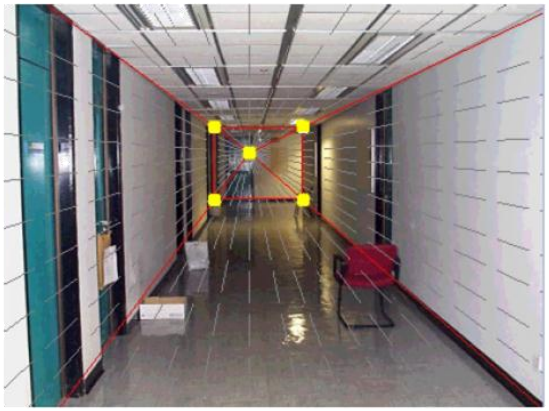
- Three, but two at infinity
- Single-point perspective

Can use the vanishing point to fit the box to the particular scene



Fitting the box volume

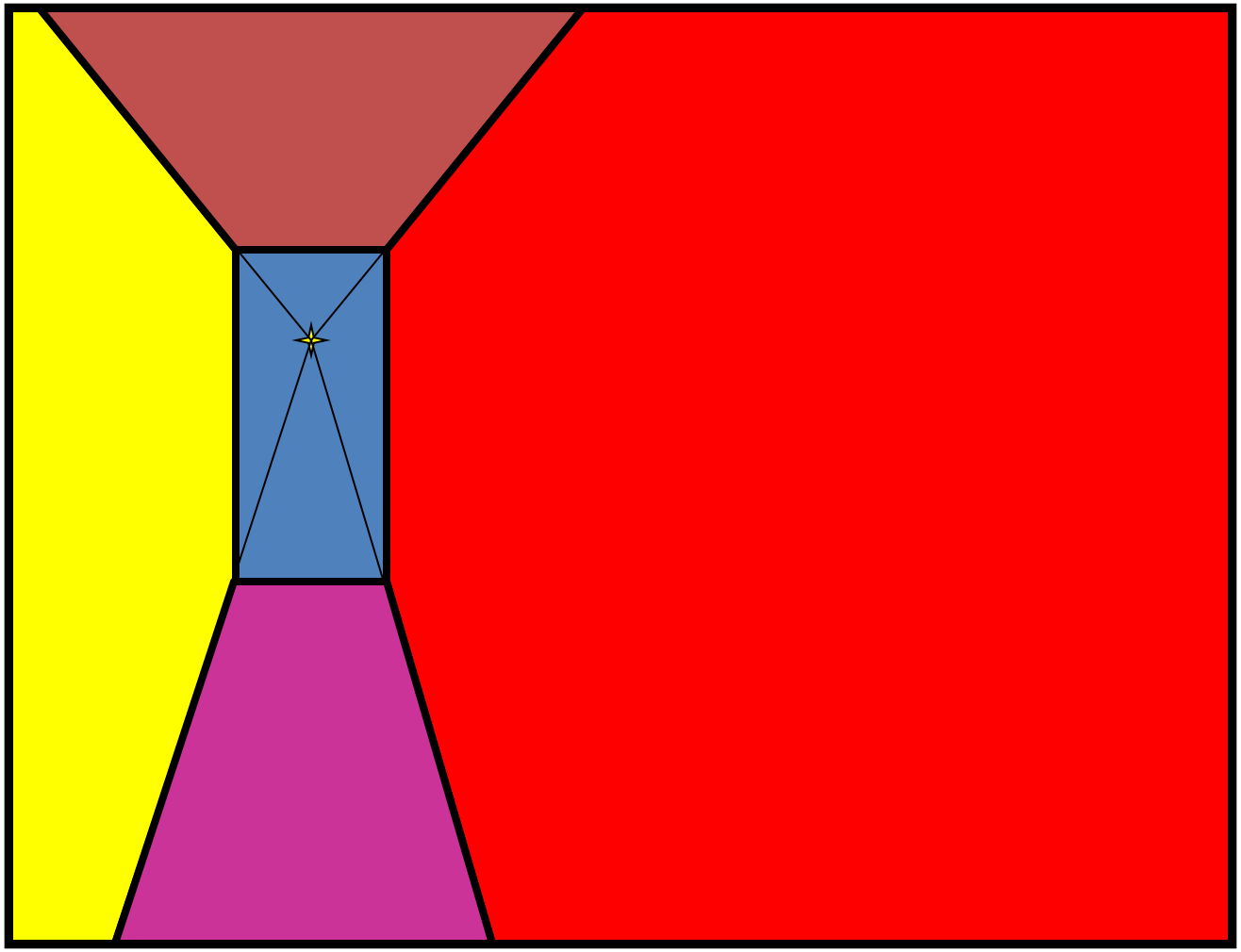




- User controls the inner box and the vanishing point placement (# of DOF???)

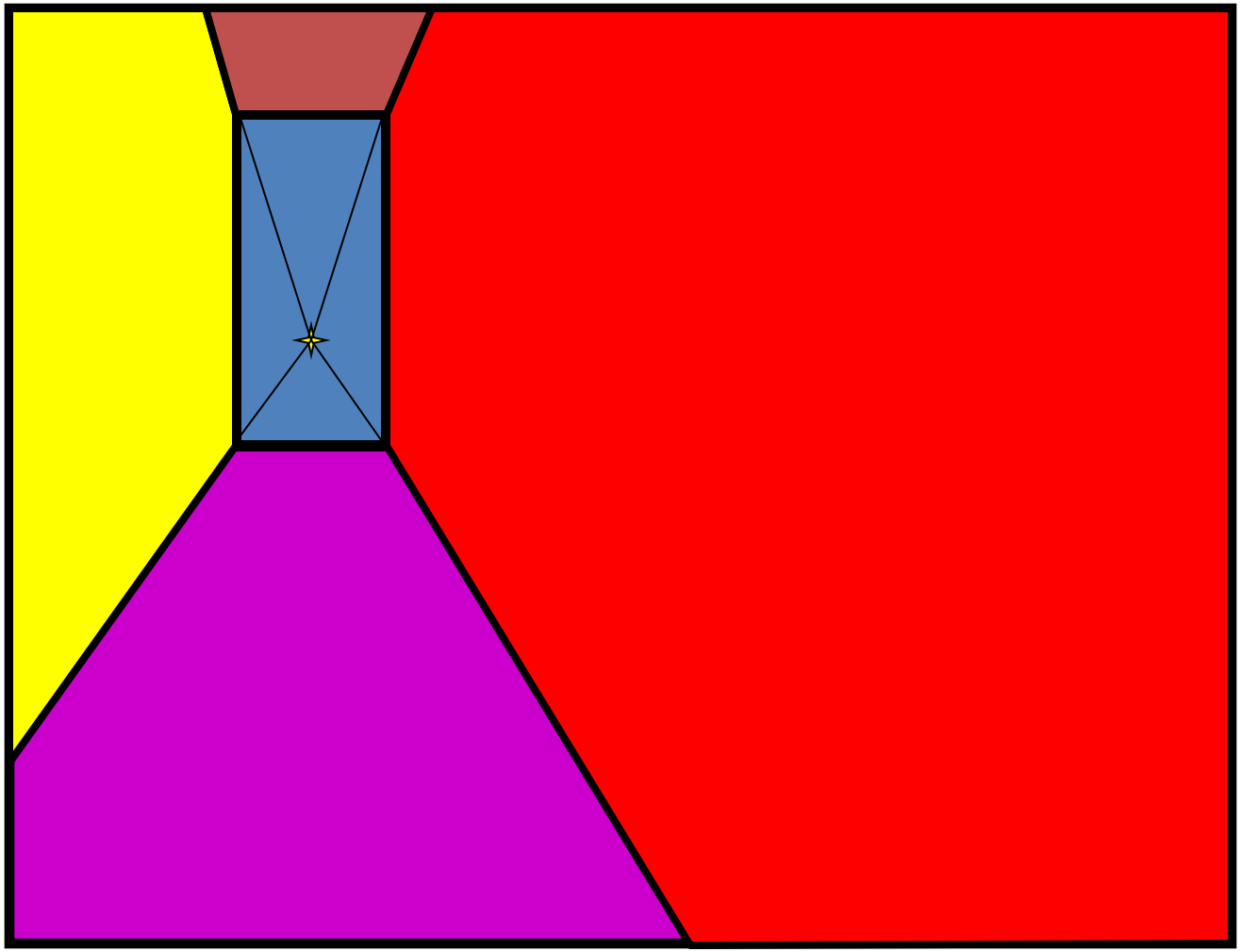
- Q: What's the significance of the vanishing point location?
- A: It's at eye (camera) level: ray from COP to VP is perpendicular to image plane
  - Under single-point perspective assumptions, the VP should be the optical center of the image

Example of user input: vanishing point and back face of view volume are defined

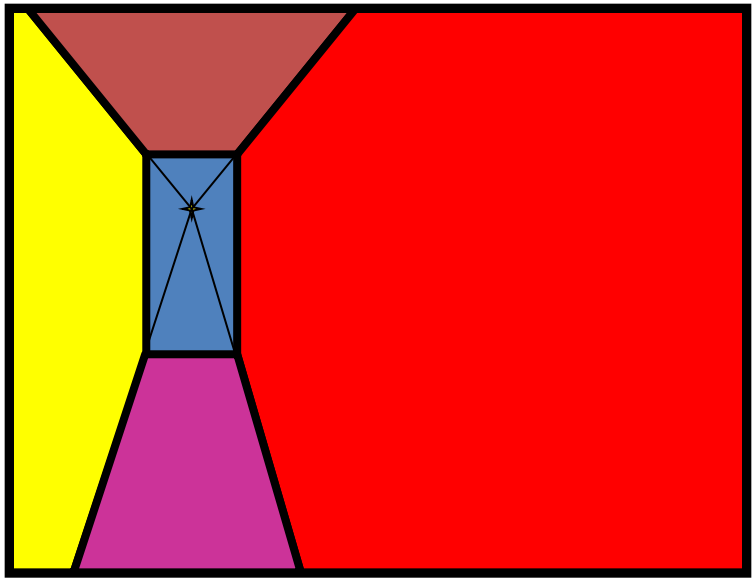


High Camera

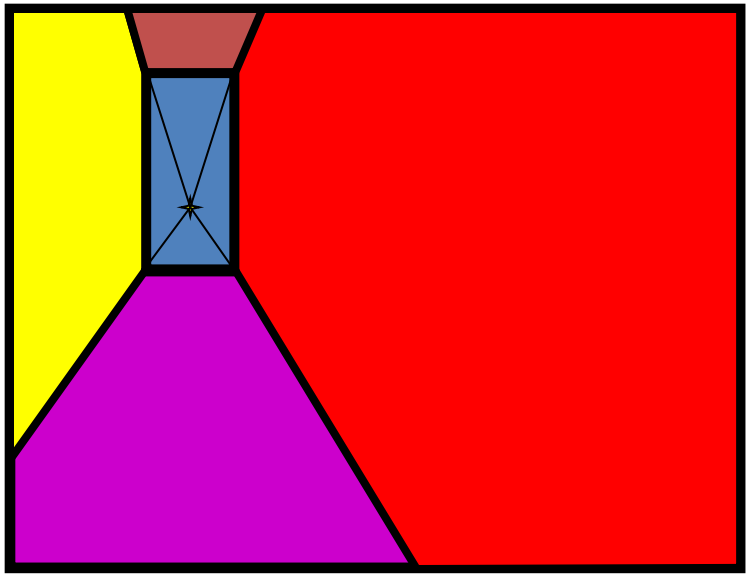
Example of user input: vanishing point and back face of view volume are defined



Comparison of how image is subdivided based on two different camera positions. You should see how moving the box corresponds to moving the eyepoint in the 3D world.

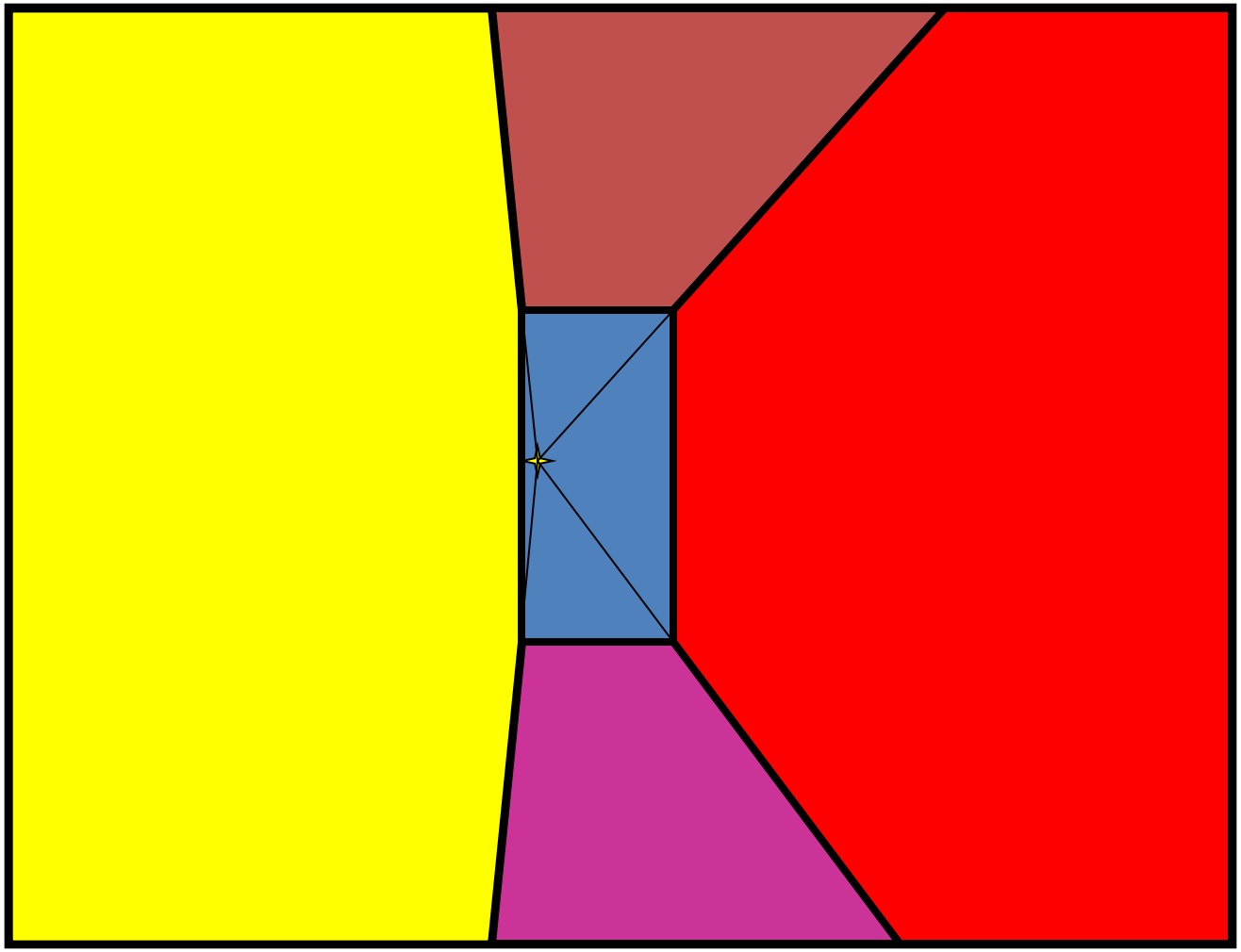


High Camera

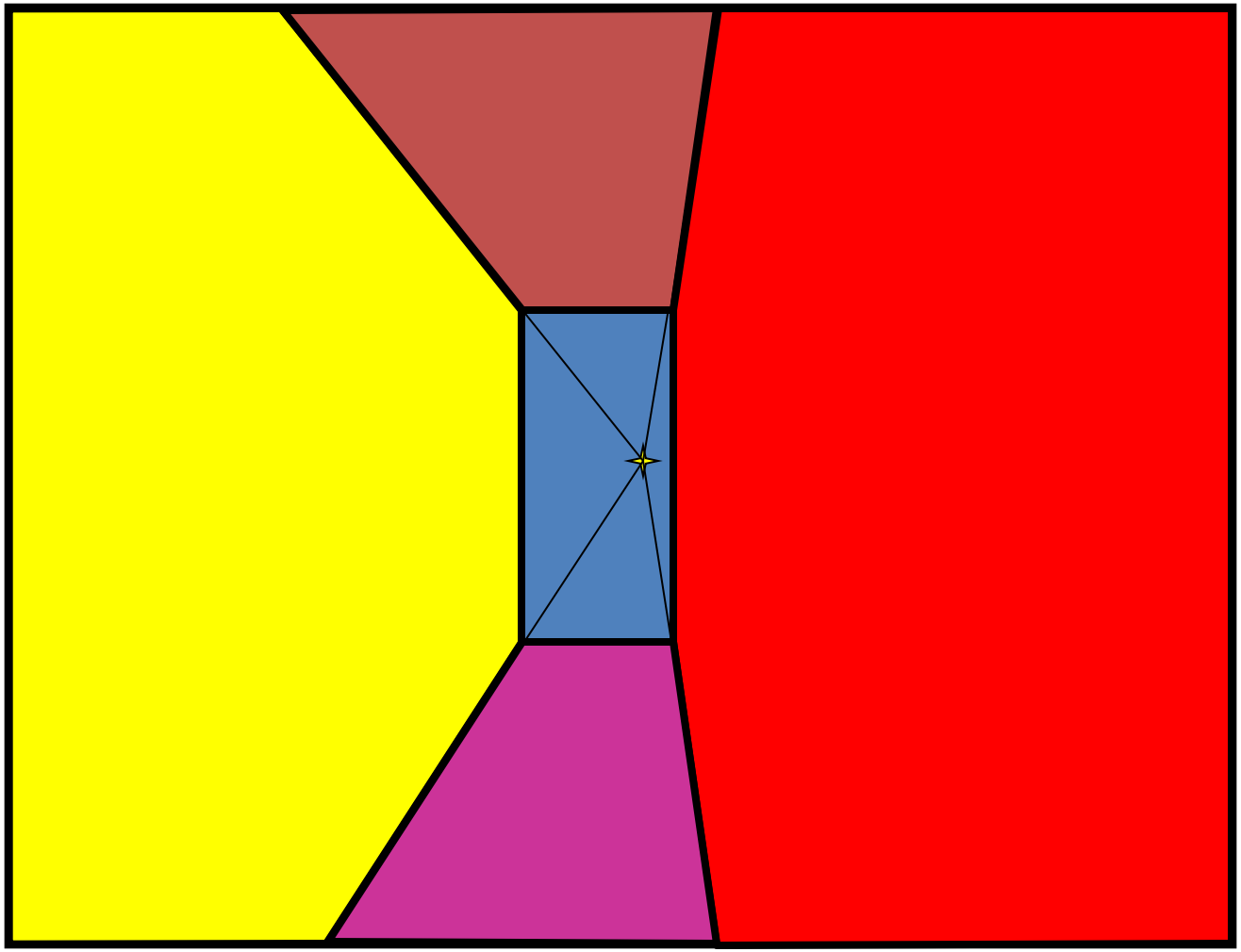


Low Camera

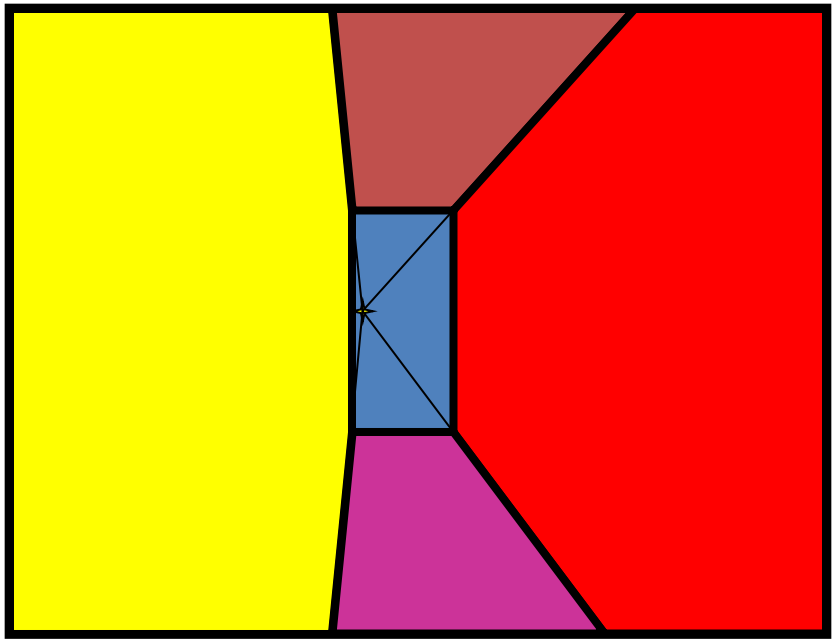
Another example of user input: vanishing point and back face of view volume are defined



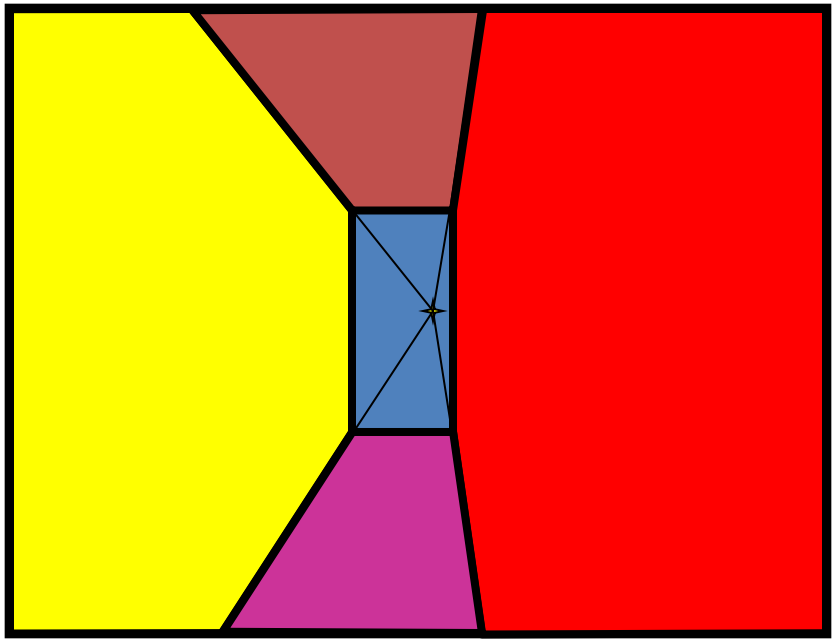
Another example of user input: vanishing point and back face of view volume are defined



Comparison of two camera placements – left and right. Corresponding subdivisions match view you would see if you looked down a hallway.



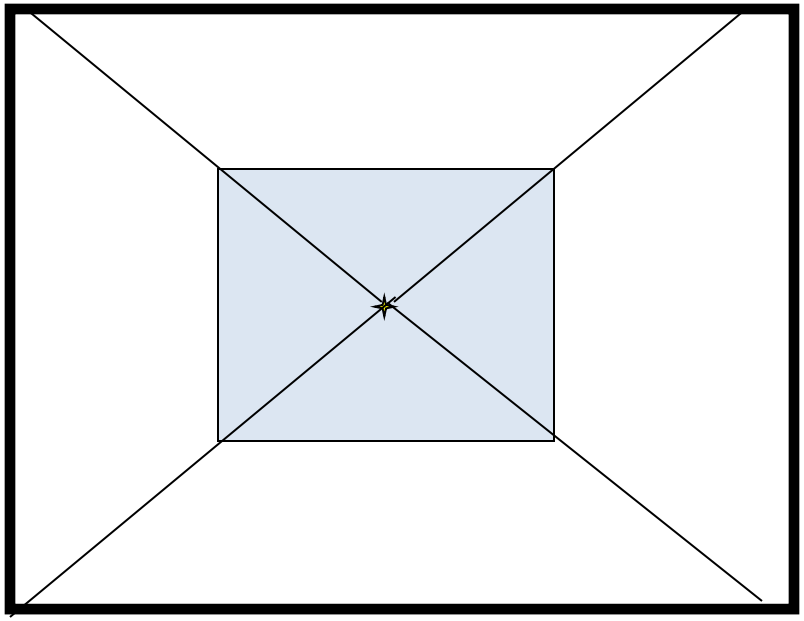
Left Camera



Right Camera

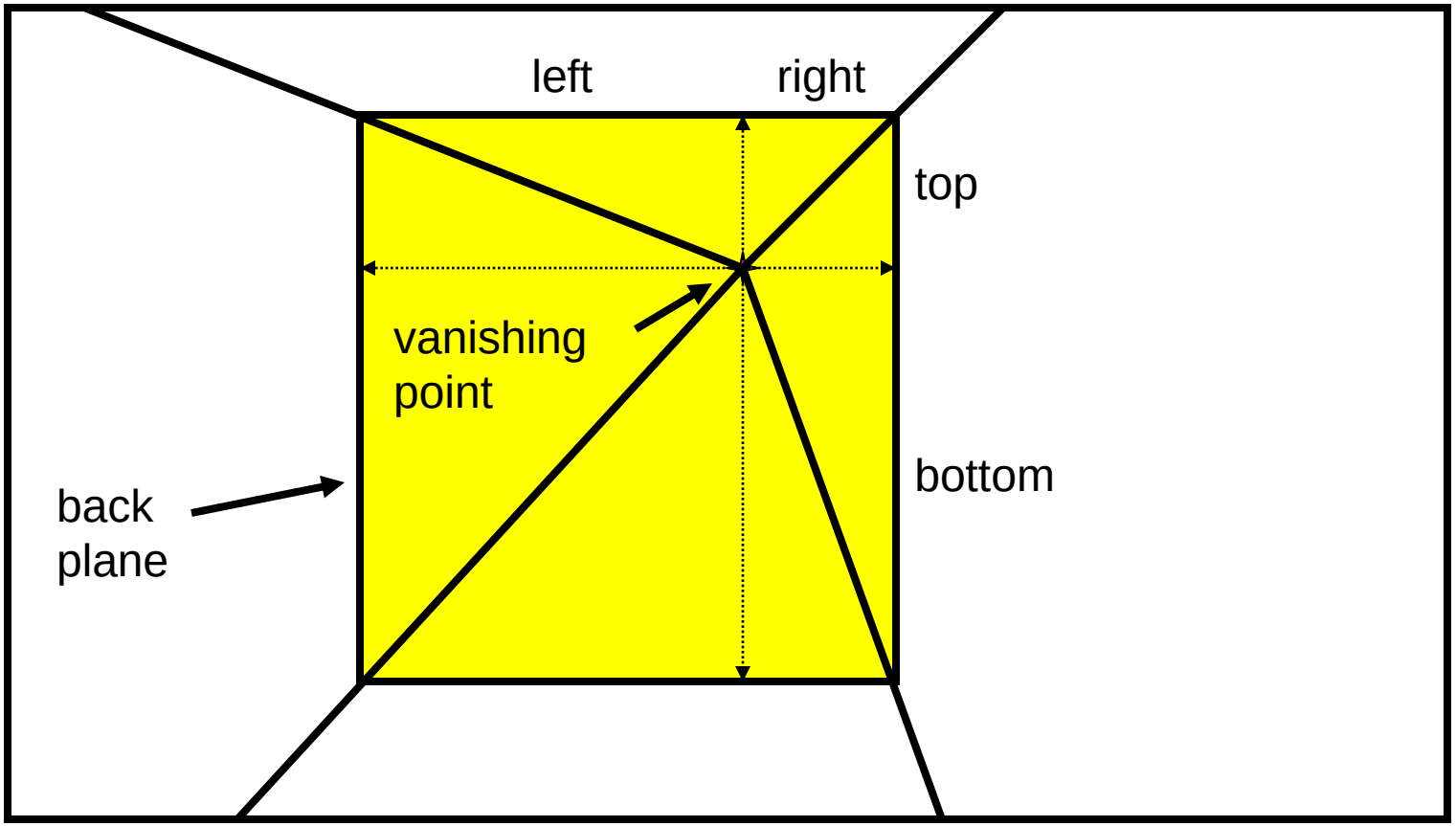
Question

- Think about the camera center and image plane…
  - What happens when we move the box?
  - What happens when we move the vanishing point?



2D to 3D conversion

- First, we can get ratios

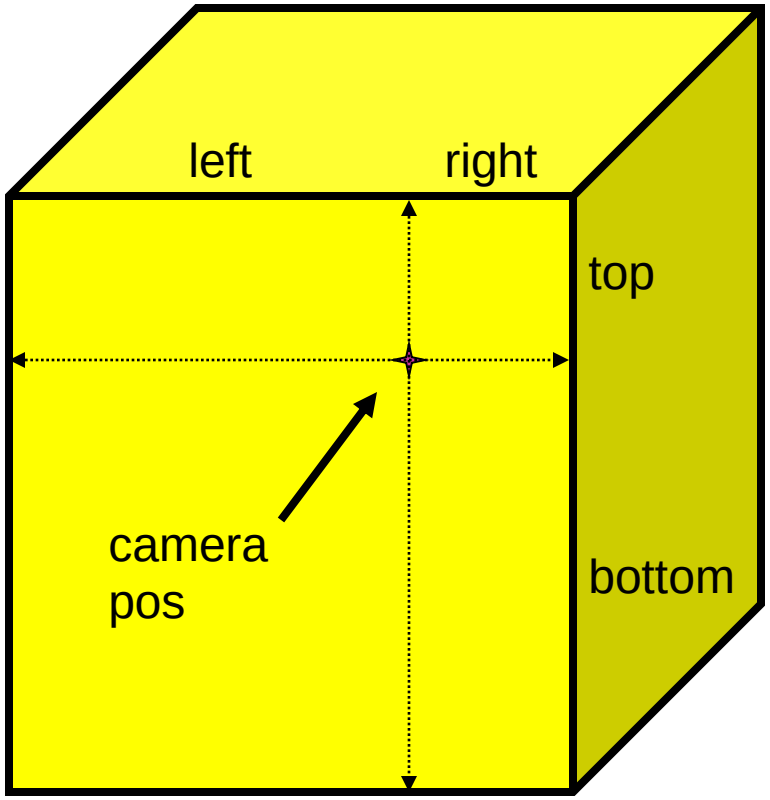


2D to 3D conversion

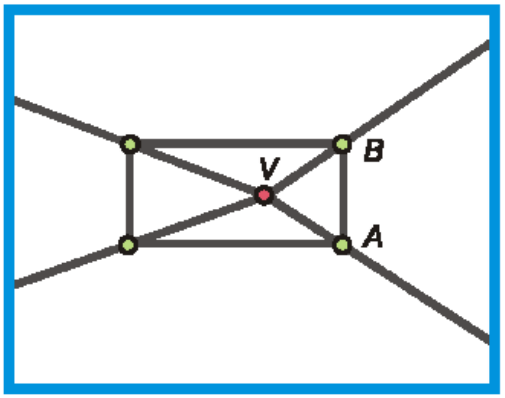
Size of user-defined back plane determines width/height throughout box (orthogonal sides)

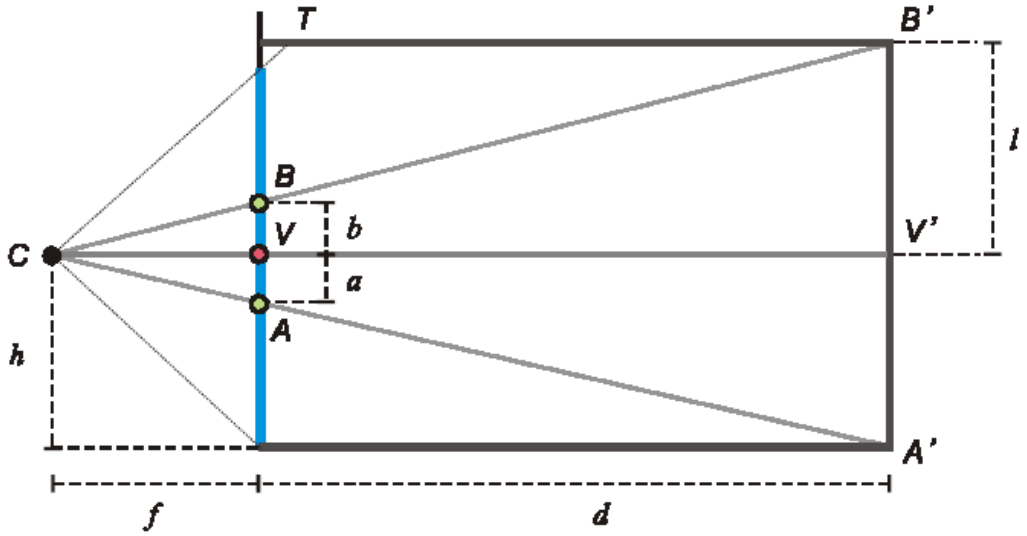
Use top versus side ratio to determine relative height and width dimensions of box

Left/right and top/bot ratios determine part of 3D camera placement



Depth of the box





- Can compute by similar triangles (CVA vs. CV'A')
- Need to know focal length f (or FOV)

- Note: can compute position on any object on the ground
  - Simple unprojection
  - What about things off the ground?

Homography

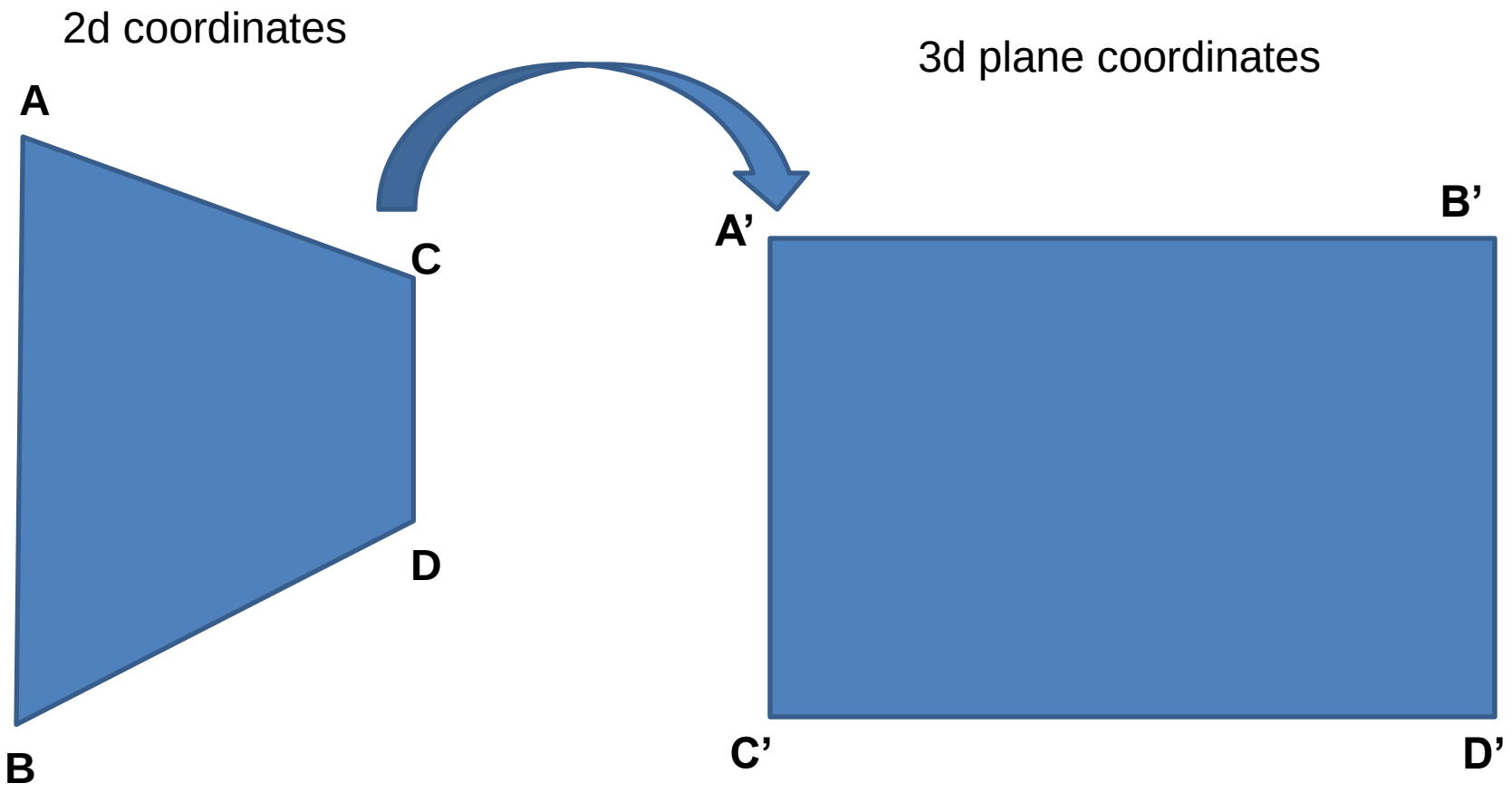
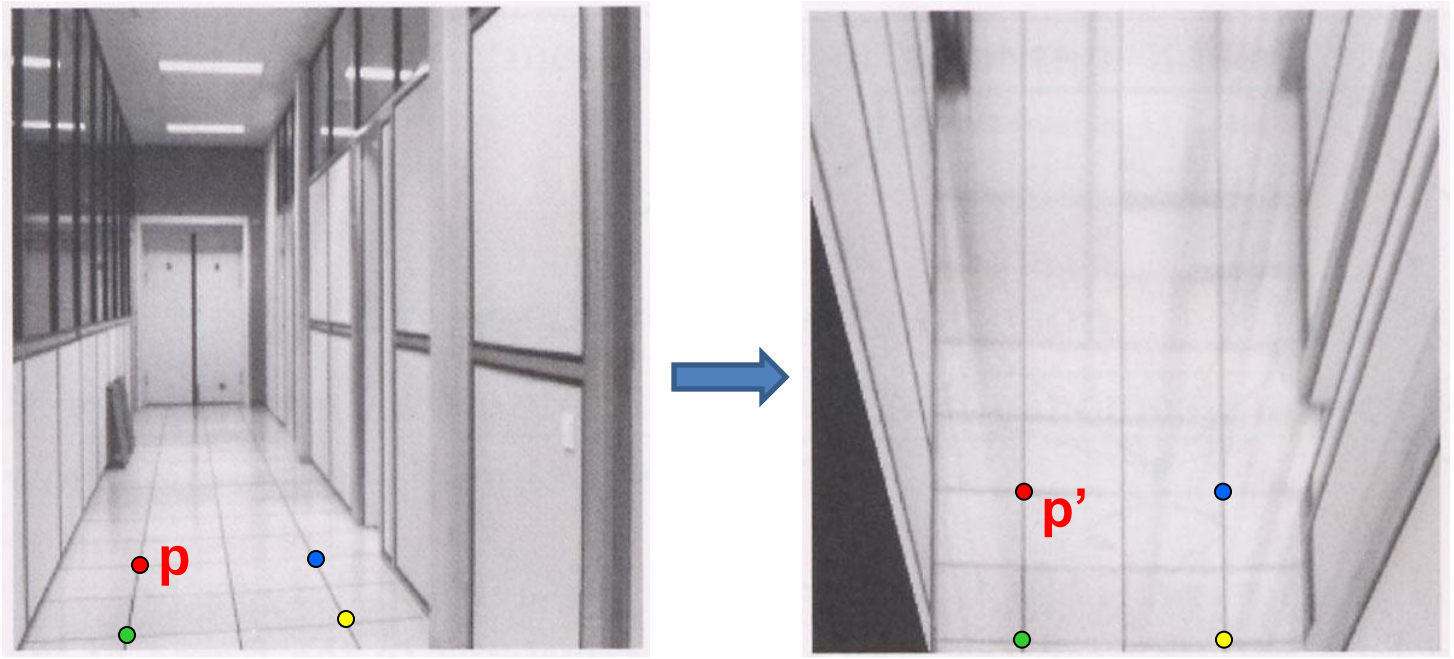


Image rectification



To unwarp (rectify) an image solve for homography **H** given **p** and **p’:** w**p’=Hp**

Computing homography

Assume we have four matched points: How do we compute homography **H**?

Direct Linear Transformation (DLT)

$$\mathbf{p}' = \mathbf{H}\mathbf{p} \qquad \mathbf{p}' = \begin{bmatrix} w'u' \\ w'v' \\ w' \end{bmatrix} \qquad \mathbf{H} = \begin{bmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{bmatrix}$$

$$\begin{bmatrix} -u & -v & -1 & 0 & 0 & 0 & uu' & vu' & u' \\ 0 & 0 & 0 & -u & -v & -1 & uv' & vv' & v' \end{bmatrix} \mathbf{h} = \mathbf{0} \qquad \mathbf{h} = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \\ h_5 \\ h_6 \\ h_7 \\ h_8 \\ h_9 \end{bmatrix}$$

Computing homography

Direct Linear Transform

$$\begin{bmatrix} -u_1 & -v_1 & -1 & 0 & 0 & 0 & u_1u_1' & v_1u_1' & u_1' \\ 0 & 0 & 0 & -u_1 & -v_1 & -1 & u_1v_1' & v_1v_1' & v_1' \\ & & & & \vdots & & & & \\ 0 & 0 & 0 & -u_n & -v_n & -1 & u_nv_n' & v_nv_n' & v_n' \end{bmatrix} \mathbf{h} = \mathbf{0} \Rightarrow \mathbf{Ah} = \mathbf{0}$$

- Apply SVD: $\boldsymbol{UDV}^T = \boldsymbol{A}$
- $\boldsymbol{h} = \boldsymbol{V}_{\text{smallest}}$ (column of $\boldsymbol{V}$ corr. to smallest singular value)

$$\mathbf{h} = \begin{bmatrix} h_1 \\ h_2 \\ \vdots \\ h_9 \end{bmatrix} \quad \mathbf{H} = \begin{bmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{bmatrix}$$

Matlab

```
[U, S, V] = svd(A);
h = V(:, end);
```

Explanations of SVD and solving homogeneous linear systems

Tour into the picture algorithm

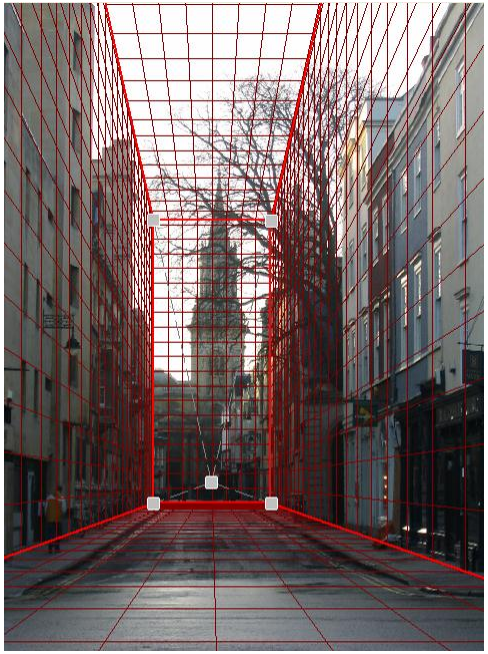
1. Set the box corners

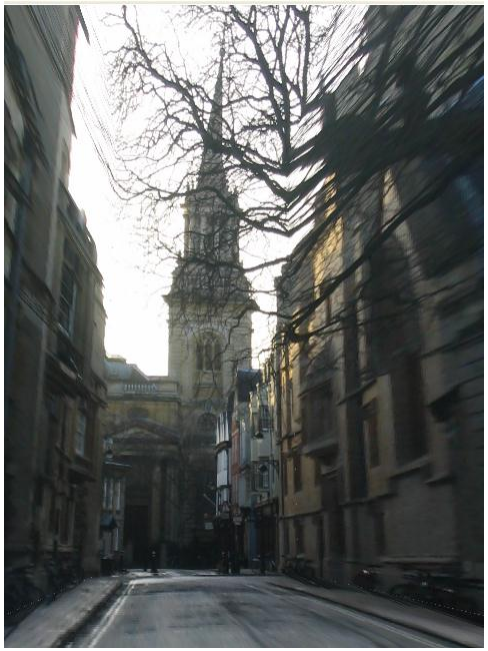
Tour into the picture algorithm

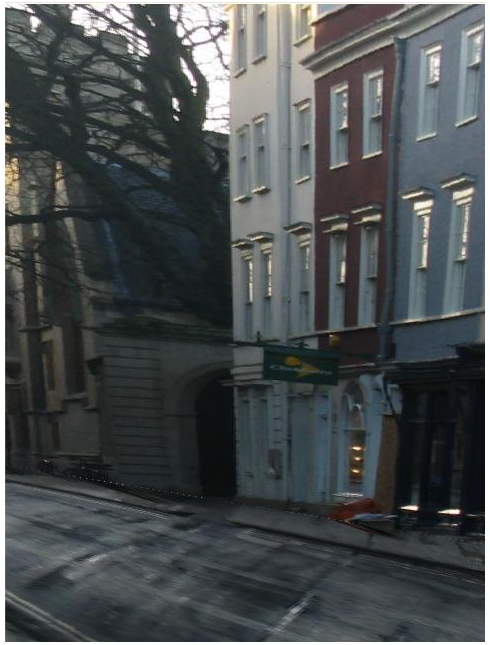
1. Set the box corners
2. Set the VP
3. Get 3D coordinates
   - Compute height, width, and depth of box
4. Get texture maps
   - homographies for each face

Result

Render from new views







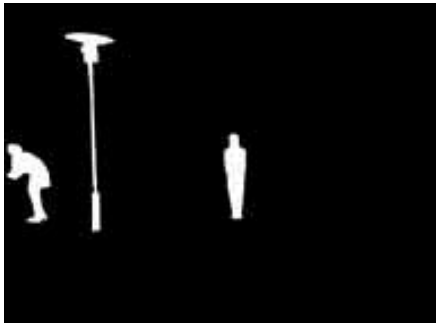
http://www.cs.cmu.edu/afs/cs.cmu.edu/academic/class/15463-f08/www/proj5/www/dmillett/

Foreground Objects

Use separate billboard for each

For this to work, three separate images used:

- Original image.
- Mask to isolate desired foreground images.
- Background with objects removed

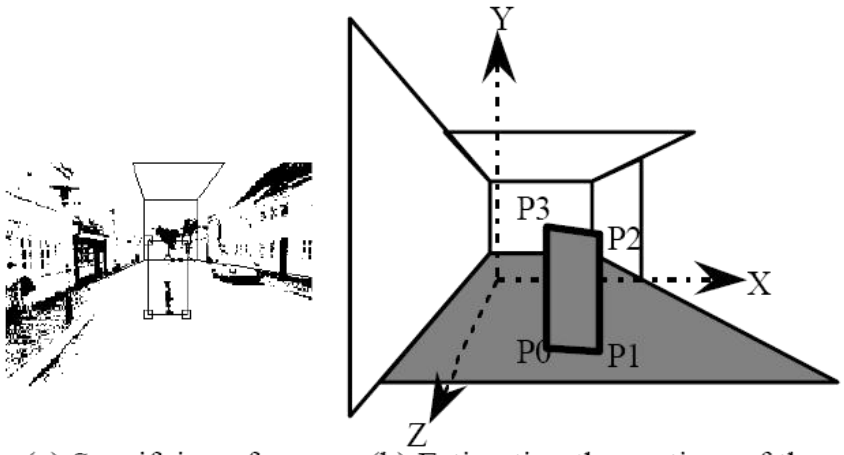


Foreground Objects

Add vertical rectangles for each foreground object

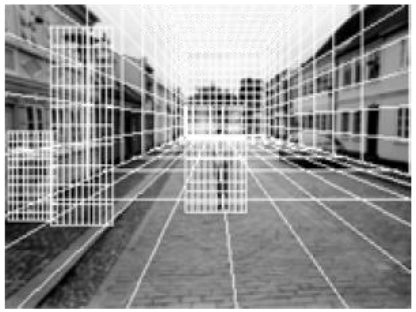
Can compute 3D coordinates P0, P1 since they are on known plane.

P2, P3 can be computed as before (similar triangles)



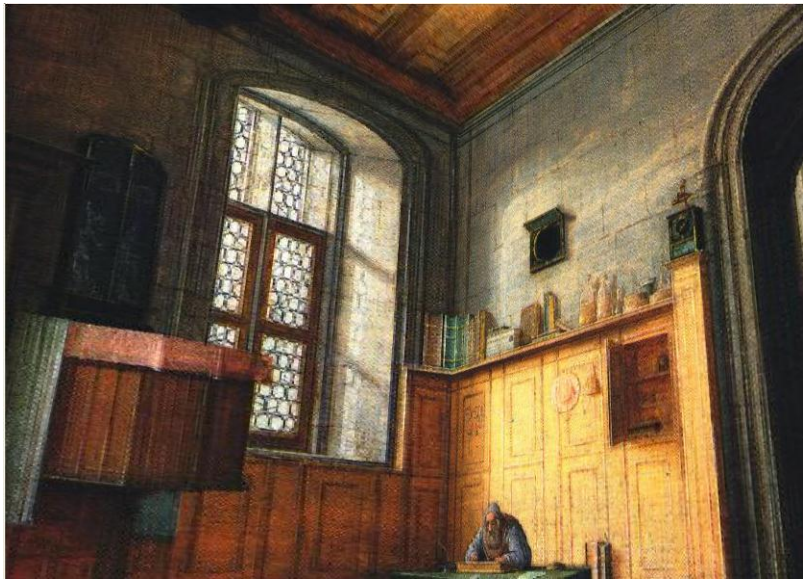
(a) Specifying of a foreground object

(b) Estimating the vertices of the foreground object model



(c) Three foreground object models

Foreground Result



Video from CMU class:
http://www.youtube.com/watch?v=dUAtdmGwcuM

Automatic Photo Pop-up

Input | Geometric Labels | Cut'n'Fold | 3D Model

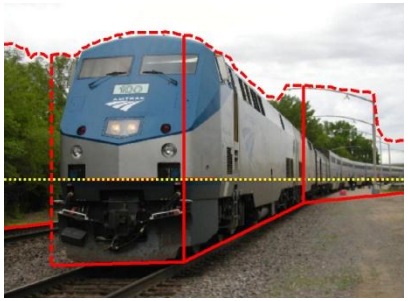
Image

Learned Models

Ground

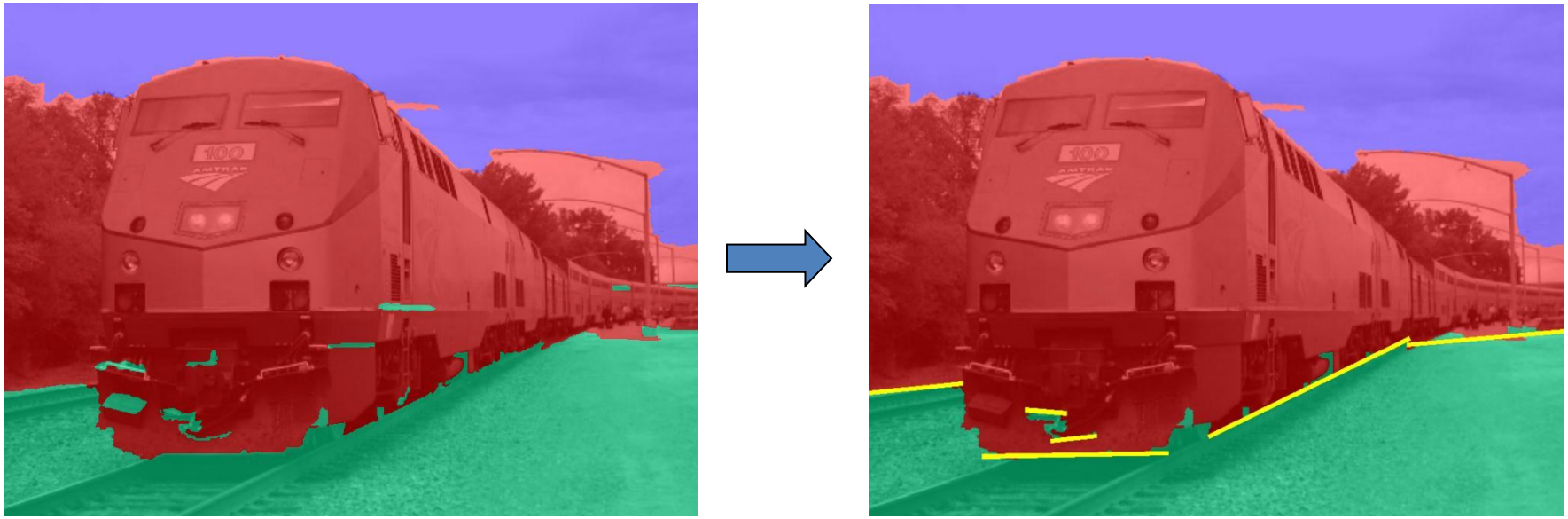
Vertical

Sky



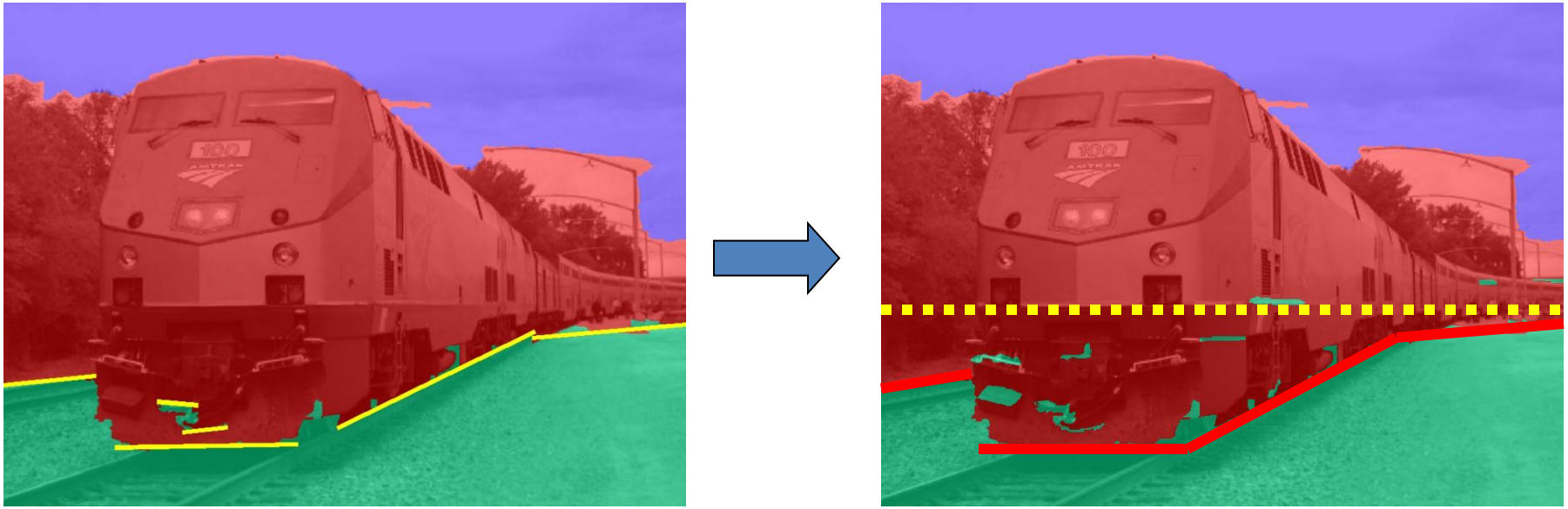
Hoiem et al. 2005

Cutting and Folding



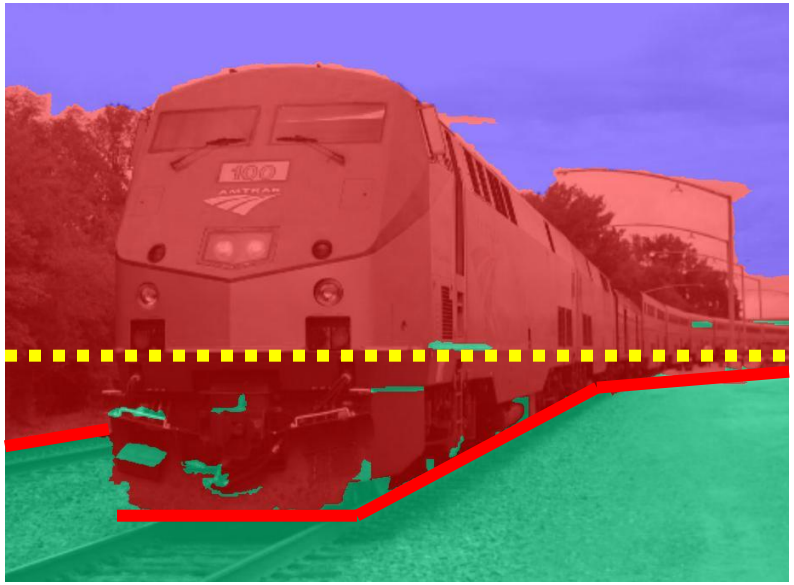
- Fit ground-vertical boundary
  - Iterative Hough transform

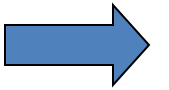
Cutting and Folding

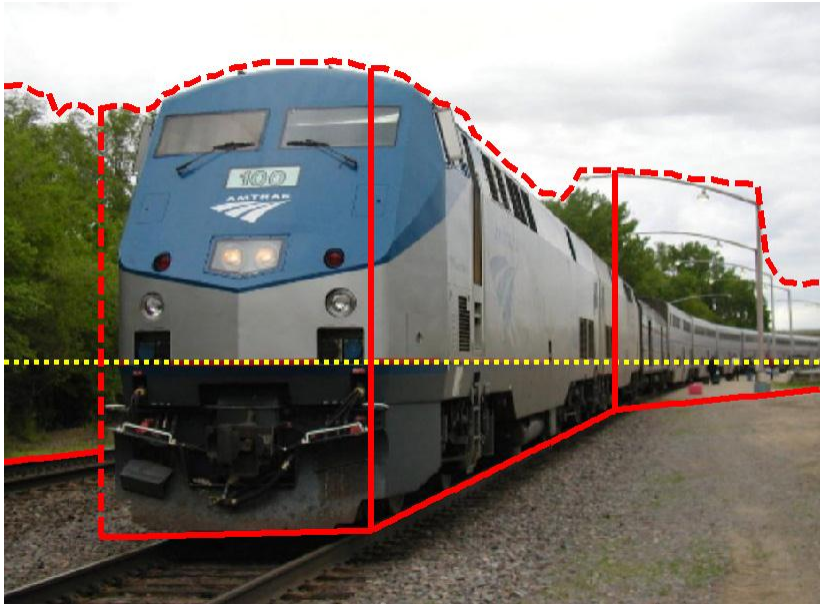


- Form polylines from boundary segments
  - Join segments that intersect at slight angles
  - Remove small overlapping polylines
- Estimate horizon position from perspective cues

Cutting and Folding

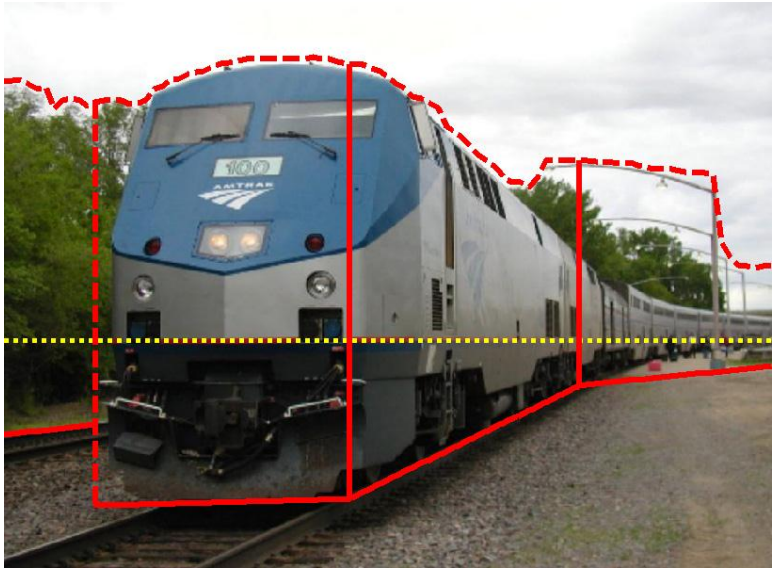






- ``Fold'' along polylines and at corners
- ``Cut'' at ends of polylines and along vertical-sky boundary

Cutting and Folding

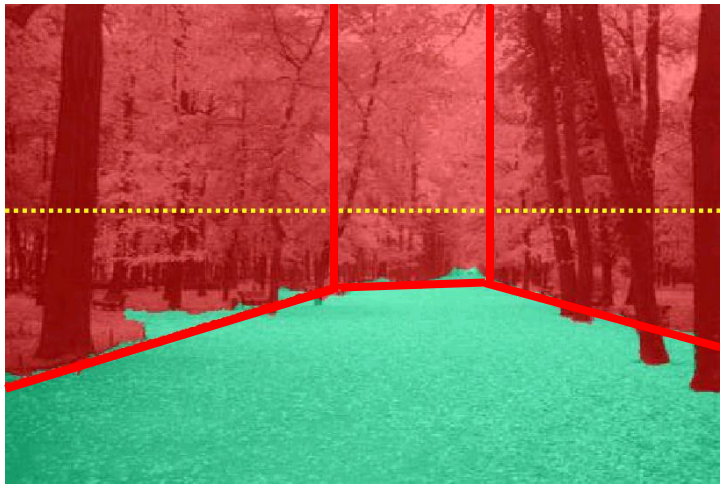


- Construct 3D model
- Texture map

Results

http://www.cs.illinois.edu/homes/dhoiem/projects/popup/

Input Image



Cut and Fold

Automatic Photo Pop-up

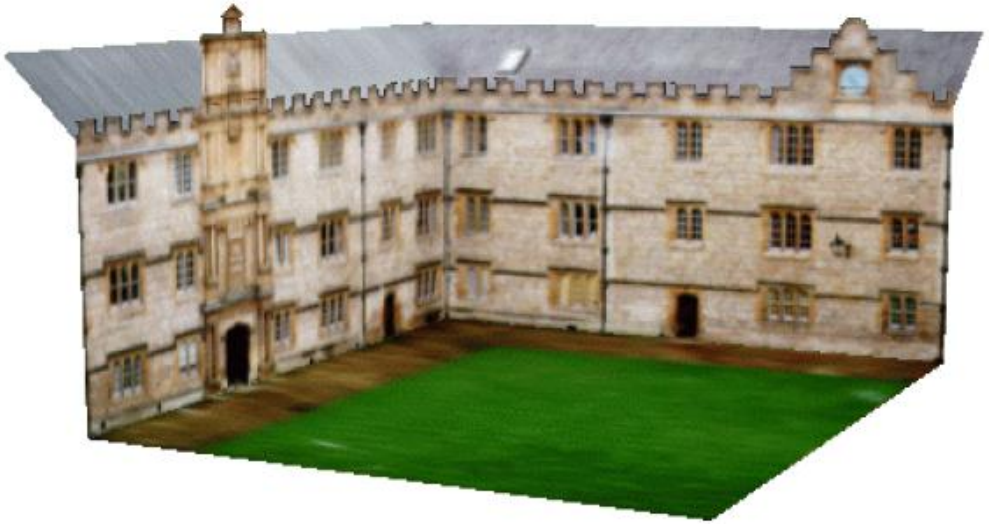
Results

Input Image

Automatic Photo Pop-up

Comparison with Manual Method

Input Image



[Liebowitz et al. 1999]

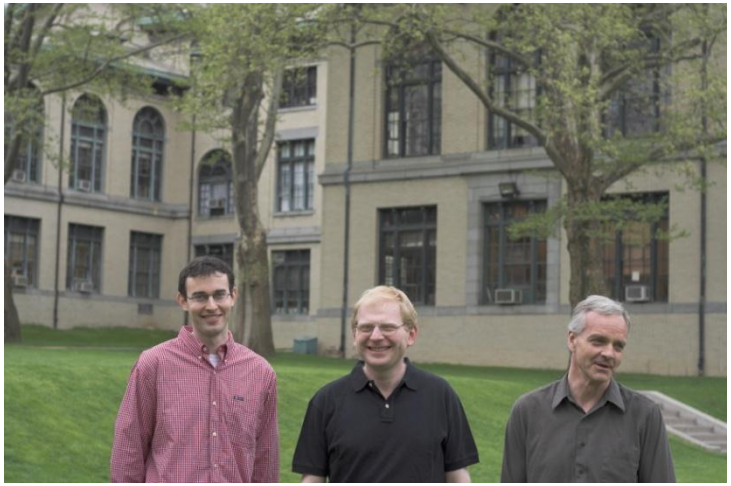
Automatic Photo Pop-up (30 sec)!

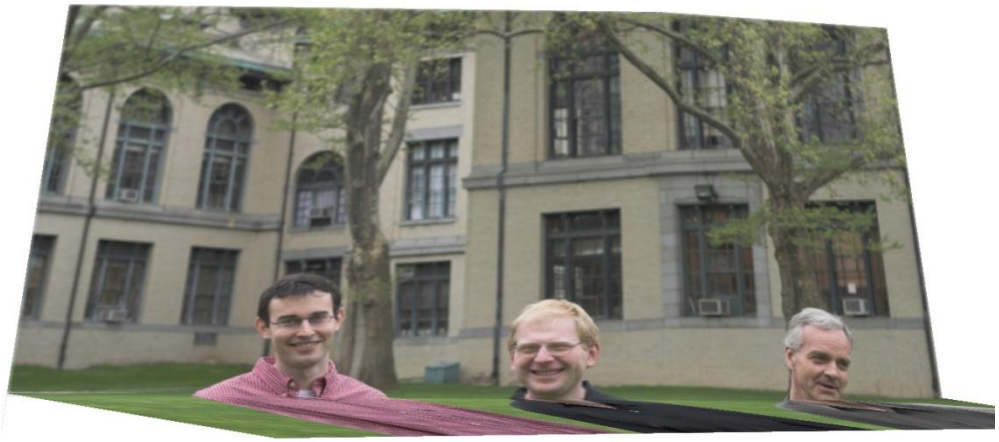
Failures

Labeling Errors

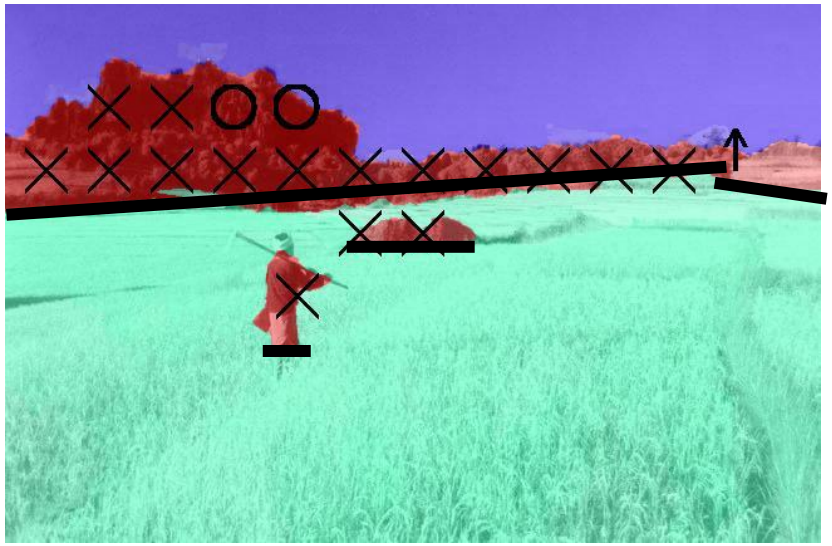
Failures

Foreground Objects

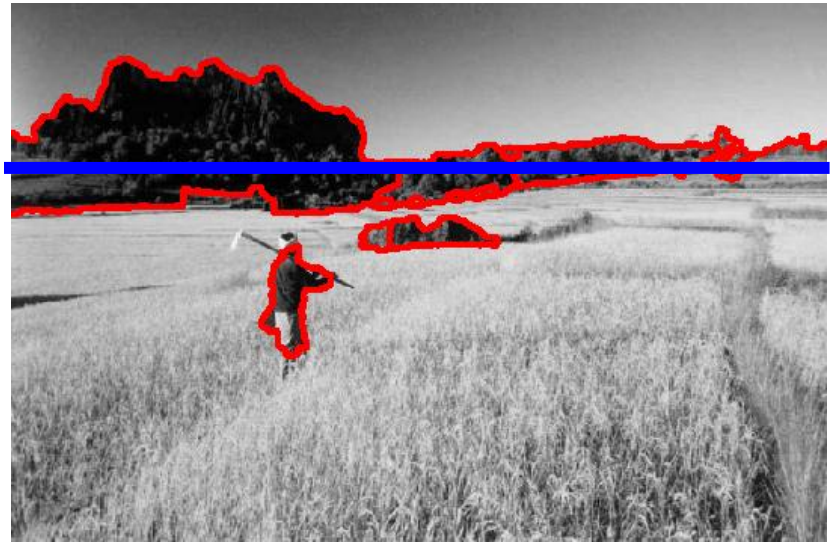




Adding Foreground Labels



Recovered Surface Labels +
Ground-Vertical Boundary Fit



Object Boundaries + Horizon

Final project ideas

- If a one-person project:
  - Interactive program to make 3D model from an image (e.g., output in VRML, or draw path for animation)

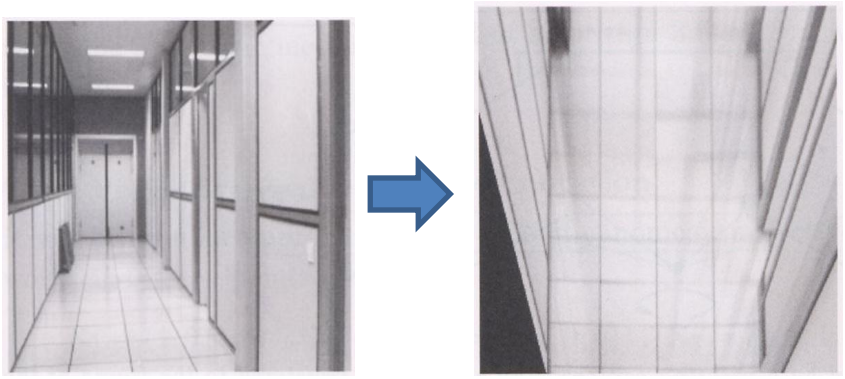
- If a two-person team, 2nd person:
  - Add tools for cutting out foreground objects and automatic hole-filling

Summary

- 2D→3D is mathematically impossible

- Need right assumptions about the world geometry

- Important tools
  - Vanishing points
  - Camera matrix
  - Homography



Next Class

- Kevin Karsch will show his work that applies many ideas from this section (cutting, texture synthesis, projective geometry, etc.)

- Next Thursday: start of new section
  - Finding correspondences automatically
  - Image stitching
  - Various forms of recognition