
HW 2 – Binary Decision Diagrams

CS 477 – Spring 2020

Revision 1.0

Assigned February 5, 2020

Due February 12, 2020, 9:00 pm

Extension 48 hours (20% penalty)

1 Change Log

1.0 Initial Release.

2 Objectives and Background

The purpose of this HW is to test your understanding of

- Binary Decision Diagrams and the Shannon Expansion

Another purpose of HWs is to provide you with experience answering non-programming written questions of the kind you may experience on the midterm and final.

3 Turn-In Procedure

The pdf for this assignment (`hw2.pdf`) should be found in the `assignments/hw2/` subdirectory of your `svn` directory for this course. Your solution should be put in that same directory. Using your favorite tool(s), you should put your solution in a file named `hw2-submission.pdf`. If you have problems generating a pdf, please seek help from the course staff. Your answers to the following questions are to be submitted electronically from within `assignments/hw2/` subdirectory by committing the file as follows:

```
git add hw2-submission.pdf
git commit -m "Turning in hw2"
git push
```

4 Problems

For each of the following propositions,

- (4 pts each) give the Shannon expansion (put it in `if_then_else` form), where you use the alphabetical ordering from least to greatest in generating the conditionals by the algorithm shown in class,
- (5 pts each) give the reduced ordered binary decision diagram (ROBDD), with the variables order smallest to largest alphabetically,
- (5 pts each) give the reduced ordered binary decision diagram (ROBDD), with the variables order reverse alphabetically,
- (3pts each) say whether it is satisfiable, and if it is, give a valuation satisfying it.

Since many of you will want to know, I use dot/graphviz to generate the pdfs for the directed graphs you need in b and c. You should feel free to draw them by hand.

1. $(A \wedge B) \vee (A \wedge C)$
2. $(A \Rightarrow (B \Rightarrow C)) \wedge ((A \Rightarrow B) \Rightarrow C)$
3. $(A \Rightarrow B) \Rightarrow ((A \wedge C) \Rightarrow (B \wedge C))$

5 Extra Credit

4. (10 pts) Show that for any proposition P and valuation of its propositional atoms v , that if v satisfies P then v satisfies the Shannon Expansion of P .

Hint: Firstly, you probably want to prove a more general result concerning partial results of the Shannon Expansion. Secondly, the Shannon Expansion is an iterative algorithm. In each pass something is getting smaller. What is it?