CS477 Formal Software Development Methods

Elsa L Gunter
2112 SC, UIUC
egunter@illinois.edu
http://courses.engr.illinois.edu/cs477

Slides mostly a reproduction of Theo C. Ruys – SPIN Beginners' Tutorial

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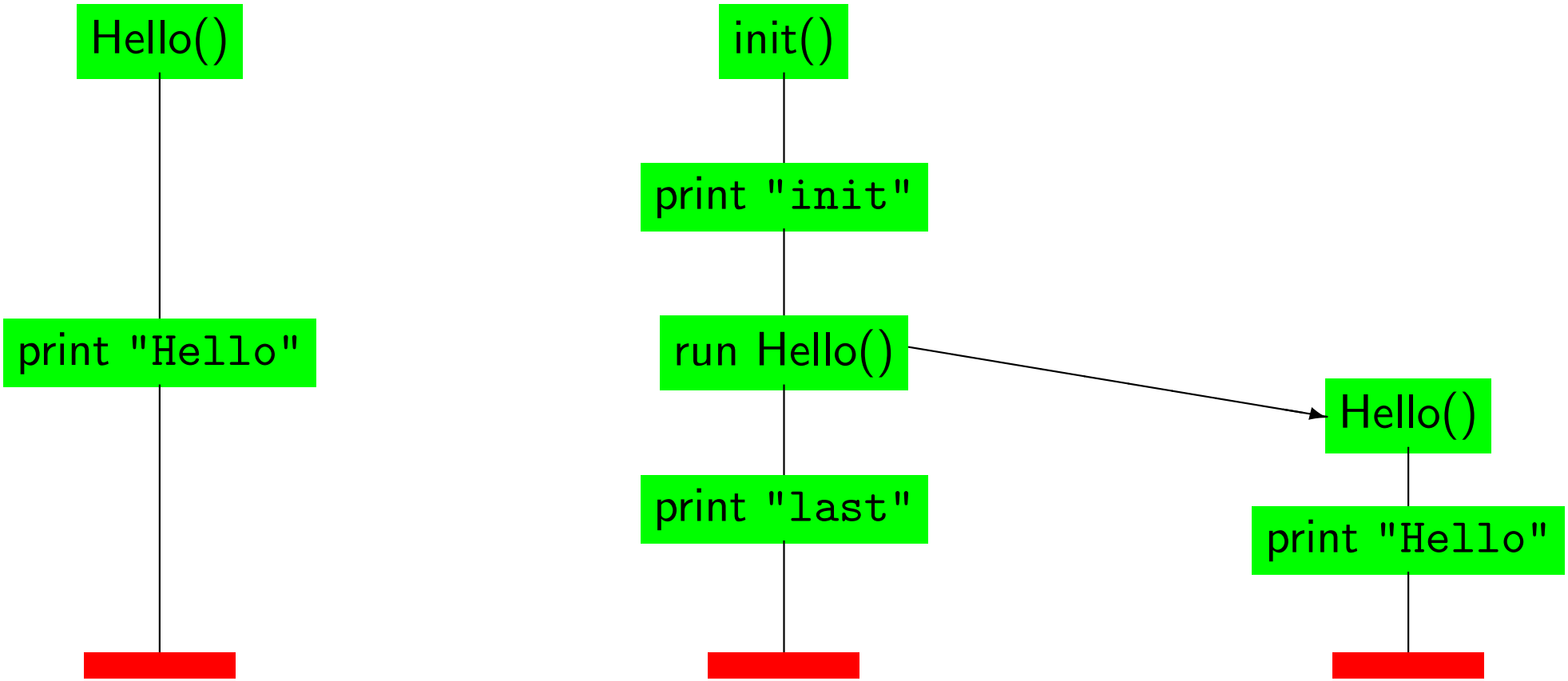
Hello World

```
/* A "Hello World" Promela model for SPIN. */
active proctype Hello() {
printf("Hello process, my pid is: %d\n", _pid);
}
init {
      int lastpid;
      printf("init process, my pid is: %d\n", _pid);
      lastpid = run Hello();
      printf("last pid was: %d\n", lastpid);
}
```

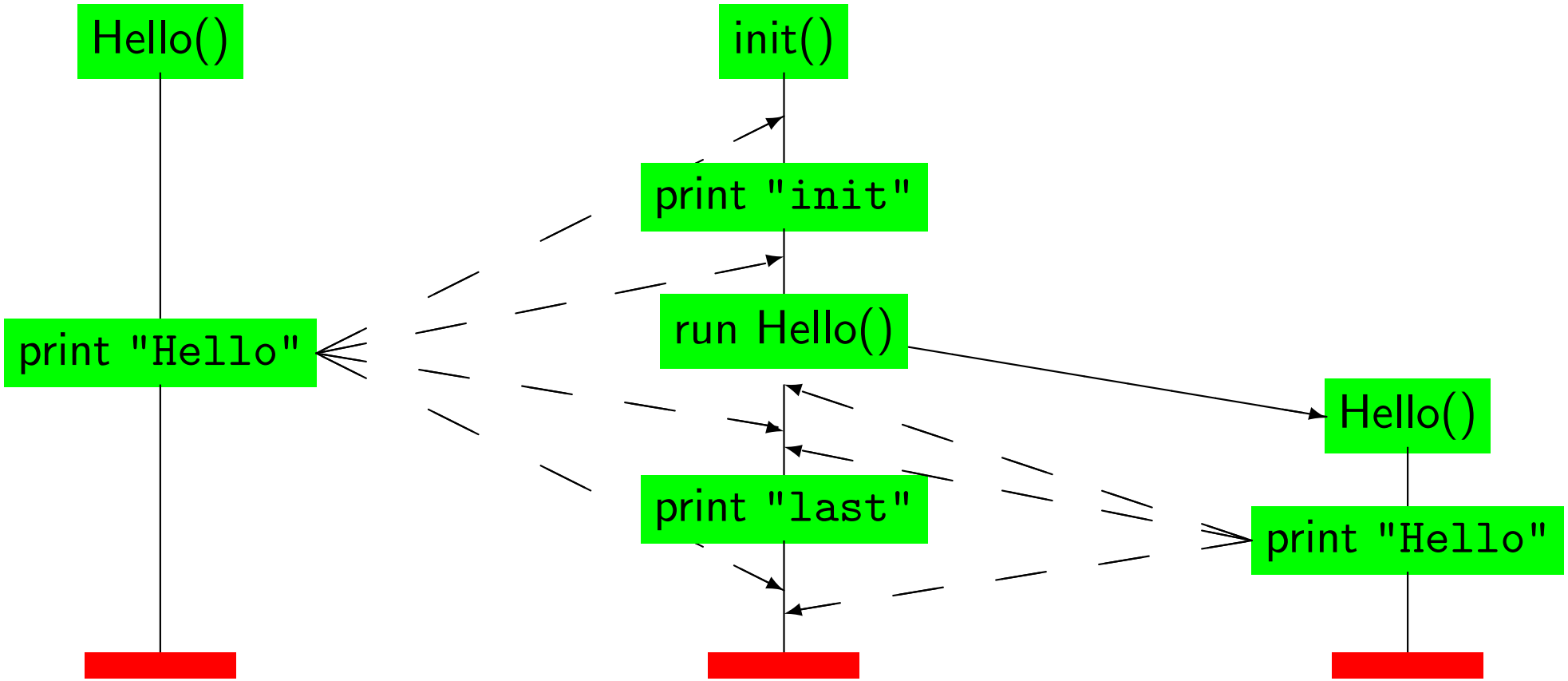
Hello World, Sample Execution

```
bash-3.2$ spin hello.pml
          init process, my pid is: 1
      Hello process, my pid is: 0
              Hello process, my pid is: 2
          last pid was: 2
3 processes created
bash-3.2$ spin hello.pml
      Hello process, my pid is: 0
          init process, my pid is: 1
          last pid was: 2
              Hello process, my pid is: 2
3 processes created
```

Hello Processes



Hello Processes Interleavings



Interleaving Semantics

- Promela processes execute concurrently.
- Non-deterministic scheduling of the processes.
- Processes are interleaved
  - Only one process can execute a statement at each point in time.
  - Exception: rendez-vous communication.
- All statements are atomic
  - Each statement is executed without interleaving it parts with other processes.
- Each process may have several different possible actions enabled at each point of execution.
  - Only one choice is made, non-deterministically (randomly).

Variables and Types (1)

- Five different (integer) basic types.
- Arrays
- Records (structs)
- Type conflicts are detected at runtime.
- Default initial value of basic variables (local and global) is 0.
- mtype (message type) one user-defined enum type

Basic types

```
bit   turn=1;        [0..1]
bool  flag;          [0..1]
byte  counter;       [0..255]
short s;             [-2^16-1.. 2^16 -1]
int   msg;           [-2^32-1.. 2^32 -1]
```

Arrays

```
byte a[27];
bit  flags[4];
```

array indicing start at 0

Typedef (records)

```
typedef Record {
  short f1;
  byte  f2;
}
Record rr;
rr.f1 = ..
```

variable declaration

Variables and Types (2)

- Variables should be declared.
- Variables can be given a value by:
  - assignment
  - argument passing
  - message passing (see communication)
- Variables can be used in expressions.

Most arithmetic, relational, and logical operators of C/Java are supported, including bitshift operators.

```
int ii;
bit bb;

bb=1;
ii=2;

short s=-1;

typedef Foo {
  bit bb;
  int ii;
};
Foo f;
f.bb = 0;
f.ii = -2;

ii*s+27 == 23;
printf("value: %d", s*s);
```

assignment =

declaration + initialisation

equal test ==

Statements (1)

- The body of a process consists of a sequence of statements. A statement is either
  - executable: the statement can be executed immediately.
  - blocked: the statement cannot be executed.

executable/blocked depends on the global state of the system.

- An assignment is always executable.
- An expression is also a statement; it is executable if it evaluates to non-zero.

`2 < 3`	always executable
`x < 27`	only executable if value of `x` is smaller `27`
`3 + x`	executable if `x` is not equal to `-3`

Statements (2)

Statements are separated by a semi-colon: ";".

- The **skip** statement is always executable.
  - "does nothing", only changes process' process counter
- A **run** statement is only executable if a new process can be created (remember: the number of processes is bounded).
- A **printf** statement is always executable (but is not evaluated during verification, of course).

```
int x;
proctype Aap()
{
  int y=1;
  skip;
  run Noot();
  x=2;
  x>2 && y==1;
  skip;
}
```

Executable if **Noot** can be created...

Can only become executable if a some other process makes **x** greater than 2.

Statements (3)

- **assert(<expr>);**
  - The **assert**-statement is always executable.
  - If **<expr>** evaluates to zero, SPIN will exit with an error, as the **<expr>** "has been violated".
  - The **assert**-statement is often used within Promela models, to check whether certain properties are valid in a state.

```
proctype monitor() {
  assert(n <= 3);
}

proctype receiver() {
  ...
  toReceiver ? msg;
  assert(msg != ERROR);
  ...
}
```

DEMO

WRONG!

Mutual Exclusion (1)

```
bit  flag;     /* signal entering/leaving the section */
byte mutex;    /* # procs in the critical section.    */

proctype P(bit i) {
  flag != 1;
  flag  = 1;
  mutex++;
  printf("MSC: P(%d) has entered section.\n", i);
  mutex--;
  flag  = 0;
}

proctype monitor() {
  assert(mutex != 2);
}

init {
  atomic { run P(0); run P(1); run monitor(); }
}
```

models:
`while (flag == 1) /* wait */;`

Problem: assertion violation!
Both processes can pass the `flag != 1` "at the same time", i.e. before `flag` is set to `1`.

starts two instances of process P

DEMO

WRONG!

Mutual Exclusion (2)

```
bit  x, y;     /* signal entering/leaving the section  */
byte mutex;    /* # of procs in the critical section.  */

active proctype A() {
  x = 1;
  y == 0;
  mutex++;
  mutex--;
  x = 0;
}

active proctype B() {
  y = 1;
  x == 0;
  mutex++;
  mutex--;
  y = 0;
}

active proctype monitor() {
  assert(mutex != 2);
}
```

Process A waits for process B to end.

Problem: invalid-end-state!
Both processes can pass execute `x = 1` and `y = 1` "at the same time", and will then be waiting for each other.

DEMO

Dekker [1962]

Mutual Exclusion (3)

```
bit  x, y;     /* signal entering/leaving the section  */
byte mutex;    /* # of procs in the critical section.  */
byte turn;     /* who's turn is it?                    */

active proctype A() {
  x = 1;
  turn = B_TURN;
  y == 0 ||
    (turn == A_TURN);
  mutex++;
  mutex--;
  x = 0;
}

active proctype B() {
  y = 1;
  turn = A_TURN;
  x == 0 ||
    (turn == B_TURN);
  mutex++;
  mutex--;
  y = 0;
}

active proctype monitor() {
  assert(mutex != 2);
}
```

Can be generalised to a single process.

First "software-only" solution to the mutex problem (for two processes).

DEMO

Bakery

Mutual Exclusion (4)

```
byte turn[2];  /* who's turn is it?              */
byte mutex;    /* # procs in critical section */

proctype P(bit i) {
  do
  :: turn[i] = 1;
     turn[i] = turn[1-i] + 1;
     (turn[1-i] == 0) || (turn[i] < turn[1-i]);
     mutex++;
     mutex--;
     turn[i] = 0;
  od
}

proctype monitor() { assert(mutex != 2); }
init { atomic {run P(0); run P(1); run monitor()}}
```

Problem (in Promela/SPIN): `turn[i]` will overrun after `255`.

More mutual exclusion algorithms in (good-old) [Ben-Ari 1990].

if-statement (1)

inspired by:
Dijkstra's guarded command language

```
if
:: choice1 -> stat1.1; stat1.2; stat1.3; …
:: choice2 -> stat2.1; stat2.2; stat2.3; …
:: …
:: choicen -> statn.1; statn.2; statn.3; …
fi;
```

- If there is at least one **choice$_i$** (guard) executable, the **if**-statement is executable and SPIN non-deterministically chooses one of the executable choices.
- If no **choice$_i$** is executable, the **if**-statement is blocked.
- The operator "**->**" is equivalent to "**;**". By convention, it is used within **if**-statements to separate the guards from the statements that follow the guards.

if-statement (2)

```
if
:: (n % 2 != 0) -> n=1
:: (n >= 0)     -> n=n-2
:: (n % 3 == 0) -> n=3
:: else         -> skip
fi
```

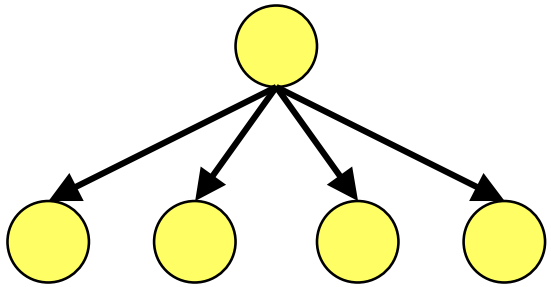
- The **else** guard becomes executable if none of the other guards is executable.

give n a random value

```
if
:: skip -> n=0
:: skip -> n=1
:: skip -> n=2
:: skip -> n=3
fi
```

skips are redundant, because assignments are themselves always executable...

non-deterministic branching



do-statement (1)

```
do
:: choice1 -> stat1.1; stat1.2; stat1.3; …
:: choice2 -> stat2.1; stat2.2; stat2.3; …
:: …
:: choicen -> statn.1; statn.2; statn.3; …
od;
```

- With respect to the choices, a **do**-statement behaves in the same way as an **if**-statement.
- However, instead of ending the statement at the end of the choosen list of statements, a **do**-statement repeats the choice selection.
- The (always executable) **break** statement exits a **do**-loop statement and transfers control to the end of the loop.

do-statement (2)

- Example – modelling a traffic light

`if`- and `do`-statements are ordinary Promela statements; so they can be nested.

```
mtype = { RED, YELLOW, GREEN } ;

active proctype TrafficLight() {
    byte state = GREEN;
    do
    ::  (state == GREEN)  -> state = YELLOW;
    ::  (state == YELLOW) -> state = RED;
    ::  (state == RED)    -> state = GREEN;
    od;
}
```

`mtype` (message type) models enumerations in Promela

Note: this `do`-loop does not contain any non-deterministic choice.

Communication

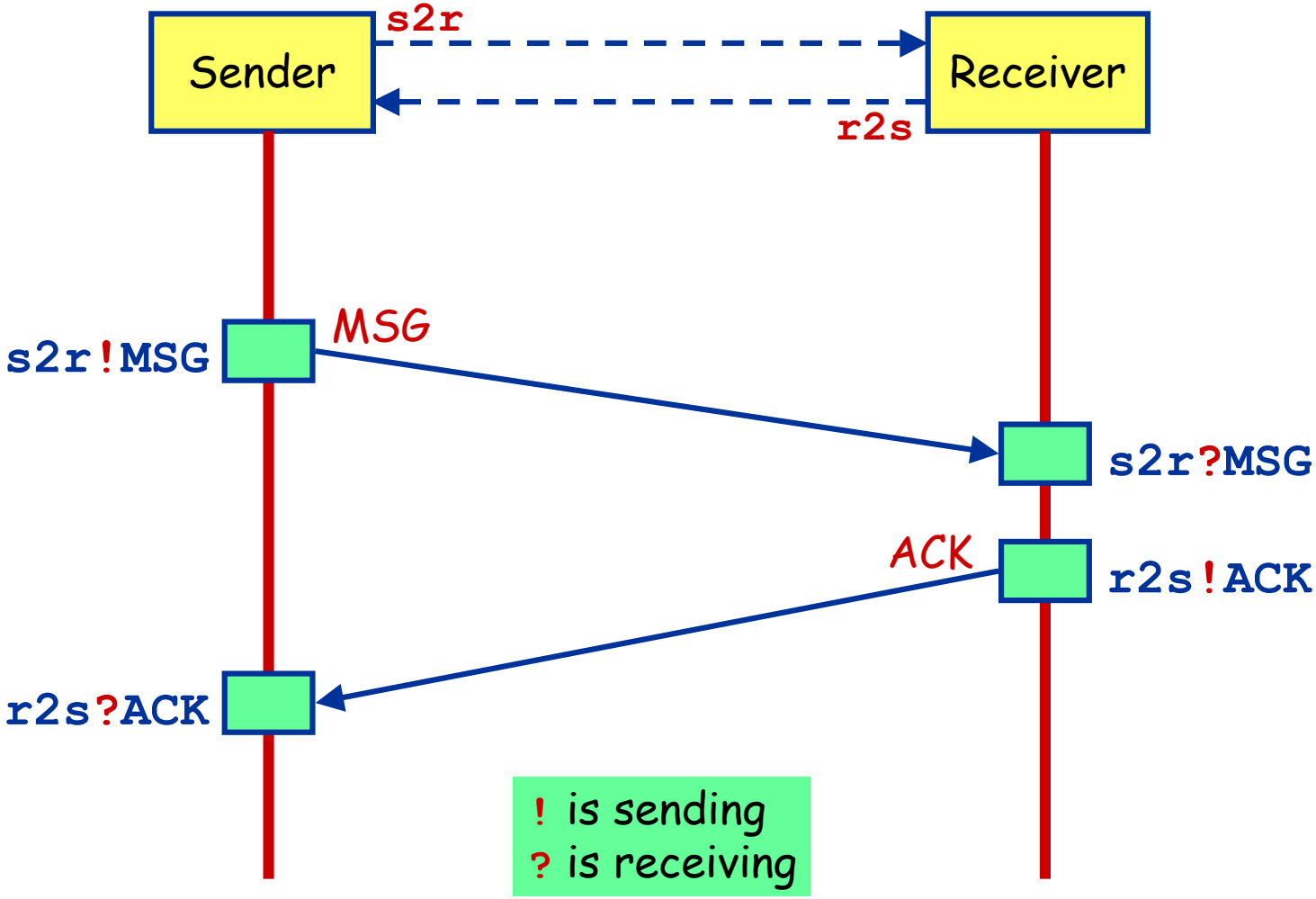
Major models of communication

1. Shared variables
   - one writes, many read later
2. Point-to-Point synchronous message passing
   - one sends, one other receives at the same time
   - send blocks until receieve can happen
3. Point-to-Point asynchronous message passing
   - one sends, one other receives some time later
   - send never blocks
4. Point-to-Point buffered message passing
   - When buffer not full behaves like asynchronous
   - When buffer full, two variations: block or drop message
   - send never blocks
5. Synchronous broadcast
   - one sends, many receive synchronously
   - First variation: send never blocks process may receive if ready to ready
   - Second variation: send blocks until all possible recipients ready to receive

Communication in SPIN

- With more or less complexity each can implement the others
- Spin supports 1 and 4 (blocks send when buffer full), but with bounded buffers
- Buffer size $= 0 \Longrightarrow$ synchronous communication
- Large buffer size approximates asynchronous communication

Communication (1)



Communication (2)

- Communication between processes is via channels:
  - message passing
  - rendez-vous synchronisation (handshake)
- Both are defined as channels:

also called:
queue or buffer

```
chan <name> = [<dim>] of {<t1>,<t2>, ... <tn>};
```

name of the channel

type of the elements that will be transmitted over the channel

number of elements in the channel
dim==0 is special case: rendez-vous

```
chan c        = [1] of {bit};
chan toR      = [2] of {mtype, bit};
chan line[2]  = [1] of {mtype, Record};
```

array of channels

Communication (3)

- channel = FIFO-buffer (for **dim>0**)

! Sending - *putting a message into a channel*

ch ! <expr$_1$>, <expr$_2$>, … <expr$_n$>;

- The values of **<expr$_i$>** should correspond with the types of the channel declaration.
- A send-statement is executable if the channel is not full.

? Receiving - *getting a message out of a channel*

<var> + <const> can be mixed

ch ? <var$_1$>, <var$_2$>, … <var$_n$>; message passing

- If the channel is not empty, the message is fetched from the channel and the individual parts of the message are stored into the **<var$_i$>**s.

ch ? <const$_1$>, <const$_2$>, … <const$_n$>; message testing

- If the channel is not empty and the message at the front of the channel evaluates to the individual **<const$_i$>**, the statement is executable and the message is removed from the channel.

Communication (4)

- Rendez-vous communication

  `<dim>` == 0

  The number of elements in the channel is now zero.

  – If send `ch!` is enabled and if there is a corresponding receive `ch?` that can be executed simultaneously and the constants match, then both statements are enabled.

  – Both statements will "handshake" and together take the transition.

- *Example:*

```
chan ch = [0] of {bit, byte};
```

  – P wants to do `ch ! 1, 3+7`

  – Q wants to do `ch ? 1, x`

  – Then after the communication, `x` will have the value `10`.

DEMO

Alternating Bit Protocol (1)

- Alternating Bit Protocol
  - To every message, the sender adds a bit.
  - The receiver acknowledges each message by sending the received bit back.
  - To receiver only excepts messages with a bit that it excepted to receive.
  - If the sender is sure that the receiver has correctly received the previous message, it sends a new message and it alternates the accompanying bit.

DEMO

Alternating Bit Protocol (2)

```
mtype {MSG, ACK};

chan toS = [2] of {mtype, bit};
chan toR = [2] of {mtype, bit};

proctype Sender(chan in, out)
{
  bit sendbit, recvbit;
  do
  :: out ! MSG, sendbit ->
       in ? ACK, recvbit;
       if
       :: recvbit == sendbit ->
          sendbit = 1-sendbit
       :: else
       fi
  od
}
```

channel length of 2

```
proctype Receiver(chan in, out)
{
  bit recvbit;
  do
  :: in ? MSG(recvbit) ->
     out ! ACK(recvbit);
  od
}

init
{
  run Sender(toS, toR);
  run Receiver(toR, toS);
}
```

Alternative notation:

```
ch ! MSG(par1, ...)
ch ? MSG(par1, ...)
```

atomic

atomic { $stat_1$; $stat_2$; ... $stat_n$ }

- can be used to group statements into an atomic sequence; all statements are executed in a single step (no interleaving with statements of other processes)
- is executable if **$stat_1$** is executable
- if a **$stat_i$** (with **i>1**) is blocked, the "atomicity token" is (temporarily) lost and other processes may do a step

no pure atomicity

- (Hardware) solution to the mutual exclusion problem:

```
proctype P(bit i) {
  atomic {flag != 1; flag = 1; }
  mutex++;
  mutex--;
  flag  = 0;
}
```

d_step

d_step { $stat_1$; $stat_2$; ... $stat_n$ }

- more efficient version of **atomic**: no intermediate states are generated and stored
- may only contain deterministic steps
- it is a run-time error if **$stat_i$ (i>1)** blocks.

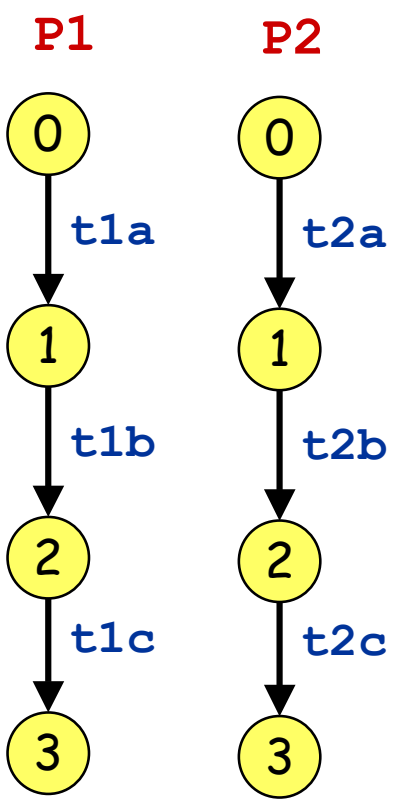
- **d_step** is especially useful to perform intermediate computations in a single transition

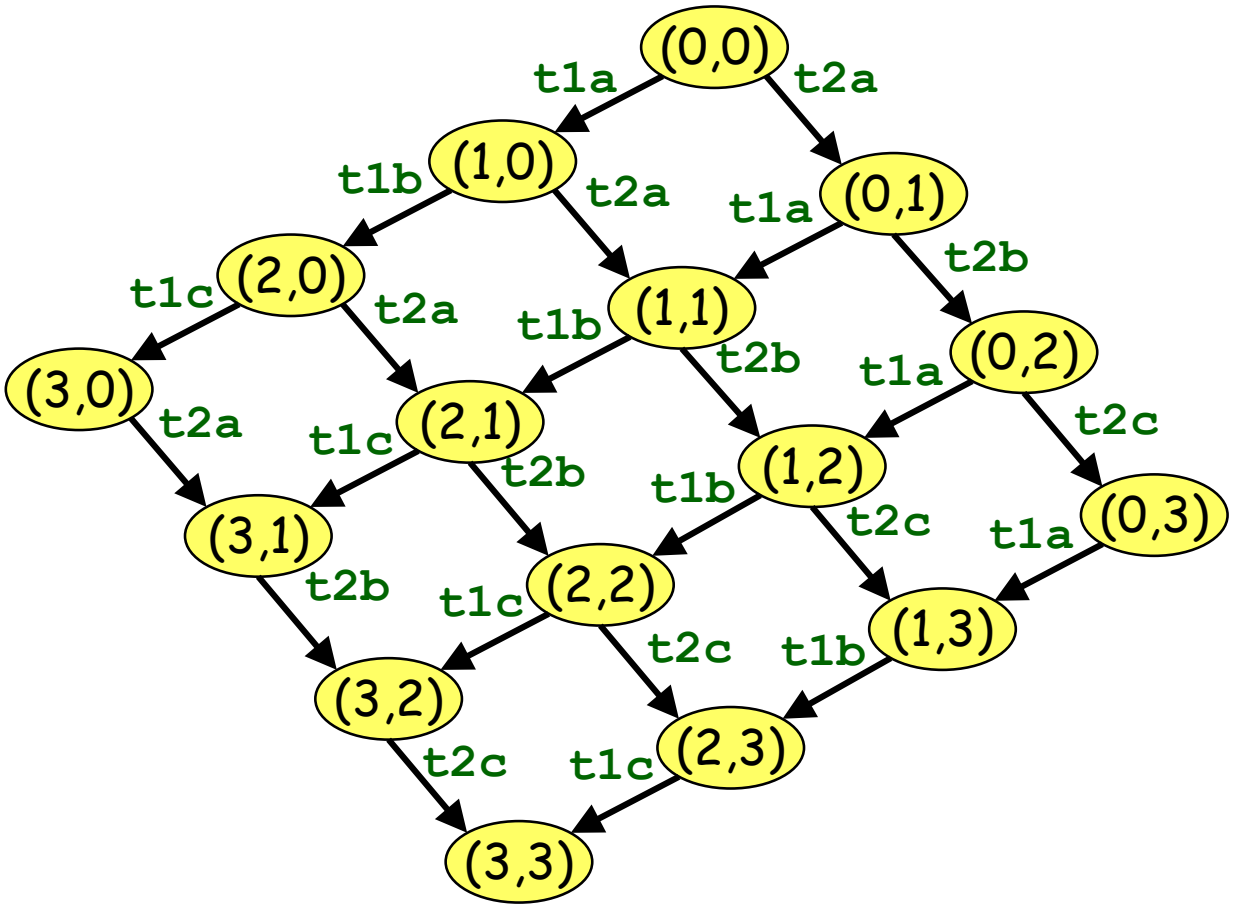
```
::  Rout?i(v) -> d_step {
        k++;
        e[k].ind = i;
        e[k].val = v;
        i=0; v=0 ;
    }
```

- **atomic** and **d_step** can be used to lower the number of states of the model

```
proctype P1() { t1a; t1b; t1c }
proctype P2() { t2a; t2b; t2c }
init { run P1(); run P2() }
```

No atomicity



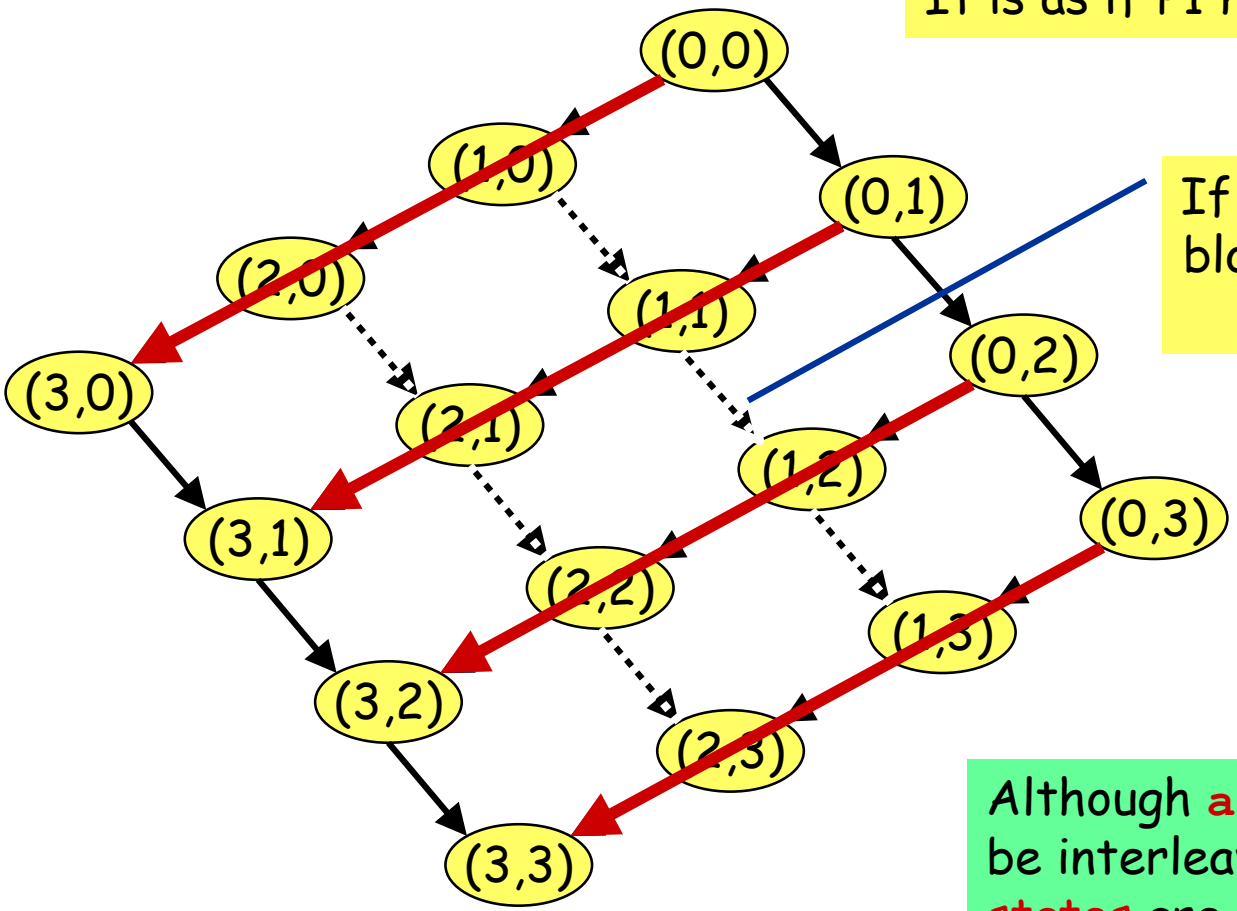


Not completely correct as each process has an implicit end-transition...

atomic

```
proctype P1() { atomic {t1a; t1b; t1c} }
proctype P2() { t2a; t2b; t2c }
init { run P1(); run P2() }
```

It is as if P1 has only one transition...



If one of P1's transitions blocks, these transitions may get executed

Although `atomic` clauses cannot be interleaved, the intermediate states are still constructed.

```
proctype P1() { d_step {t1a; t1b; t1c} }
proctype P2() { t2a; t2b; t2c }
init { run P1(); run P2() }
```

d_step

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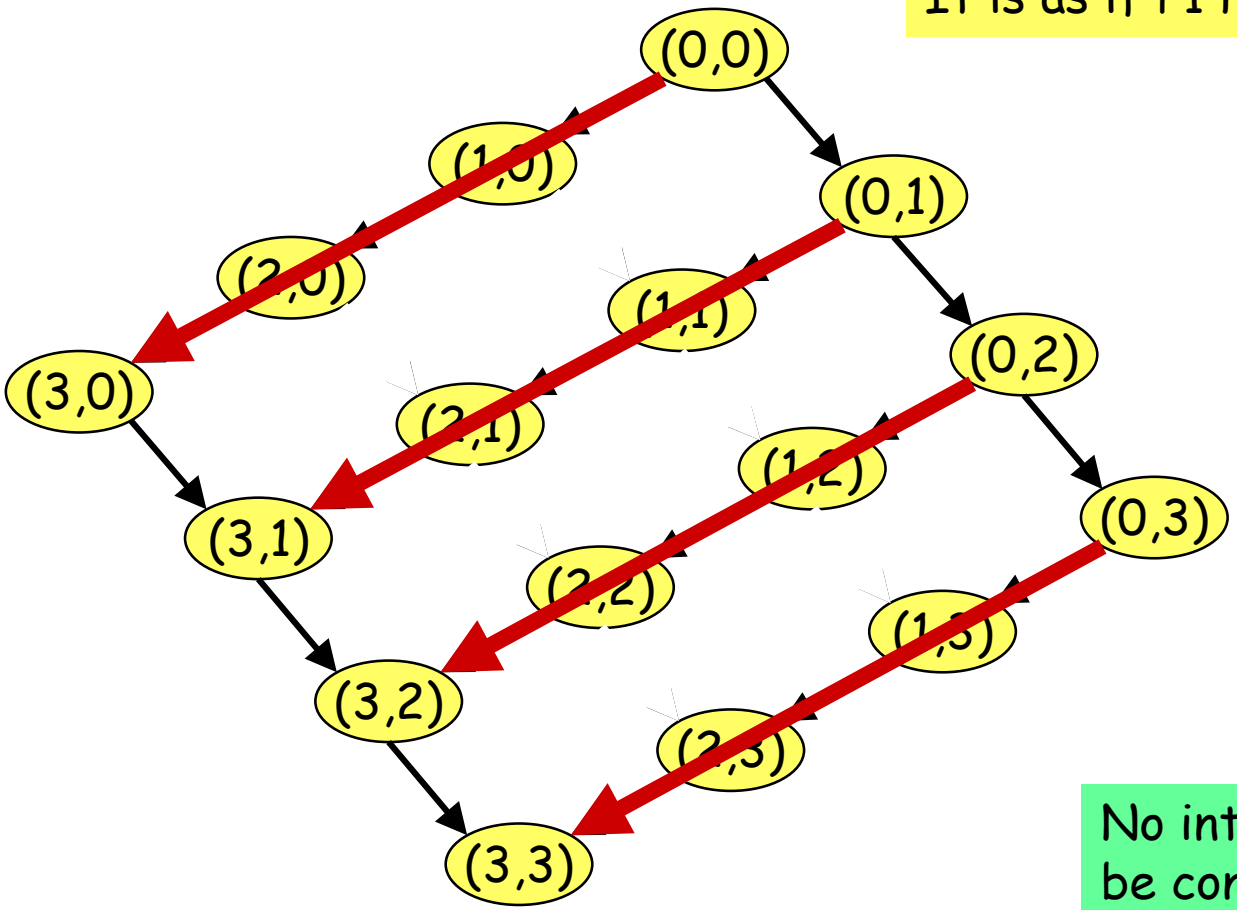

No intermediate states will be constructed.

Checking for pure atomicity

- Suppose we want to check that none of the atomic clauses in our model are ever blocked (i.e. pure atomicity).

1. Add a global bit variable:

```
bit aflag;
```

2. Change all atomic clauses to:

```
atomic {
   stat1;
   aflag=1;
   stat2

   ...

   statn
   aflag=0;
}
```

3. Check that `aflag` is always 0.

```
[]!aflag
```

e.g.

```
active process monitor {
   assert(!aflag);
}
```

`timeout` (1)

- Promela does not have real-time features.
  - In Promela we can only specify functional behaviour.
  - Most protocols, however, use timers or a timeout mechanism to resend messages or acknowledgements.

- **`timeout`**
  - SPIN's **`timeout`** becomes executable if there is no other process in the system which is executable
  - so, **`timeout`** models a global timeout
  - **`timeout`** provides an escape from deadlock states
  - beware of statements that are always executable…

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goto

goto label

- transfers execution to **label**
- each Promela statement might be labelled
- quite useful in modelling communication protocols

```
wait_ack:
  if
  :: B?ACK -> ab=1-ab ; goto success
  :: ChunkTimeout?SHAKE ->
     if
     :: (rc < MAX)  -> rc++; F!(i==1),(i==n),ab,d[i];
                       goto wait_ack
     :: (rc >= MAX) -> goto error
     fi
  fi ;
```

Timeout modelled by a channel.

Part of model of BRP

unless

```
{ <stats> } unless { guard; <stats> }
```

- Statements in *<stats>* are executed until the first statement (*guard*) in the escape sequence becomes executable.
- resembles exception handling in languages like Java
- *Example:*

```
proctype MicroProcessor() {
  {
    ...
    /* execute normal instructions */
  }
  unless { port ? INTERRUPT; ... }
}
```

unless

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    ...
    /* execute normal instructions */
  }
  unless { port ? INTERRUPT; ... }
}
```

`inline` - poor man's procedures

- Promela also has its own macro-expansion feature using the `inline`-construct.

```
inline init_array(a) {
  d_step {
    i=0;
    do
    :: i<N  -> a[i] = 0; i++
    :: else -> break
    od;
    i=0;
  }
}
```

Should be declared somewhere else (probably as a local variable).

Be sure to reset temporary variables.

  - error messages are more useful than when using `#define`
  - cannot be used as expression
  - all variables should be declared somewhere else