CS477 Formal Software Development Methods

Elsa L Gunter 2112 SC, UIUC egunter@illinois.edu http://courses.engr.illinois.edu/cs477

Slides based in part on previous lectures by Mahesh Vishwanathan, and by Gul Agha $$_{\rm January \ 21, \ 2014}$$

CS477 Formal Software Develo

Contact Information

- Office: 2112 SC
- Office Hours:
 - Wednesdays 11:00am 11:50am
 - Fridays 11:00am 12:30pm
 - Also by appointmentMay add more if desirable
- Email: egunter@illinois.edu
- No TA this semester

Course Website

Elsa L Gunter ()

- http://courses.engr.illinois.edu/cs477
- Main page summary of news items
- Policy rules governing course
- Lectures syllabus and slides
- MPs information about homework
- Exams exam dates, preparation
- Unit Projects for 4 credit students
- Resources tools, subject references
- FAQ

Some Course References

• No required textbook

sa L Gunter ()

- Software reliability methods, Doron A. Peled. Springer-Verlag New York, Inc.
- The Spin model checker primer and reference manual, Gerard J. Holzmann. Addison-Wesley, Pearson Education.
- The Temporal Logic of Reactive and Concurrent Systems:Specification, Zohar Manna and Amir Pnueli. Springer-Verlag.
- Model Checking, Edmund M. Clarke Jr., Orna Grumberg, Doron A. Peled. MIT Press.
- Reference papers found in resources on the course website
 Will grow over the semester

Course Grading

Elsa L Gunter ()

- Homework 30%
 - Four to five theory homeworks
 - Four to five tool exercises
 - Tool exercises may require access to EWS machines.
 Handed in using svn
 - Late submission penalty: 20% of total assignment value
- Midterm 30%
 - Take-home March 14
 - DO NOT MISS EXAM DATE!
- Final 40% Take-home Date TBA
- $\bullet\,$ Fourth Unit Credit additional 33%

Why Formal Methods?

Elsa L Gunter ()



AT&T Network Outage



AT&T

- 1990: AT&T # 4ESS long distance switch carried all long distance calls in USA, including for Air Traffic Control
- Jan 15, 1990 switch in New York crashes; reboot causes neighboring switches to crash, reboot
- 114 switches caught in oscillating crash reboot cycle
- Over 60,000 people with no phone service
- No inter-airport ATC communication
 - eventually amateur ham radio help with volunteer network

AT&T Network Outage



AT&T

Elsa L Gunter ()

Pentium Chip

- Short-Term Fix: Reload earlier version of 4ESS OS on all switches
- April 1990: AT&T Bell Labs creates new center Computing Sciences Research Center to try to assure never again
 - I was its first employee
- Bug:
 - Many contributing causes
 - One fatal contribution: a misplaced semicolon
 - $\bullet\,$ Could have been caught by a stronger type system

Pentium Chip

Elsa L Gunter ()



- Intel released Pentium in March 1993
- In October 1994, Prof. Thomas Nicely discovers that certain floating point divisions produce errors



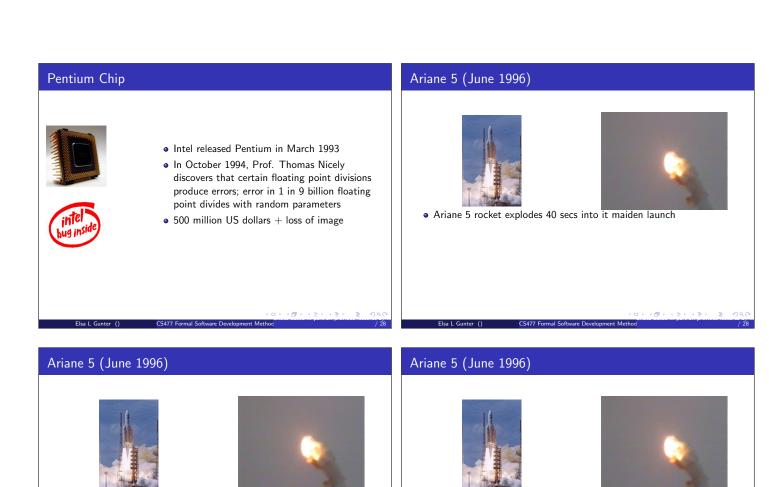


CS477 Formal Software Develop

• In October 1994, Prof. Thomas Nicely discovers that certain floating point divisions produce errors; error in 1 in 9 billion floating point divides with random parameters



er ()



- Ariane 5 rocket explodes 40 secs into it maiden launch due to a software bug!
 - A conversion of a 64-bit floating point number to a 16-bit unsigned integer was erroneously applied to a number outside the valid range

Ariane 5 (June 1996)

Elsa L Gunter ()

Flsa | Gunter ()

software bug!





 Ariane 5 rocket explodes 40 secs into it maiden launch due to a software bug!

• Ariane 5 rocket explodes 40 secs into it maiden launch due to a

CS477 Formal Se

- A conversion of a 64-bit floating point number to a 16-bit unsigned integer was erroneously applied to a number outside the valid range
- Loss of more than 500 million US dollars

Boeing 777

Elsa L Gunter ()

nter ()



• Problems with databus and flight management software delay assembly and integration of fly-by-wire system by more than one year

CS477 Formal Software Development M



• Certified to be safe in April 1995

Boeing 777



CS477 Formal Soft

- Problems with databus and flight management software delay assembly and integration of fly-by-wire system by more than one year
- Certified to be safe in April 1995
- Total development cost 3 billion

Boeing 777

Elsa L Gunter ()



- Problems with databus and flight management software delay assembly and integration of fly-by-wire system by more than one year
- Certified to be safe in April 1995

CS477 Formal

• Total development cost 3 billion; software integration and validation costs were about one-third.

Malaysian Airlines

Elsa I. Gunter ()

• A Boeing 777 plane operated by Malaysian Airlines, flying from Perth to Kuala Lumpur in August 2005, experiences problems

Malaysian Airlines

Elsa L Gunter ()

- A Boeing 777 plane operated by Malaysian Airlines, flying from Perth to Kuala Lumpur in August 2005, experiences problems
 - The plane suddenly zoomed up 3000 feet. The pilot's efforts at gaining manual control succeeded after a physical struggle, and the passengers were safely flown back to Australia.

Malaysian Airlines

lsa L Gunter ()

- A Boeing 777 plane operated by Malaysian Airlines, flying from Perth to Kuala Lumpur in August 2005, experiences problems
 - The plane suddenly zoomed up 3000 feet. The pilot's efforts at gaining manual control succeeded after a physical struggle, and the passengers were safely flown back to Australia.
- Cause: Defective software provided incorrect data about the plane's speed and accelaration.

Malaysian Airlines

Wall Street Journal Analysis

• "Plane makers are accustomed to testing metals and plastics under almost every conceivable kind of extreme stress, but it's impossible to run a big computer program through every scenario to detect bugs that invariably crop up."

Malaysian Airlines

Wall Street Journal Analysis

- "Plane makers are accustomed to testing metals and plastics under almost every conceivable kind of extreme stress, but it's impossible to run a big computer program through every scenario to detect bugs that invariably crop up."
- "... problems in aviation software stem not from bugs in code of a single program but rather from the interaction between two different parts of a plane's computer system."

Malaysian Airlines Wall Street Journal Analysis

Elsa L Gunter ()

• "Plane makers are accustomed to testing metals and plastics under almost every conceivable kind of extreme stress, but it's impossible to run a big computer program through every scenario to detect bugs that invariably crop up."

CS477 Formal Softw

- "... problems in aviation software stem not from bugs in code of a single program but rather from the interaction between two different parts of a plane's computer system."
- "... Boeing issued a safety alert advising, ..., pilots should immediately disconnect autopilot and might need to exert an unusually strong force on the controls for as long as two minutes to regain normal flight."

Why Formal Methods?

• To catch bugs

sa L Gunter ()

- To eliminate whole classes of errors
- Contrast: Testing

Testing	Formal Methods		
Can find errors in systems	Can find errors in systems		
Gen works on actual code	Gen work on abstract model		
maybe simulated env	of code and environment		
Can't show errors don't exist	Can show certain types		
	of errors can't exist		
Can't show system error-free	Can't show system error-free		

Formal Methods Limitations

- Can be expensive
 - Only used fully on safety-critical system components
- Can only prove model of system satisfies given property ("requirements")
 - Model may be wrong
 - requirements may be inadequate or wrong

What Are Formal Methods?

- Method of finding errors in
 - Hardware
 - Software
 - Distributed Systems
 - Computer-Human Operator Systems
 - ...
- Not a way to guarantee nothing will go wrong

What Are Formal Methods?

- Formal Methods are the application of rigorous mathematics to the
 - specification
 - modeling
 - implemetation, and
 - verifcation
 - of systems with programmable components
 - Software
 - Hardware
 - Control Systems
 - Combined Computer Human Operator Systems, ...

CS477 Formal Software De

• via computer programs implementing the math

What Types of Maths?

- Sets, Graphs, Trees
- Automata
- Logic and Proof Theory, Temporal Logics
- Process Algebras
- Induction, especially structural induction and well-founded induction, inductive relations
- Category Theory
- Probability
- . . .
- Differential Equations, PDEs
- . . .

What Types of Tools?

Elsa L Gunter ()

- Type Checkers, Type Inference

 Java, ML (Ocaml, Standard ML), Haskell, ...

 Model Checkers, SAT solvers
- SPIN, NuSMV, Mocha, SAL, ...
- Interactive Theorem Provers
 Isabelle, Coq, HOL4, PVS, ...
- Runtime Monitoring
 - JavaMOP

Course Overview

Elsa I. Gunter ()

• Review of basic math underlying most formal methods

CS477 Formal Software D

- $\bullet\,$ Intro to interactive theorem proving
- Intro to Isabelle/HOL
- Floyd-Hoare Logic (aka Axiomatic Semantics)
 - Verification ConditionsVerification Condition Generators (VCGs)
- Rewrite Logic
- Intro to Maude
- Operation Semantics
 Structured Oper. Sem., Transition Sem., Contexts Reduction Sem.
- Models of Concurrency
 - Finite State Automata, Buchi Automata, Concurrent Game Structures, Petri Nets

Course Overview

Elsa L Gunter ()

- Temporal Logics
 - LTL
 - CTL
- Model Checkers
 - SpinNuSMV
 - SAL
- Process Algebras, Pi Calculus, CSP, Actors
 - Intro to FDR
 - Intro to Rebeca
- Type Systems
 - Type Soundness
 - Dependent Types, Liquid Types, DML
 - Communication Types (aka Session Types)
 - Runtime Type Checking, Runtime Verification

Course Objectives

Elsa L Gunter ()

- How to do proofs in Hoare Logic, and what role a loop invaraint plays
- How to use finite automata to model computer systems
- How to express properties of concurrent systems in a temporal logic
- How to use a model checker to verify / falsify a temporal safety property of a concurrent system
- The connection between types and propgram properties
- What type soundness does and does not guarantee about a well-typed program

Propositional Logic

The Language of Propositional Logic

- Begins with constants {T, F}
- Assumes countable set *AP* of propositional variables, a.k.a. propositional atoms, a.k.a. atomic propositions
- Assumes logical connectives: \land (and); \lor (or); \neg (not); \Rightarrow (implies); \Leftrightarrow = (if and only if)
- The set of propositional formulae PROP is the inductive closure of these as follows:
 - {**T**, **F**} ⊆ *PROP*

Elsa L Gunter ()

Elsa L Gunter ()

p

true true q

true

false

false true true false false true

Truth Tables

- $\{1, r\} \subseteq river$ $AP \subseteq PROP$ if $A \in PROP$ then $(A) \in PROP$ and $\neg A \in A$ if $A \in PROP$ and $B \in PROP$ then $(A \land B) \in PROP$, (A \cdot B) = PROP. $(A \lor B) \in PROP$, $(A \Rightarrow B) \in PROP$, $(A \Leftrightarrow B) \in PROP$.
- Nothing else is in PROP
- Informal definition; formal definition requires math foundations, set theory, fixed point theorem \ldots

Semantics of Propositional Logic: Model Theory

CS477 Formal Soft

Standard Model of Propositional Logic (cont)

- Standard interpretation \mathcal{I}_{v} defined by structural induction on formulae:
 - $\mathcal{I}_{\nu}(\mathsf{T}) = \text{true} \text{ and } \mathcal{I}_{\nu}(\mathsf{F}) = \text{false}$
 - If $a \in AP$ then $\mathcal{I}_v(a) = v(a)$
 - For $p \in PROP$, if $\mathcal{I}_{v}(p) = \text{true}$ then $\mathcal{I}_{v}(\neg p) = \text{false}$, and if
 - $\mathcal{I}_{\nu}(p) = \text{false then } \mathcal{I}_{\nu}(\neg p) = \text{true}$

CS477 Formal Se

Interpretation function often described by truth table

 $\neg p$

false

false

- For $p, q \in PROP$
 - If $\mathcal{I}_{v}(p) = ext{true}$ and $\mathcal{I}_{v}(q) = ext{true}$, then $\mathcal{I}_{v}(p \wedge q) = ext{true}$, else
 - $\mathcal{I}_v(p \wedge q) = \mathrm{false}$ • If $\mathcal{I}_{v}(p) = \text{true or } \mathcal{I}_{v}(q) = \text{true, then } \mathcal{I}_{v}(p \lor q) = \text{true, else}$
 - $\mathcal{I}_{v}(p \lor q) = \text{false}$
 - If $\mathcal{I}_{\nu}(q) = \text{true or } \mathcal{I}_{\nu}(p) = \text{false, then } \mathcal{I}_{\nu}(p \Rightarrow q) = \text{true, else}$ $\mathcal{I}_v(p \Rightarrow q) = \text{false}$
 - If $\mathcal{I}_{\nu}(p) = \mathcal{I}_{\nu}(q)$ then $\mathcal{I}_{\nu}(p \Leftrightarrow q) = \text{true}$, else $\mathcal{I}_{\nu}(p \Leftrightarrow q) = \text{false}$

 $p \land q \quad p \lor q \quad p \Rightarrow q \quad p \Leftrightarrow q$

Semantics of Propositional Logic: Model Theory

Model for Propositional Logic has three parts

- Mathematical set of values used as meaning of propositions
- Interpretation function giving meaning to props built from logical connectives, via structural recursion

Standard Model of Propositional Logic

- $\mathcal{B} = \{ true, false \}$ boolean values
- $v : AP \rightarrow B$ a valuation
- Interpretation function

Truth Tables

sa L Gunter ()

Interpretation function often described by truth table

р	q	$\neg p$	$p \wedge q$	$p \lor q$	$p \Rightarrow q$	$p \Leftrightarrow q$
true	true					
true	false					
false	true					
false	false					

Truth Tables

Interpretation function often described by truth table

p	q	$\neg p$	$p \wedge q$	$p \lor q$	$p \Rightarrow q$	$p \Leftrightarrow q$
true	true	false	true			
true	false	false	false			
false	true	true	false			
false	false	true	false			

Truth Tables

Interpretation function often described by truth table

р	q	¬ <i>p</i>	$p \wedge q$	$p \lor q$	$p \Rightarrow q$	$p \Leftrightarrow q$
true	true	false	true	true		
true	false	false	false	true		
false	true	true	false	true		
false	false	true	false	false		

Truth Tables

Elsa L Gunter ()

Interpretation function often described by truth table

р	q	$\neg p$	$p \wedge q$	$p \lor q$	$p \Rightarrow q$	$p \Leftrightarrow q$
true	true	false	true	true	true	
true	false	false	false	true	false	
false	true	true	false	true	true	
false	false	true	false	false	true	

CS477 Formal Software Development Met

Truth Tables

Elsa L Gunter ()

Elsa L Gunter ()

Interpretation function often described by truth table

CS477 Formal Software Develo

р	q	$\neg p$	$p \wedge q$	$p \lor q$	$p \Rightarrow q$	$p \Leftrightarrow q$
true	true	false	true	true	true	true
true	false	false	false	true	false	false
false	true	true	false	true	true	false
false	false	true	false	false	true	true

CS477 Formal Software Develop

nt Me

ロンスロシスロンスロンス