

Some reminders about logistics. See the course webpage for full details.

- Submission Policy: Submit psets via gradescope. Student psets must obey the following constraints:
 - Each problem starts on its own page.
 - The first page has the following metadata:
 - * author(s) of the problem set
 - \cdot name(s)
 - netid(s)
 - * pset number
 - * list of collaborators
- Collaboration Policy: For this problem set, each student must work independently and submit their own solutions. For the remaining problem sets, students are allowed to work in groups of up to three.
- Late Policy: Late psets are not accepted. Instead, several lowest-scoring pset problems will be dropped from a students score.

All problems are of equal value.

- 1. Solve the following recurrences, by giving an asymptotically tight bound of the form $\Theta(f(n))$ where f(n) is a standard and well-known function. Assume as a base case that T(n) = 2 for $n \le 16$. No proofs are necessary.
 - (a) $T(n) = T(n/3) + n^2$.
 - (b) T(n) = 4T(n-2) + 5.
 - (c) $T(n) = n^{1/2}T(n^{1/2}) + n$.
 - (d) T(n) = 3T(n/3) + n.
 - (e) $T(n) = 4T(n^{1/2}) + \log n$.
- 2. French Flag Walk. Erickson Chapter 5, Problem #16 (http://jeffe.cs.illinois.edu/teaching/algorithms/book/05-graphs.pdf).
- 3. A class of m students will be taking an exam in a room. The room has n^2 tables, one on each point in the grid $\{1, \ldots, n\} \times \{1, \ldots, n\}$. Each student sits at an independent and uniformly randomly chosen table.
 - (a) Compute the expected number of students who sit at a table that is also occupied by another student.

- (b) A student is socially distanced if they sit at a table (i, j), and no other student sits in any of the tables $\{(i, j), (i+1, j), (i-1, j), (i, j+1), (i, j-1)\}$ (note that these 5 locations may not be locations of actual tables). Compute the expected number of socially distanced students.
- (c) Suppose that out of the m students, k are ill. A non-ill student sitting at (i, j) is then exposed if, (a) an ill student also sits at (i, j), or (b) at least two ill students sit in the locations $\{(i+1, j), (i-1, j), (i, j+1), (i, j-1)\}$. Compute the expected number of exposed students.

changelog

$\mathbf{v1} \to \mathbf{v2}$

- problem 3(b),3(c): Clarified the neighbor relation between tables.
- problem 3(c): Clarified the definition of exposed students to mean they were not ill to begin with.