# CS 466 Introduction to Bioinformatics 

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## Biological sequences

## DNA



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DNA to chromosome


## What is RNA?

RNA = ribonucleic acid

- "U" instead of "T"
- Usually single stranded
- Has base-pairing capability
- Can form simple non-linear structures
- Life may have started with RNA

(a)

(b)


## Protein sequence



## A short summary: string transformation

- DNA = nucleotide sequence
- Alphabet size $=4(\mathrm{~A}, \mathrm{C}, \mathrm{G}, \mathrm{T})$
- DNA to mRNA (single stranded)
- Alphabet size $=4(\mathrm{~A}, \mathrm{C}, \mathrm{G}, \mathrm{U})$
- mRNA to amino acid sequence
- Alphabet size = 20
- Amino acid sequence "folds" into 3-dimensional protein


## Phylogenetic Tree of Life

## Bacteria

Archaea

## Eucarya


determined by DNA sequences

## Evolution theory

- All organisms share the genetic code
- Similar genes across species
- Probably had a common ancestor
- Genomes are a wonderful resource to trace back the history of life


## Evolutionary process of sequences

- Substitutions
- Insertions and Deletions
- Representing an alignment; "gaps"

Evolution direction | ATTTTCCC |  |
| :--- | :--- |
| ATTTTACC | substitution: C->A |
| AT TTACC | deletion: T |
| AT TTACGC | insertion: G |

## Sequence alignment

Correspondence between bases of two DNA sequences, or between amino acids of two protein sequences

Alignment : $2 \times \mathrm{k}$ matrix $(\mathrm{k} \geq \mathrm{m}, \mathrm{n})$

$$
\begin{array}{lll}
\mathrm{V}=\mathrm{ACCTGGTAAA} & \mathrm{n}=10 & 8 \text { matches } \\
\mathrm{W}=\mathrm{ACTGCGTATA} & \mathrm{~m}=10 & 1 \text { mismatches } \\
& & 1 \text { deletions } \\
& 1 \text { insertions }
\end{array}
$$

| V | A | C | C | T | G | - | G | T | A | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| W |  |  |  |  |  |  |  |  |  |  |
| A | A |  |  |  |  |  |  |  |  |  |

## Applications of sequence alignment

- Find similarity between two DNA sequences that have evolved from a common ancestor
- Estimate evolutionary "distance" (time) between two related sequences, e.g., phylogeny reconstruction
- Enables inferences about evolutionary process, e.g., A map of recent positive selection in the Human Genome - Voight et al, PLoS Bio, 2006.


## Applications of sequence alignment

- Sequence alignments of RNA or amino acid sequences help in structure prediction


Query ${ }^{\mathbf{W}}$ ydpsdepiaeapfkfdmelddlpkeklkelifeetarfqpg 335
ident
Sbjct MA--rdpqrylviqgdermhlpsptdsnfyralmdvvdadeyl 29


## How to compute an alignment?

Alignment : $2 \times \mathrm{k}$ matrix $(\mathrm{k} \geq \mathrm{m}, \mathrm{n})$

| $\mathrm{V}=\mathrm{ACCTGGTAAA}$ | $\mathrm{n}=10$ | 8 matches |
| :--- | :--- | :--- | :--- |
| $\mathrm{W}=\mathrm{ACTGCGTATA}$ | $\mathrm{m}=10$ | 1 mismatches |
|  |  | 1 deletions |
|  |  | 1 insertions |


| V | A | C | C | T | G | - | G | T | A | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| W |  |  |  |  |  |  |  |  |  |  |
| W | A | C | - | T | G | C | G | T | A | T |

## "Goodness" of alignments

Given two sequences, there are many possible alignments

ATTTTCCC<br>ATTTACGC

```
ATTT-TCCC
ATTTA-CGC
```


## ATTTTCCC

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## ATTTTCCC

ATTTACGC

Edit distance: the total number of substitutions, insertions and deletions needed to transform one sequence to another

## "Goodness" of alignments

Given two sequences, there are many possible alignments

ATTTTCCC<br>ATTTACGC

distance=2

```
ATTT-TCCC
ATTTA-CGC
```

distance=3

## ATTTTCCC ATTTACGC

distance=16

Edit distance: the total number of substitutions, insertions and deletions needed to transform one sequence to another

## How to compute the best alignment?

## Enumeration of all possible alignments



A-GCDEF
AFGCDE-

## Introduction to dynamic programming

A simplified example

## Manhattan tourist problem

Imagine seeking a path (from source to sink) to travel (only eastward and southward) with the most number of attractions (*) in the Manhattan grid


## Problem formulation

Goal: Find a "most weighted" path in a weighted grid. (Weights may not be just 0/1.)

Input: A weighted grid $\mathbf{G}$ with two distinct vertices, one labeled "source" and the other labeled "sink"

Output: A "most weighted" path in G from "source" to "sink"

## An example



## Would a greedy algorithm work?



## How about a recursive solution?

Function MT( $n, m$ )

1. $x=M T(n-1, m)+$
weight of the edge from $(n-1, m)$ to $(n, m)$
2. $\quad y=M T(n, m-1)+$
weight of the edge from $(n, m-1)$ to $(n, m)$
3. return $\max \{x, y\}$

MT(x, y) returns the "most weighted" path from point ( $x, y$ ) to the "sink".

## Why this is not efficient?

- MT(n,m) needs MT(n, m-1) and MT(n-1, m)
- Both of these need MT(n-1, m-1)
- So MT(n-1, m-1) will be computed at least twice
- Dynamic programming: the same idea as this recursive algorithm, but keep all intermediate results in a table and reuse

