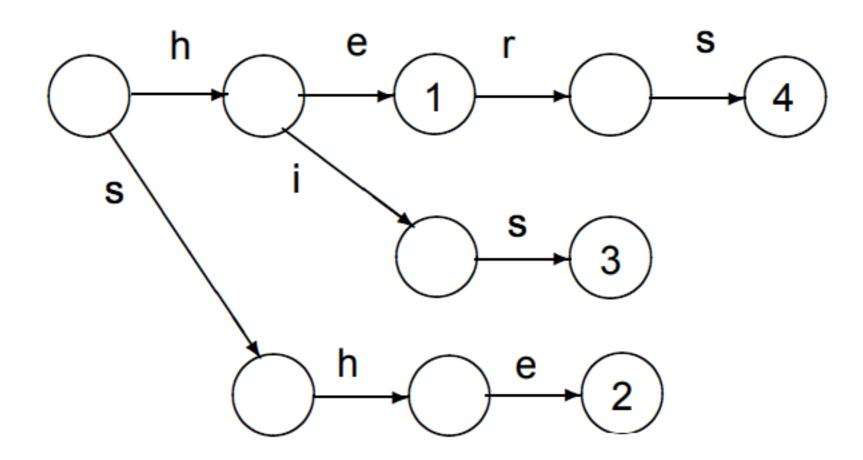
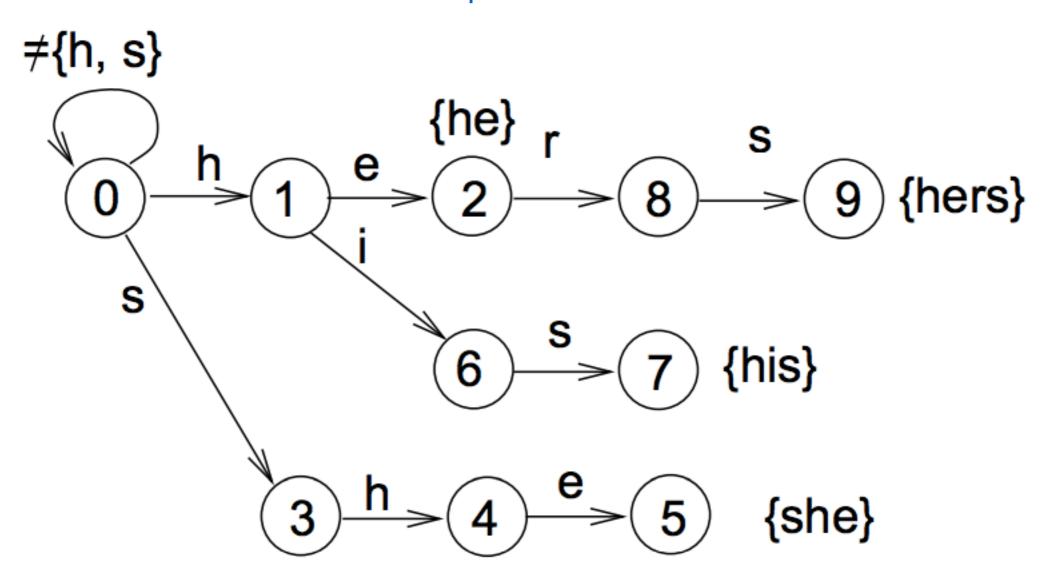
## Aho-Corasick algorithm

A keyword tree for  $P = \{he, she, his, hers\}$ :



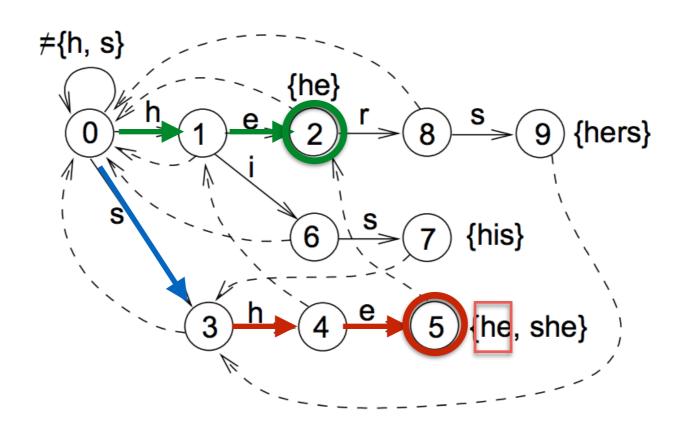
# Aho-Corasick algorithm

Add pattern labels



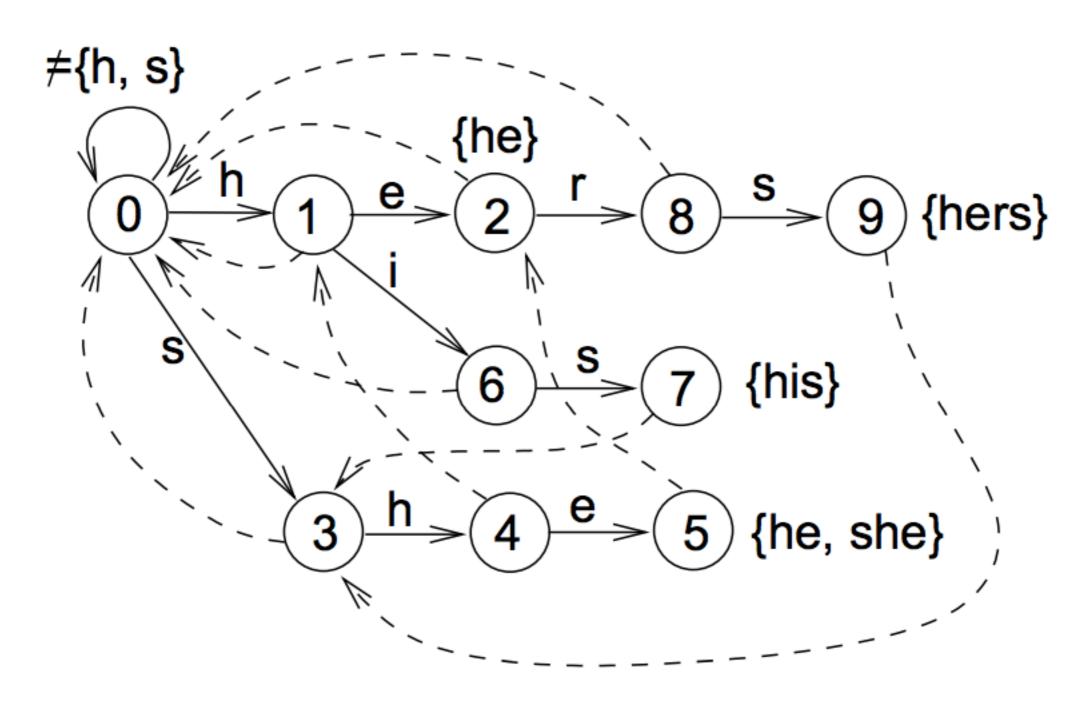
## Adding failing edges

- If currently at node q representing word L(q), find the longest proper suffix of L(q) that is a prefix of some pattern, and go to the node representing that prefix. Insert the labels of the pointed node (if there is any) to node q's set of labels.
- Example: node q = 5, L(q) = she; longest proper suffix that is a prefix of some pattern: "he". Dashed edge to node q'=2



## Aho-Corasick Algorithm

Add Failing Edges and Labels



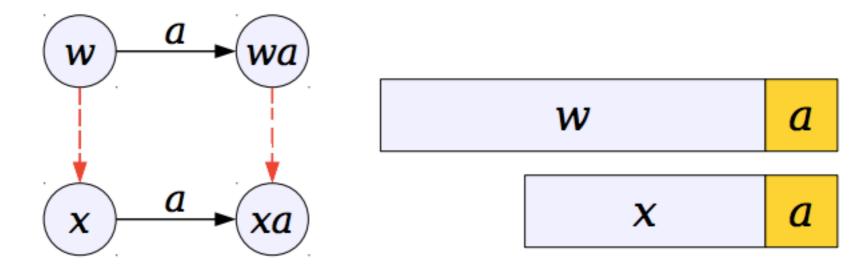
## Aho-Corasick Algorithm: Construction

What about a naive algorithm?

## A better algorithm: intuition

Suppose we already know the failing edge from a node **w** to **x**. If we follow a solid edge with label **a**, there are two possibilities:

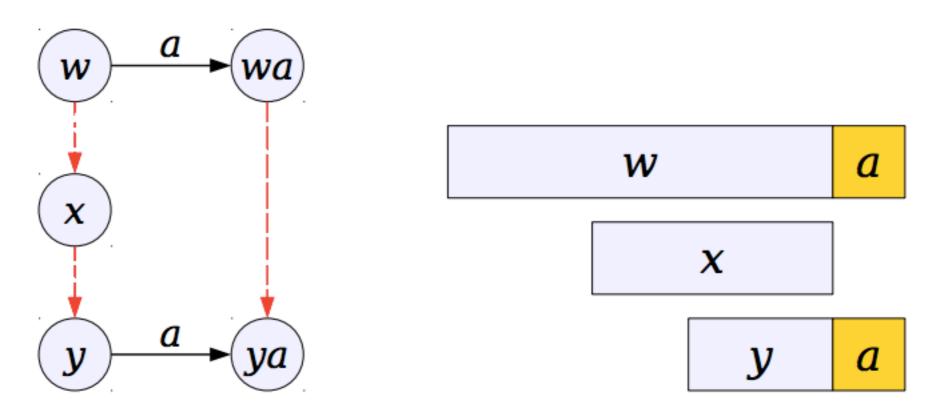
• Case 1: xa exists.



## A better algorithm: intuition

Suppose we already know the failing edge from a node **w** to **x**. If we follow a solid edge with label **a**, there are two possibilities:

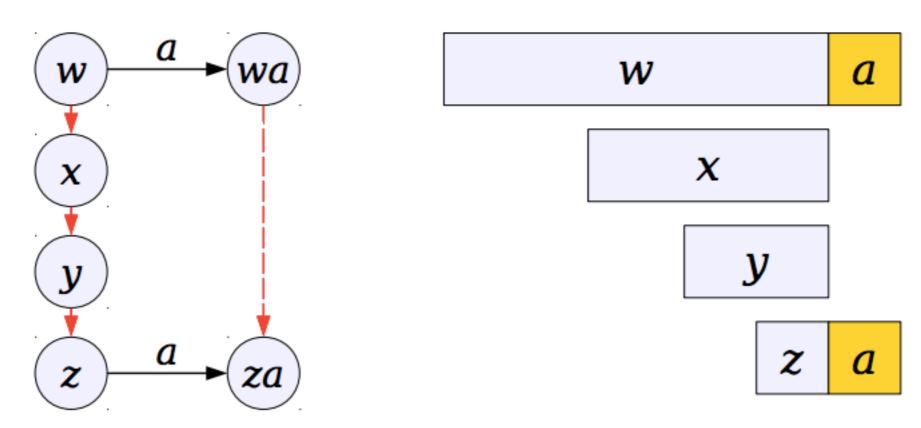
Case 2: xa does not exist.



## A better algorithm: intuition

Suppose we already know the failing edge from a node **w** to **x**. If we follow a solid edge with label **a**, there are two possibilities:

Case 2: xa does not exist.



## Constructing failing edge for a node

- To construct the failing edge for a node wa:
  - Follow w's failing edge to node x.
  - If node xa exists, wa has a failing edge to xa.
  - Otherwise, follow x's failing edge and repeat.
  - If you need to follow all the way back to the root, then wa's failing edge points to the root.
- Observation 1: Failing edges point from longer strings to shorter strings.
- Observation 2: If we precompute failing edges for nodes in ascending order of string length, all of the information needed for the above approach will be available at the time we need it.

## Complexity

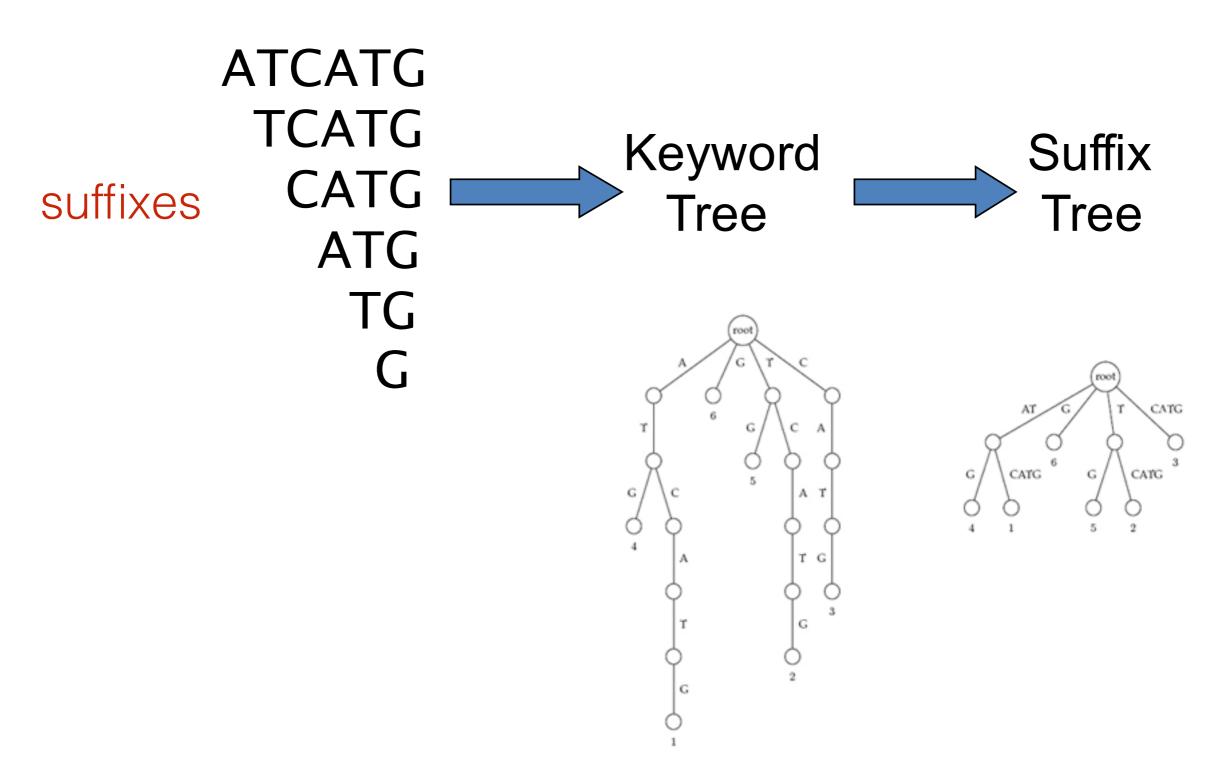
- Focus on the time to fill in the failing edges for a single pattern of length n.
  - The failing edges moves one-step backward because it always points to a shorter string.
  - The solid edges moves one-step forward.
  - We cannot take more steps backward than forward.
    Therefore, across the entire construction, we can take at most **n** steps backward for this pattern.
- Total time required to construct failing edges for a pattern of length n: O(n).
- Total time required to construct failing edges for all k patterns: O(kn).

#### A different approach: suffix tree

- Build a tree from the text
- Used if the text is expected to be the same during several pattern queries
- Tree building is O(m) where m is the size of the text. This is preprocessing.
- Given any pattern of length n, we can answer if it occurs in text in O(n) time
- Suffix tree = "modified" keyword tree of all suffixes of text

#### Construct a suffix tree

Text: ATCATG

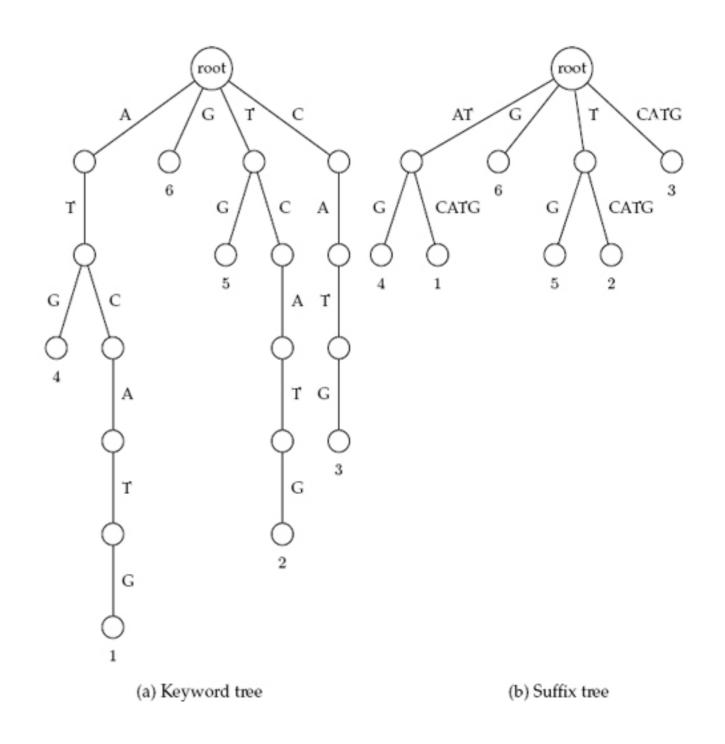


#### Suffix tree = Collapsed Keyword Tree on Suffixes

Similar to keyword trees, except edges that form paths are collapsed

- Each edge is labeled with a substring of a text for less space
- All internal edges have at least two outgoing edges
- Leaves labeled by the location of the suffix on the text.

Text: ATCATG

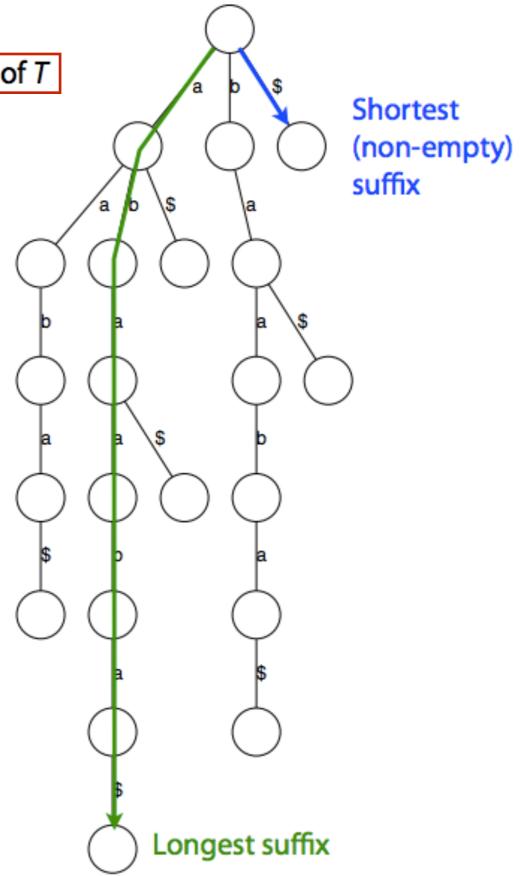


add special terminal character \$ to the end of T

T: abaaba T\$: abaaba\$

Each path from root to leaf represents a suffix; each suffix is represented by some path from root to leaf

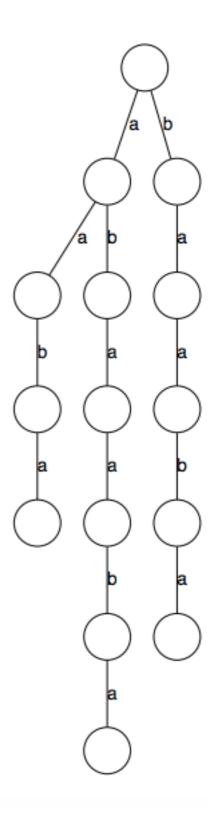
Would this still be the case if we hadn't added \$?



T: abaaba

Each path from root to leaf represents a suffix; each suffix is represented by some path from root to leaf

Would this still be the case if we hadn't added \$? No



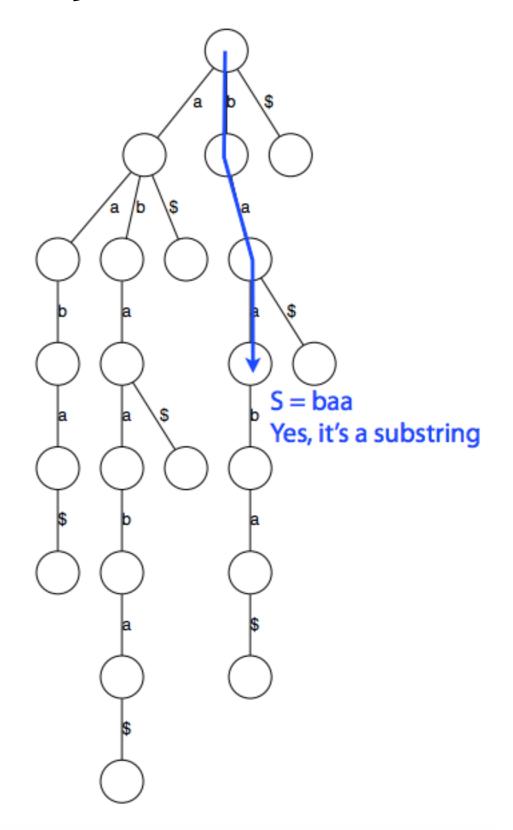
How do we check whether a string S is a substring of T?

Note: Each of T's substrings is spelled out along a path from the root. I.e., every substring is a prefix of some suffix of T.

Start at the root and follow the edges labeled with the characters of *S* 

If we "fall off" the trie -- i.e. there is no outgoing edge for next character of S, then S is not a substring of T

If we exhaust S without falling off, S is a substring of T



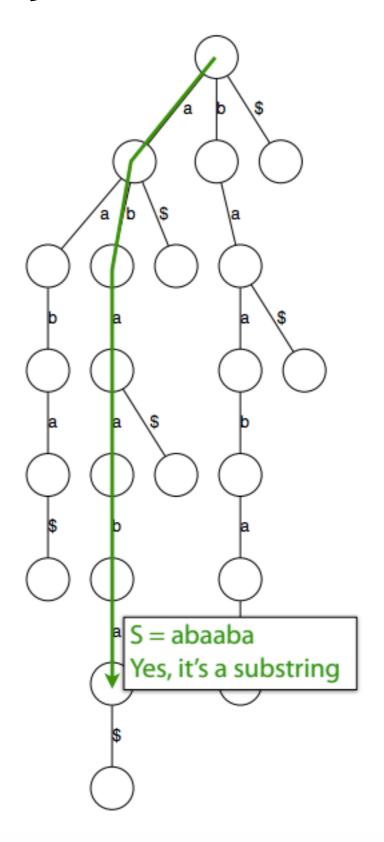
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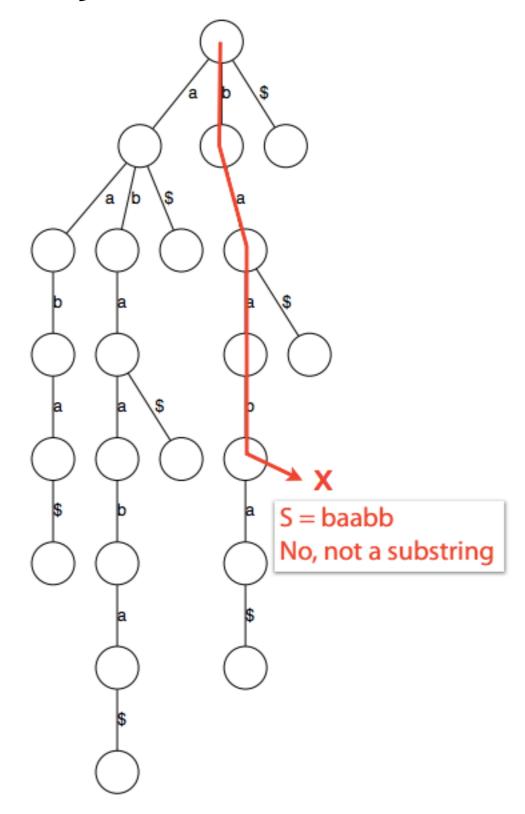
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## Summary

 Keyword and suffix trees are used to find patterns in a text

- Keyword trees:
  - Build keyword tree of patterns, and thread text through it
  - Usage: checking a set of patterns within various texts
- Suffix trees:
  - Build suffix tree of text, and thread patterns through it
  - Usage: checking various patterns in the same text