

CS447: Natural Language Processing

<http://courses.engr.illinois.edu/cs447>

# Lecture 19: Linguistically Expressive Grammars

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Part 1:  
Grammars in NLP:  
what and why

# What is grammar?

## Grammar formalisms

(= linguists' programming languages)

A precise way to define and describe the structure of sentences.

(N.B.: There are many different formalisms out there, which each define their own data structures and operations)

## Specific grammars

(= linguists' programs)

Implementations (in a particular formalism) for a particular language (English, Chinese,.....)

(NB: any practical parser will need to also have a model/scoring function to identify which grammatical analysis should be assigned to a given sentence)

# Why study grammar?

## **Linguistic questions:**

What kind of constructions occur in natural language(s)?

## **Formal questions:**

Can we define formalisms that allow us to characterize which strings belong to a language?

Those formalisms have appropriate weak generative capacity

Can we define formalisms that allow us to map sentences to their appropriate structures?

Those formalisms have appropriate strong generative capacity

## **Practical applications (Syntactic/Semantic Parsing):**

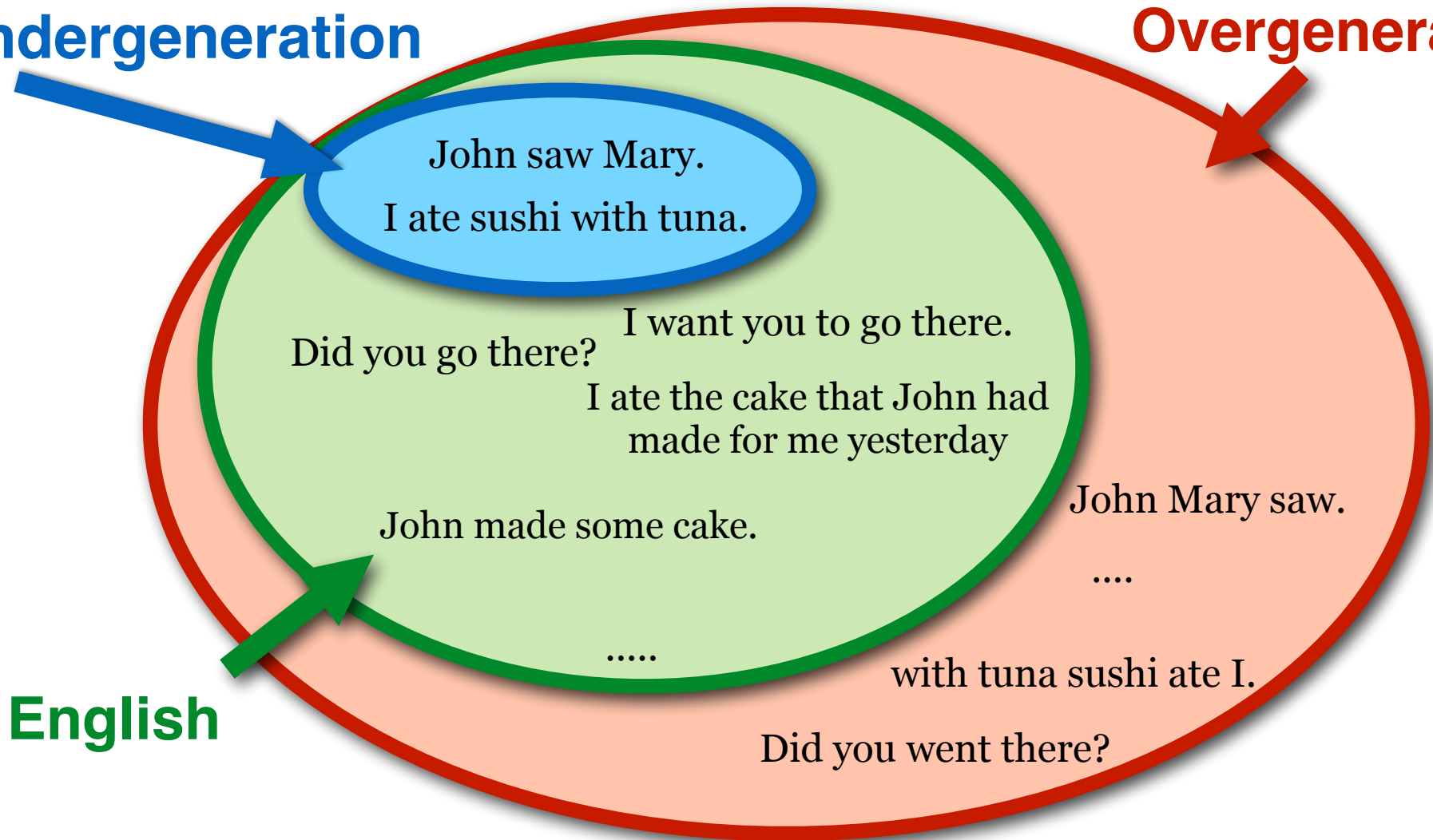
Can we identify the grammatical structure of sentences?

Can we translate sentences to appropriate meaning representations?

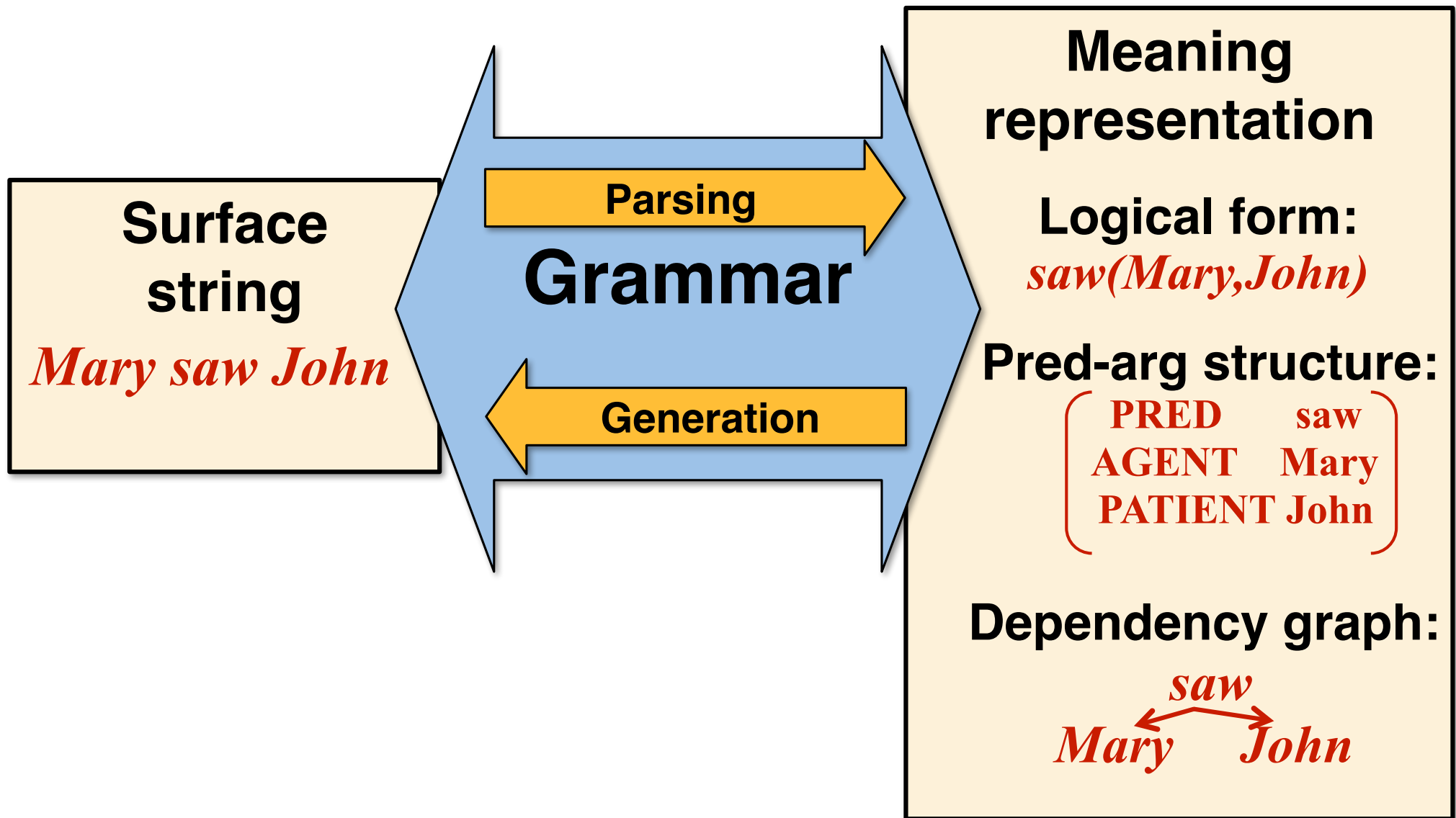
# Can we define a program that generates all English sentences?

**Undergeneration**

**Overgeneration**



# Syntax as an interface to semantics



# Grammar formalisms

Formalisms provide a formal **language** in which linguistic theories can be expressed and implemented

Formalisms define **elementary objects** (trees, strings, feature structures) and **recursive operations** which generate complex objects from simple objects.

Different formalisms may impose different **constraints** (e.g. on the kinds of dependencies they can capture)

# What makes a formalism “expressive”?

“Expressive” formalisms are richer than context-free grammars.

Different formalisms use different mechanisms, data structures and operations to **go beyond CFGs**



# Examples of expressive grammar formalisms

## **Tree-adjoining Grammar (TAG):**

Fragments of phrase-structure trees

## **Combinatory Categorical Grammar (CCG):**

Syntactic categories paired with meaning representations

## **Lexical-functional Grammar (LFG):**

Annotated phrase-structure trees (c-structure)  
linked to feature structures (f-structure)

## **Head-Driven Phrase Structure Grammar (HPSG):**

Complex feature structures (Attribute-value matrices)

Part 2:  
Why go beyond  
CFGs?

# The dependencies so far:

## Arguments:

Verbs take arguments: subject, object, complements, ...

**Heads subcategorize for their arguments**

## Adjuncts/Modifiers:

Adjectives modify nouns, adverbs modify VPs or adjectives,  
PPs modify NPs or VPs

**Modifiers subcategorize for the head**

Typically, these are *local* dependencies: they can be expressed *within individual CFG rules*

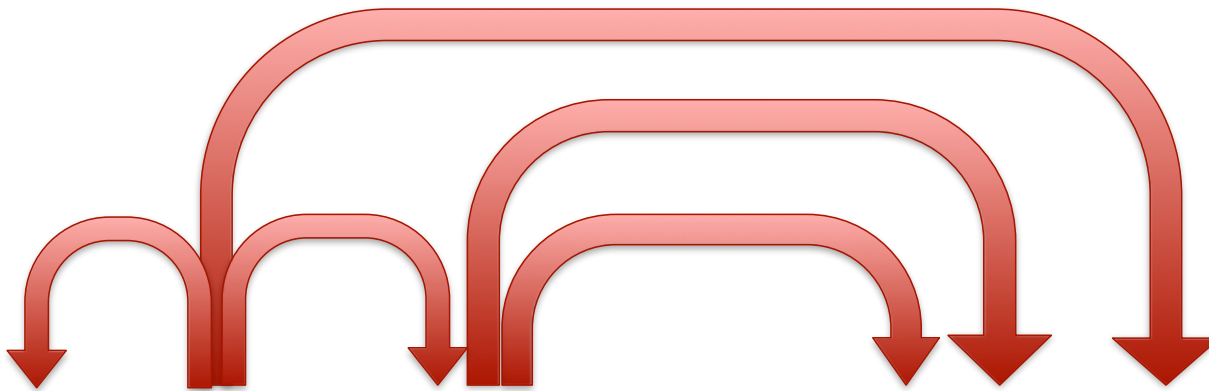
  
VP → Adv Verb NP

# Context-free grammars

CFGs capture only **nested** dependencies

The dependency graph is a **tree**

The dependencies **do not cross**

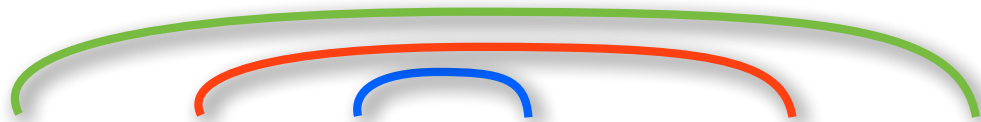


# German: center embedding

...daß ich [Hans schwimmen] sah  
...that I Hans swim saw  
...that I saw [Hans swim]

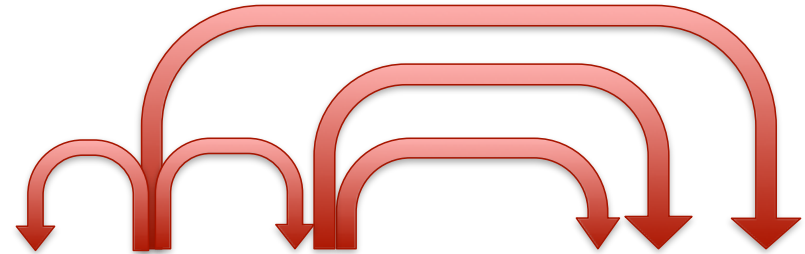
...daß ich [Maria [Hans schwimmen] helfen] sah  
...that I Maria Hans swim help saw  
...that I saw [Mary help [Hans swim]]

...daß ich [Anna [Maria [Hans schwimmen] helfen] lassen] sah  
...that I Anna Maria Hans swim help let saw  
...that I saw [Anna let [Mary help [Hans swim]]]

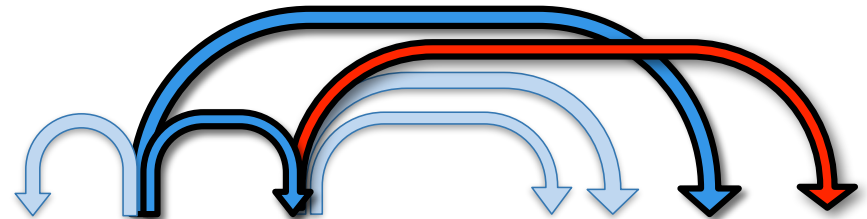
The diagram consists of three nested, upward-curving arcs above the text. The innermost arc is blue and connects the words 'Hans' and 'schwimmen'. The middle arc is red and connects the words 'Maria' and 'helfen'. The outermost arc is green and connects the words 'Anna' and 'lassen'.

# Dependency structures in general

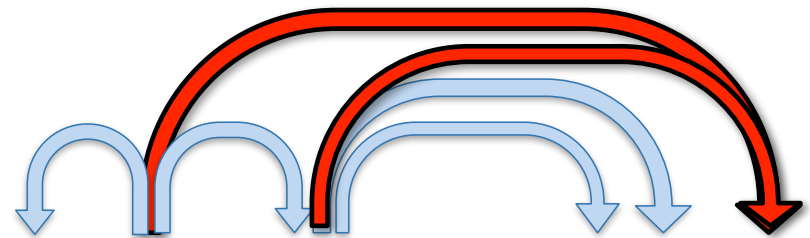
Nested (projective)  
dependency trees  
(CFGs)



Non-projective  
dependency trees

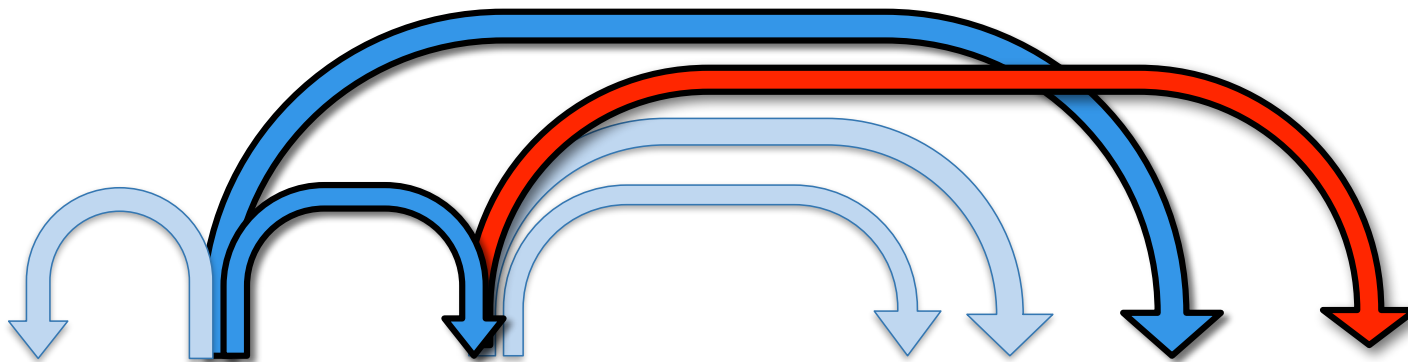


Non-local dependency  
graphs



# Beyond CFGs: Nonprojective dependencies

Dependencies form a **tree with crossing branches**



# Dutch: Cross-Serial Dependencies

...dat ik Hans zag zwemmen

...that I Hans saw swim

...that I saw [Hans swim]

...dat ik Maria Hans zag helpen zwemmen

...that I Maria Hans saw help swim

...that I saw [Mary help [Hans swim]]

...dat ik Anna Maria Hans zag laten helpen zwemmen

...that I Anna Maria Hans saw let help swim

...that I saw [Anna let [Mary help [Hans swim]]]

Such **cross-serial** dependencies require  
*mildly context-sensitive grammars*



# Other crossing (non-projective) dependencies

**(Non-local) scrambling:** In a sentence with multiple verbs, the argument of a verb appears in a different clause from that which contains the verb (arises in languages with freer word order than English)

*Die Pizza hat Klaus versprochen zu bringen*

The pizza has Klaus promised to bring

*Klaus has promised to bring the pizza*

**Extraposition:** Here, a modifier of the subject NP is moved to the end of the sentence

The guy is coming who is wearing a hat

Compare with the non-extrapolated variant

The [guy who is wearing a hat] is coming

**Topicalization:** Here, the argument of the embedded verb is moved to the front of the sentence.

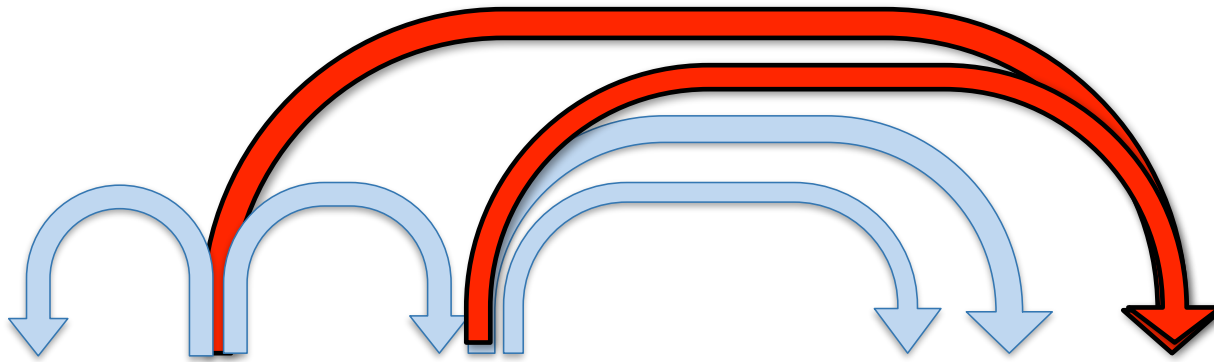
*Cheeseburgers, I [thought [he likes]]*

# Beyond CFGs: Nonlocal dependencies

Dependencies form a **DAG**  
(a node may have **multiple incoming edges**)

Arise in the following constructions:

- **Control** (*He has **promised** me to **go***), **raising** (*He **seems** to **go***)
- **Wh-movement** (*the **man** who you **saw** yesterday **is** here again*),
- **Non-constituent** coordination  
(right-node raising, gapping, argument-cluster coordination)



# Wh-Extraction (e.g. in English)

## Relative clauses:

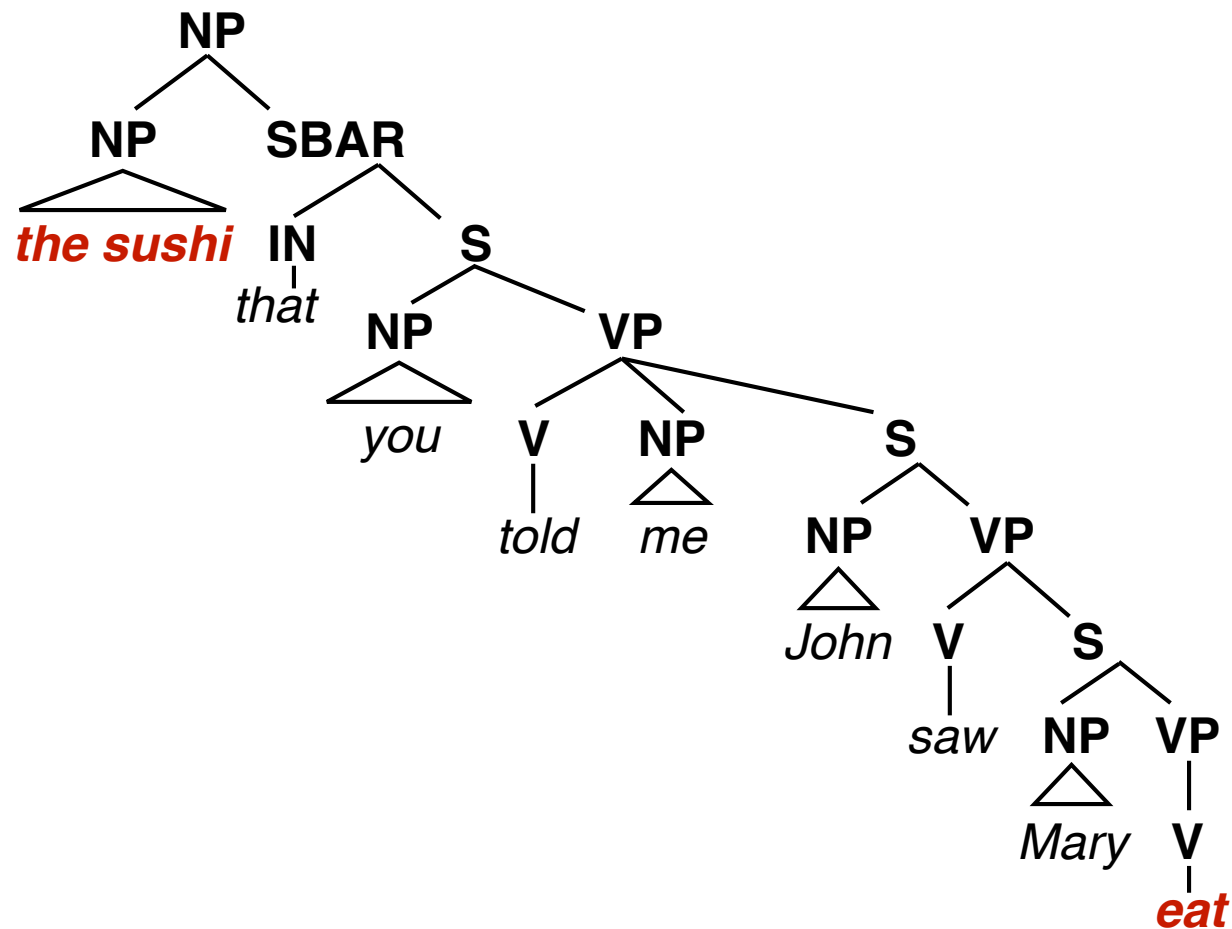
*the **sushi** that [you told me [John saw [**Mary eat**]]]*

## Wh-Questions:

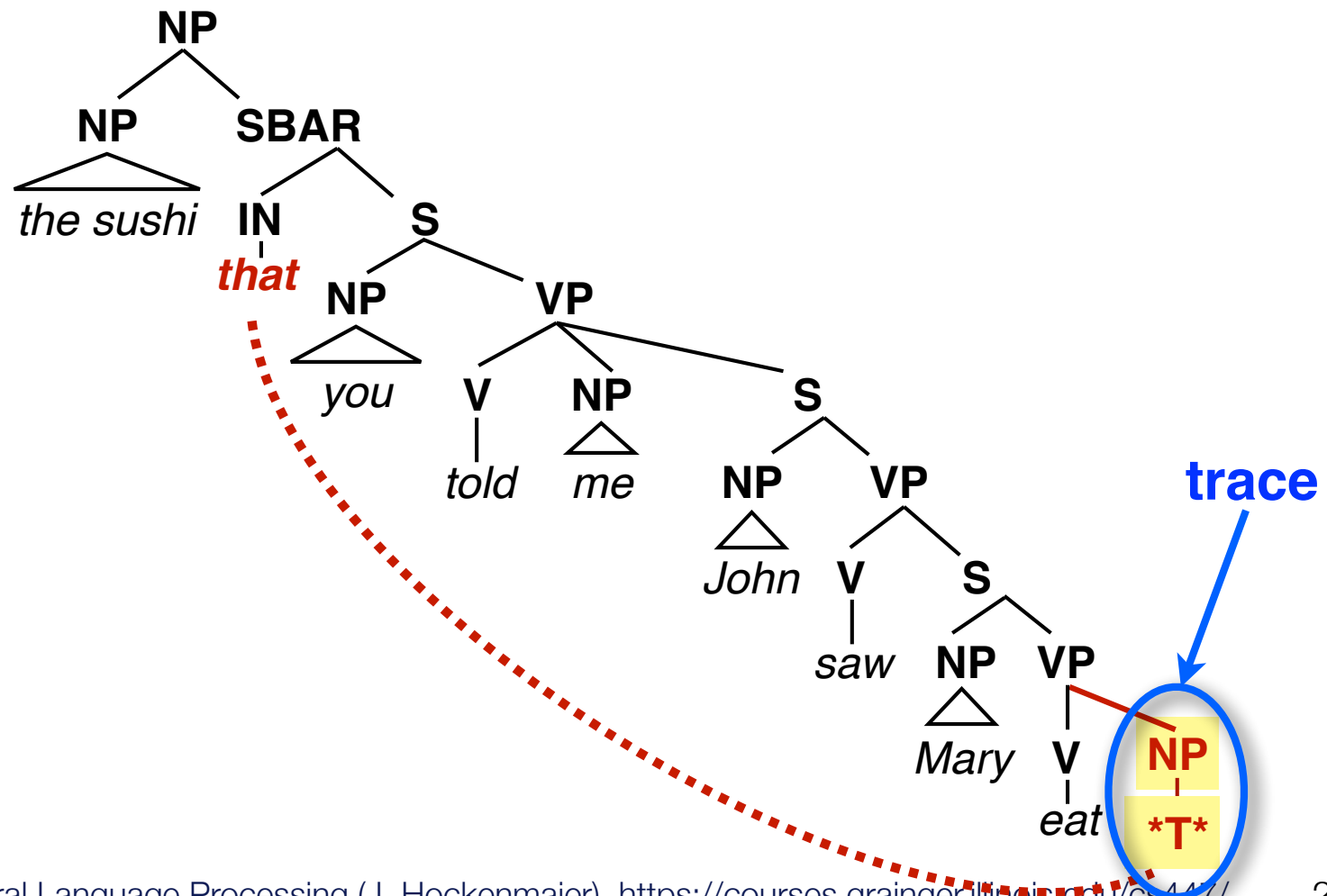
*'**what** [did you tell me [John saw [**Mary eat** ]]]?'*

**Wh-questions** (what, who, ...) and relative clauses contain so-called *unbounded* nonlocal dependencies because the verb that subcategorizes for the moved NP may be arbitrarily deeply embedded in the tree. Linguists call this phenomenon **wh-extraction** (wh-movement).

# As a phrase structure tree:



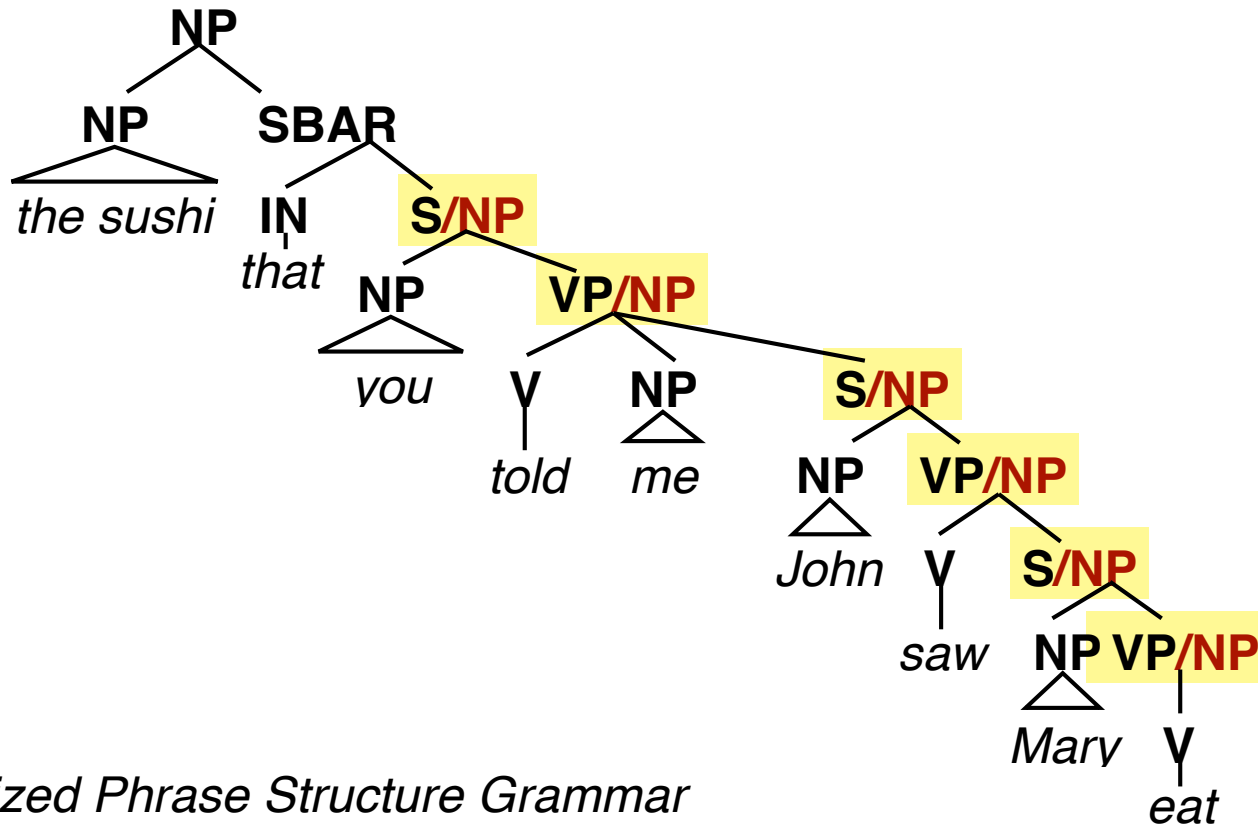
# The trace analysis of wh-extraction



# Slash categories for wh-extraction

Because only one element can be extracted, we can use **slash categories**.

This is still a CFG: the set of nonterminals is finite.



*Generalized Phrase Structure Grammar*  
(GPSG), Gazdar et al. (1985)

Part 3:  
Feature structure  
Grammars

# Why feature structures

Feature structures form the basis for many grammar formalisms used in computational linguistics.

Feature structure grammars (aka **attribute-value grammars**, or **unification grammars**) can be used as

- a more compact way of representing rich CFGs
- a way to represent more expressive grammars





# Simple grammars overgenerate

$S \rightarrow NP VP$   
 $VP \rightarrow Verb NP$   
 $NP \rightarrow Det Noun$   
 $Det \rightarrow the \mid a \mid these$   
 $Verb \rightarrow eat \mid eats$   
 $Noun \rightarrow cake \mid cakes \mid student \mid students$

This generates ungrammatical sentences like  
“*these student eats a cakes*”

We need to capture (number/person) agreement

# Refining the nonterminals

$$\begin{aligned} S &\rightarrow NP_{sg} VP_{sg} \\ S &\rightarrow NP_{pl} VP_{pl} \\ VP_{sg} &\rightarrow VerbSg NP \\ VP_{pl} &\rightarrow VerbPl NP \\ NP_{sg} &\rightarrow DetSg NounSg \\ DetSg &\rightarrow the \mid a \\ &\dots \quad \dots \quad \dots \end{aligned}$$

This yields **very large grammars**.

What about person, case, ...?

Difficult to capture **generalizations**

(Subject and verb have to have number agreement)

*NP<sub>sg</sub>*, *NP<sub>pl</sub>* and *NP* are three distinct nonterminals

# Feature structures

Replace atomic categories with feature structures:

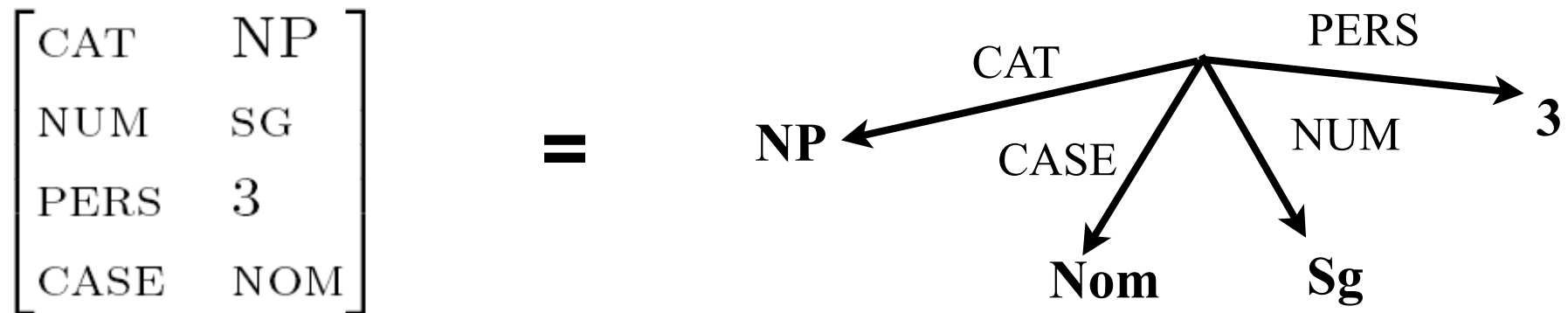
$$\begin{bmatrix} \text{CAT} & \text{NP} \\ \text{NUM} & \text{SG} \\ \text{PERS} & 3 \\ \text{CASE} & \text{NOM} \end{bmatrix}$$
$$\begin{bmatrix} \text{CAT} & \text{VP} \\ \text{NUM} & \text{SG} \\ \text{PERS} & 3 \\ \text{VFORM} & \text{FINITE} \end{bmatrix}$$

A **feature structure** is a list of **features** (= attributes, e.g. CASE), and **values** (e.g. NOM).

We often represent feature structures as **attribute value matrices (AVMs)**

Usually, values are **typed** (to avoid CASE:SG)

# Feature structures as directed graphs



# Complex feature structures

We distinguish between **atomic** and **complex** feature values.

A complex value is a feature structure itself.

This allows us to capture better generalizations.

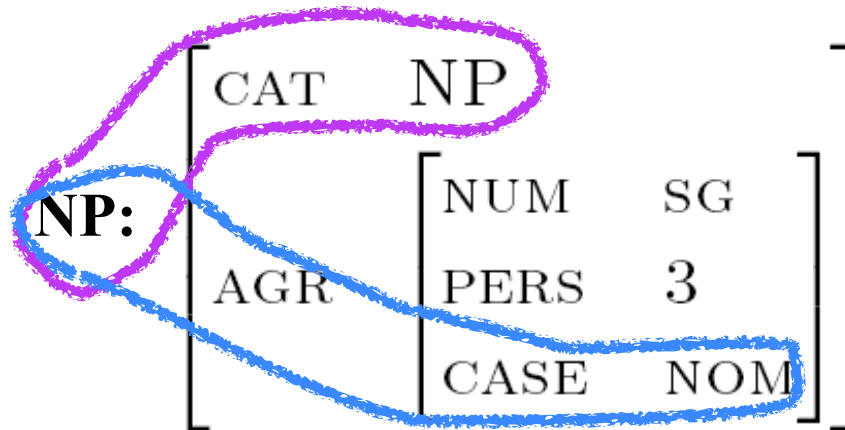
Only atomic values:

$$\begin{bmatrix} \text{CAT} & \text{NP} \\ \text{NUM} & \text{SG} \\ \text{PERS} & 3 \\ \text{CASE} & \text{NOM} \end{bmatrix}$$

Complex values:

$$\begin{bmatrix} \text{CAT} & \text{NP} \\ & \begin{bmatrix} \text{NUM} & \text{SG} \\ \text{PERS} & 3 \\ \text{CASE} & \text{NOM} \end{bmatrix} \\ \text{AGR} & \end{bmatrix}$$

# Feature paths



A **feature path** allows us to identify particular values in a feature structure:

$\langle \text{NP CAT} \rangle = \text{NP}$

$\langle \text{NP AGR CASE} \rangle = \text{NOM}$

# Unification

Two feature structures **A** and **B** **unify** ( $A \sqcup B$ ) if they can be merged into one consistent feature structure **C**:

$$\begin{bmatrix} \text{CAT} & \text{NP} \\ \text{NUM} & \text{SG} \\ \text{CASE} & \text{NOM} \end{bmatrix} \sqcup \begin{bmatrix} \text{CAT} & \text{NP} \\ \text{PERS} & 3 \end{bmatrix} = \begin{bmatrix} \text{CAT} & \text{NP} \\ \text{NUM} & \text{SG} \\ \text{PERS} & 3 \\ \text{CASE} & \text{NOM} \end{bmatrix}$$

Otherwise, unification **fails**:

$$\begin{bmatrix} \text{CAT} & \text{NP} \\ \text{NUM} & \text{SG} \\ \text{CASE} & \text{NOM} \end{bmatrix} \sqcup \begin{bmatrix} \text{CAT} & \text{NP} \\ \text{NUM} & \text{PL} \end{bmatrix} = \emptyset$$

# PATR-II style feature structures

CFG rules are augmented with constraints:

$$\mathbf{A}_0 \rightarrow \mathbf{A}_1 \dots \mathbf{A}_n$$

{set of constraints}

There are two kinds of constraints:

**Unification constraints:**

$$\langle \mathbf{A}_i \text{ feature-path} \rangle = \langle \mathbf{A}_j \text{ feature-path} \rangle$$

**Value constraints:**

$$\langle \mathbf{A}_i \text{ feature-path} \rangle = \text{atomic value}$$



# A grammar with feature structures

|             |  |   |   |                    |
|-------------|--|---|---|--------------------|
| <b>S</b>    | <b>→ NP VP</b>                               |   | <b>Grammar rule</b>                           |                    |
|             | $\langle \mathbf{NP} \mathit{NUM} \rangle$   | = | $\langle \mathbf{VP} \mathit{NUM} \rangle$    | <b>Constraints</b> |
|             | $\langle \mathbf{NP} \mathit{CASE} \rangle$  | = | <i>nom</i>                                    |                    |
| <b>NP</b>   | <b>→ DT NOUN</b>                             |   | <b>Grammar rule</b>                           |                    |
|             | $\langle \mathbf{NP} \mathit{NUM} \rangle$   | = | $\langle \mathbf{NOUN} \mathit{NUM} \rangle$  | <b>Constraints</b> |
|             | $\langle \mathbf{NP} \mathit{CASE} \rangle$  | = | $\langle \mathbf{NOUN} \mathit{CASE} \rangle$ |                    |
| <b>NOUN</b> | <b>→ <i>cake</i></b>                         |   | <b>Lexical entry</b>                          |                    |
|             | $\langle \mathbf{NOUN} \mathit{NUM} \rangle$ | = | <i>sg</i>                                     | <b>Constraints</b> |

# With complex feature structures

|          |                                  |   |                                 |                    |
|----------|----------------------------------|---|---------------------------------|--------------------|
| <b>S</b> | <b>→ NP VP</b>                   |   | <b>Grammar rule</b>             |                    |
|          | $\langle \text{NP AGR} \rangle$  | = | $\langle \text{VP AGR} \rangle$ | <b>Constraints</b> |
|          | $\langle \text{NP CASE} \rangle$ | = | <i>nom</i>                      |                    |

|           |                                 |   |                                   |                    |
|-----------|---------------------------------|---|-----------------------------------|--------------------|
| <b>NP</b> | <b>→ DT NOUN</b>                |   | <b>Grammar rule</b>               |                    |
|           | $\langle \text{NP AGR} \rangle$ | = | $\langle \text{NOUN AGR} \rangle$ | <b>Constraints</b> |

|             |                                       |   |                      |                    |
|-------------|---------------------------------------|---|----------------------|--------------------|
| <b>NOUN</b> | <b>→ <i>cake</i></b>                  |   | <b>Lexical entry</b> |                    |
|             | $\langle \text{NOUN AGR NUM} \rangle$ | = | <i>sg</i>            | <b>Constraints</b> |

**Complex feature structures** can capture **better generalizations** (and hence require fewer constraints) — cf. the previous slide

# The head feature

Instead of implicitly specifying heads for each rewrite rule, let us define a **head feature**.

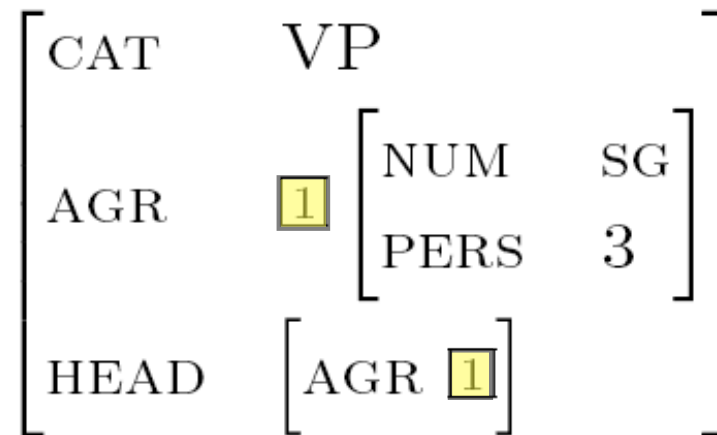
The head of a VP has the same agreement feature as the VP itself:

$$\left[ \begin{array}{l} \text{CAT} \\ \text{AGR} \\ \text{HEAD} \end{array} \begin{array}{l} \text{VP} \\ \left[ \begin{array}{l} \text{NUM} \quad \text{SG} \\ \text{PERS} \quad 3 \end{array} \right] \\ \left[ \begin{array}{l} \text{AGR} \\ \left[ \begin{array}{l} \text{NUM} \quad \text{SG} \\ \text{PERS} \quad 3 \end{array} \right] \end{array} \right] \end{array} \right]$$

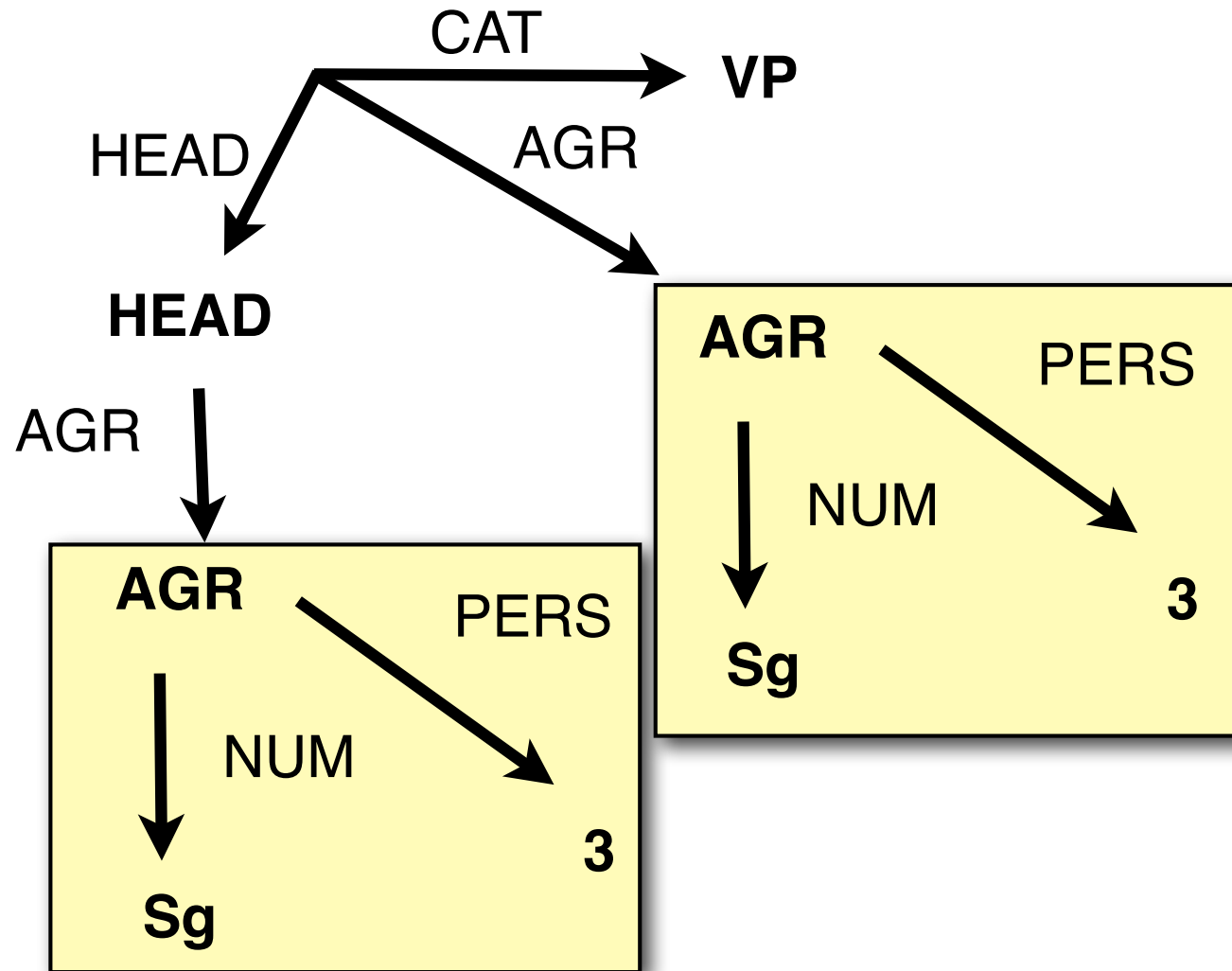
# Re-entrancies

What we *really* want to say is that the agreement feature of the head is *identical* to that of the VP itself.

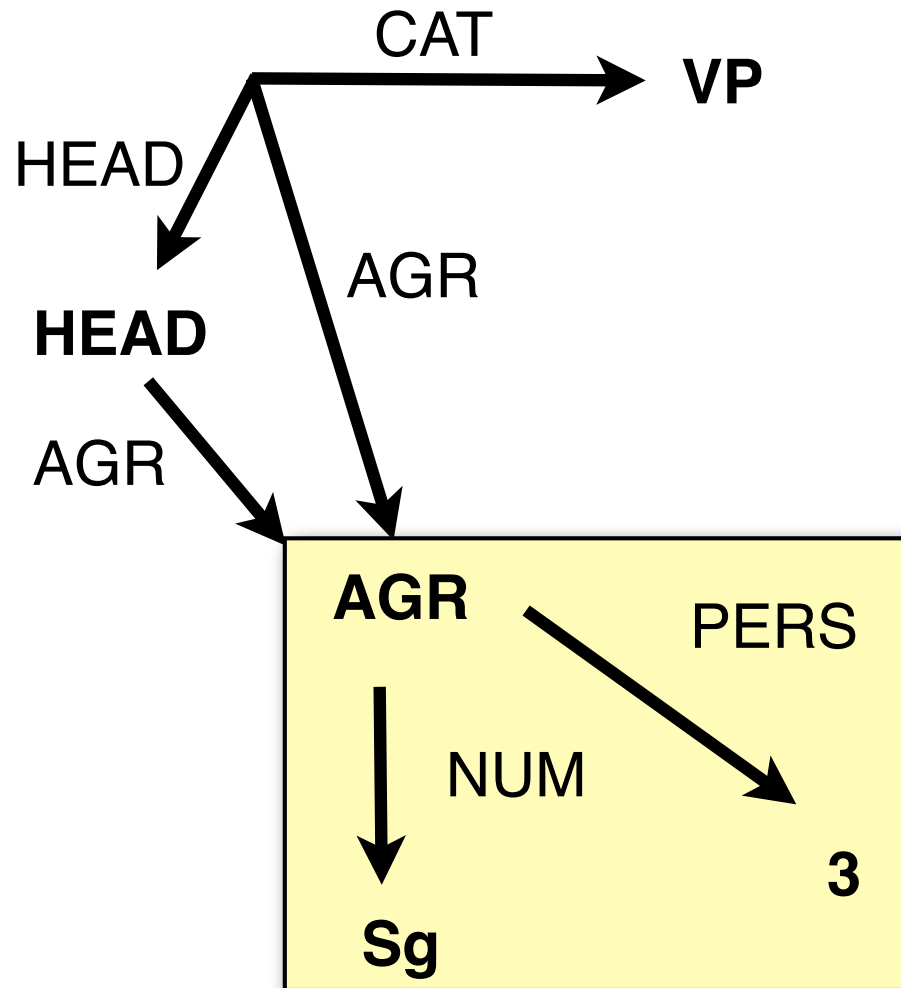
This corresponds to a **re-entrancy** in the FS (indicated via coindexation **1** )



# Re-entrancies — not like this:



# Re-entrancies — but like this:



# Attribute-Value Grammars and CFGs

If every feature can only have **a finite set of values**, any attribute-value grammar can be compiled out into a (possibly huge) context-free grammar



# Going beyond CFGs

The **power-of-2 language**:  $L_2 = \{w^i \mid i \text{ is a power of } 2\}$

$L_2$  is a (fully) context-sensitive language.

(*Mildly* context-sensitive languages have the **constant growth property** (the length of words always increases by a constant factor  $c$ ))

Here is a feature grammar which generates  $L_2$ :

$$A \rightarrow a$$

$$\langle A \ F \rangle = 1$$

$$A \rightarrow A_1 \ A_2$$

$$\langle A \ F \rangle = \langle A_1 \rangle$$

$$\langle A \ F \rangle = \langle A_2 \rangle$$



Part 4:  
Tree-Adjoining  
Grammar

# (Lexicalized) Tree-Adjoining Grammar

TAG is a **tree-rewriting formalism**:

TAG defines operations (**substitution, adjunction**) on trees.

The **elementary objects** in TAG are trees (not strings)

TAG is **lexicalized**:

Each elementary tree is **anchored** to a lexical item (word)

“**Extended domain of locality**”:

The elementary tree contains all arguments of the anchor.

TAG requires a linguistic theory which specifies the shape of these elementary trees.

TAG is **mildly context-sensitive**:

can capture Dutch cross-serial dependencies

but is still efficiently parseable

AK Joshi and Y Schabes (1996)  
Tree Adjoining Grammars.  
In G. Rosenberg and A. Salomaa,  
Eds., Handbook of Formal

# Mildly context-sensitive grammars

**Contain all context-free grammars/languages**

**Can be parsed in polynomial time** (TAG/CCG:  $O(n^6)$ )

(*Strong* generative capacity) capture certain kinds of dependencies: **nested** (like CFGs) and **cross-serial** (like the Dutch example), but not the MIX language:

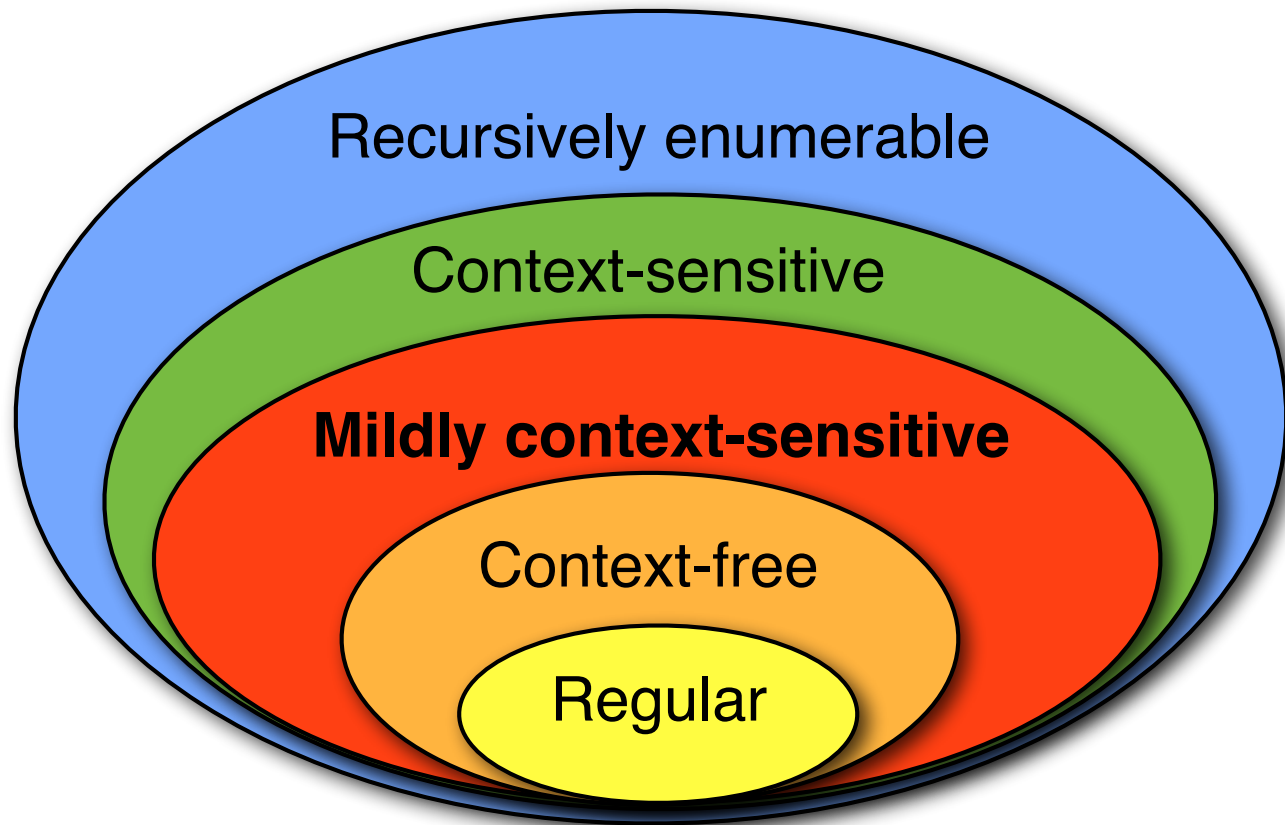
MIX: the set of strings  $w \in \{a, b, c\}^*$  that contain equal numbers of *as*, *bs* and *cs*

Have the **constant growth** property:

the length of strings grows in a linear way

The power-of-2 language  $\{a^{2^n}\}$  does not have the constant growth property.

# The Chomsky Hierarchy

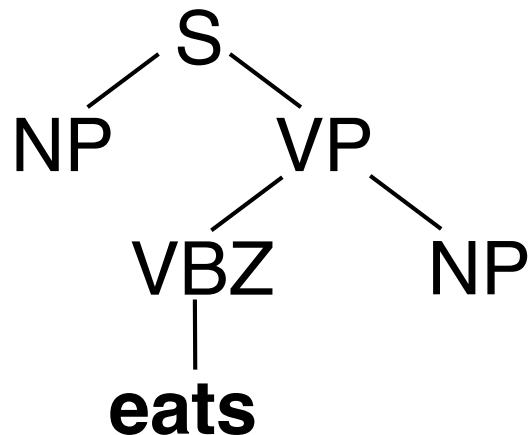


# Extended domain of locality

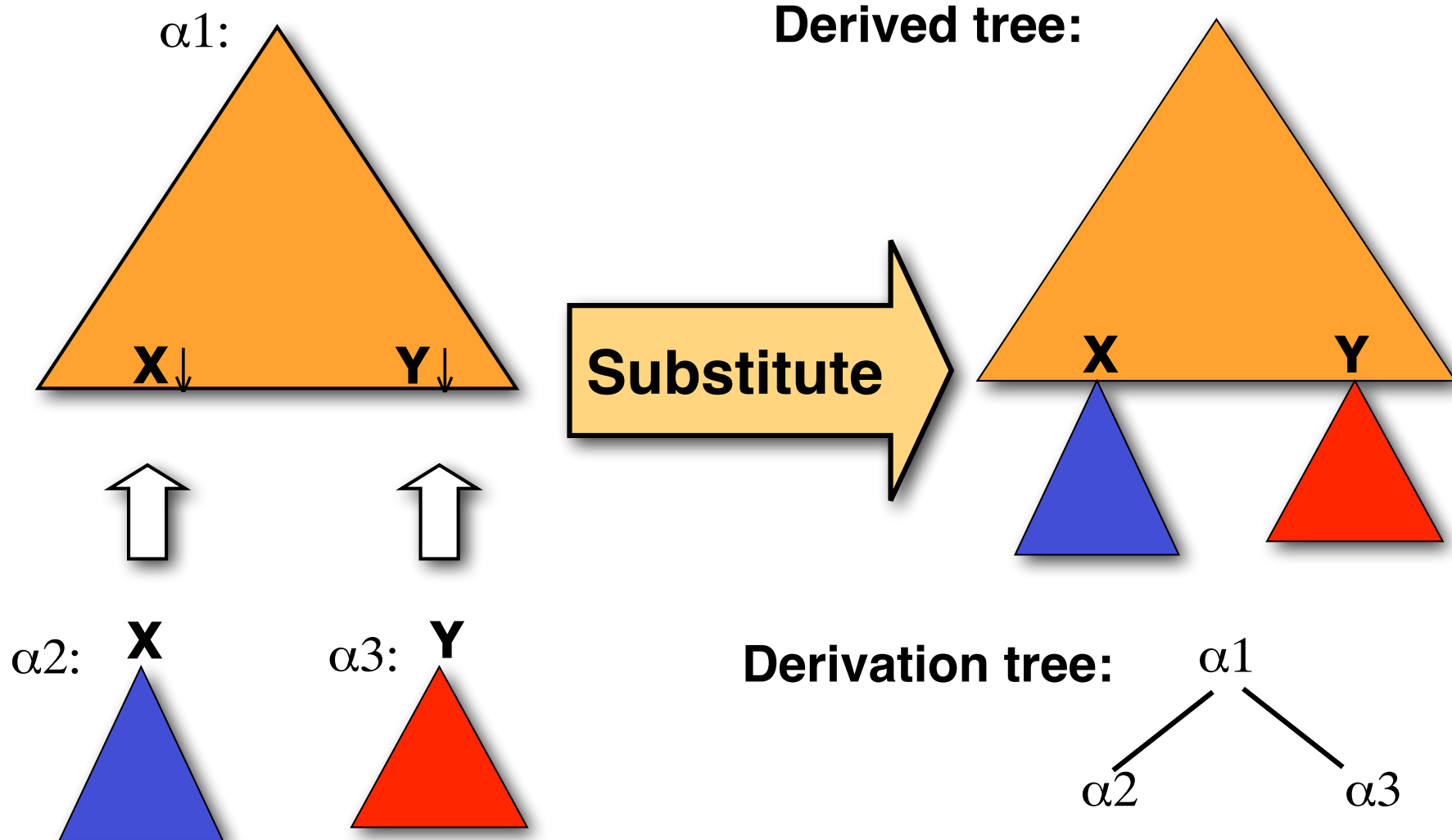
We want to capture **all arguments of a word** in a **single elementary object**.

We also want to retain certain syntactic structures (e.g. VPs).

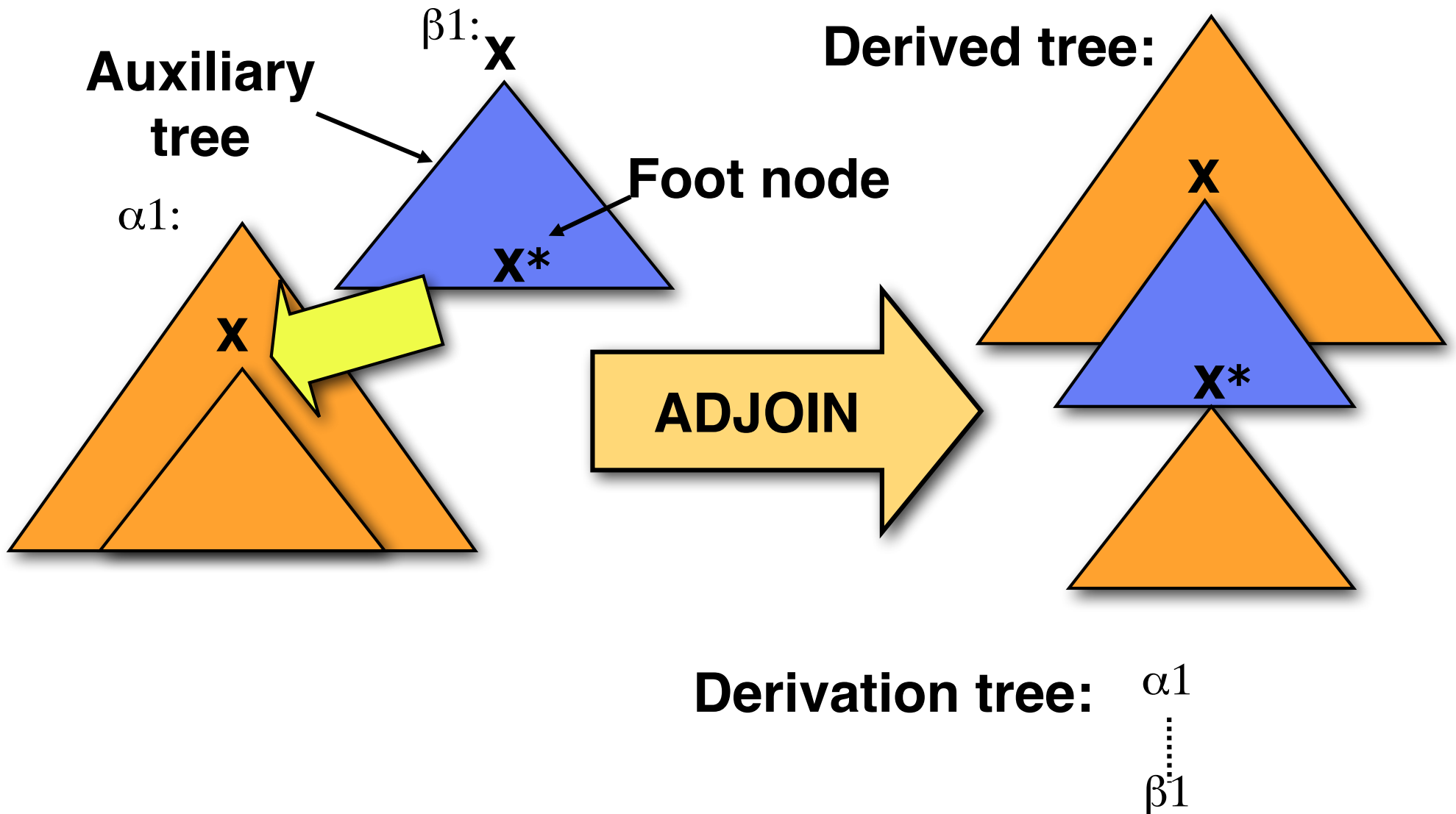
Our elementary objects are **tree fragments**:



# TAG substitution (arguments)

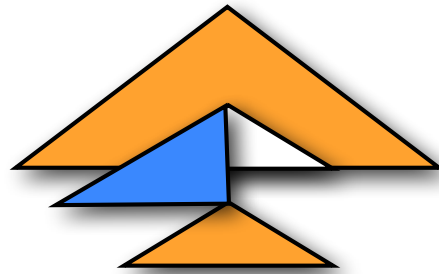


# TAG adjunction

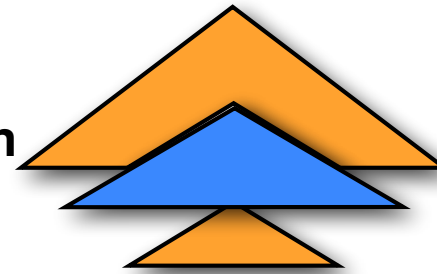


# The effect of adjunction

**TIG:**  
sister  
adjunction



**TAG:**  
wrapping  
adjunction



No adjunction: TSG (Tree substitution grammar)

TSG is context-free

Sister adjunction: TIG (Tree insertion grammar)

TIG is also context-free, but has a linguistically more adequate treatment of modifiers

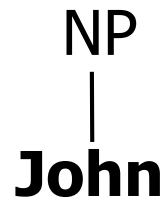
Wrapping adjunction: TAG (Tree-adjoining grammar)

TAG is mildly context-sensitive



# A small TAG lexicon

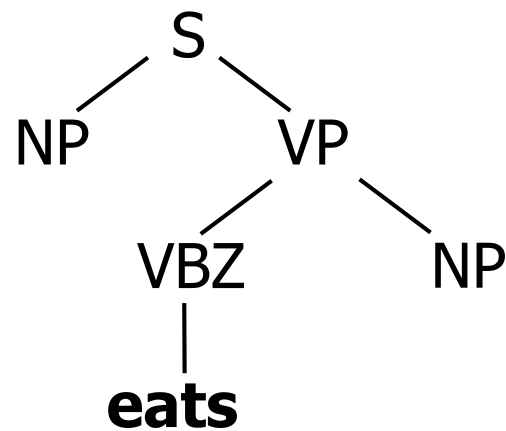
$\alpha_2$ :



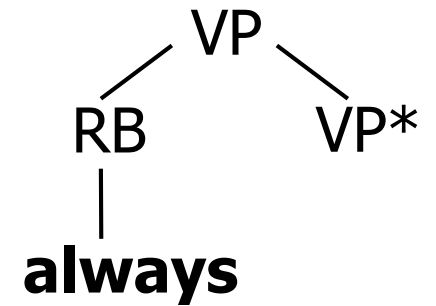
$\alpha_3$ :



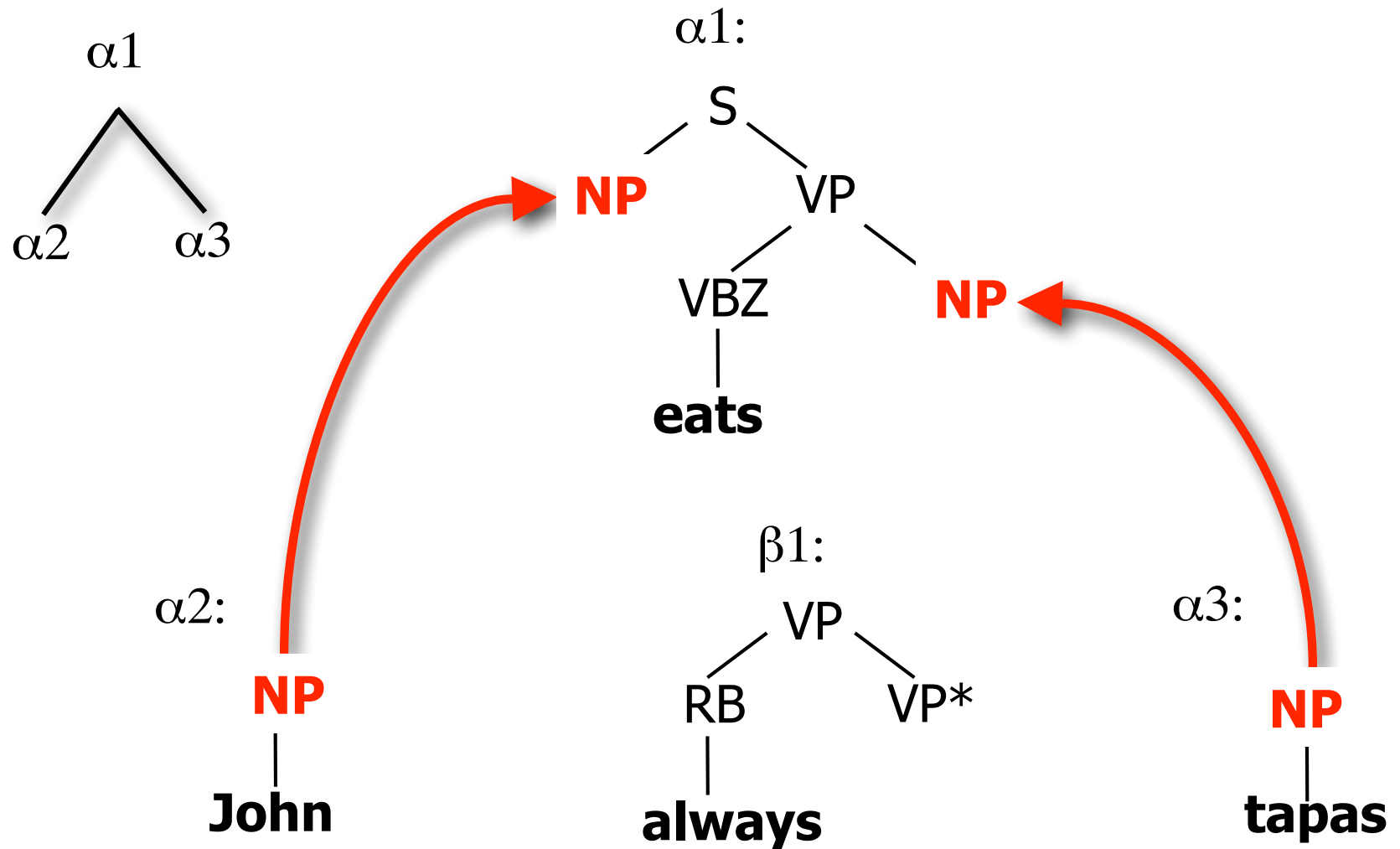
$\alpha_1$ :



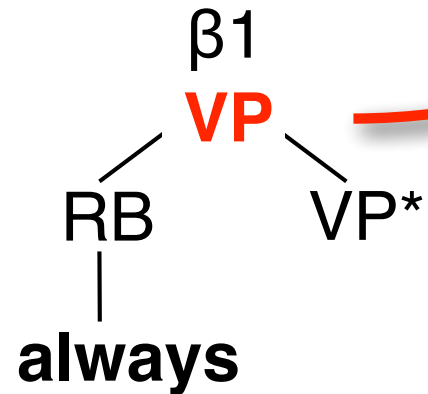
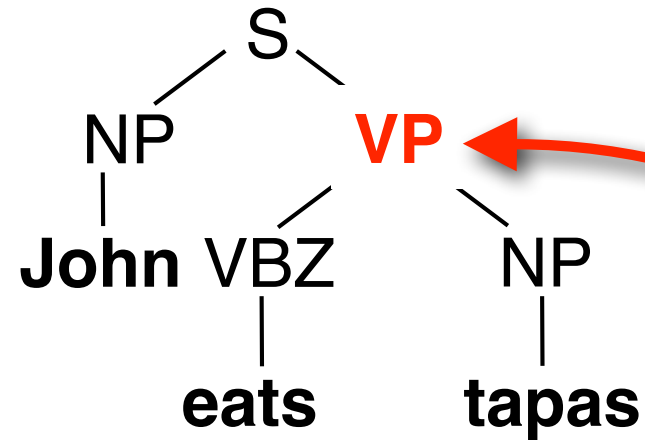
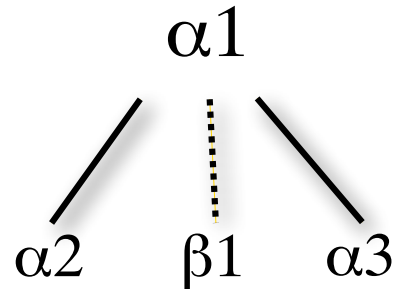
$\beta_1$ :



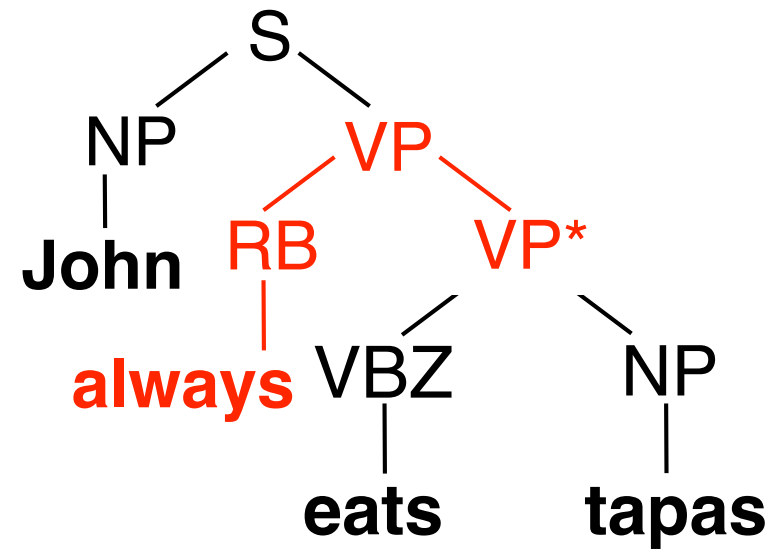
# A TAG derivation



# A TAG derivation

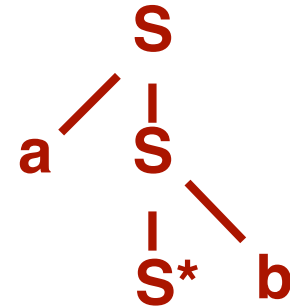
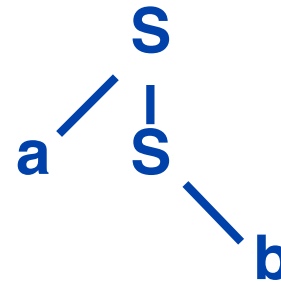


# A TAG derivation

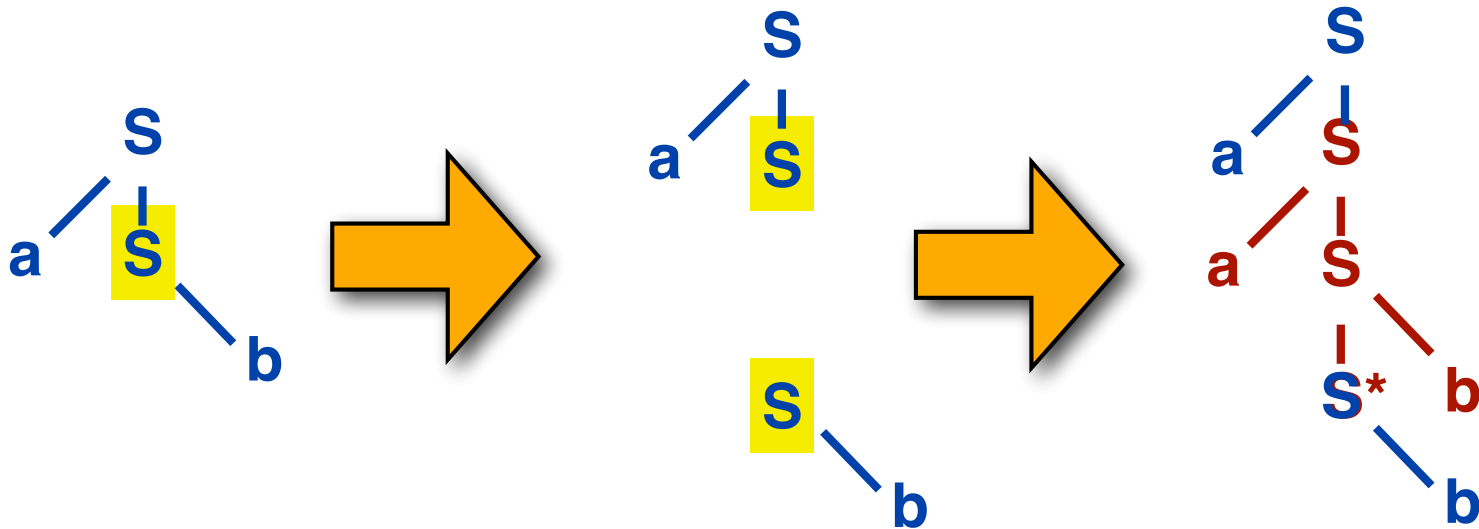


# $a^n b^n$ : Cross-serial dependencies

Elementary trees:



Deriving **aabb**



Part 5:  
(Combinatory)  
Categorial Grammar

# CCG: the machinery

## Categories:

specify subcat lists of words/constituents.

## Combinatory rules:

specify how constituents can combine.

## The lexicon:

specifies which categories a word can have.

## Derivations:

spell out process of combining constituents.

# CCG categories

Simple (atomic) categories: **NP, S, PP**

Complex categories (functions):

Return a **result** when combined with an **argument**

|                       |  |
|-----------------------|--|
| VP, intransitive verb | <b>S\NP</b>  |
| Transitive verb       | <b>(S\NP)/NP</b>   |
| Adverb                | <b>(S\NP)\(S\NP)</b>   |
| Prepositions          | <b>((S\NP)\(S\NP))/NP</b><br><b>(NP\NP)/NP</b><br><b>PP/NP</b> |



# CCG categories are functions

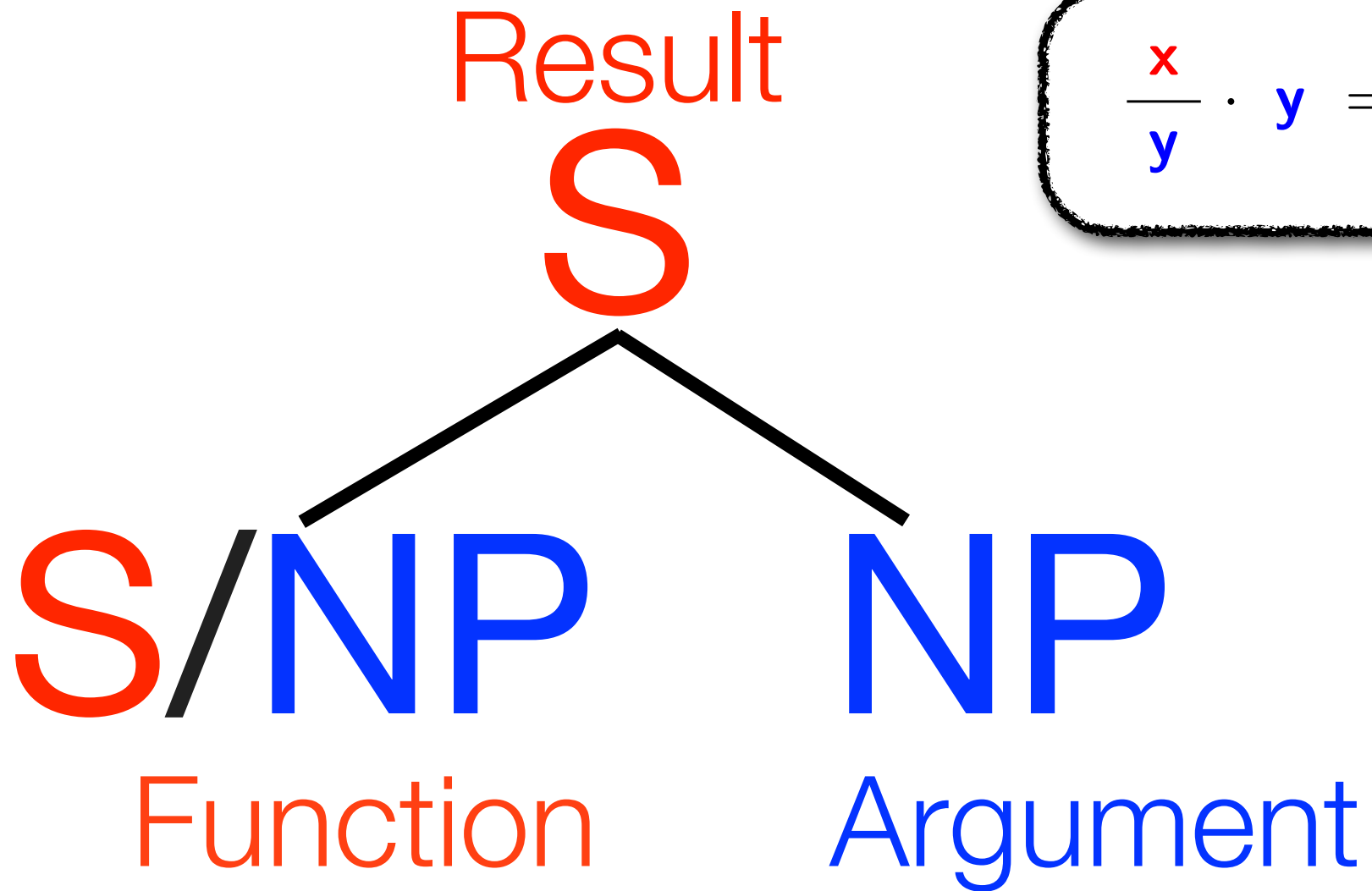
CCG has a few atomic categories, e.g

**S, NP, PP**

All other CCG categories are **functions**:

**S** / **NP**  
Result Dir. Argument

# Rules: Function application



# Rules: Function application

Result  
S

$$y \cdot \frac{x}{y} = x$$

NP

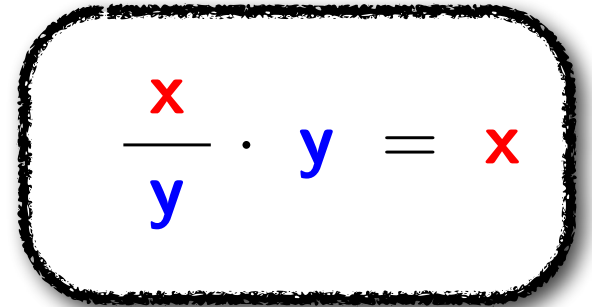
S \ NP

Argument

Function

# Rules: Function application

Result  
**S \ NP**


$$\frac{x}{y} \cdot y = x$$

**(S \ NP) / NP**

Function

**NP**

Argument

# Function application

## Forward application ( $>$ ):

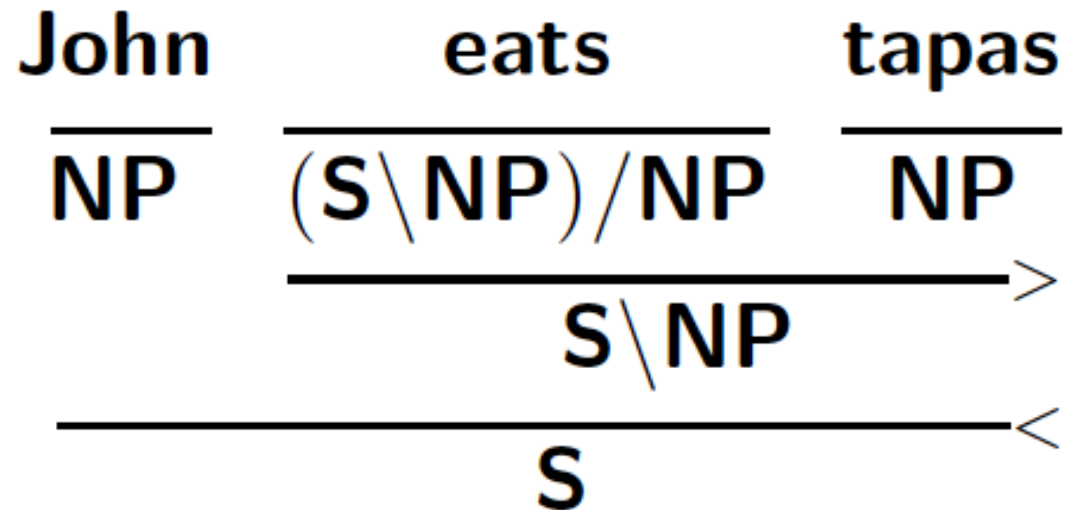
$(S \backslash NP) / NP$     $NP$     $\Rightarrow_{>}$     $S \backslash NP$   
eats   tapas   eats tapas

## Backward application ( $<$ ):

$NP$     $S \backslash NP$     $\Rightarrow_{<}$     $S$   
John   eats tapas   John eats tapas

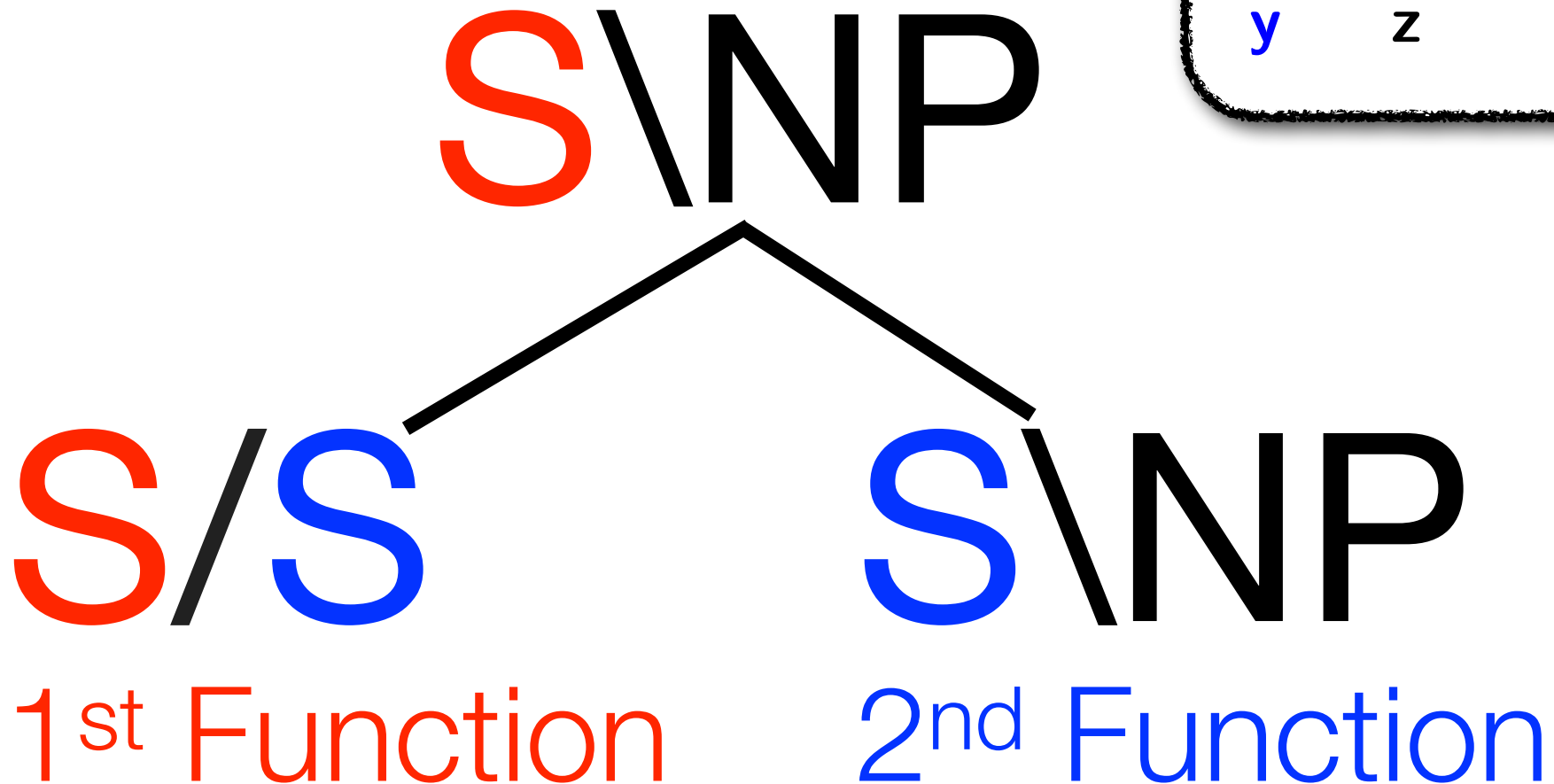
**Combines function  $X/Y$  or  $X \backslash Y$  with argument  $Y$  to yield result  $X$**   
Used in all variants of categorial grammar

# A (C)CG derivation

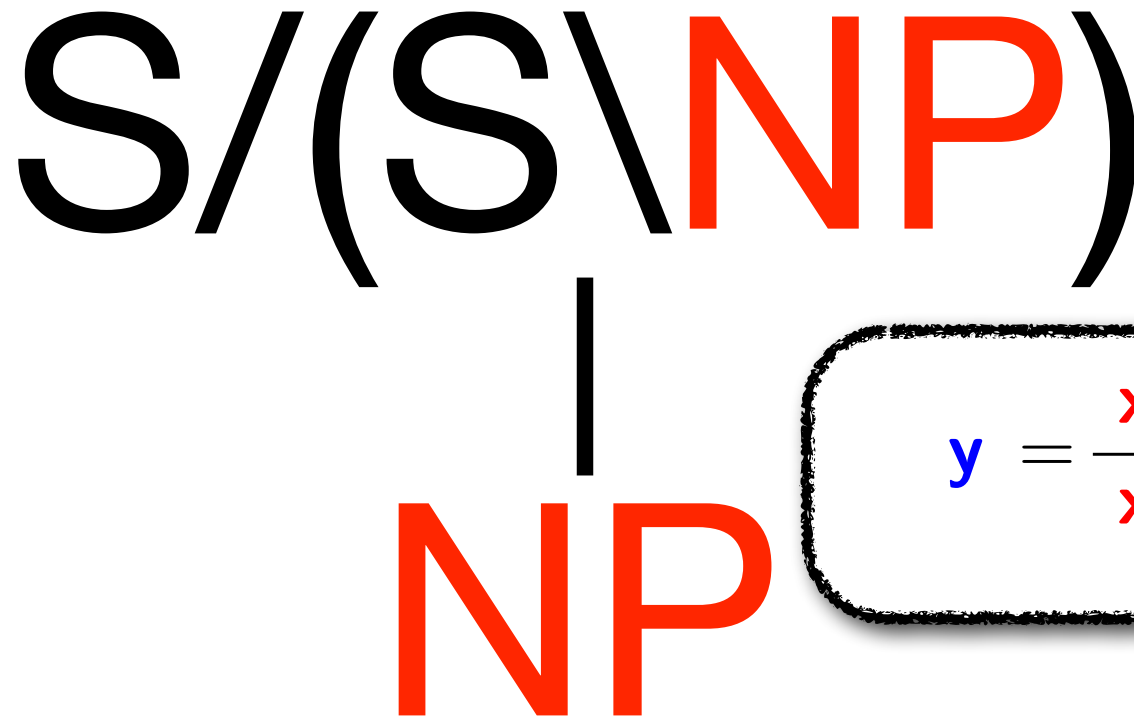


# Rules: Function Composition

$$\frac{x}{y} \cdot \frac{y}{z} = \frac{x}{z}$$



# Rules: Type-Raising



$$y = \frac{x}{x} \cdot y = \frac{x}{\left(\frac{x}{y}\right)}$$



# Type-raising and composition

**Type-raising:**  $X \rightarrow T/(T \backslash X)$

**Turns an argument into a function.**

NP  $\rightarrow$  S/(S \ NP) (subject)

NP  $\rightarrow$  (S \ NP) \ ((S \ NP) / NP) (object)

**Harmonic composition:**  $X/Y \ Y/Z \rightarrow X/Z$

**Composes two functions (complex categories),**  
same slashes

(S \ NP) / PP   PP / NP  $\rightarrow$  (S \ NP) / NP

S / (S \ NP)   (S \ NP) / NP  $\rightarrow$  S / NP

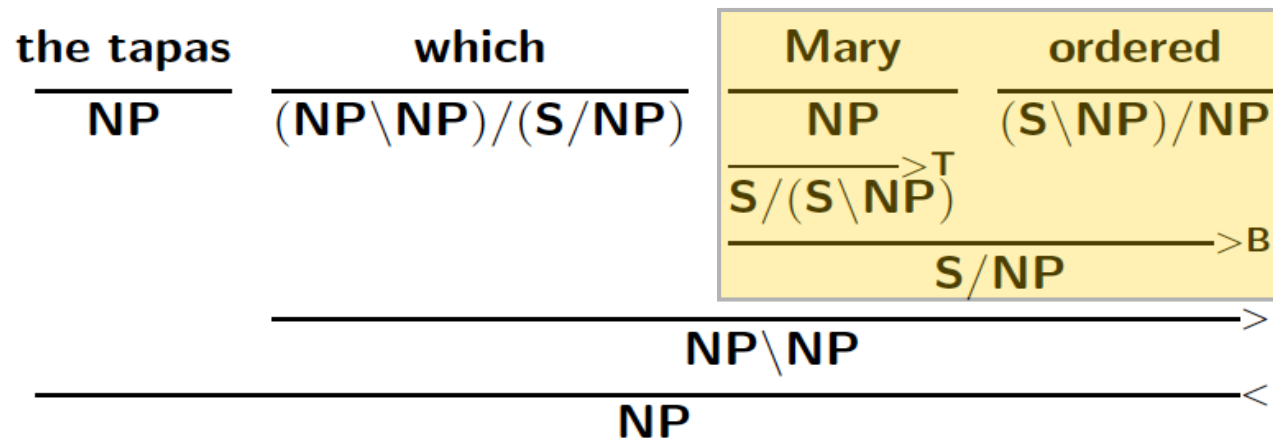
**Crossing composition:**  $X/Y \ Y \backslash Z \rightarrow X \backslash Z$

**Composes two functions (complex categories),**  
different slashes

(S \ NP) / S   S \ NP  $\rightarrow$  (S \ NP) \ NP

# Type-raising and composition

Wh-movement (relative clause):



Right-node raising:

