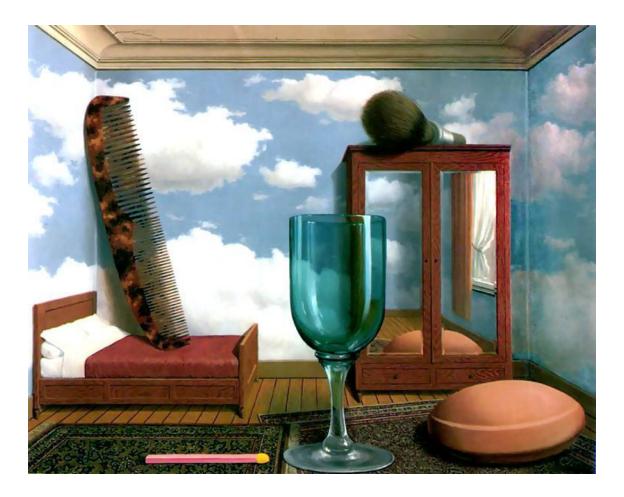
## Single-view Metrology and Cameras

10/10/17



#### Computational Photography Derek Hoiem, University of Illinois

## Project 2 Results

- Incomplete list of great project pages
  - <u>Haohang Huang</u>: Best presented project; nice iterative results and demonstration, animations for hole filling
  - <u>Xiaotian Le</u>: Runner Up Project: Cool Sliding Window to demonstrate difference in textures (most liked)
  - <u>Xiaoyan Wang</u>: Runner Up Project: Cool QR Code Texture Transfer and Toast results
  - <u>Kartik Agarwal</u>: Overall nice project
  - Ho Yin Au: Nice seam finding results
  - Yuanzhe Rijn Bian: Nice Einstein Toast Result
  - Yundi Fei: Nice seam finding results
  - Zih Siou Hung: Nice Van Gogh texture transfer onto a cat
  - Brendan Wilson (synthesized pattern): Very unique texture patterns that were explored
  - Zexuan Zhong: Best hole filling exploration

## Texture synthesis





Brendan Wilson

## Texture synthesis



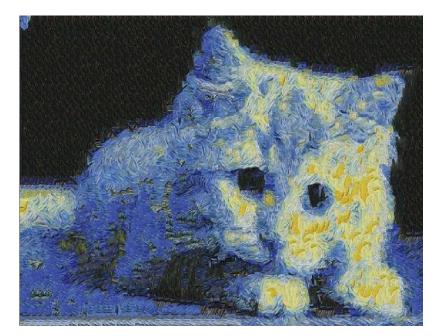


Brendan Wilson

#### Texture transfer

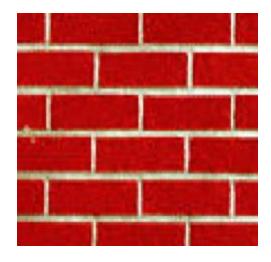


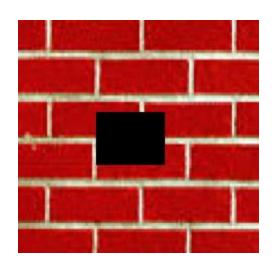


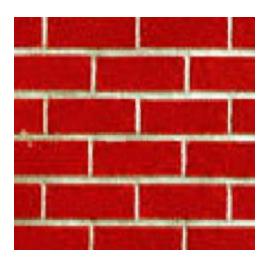


Zih Siou Hung

## Hole filling







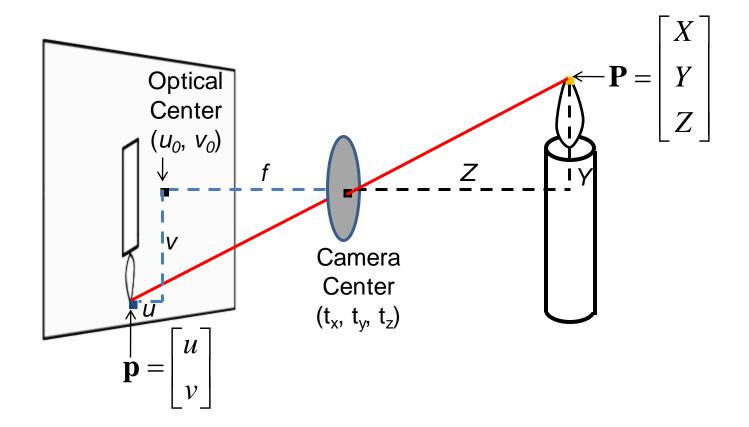




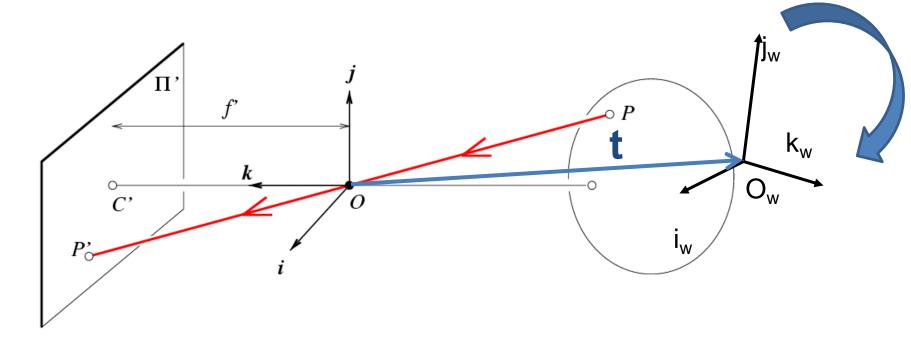


#### Zexuan Zhong

### **Review: Pinhole Camera**



## **Review: Projection Matrix**



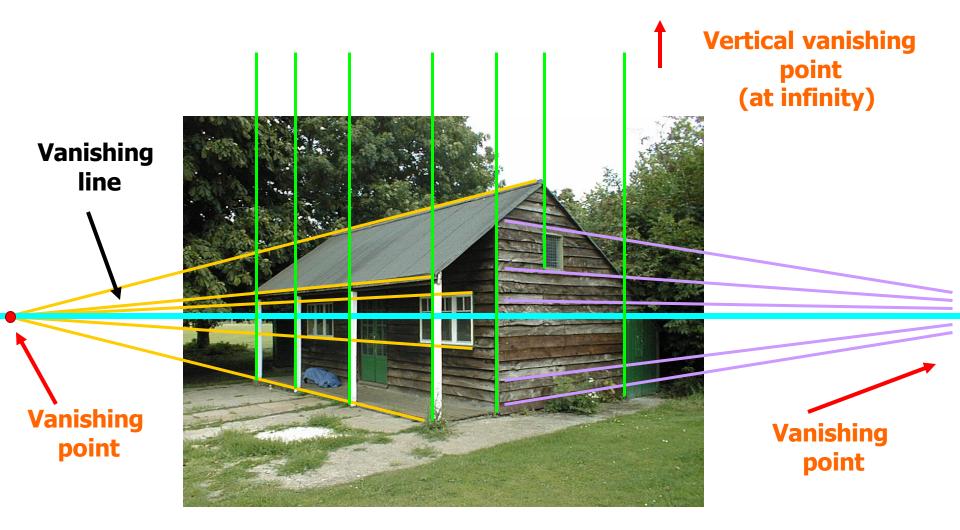
R

$$\mathbf{X} = \mathbf{K} \begin{bmatrix} \mathbf{R} & \mathbf{t} \end{bmatrix} \mathbf{X} \Longrightarrow w \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f & s & u_0 \\ 0 & \alpha f & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

## Take-home questions from last week

- Suppose the camera axis is in the direction of (x=0, y=0, z=1) in its own coordinate system. What is the camera axis in world coordinates given the extrinsic parameters *R*, *t*
- Suppose a camera at height y=h (x=0,z=0) observes a point at (u,v) known to be on the ground (y=0). Assume R is identity. What is the 3D position of the point in terms of f, u<sub>0</sub>, v<sub>0</sub>?

## **Review: Vanishing Points**



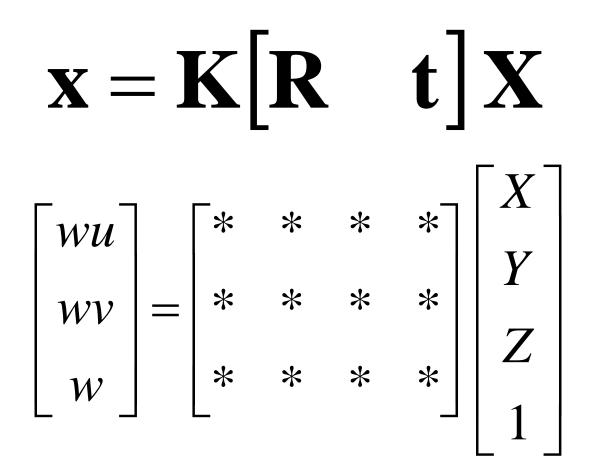
### Perspective and weak perspective



## This class

- How can we calibrate the camera?
- How can we measure the size of objects in the world from an image?
- What about other camera properties: focal length, field of view, depth of field, aperture, f-number?
- How to do "focus stacking" to get a sharp picture of a nearby object
- How the "vertigo effect" works

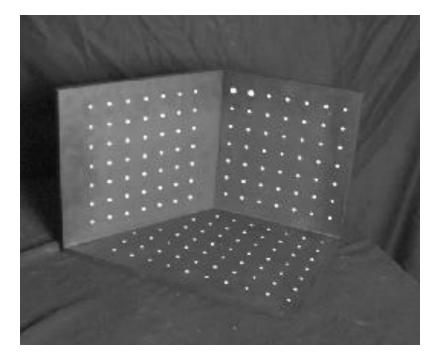
#### How to calibrate the camera?



## Calibrating the Camera

Method 1: Use an object (calibration grid) with known geometry

- Correspond image points to 3d points
- Get least squares solution (or non-linear solution)

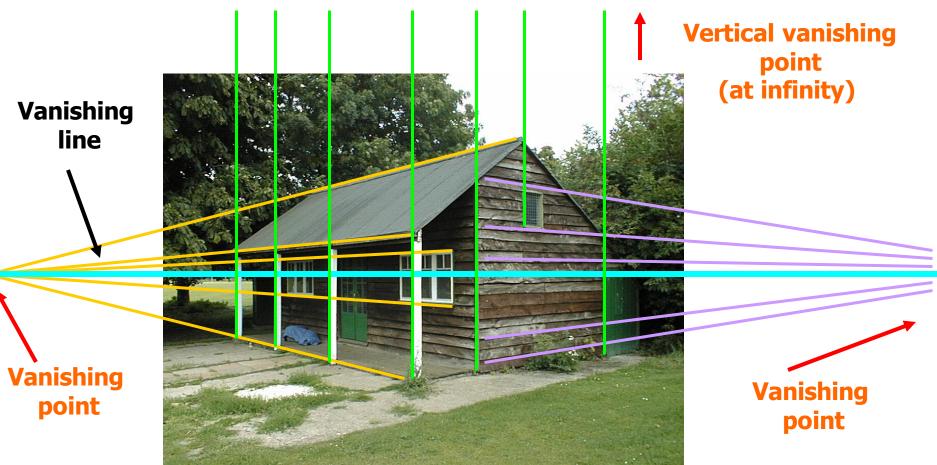


$$\begin{bmatrix} wu \\ wv \\ w \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

## Calibrating the Camera

#### Method 2: Use vanishing points

 Find vanishing points corresponding to orthogonal directions



## Take-home question (for later)

Suppose you have estimated finite three vanishing points corresponding to orthogonal directions:

- 1) How to solve for intrinsic matrix? (assume K has three parameters)
  - The transpose of the rotation matrix is its inverse
  - Use the fact that the 3D directions are orthogonal
- 2) How to recover the rotation matrix that is aligned with the 3D axes defined by these points?
  - In homogeneous coordinates, 3d point at infinity is (X, Y, Z, 0)

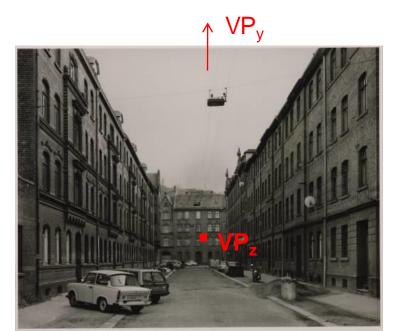
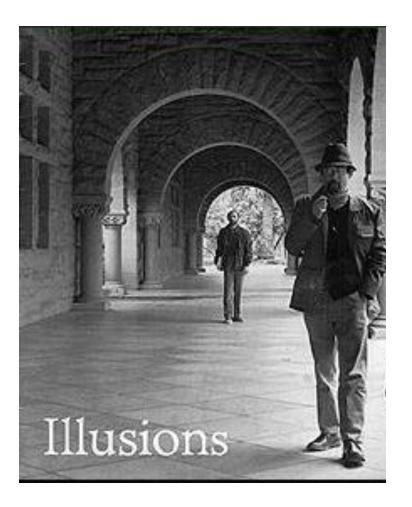




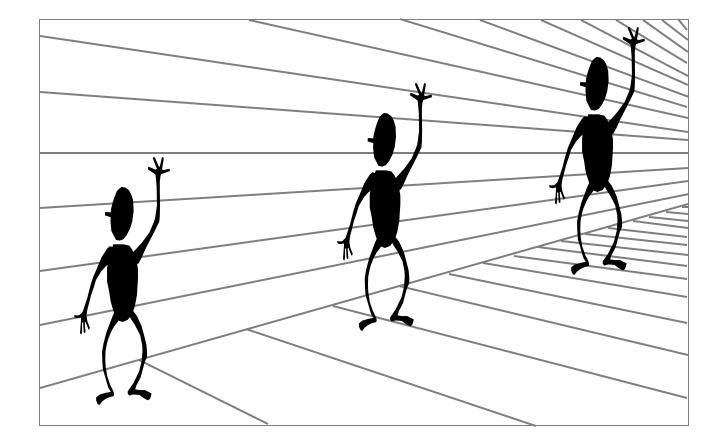
Photo from online Tate collection

# How can we measure the size of 3D objects from an image?



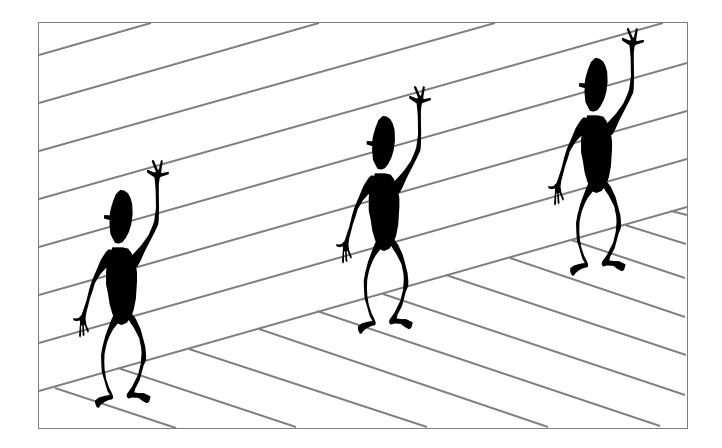
Slide by Steve Seitz

#### Perspective cues



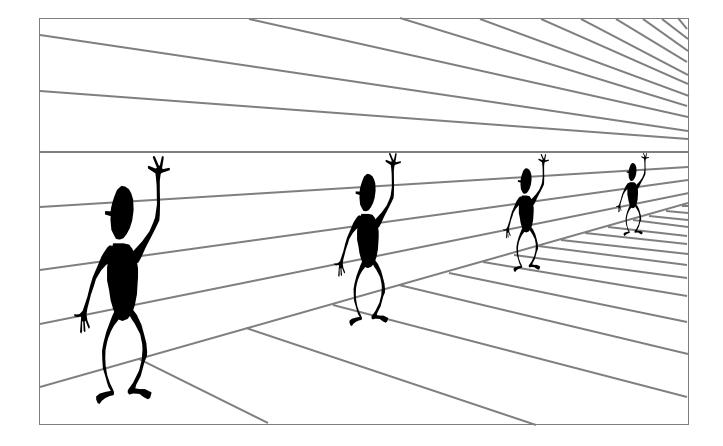
Slide by Steve Seitz

#### Perspective cues



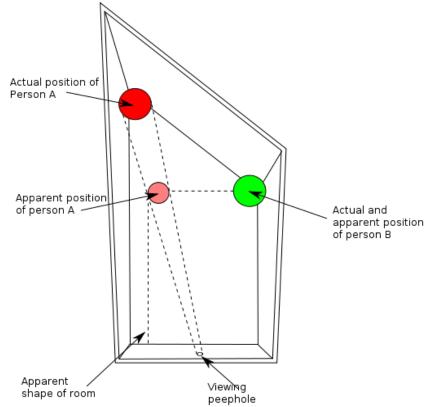
Slide by Steve Seitz

#### Perspective cues

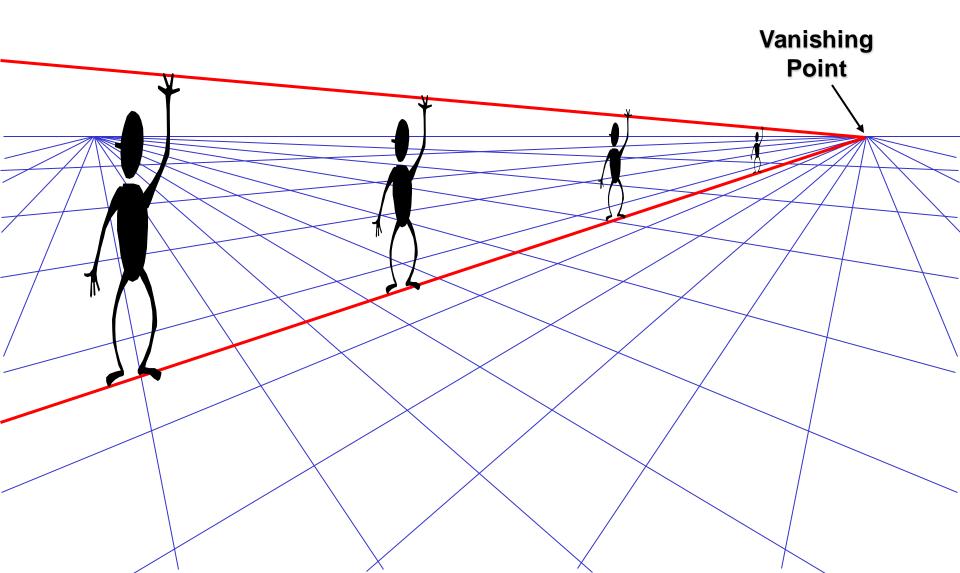


#### Ames Room

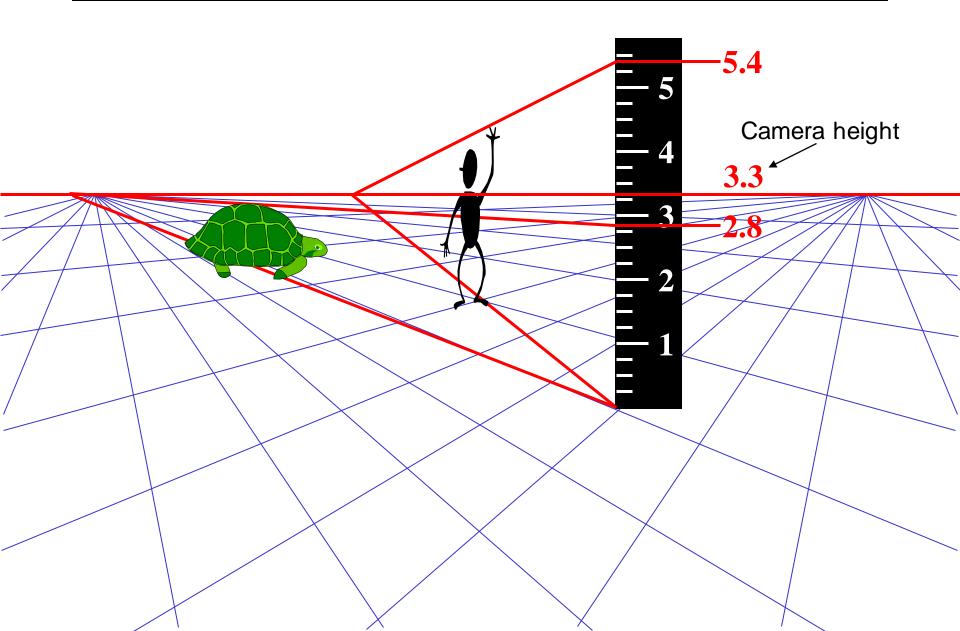




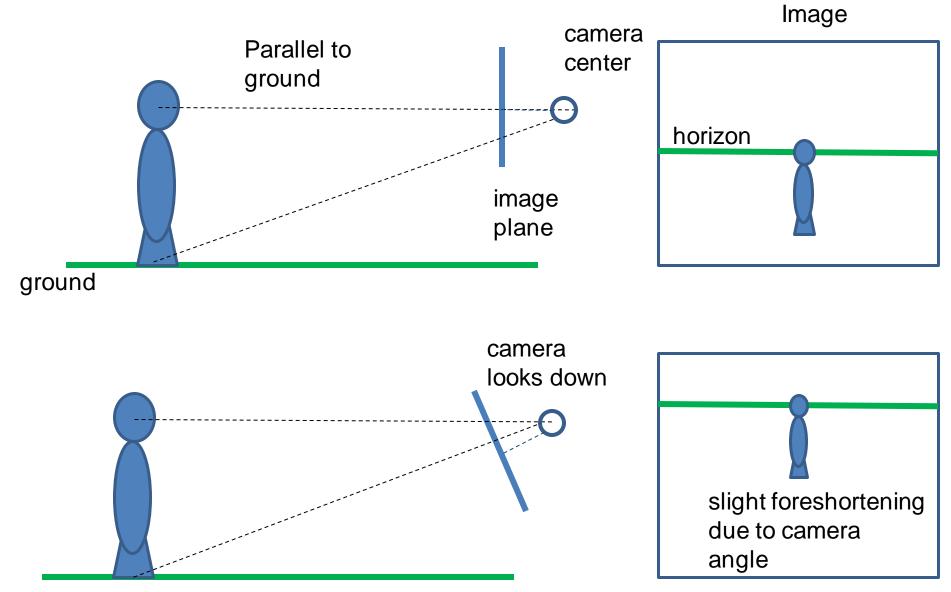
## Comparing heights



## Measuring height



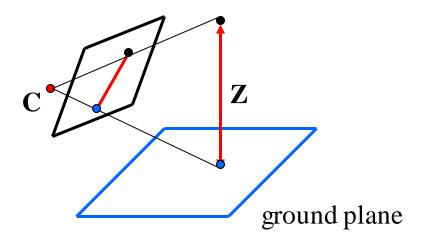
## Two views of a scene



# Which is higher – the camera or the parachute?



## Measuring height without a giant ruler



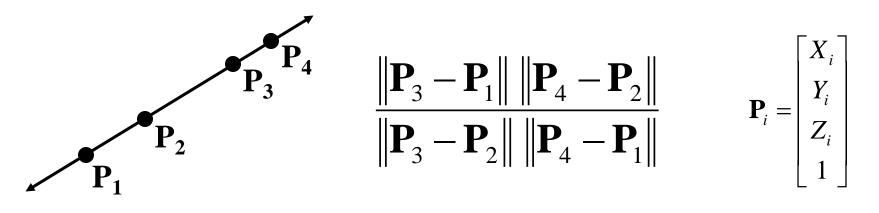
#### Compute Z from image measurements

• Need a reference object

### The cross ratio

#### A Projective Invariant

- Something that does not change under projective transformations (including perspective projection)
- The cross-ratio of 4 collinear points



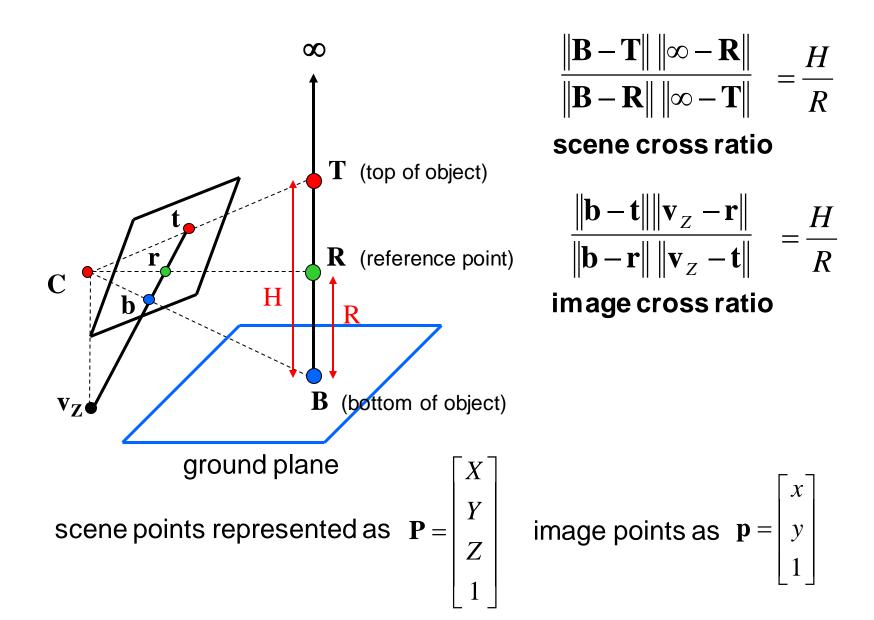
Can permute the point ordering

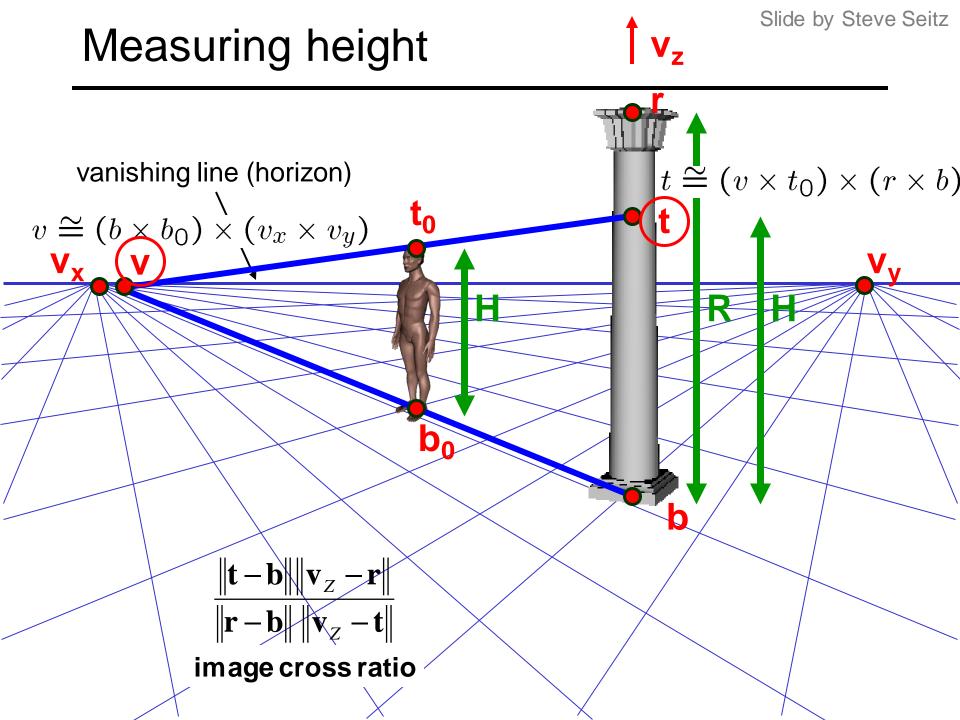
 $\frac{\|\mathbf{P}_{1}-\mathbf{P}_{3}\|\|\mathbf{P}_{4}-\mathbf{P}_{2}\|}{\|\mathbf{P}_{1}-\mathbf{P}_{2}\|\|\mathbf{P}_{4}-\mathbf{P}_{3}\|}$ 

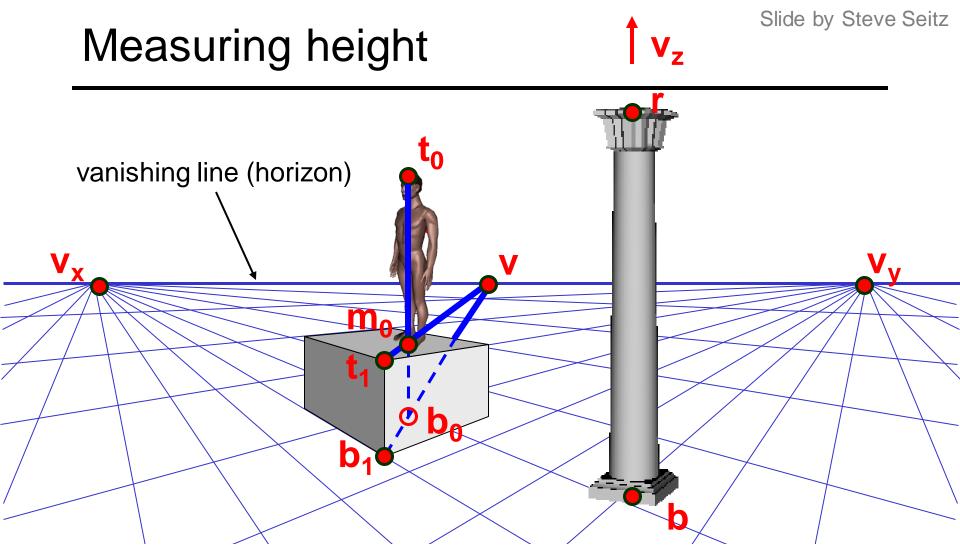
• 4! = 24 different orders (but only 6 distinct values)

This is the fundamental invariant of projective geometry

## Measuring height







What if the point on the ground plane **b**<sub>0</sub> is not known?

- Here the guy is standing on the box, height of box is known
- Use one side of the box to help find  $\mathbf{b}_0$  as shown above

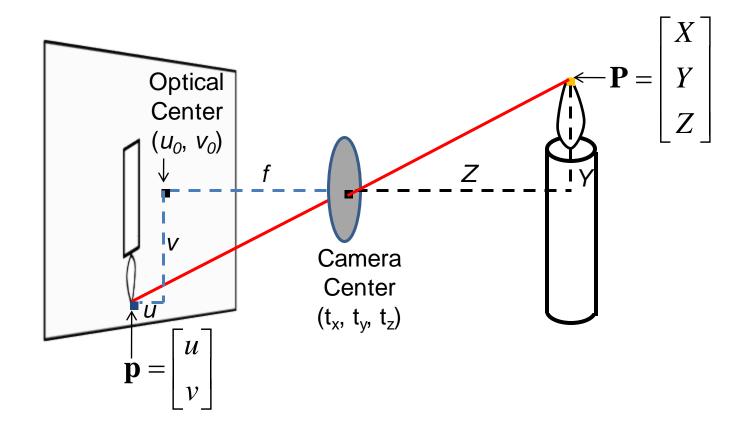
## Take-home question

Assume that the man is 6 ft tall

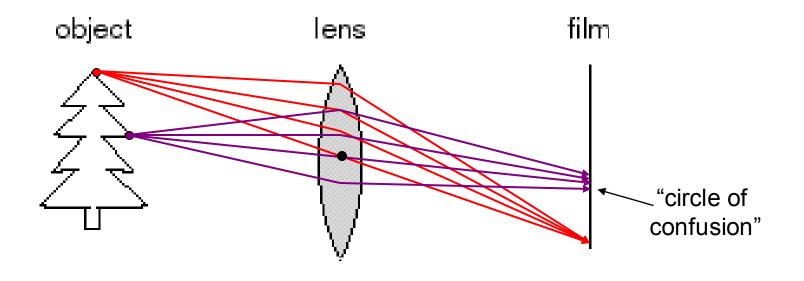
- What is the height of the front of the building?
- What is the height of the camera?



# Beyond the pinhole: What about focus, aperture, DOF, FOV, etc?

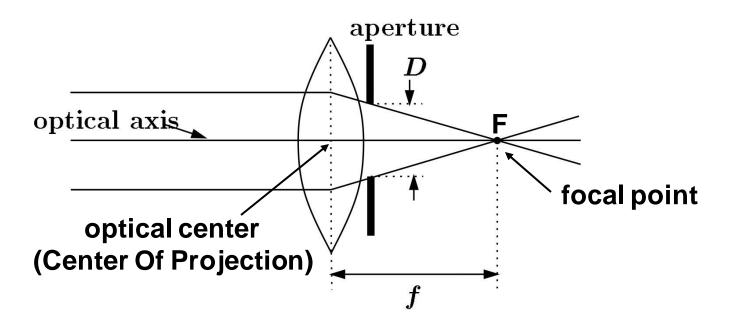


## Adding a lens



- A lens focuses light onto the film
  - There is a specific distance at which objects are "in focus"
    - other points project to a "circle of confusion" in the image
  - Changing the shape of the lens changes this distance

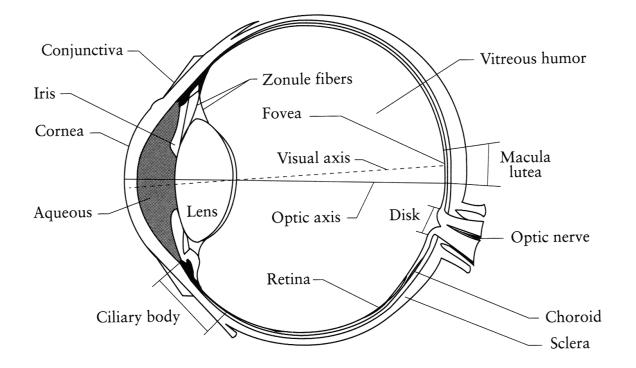
## Focal length, aperture, depth of field



A lens focuses parallel rays onto a single focal point

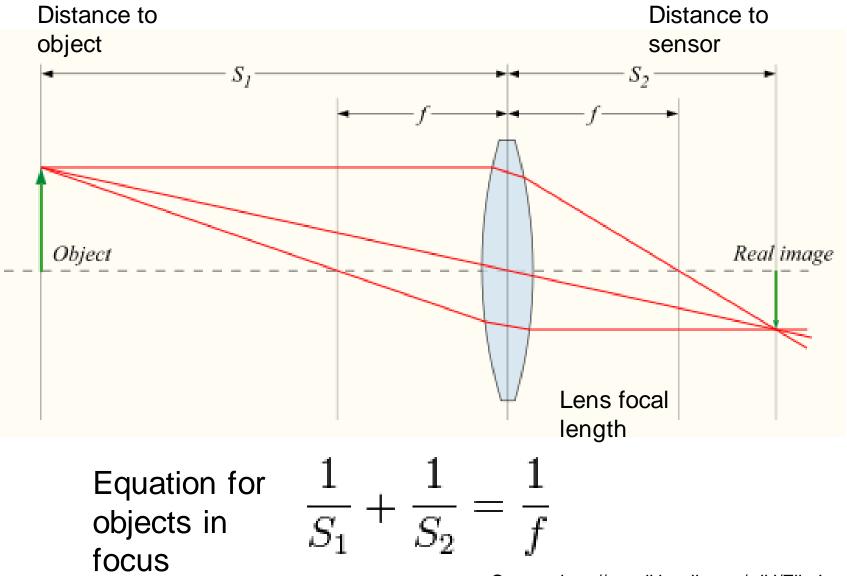
- focal point at a distance f beyond the plane of the lens
- Aperture of diameter D restricts the range of rays

## The eye



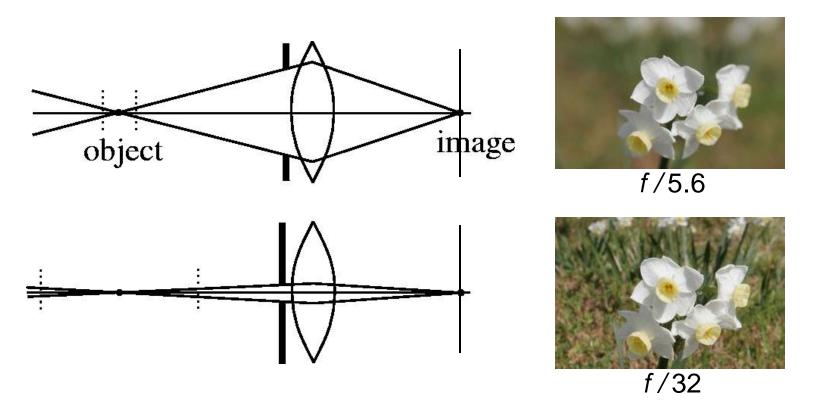
- The human eye is a camera
  - Iris colored annulus with radial muscles
  - Pupil the hole (aperture) whose size is controlled by the iris

## Focus with lenses



Source: http://en.wikipedia.org/wiki/File:Lens3.svg

# The aperture and depth of field



Changing the aperture size or focusing distance affects depth of field f-number (f/#) =focal\_length / aperture\_diameter (e.g., f/16 means that the focal length is 16 times the diameter) When you change the f-number, you are changing the aperture

Flower images from Wikipedia <u>http://en.wikipedia.org/wiki/Depth\_of\_field</u>

#### Varying the aperture

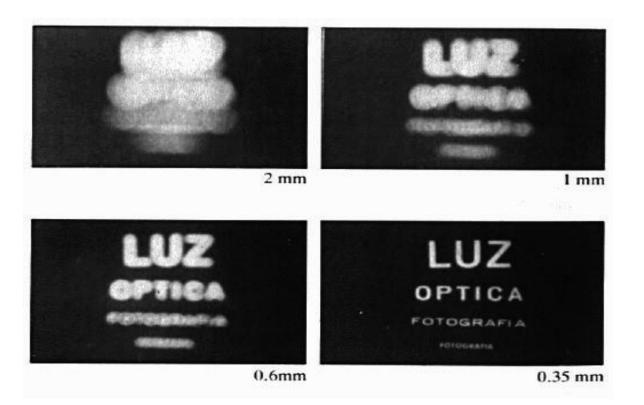




Small aperture = large DOF

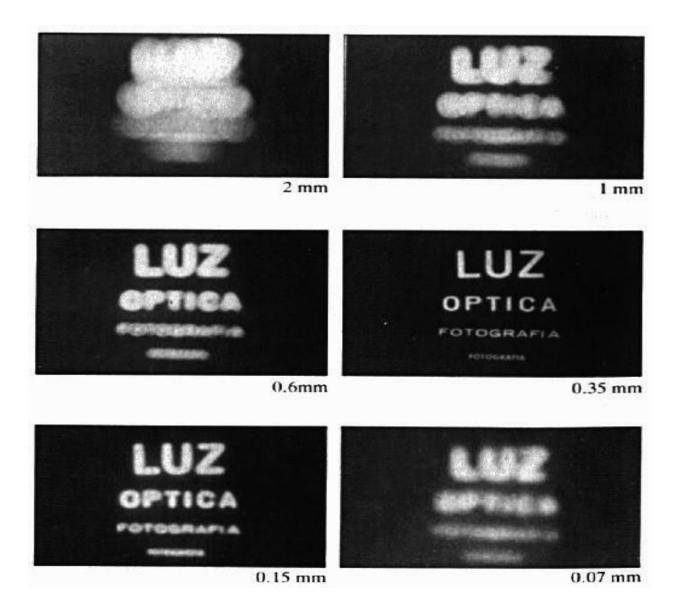
Large aperture = small DOF

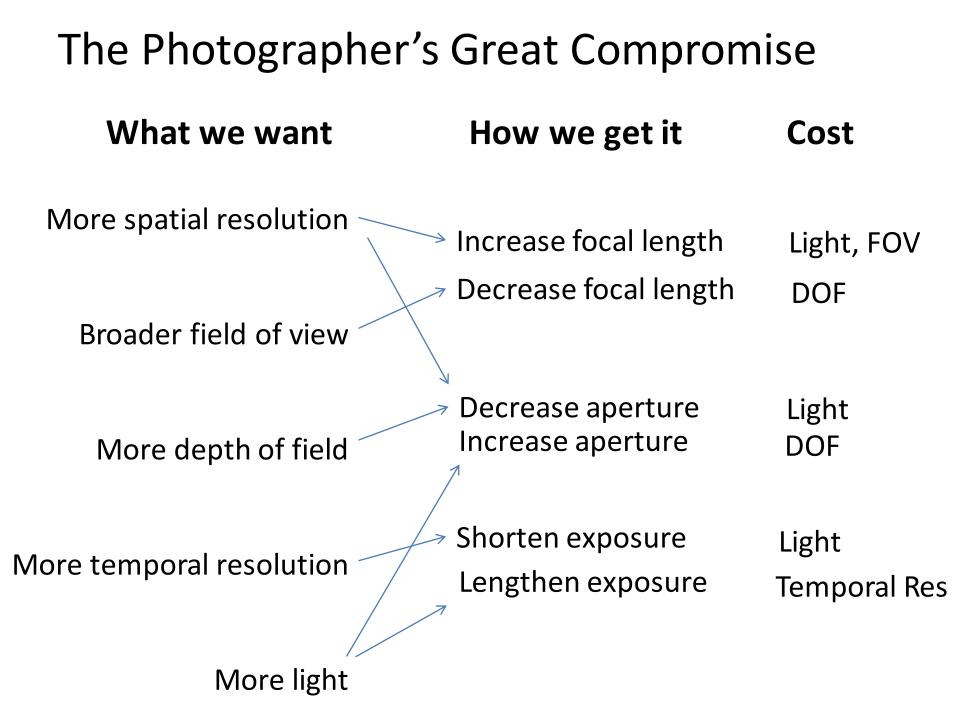
# Shrinking the aperture



- Why not make the aperture as small as possible?
  - Less light gets through
  - Diffraction effects

### Shrinking the aperture





#### Difficulty in macro (close-up) photography

- For close objects, we have a small relative DOF
- Can only shrink aperture so far

How to get both bugs in focus?



# Solution: Focus stacking

1. Take pictures with varying focal length



Example from <a href="http://www.wonderfulphotos.com/articles/macro/focus\_stacking/">http://www.wonderfulphotos.com/articles/macro/focus\_stacking/</a>

# Solution: Focus stacking

- 1. Take pictures with varying focal length
- 2. Combine



#### Focus stacking



http://www.wonderfulphotos.com/articles/macro/focus\_stacking/

#### Focus stacking

How to combine?

Web answer: With software (Photoshop, CombineZM)

How to do it automatically?

### Focus stacking

#### How to combine?

- 1. Align images (e.g., using corresponding points)
- 2. Two ideas
  - a) Mask regions by hand and combine with pyramid blend
  - b) Gradient domain fusion (mixed gradient) without masking

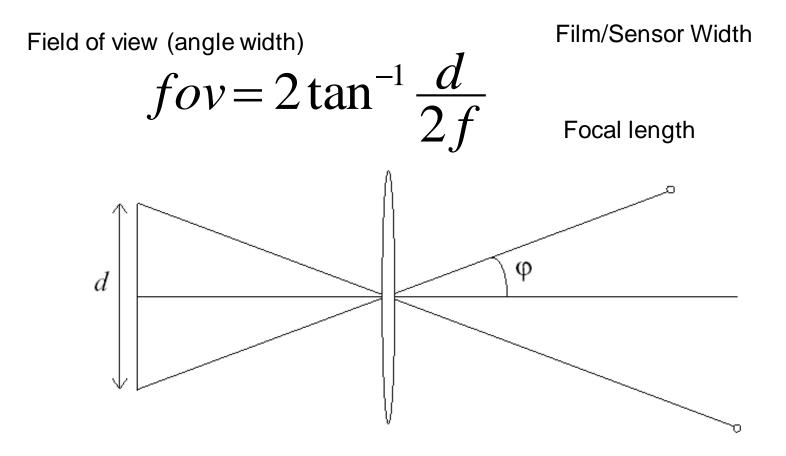
Automatic solution would make an interesting final project

Recommended Reading:

http://www.digital-photographyschool.com/an-introduction-to-focusstacking

http://www.zen20934.zen.co.uk/photograph y/Workflow.htm#Focus%20Stacking

#### Relation between field of view and focal length



# Dolly Zoom or "Vertigo Effect"

#### http://www.youtube.com/watch?v=NB4bikrNzMk



How is this done?

Zoom in while moving away

http://en.wikipedia.org/wiki/Focal\_length

# Dolly zoom (or "Vertigo effect")

Field of view (angle width)  

$$fov = 2 \tan^{-1} \frac{d}{2f}$$
 Film/Sensor Width  
Focal length  
 $2 \tan \frac{fov}{2} = \frac{width}{distance}$ 

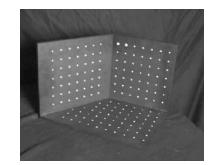
Distance between object and camera

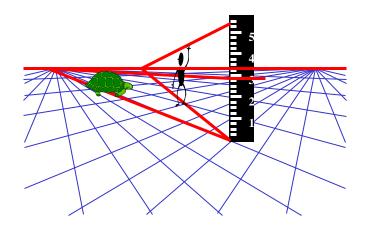
# Things to remember

 Can calibrate using grid or VP

• Can measure relative sizes using VP

• Effects of focal length, aperture + tricks







#### Next class

- Go over take-home questions from today
- Single-view 3D Reconstruction