

# Computational Approaches to Cameras

11/12/15

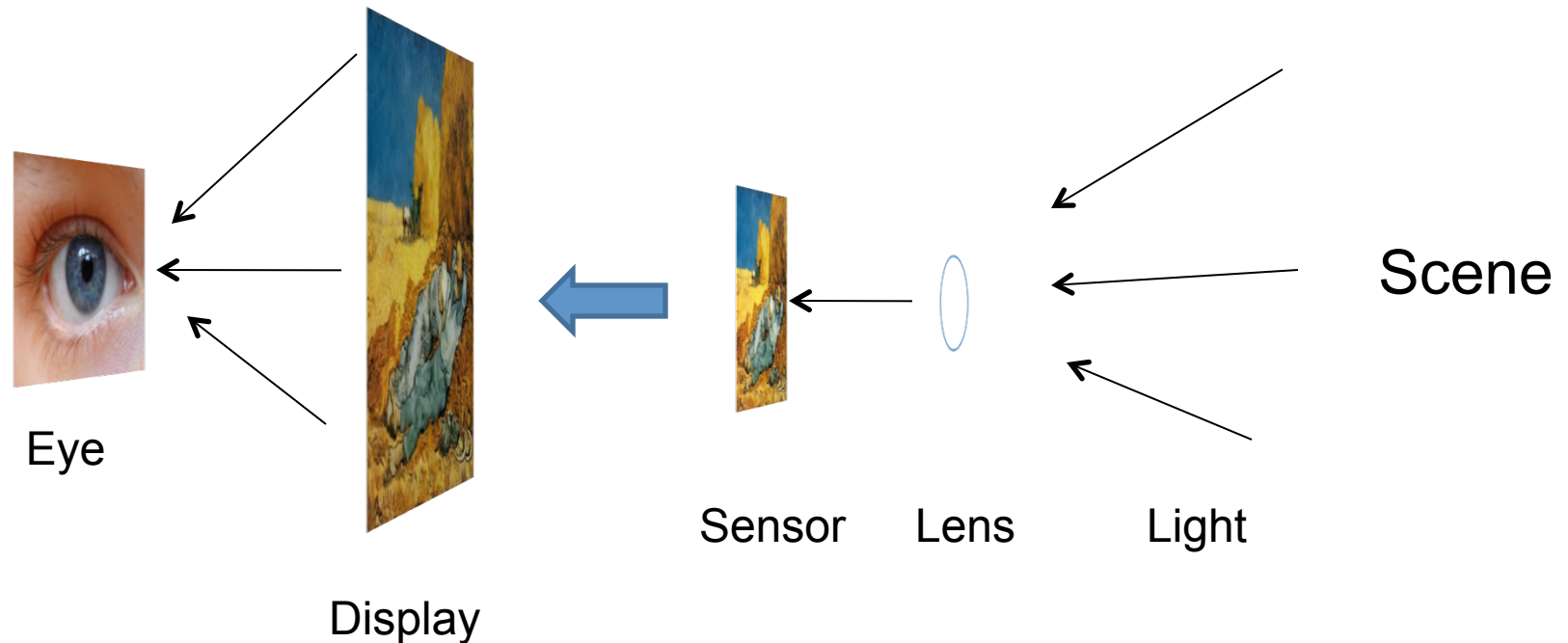


Magritte , *The False Mirror* (1935)

Computational Photography  
Derek Hoiem, University of Illinois

# Conventional cameras

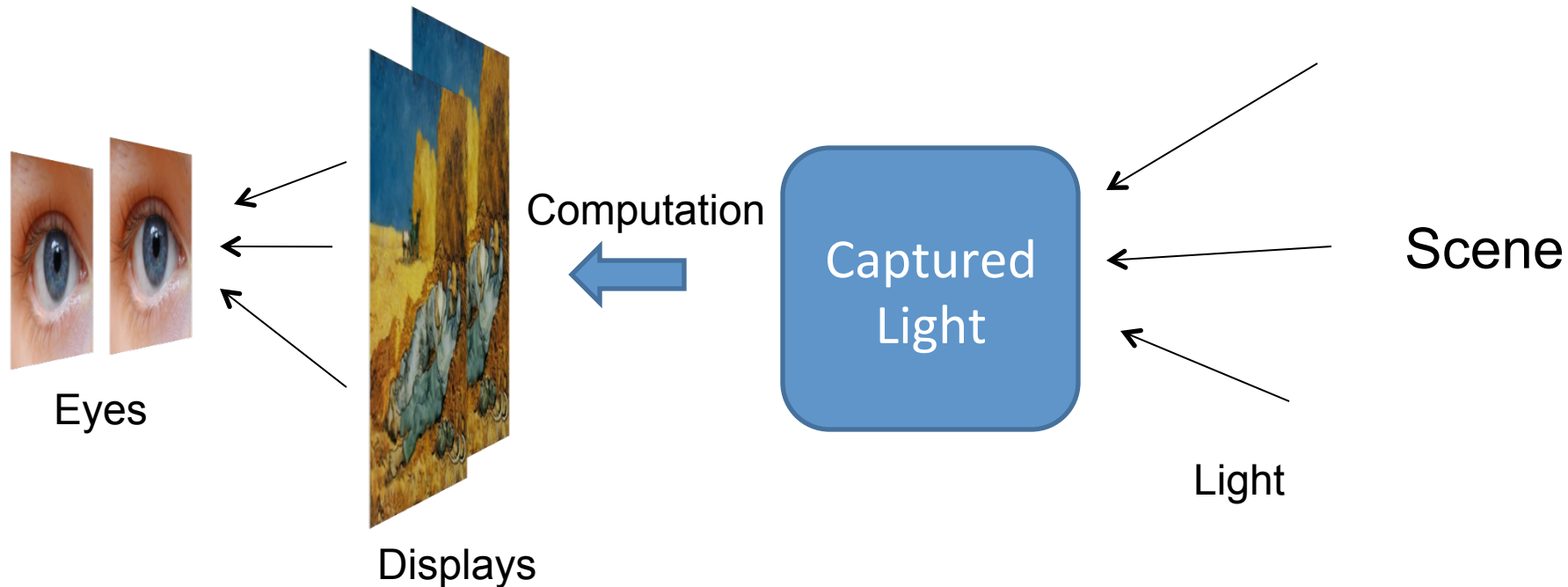
- Conventional cameras are designed to capture light in a medium that is directly viewable





# Computational cameras

- With a computational approach, we can capture light and then figure out what to do with it



# Questions for today

- How can we represent all of the information contained in light?
- What are the fundamental limitations of cameras?
- What sacrifices have we made in conventional cameras? For what benefits?
- How else can we design cameras for better focus, deblurring, multiple views, depth, etc.?

How can we represent all of the  
information contained in light?

# Representing Light: The Plenoptic Function

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Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The Plenoptic Function (Adelson & Bergen)

Let's start with a stationary person and try to parameterize everything that he can see...

# Grayscale snapshot

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$$P(\theta, \phi)$$

is intensity of light

- Seen from a single view point
- At a single time
- Averaged over the wavelengths of the visible spectrum

(can also do  $P(x, y)$ , but spherical coordinate are nicer)

# Color snapshot

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$$P(\theta, \phi, \lambda)$$

is intensity of light

- Seen from a single view point
- At a single time
- As a function of wavelength

# A movie

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$$P(\theta, \phi, \lambda, t)$$

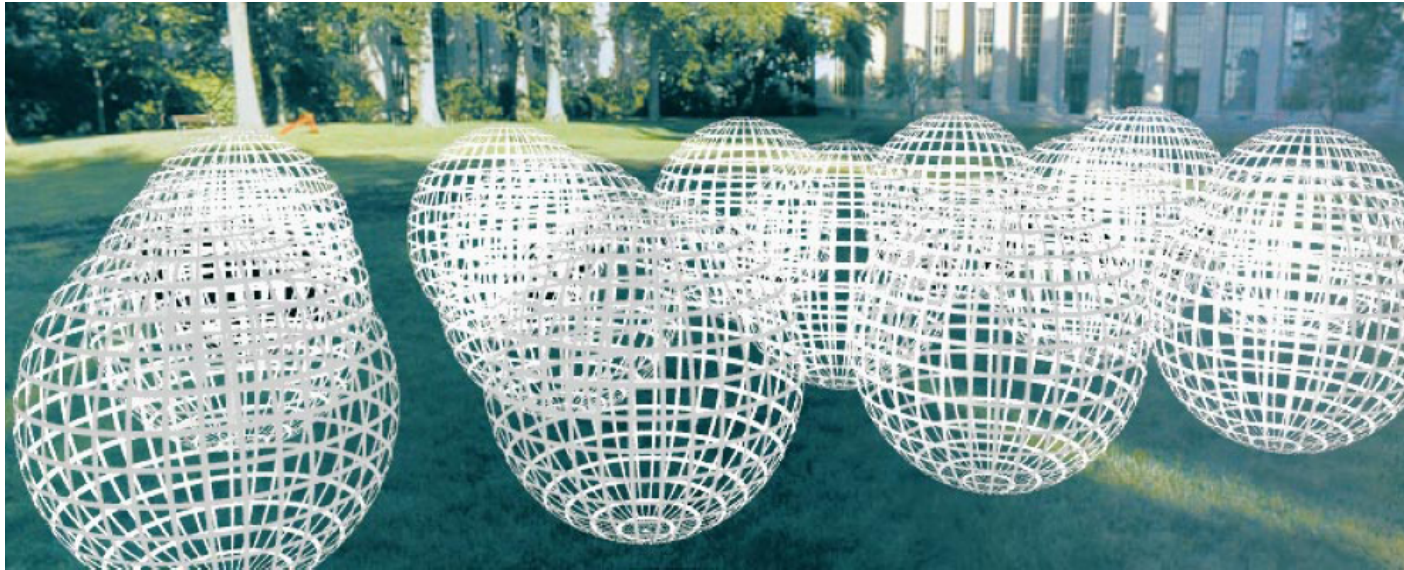
is intensity of light

- Seen from a single view point
- Over time
- As a function of wavelength



# Holographic movie

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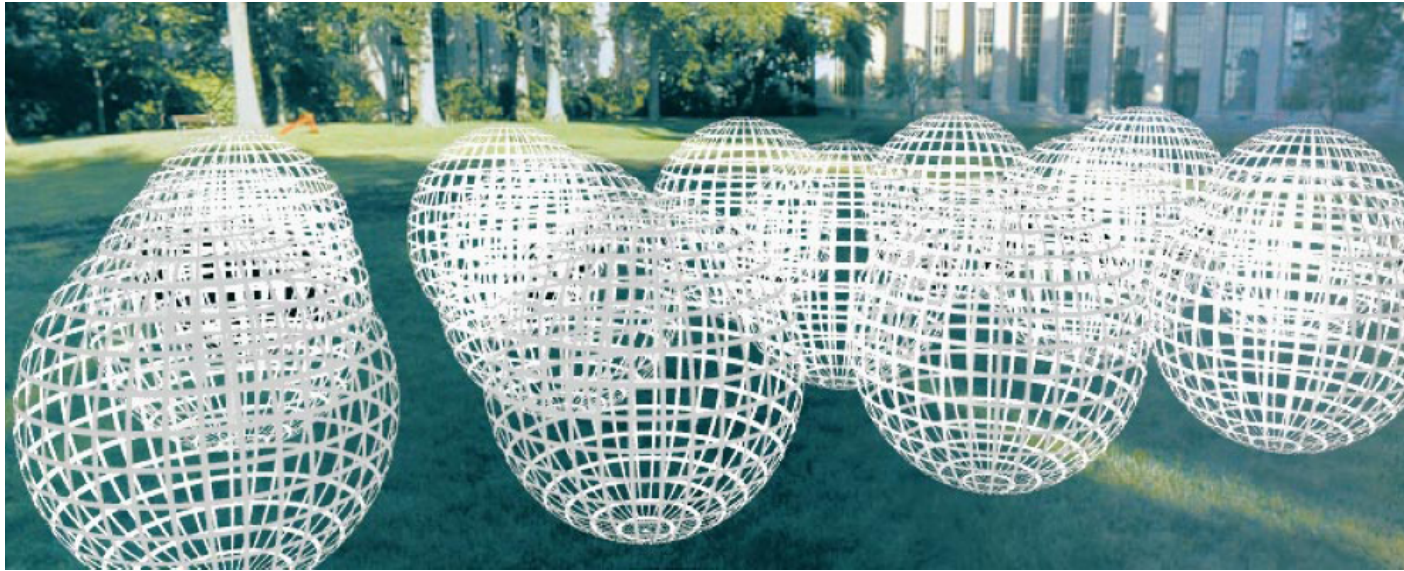
$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

is intensity of light

- Seen from ANY viewpoint
- Over time
- As a function of wavelength

# The Plenoptic Function

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$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

- Can reconstruct every possible view, at every moment, from every position, at every wavelength
- Contains every photograph, every movie, everything that anyone has ever seen!

# Full Plenoptic Camera

Records position and orientation of each ray  
at each time and wavelength

$$P(V_x, V_y, V_z, \theta, \phi, t, \lambda)$$

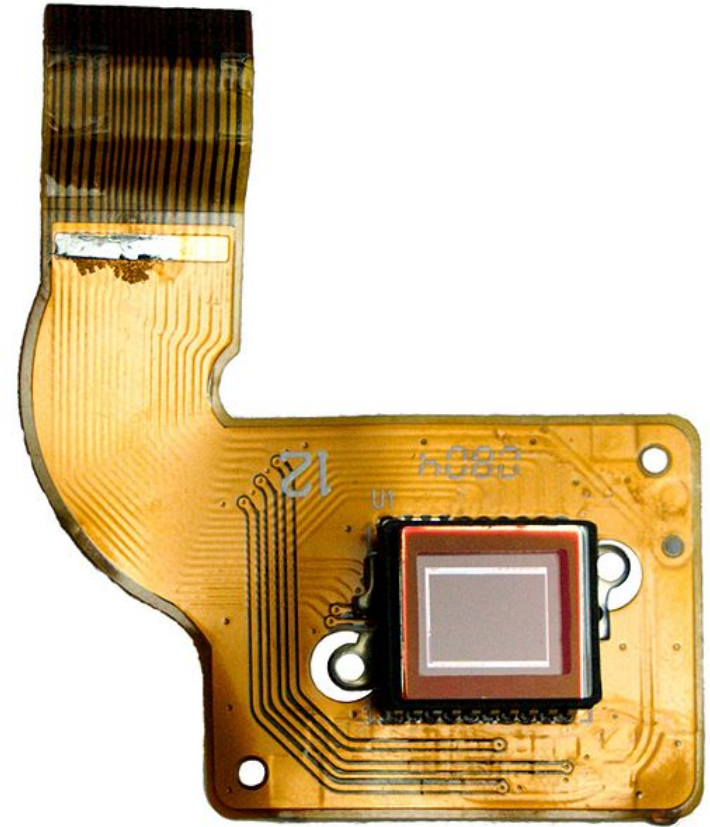
What fundamentally limits cameras?

# Representing light

The atomic element of light: ~~a pixel~~ **a ray**

# Fundamental limitations and trade-offs

- Only so much light in a given area to capture
- Basic sensor accumulates light at a set of positions from all orientations, over all time
- We want **intensity** of light at a **given time** at **one position** for a **set of orientations**
- Solutions:
  - funnel, constrain, redirect light
  - change the sensor



CCD inside camera

What sacrifices does the conventional camera make? For what gains?



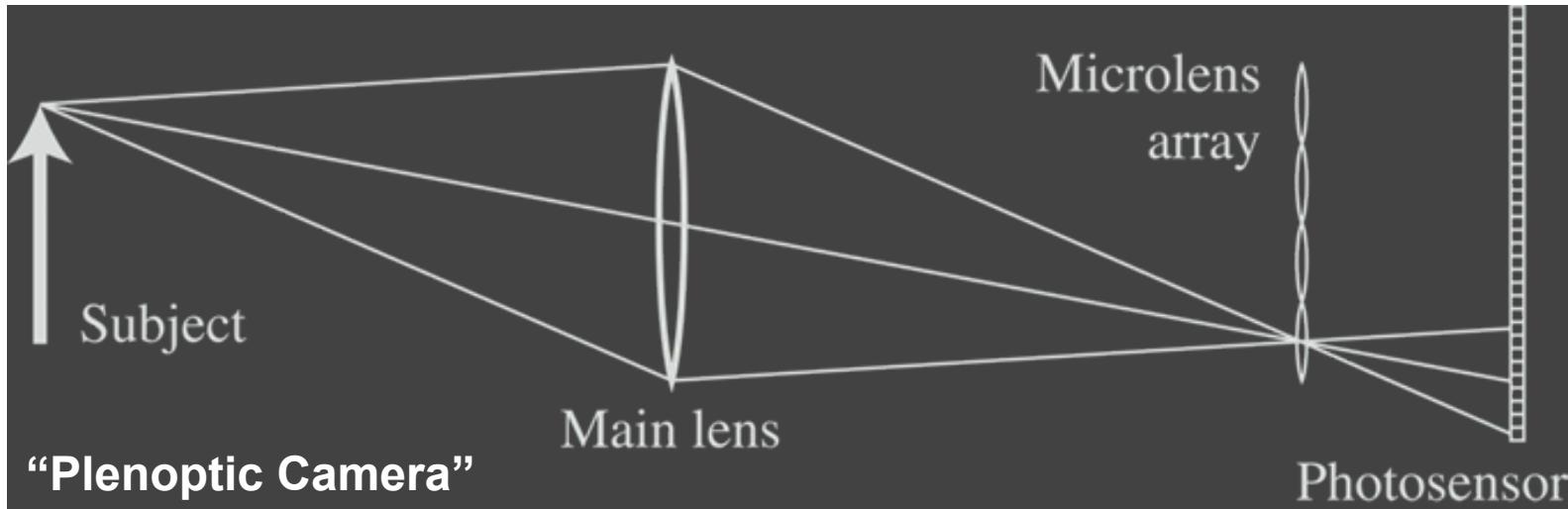
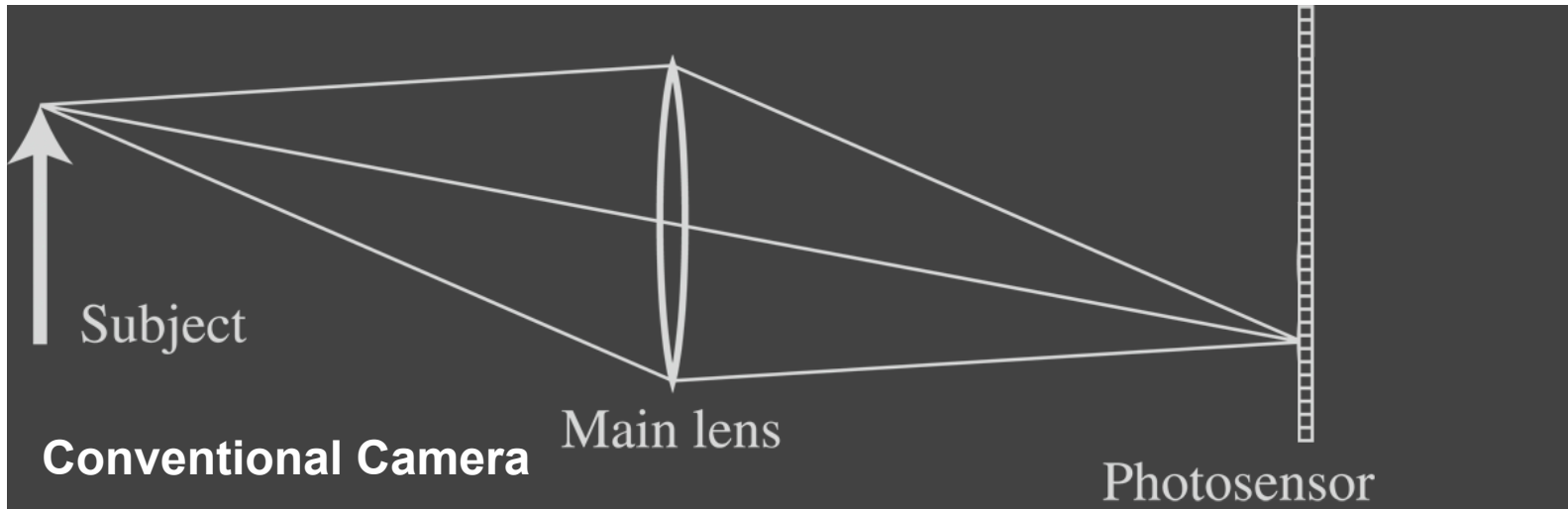
# Trade-offs of conventional camera

- Add a pinhole
  - ✓ Pixels correspond to small range of orientations at the camera center, instead of all gathered light at one position
  - ✗ Much less light hits sensor
- Add a lens
  - ✓ More light hits sensor
  - ✗ Limited depth of field
  - ✗ Chromatic aberration
- Add a shutter
  - Capture average intensity at a particular range of times
- Increase sensor resolution
  - ✓ Each pixel represents a smaller range of orientations
  - ✗ Less light per pixel
- Controls: aperture size, focal length, shutter time

How else can we design cameras?

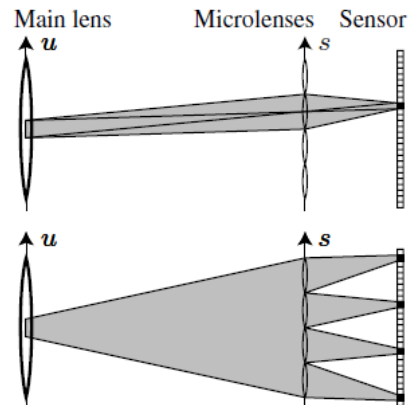
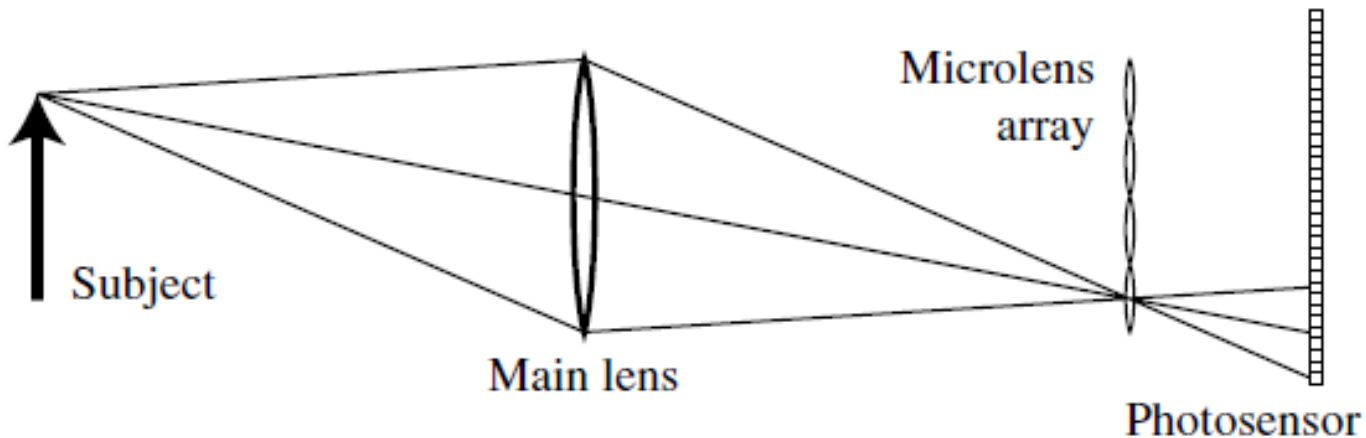
What do they sacrifice/gain?

# 1. Light Field Photography with “Plenoptic Camera”



# Light field photography

- Like replacing the human retina with an insect compound eye
- Records where light ray hits the lens



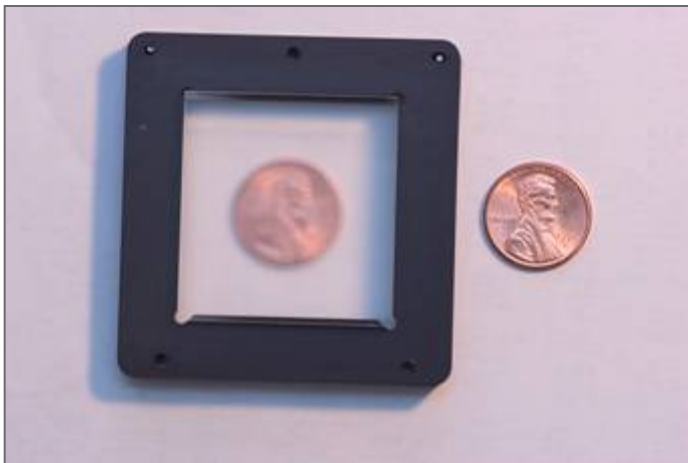
# Stanford Plenoptic Camera [Ng et al 2005]



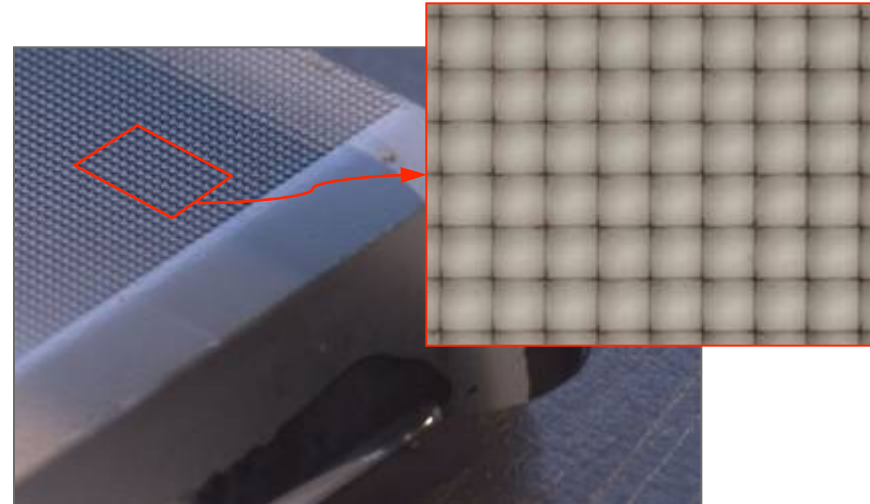
Contax medium format camera



Kodak 16-megapixel sensor



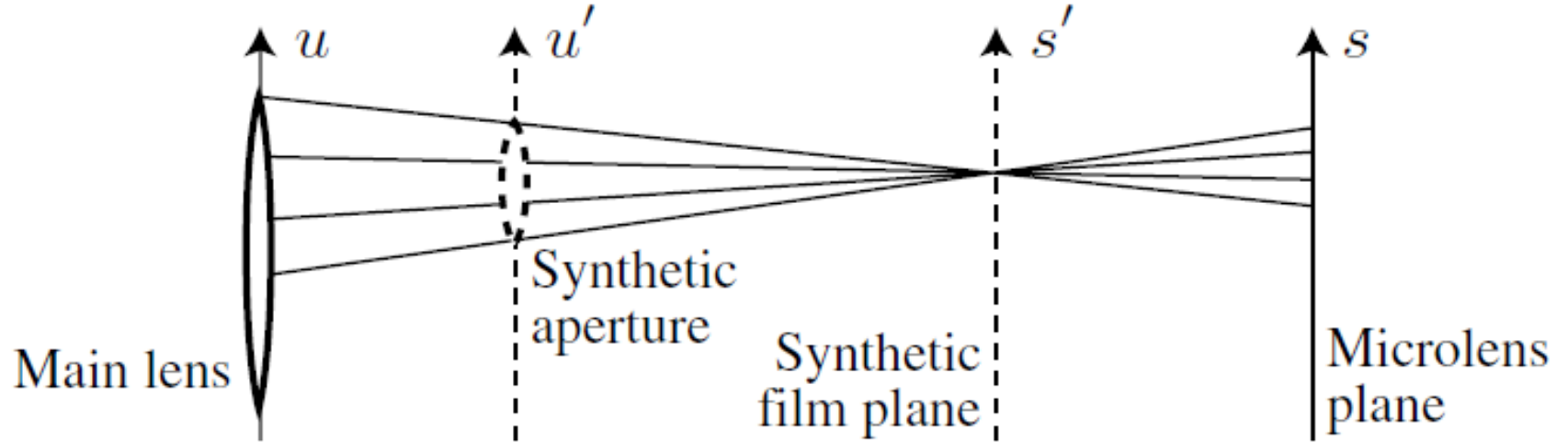
Adaptive Optics microlens array



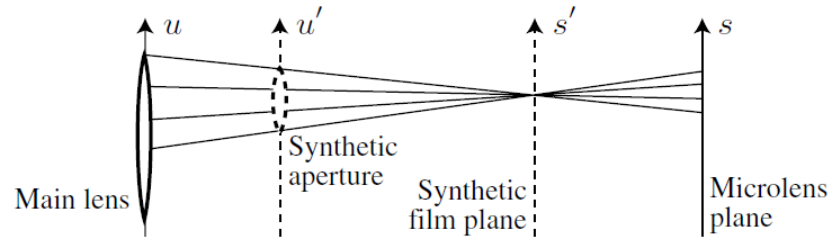
125 $\mu$  square-sided microlenses

$$4000 \times 4000 \text{ pixels} \div 292 \times 292 \text{ lenses} = 14 \times 14 \text{ pixels per lens}$$

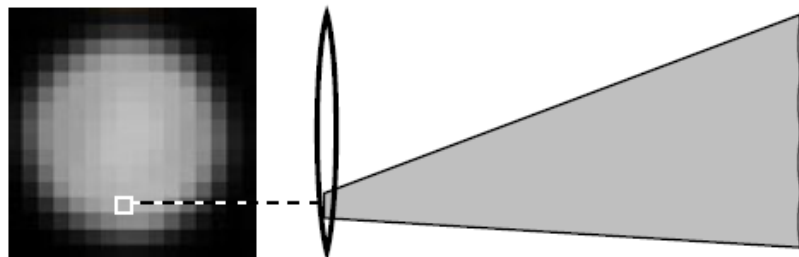
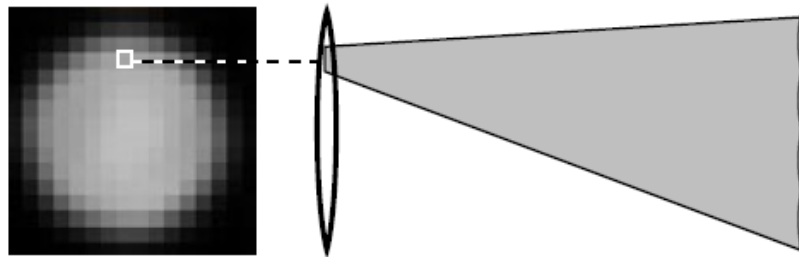
# Light field photography: applications



# Light field photography: applications



Change in  
viewpoint

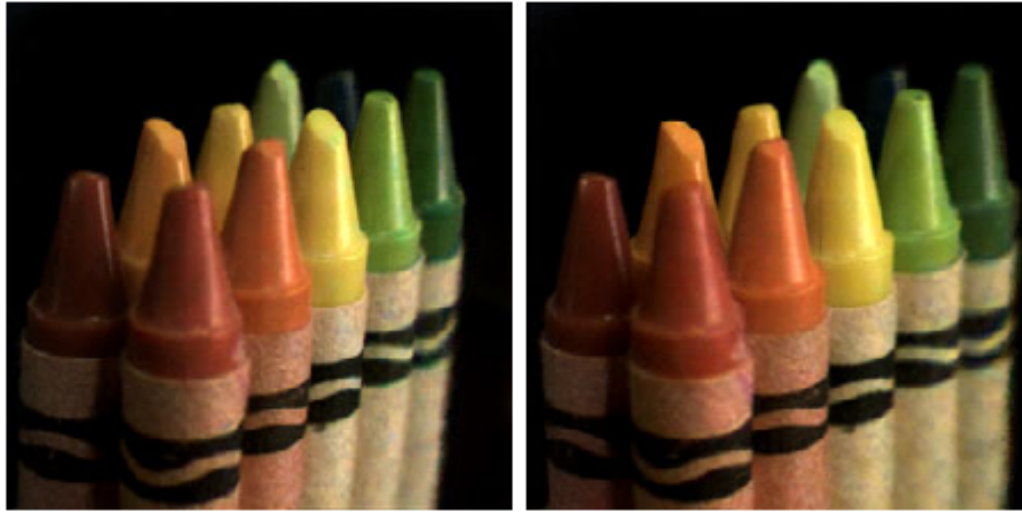




# Light field photography: applications

## Change in viewpoint

Lateral



Along Optical Axis



# Digital Refocusing



# Light field photography w/ microlenses

- We gain
  - Ability to refocus or increase depth of field
  - Ability for small viewpoint shifts
- What do we lose (vs. conventional camera)?

## 2. Coded apertures

# **Image and Depth from a Conventional Camera with a Coded Aperture**

**Anat Levin, Rob Fergus,  
Frédo Durand, William Freeman**

**MIT CSAIL**

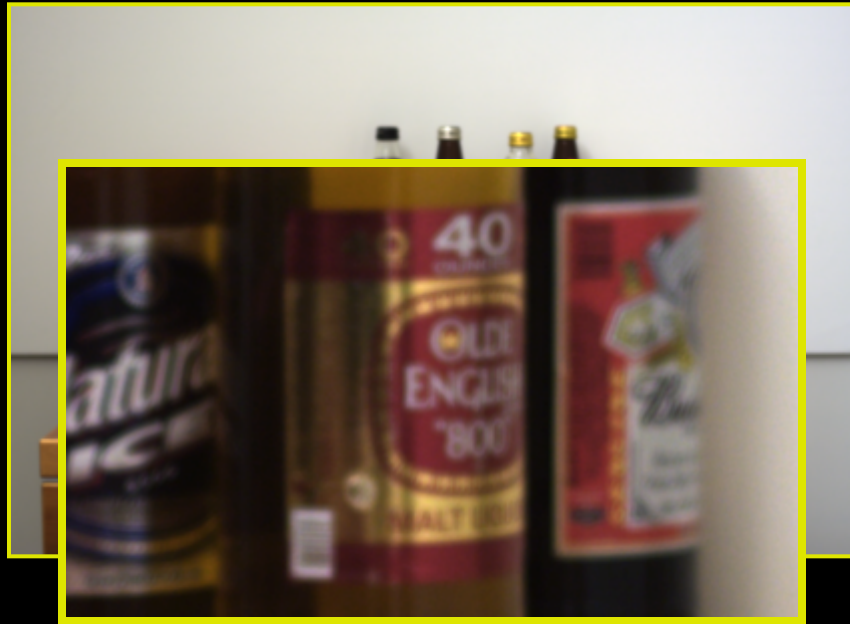
**Single input image:**



**Output #1: Depth map**



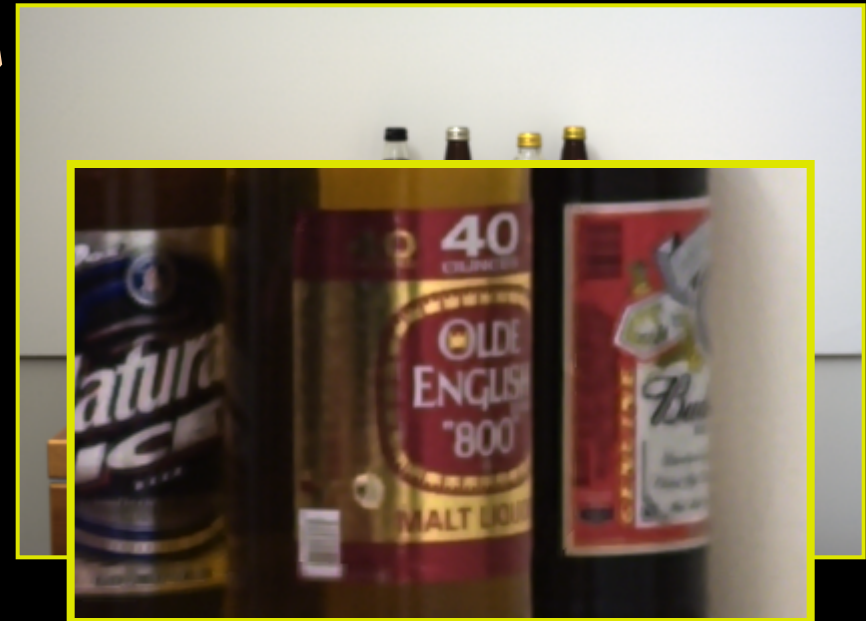
**Single input image:**



**Output #1: Depth map**



**Output #2: All-focused image**





# Lens and defocus

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Lens' aperture

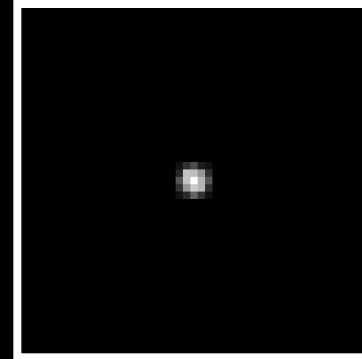
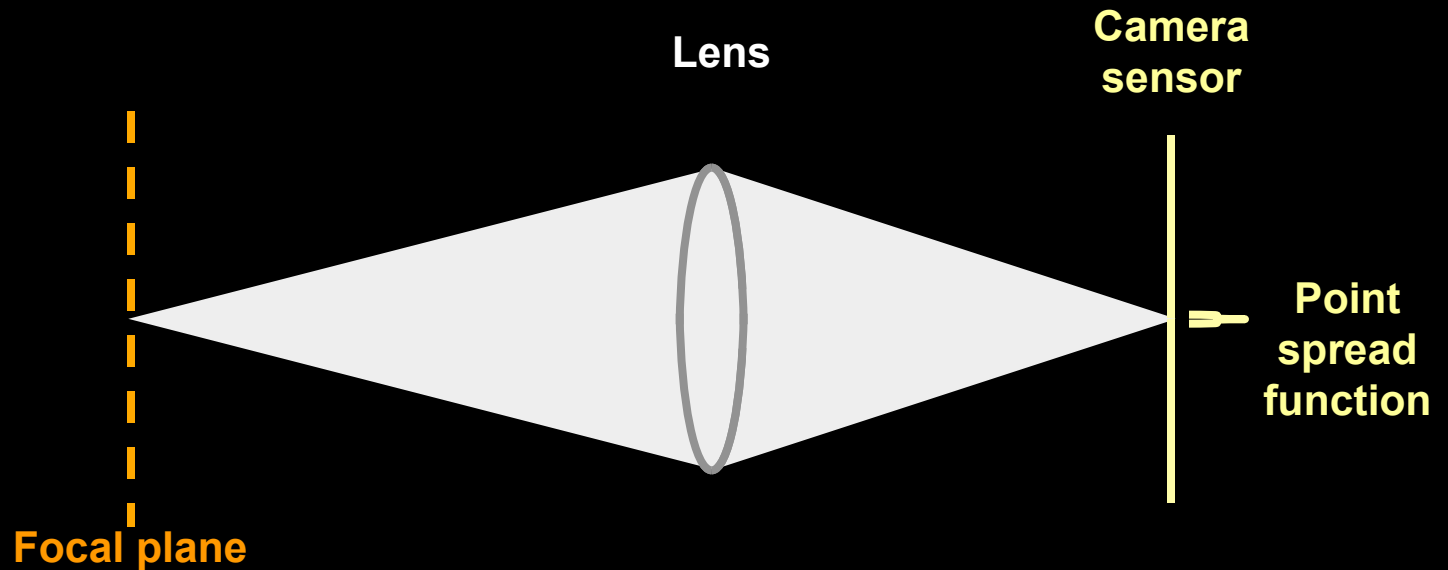


Image of a point  
light source



# Lens and defocus

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Lens' aperture

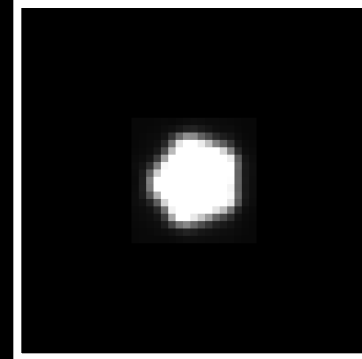
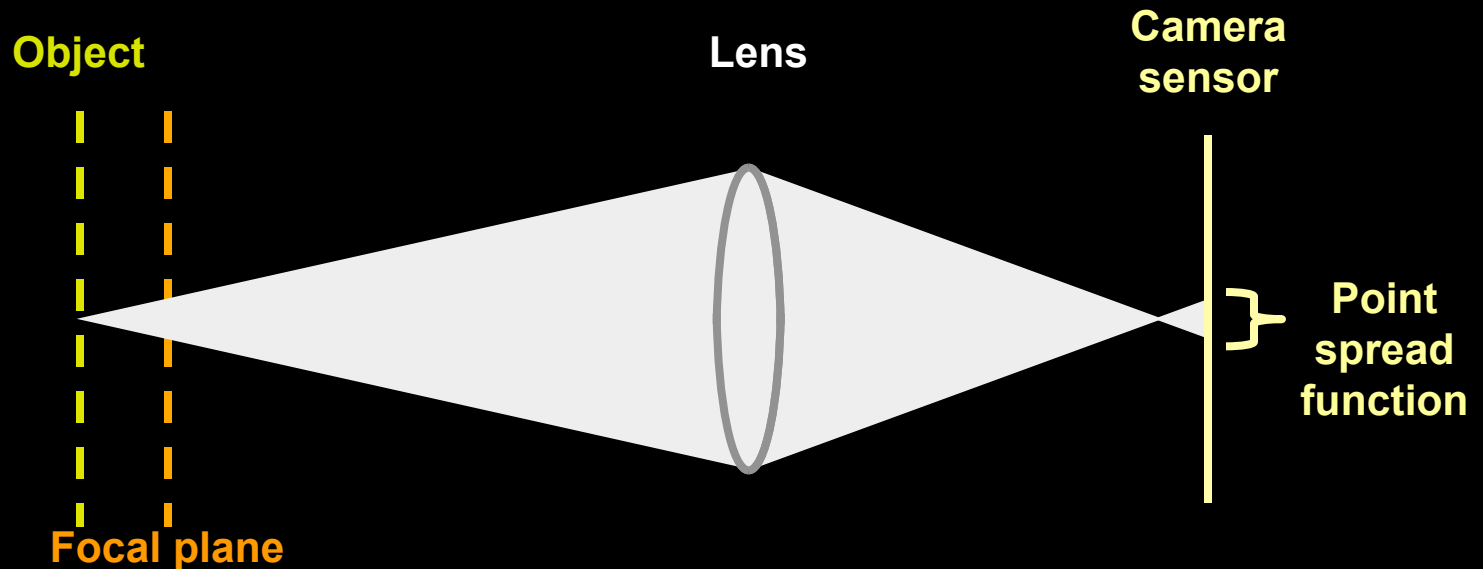


Image of a  
defocused point  
light source



# Lens and defocus

---

Lens' aperture

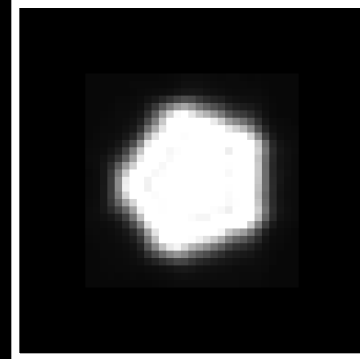
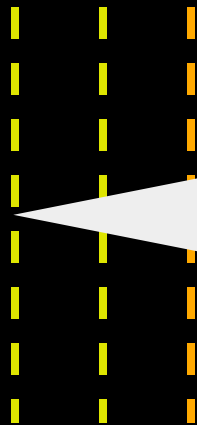


Image of a  
defocused point  
light source

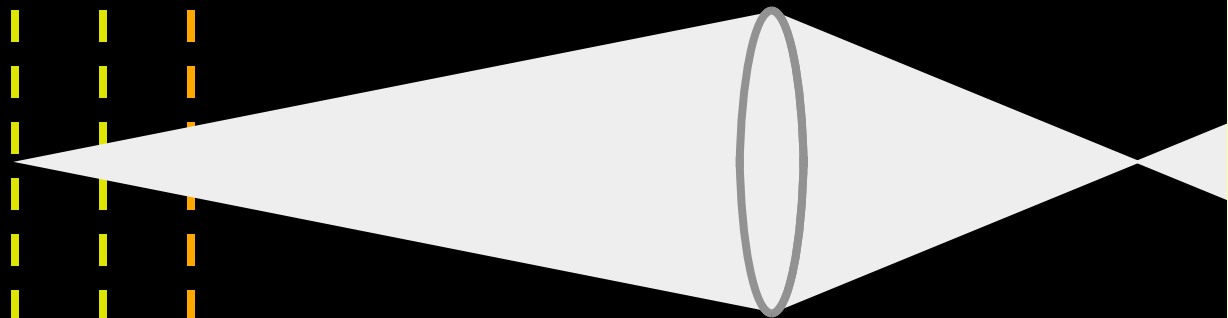
Object

Lens

Camera  
sensor



Focal plane



Point  
spread  
function

# Lens and defocus

Lens' aperture

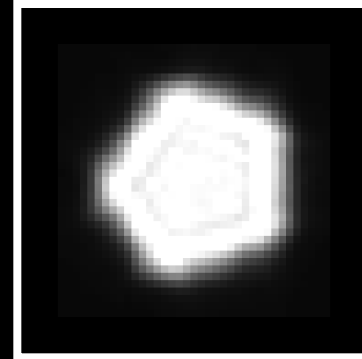
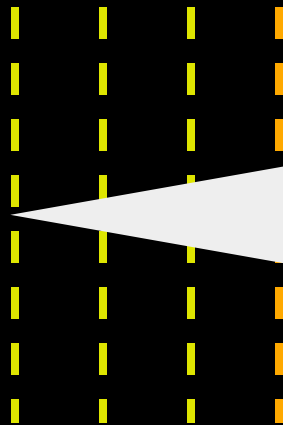


Image of a  
defocused point  
light source

Object

Lens

Camera  
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Focal plane

Point  
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function

# Lens and defocus

---

Lens' aperture

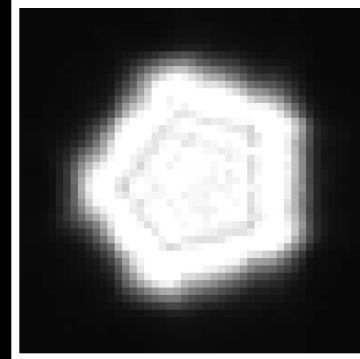
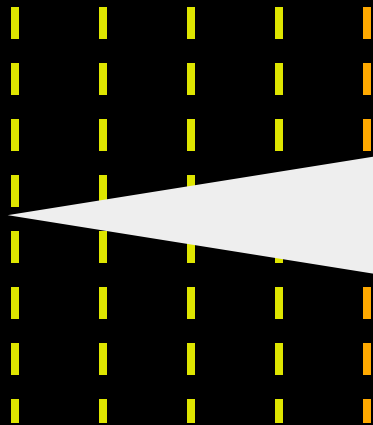


Image of a  
defocused point  
light source

Object

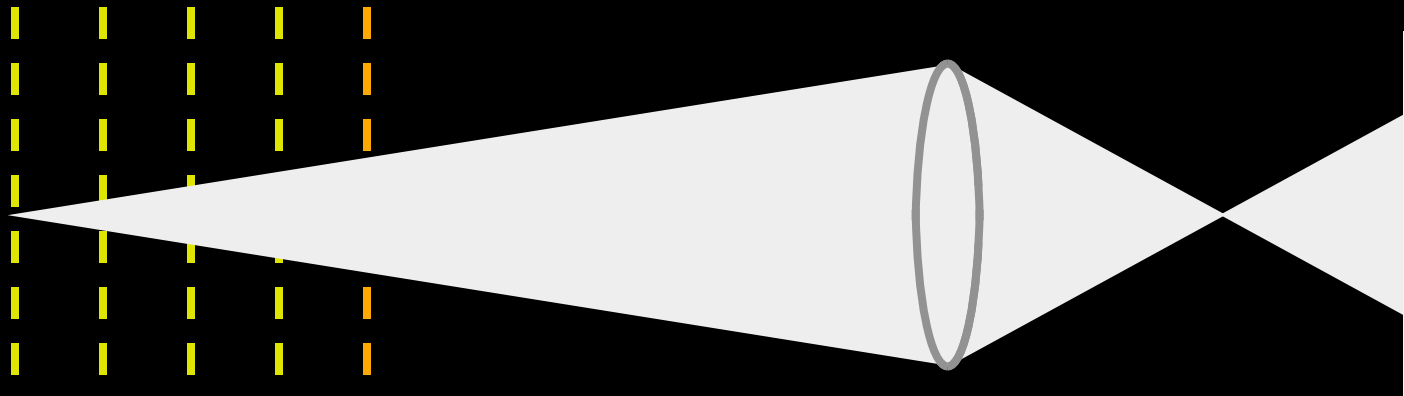
Lens

Camera  
sensor



Focal plane

Point  
spread  
function



# Depth and defocus

Out of focus



In focus



**Depth from defocus:**

Infer depth by analyzing  
local scale of defocus blur

*ill posed*

# Challenges

---

- Hard to discriminate a smooth scene from defocus blur

?

Out of focus



- Hard to undo defocus blur



Input



Ringings with conventional  
deblurring algorithm

# Key ideas

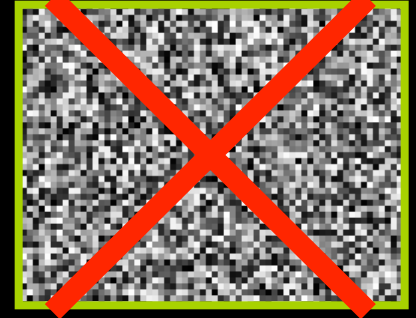
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- **Exploit prior on natural images**

- Improve deconvolution
- Improve depth discrimination



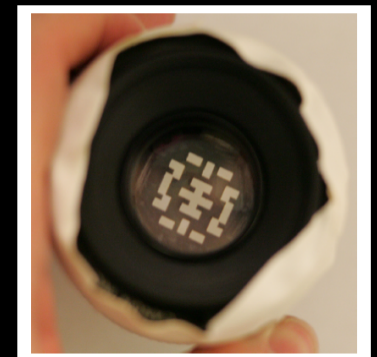
Natural



Unnatural

- **Coded aperture (mask inside lens)**

- make defocus patterns different from natural images and easier to discriminate



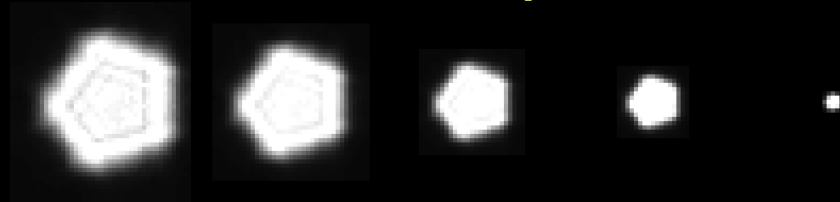


# Defocus as local convolution

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Calibrated blur kernels at different depths



# Defocus as local convolution



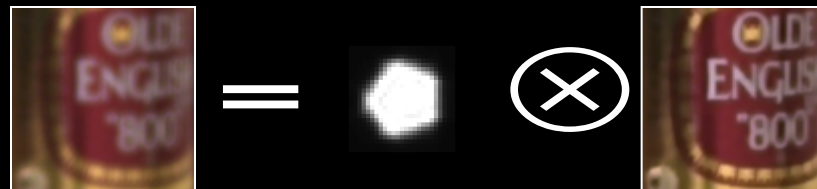
$$y = f_k \otimes x$$

Local sub-window      Calibrated blur kernels at depth  $k$       Sharp sub-window

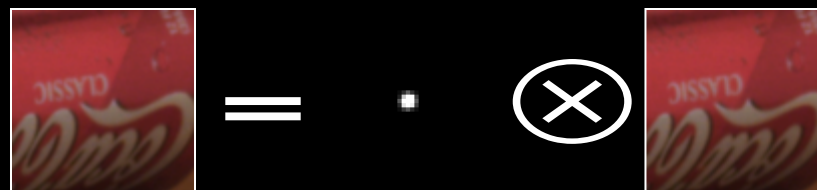
Depth  $k=1$ :



Depth  $k=2$ :

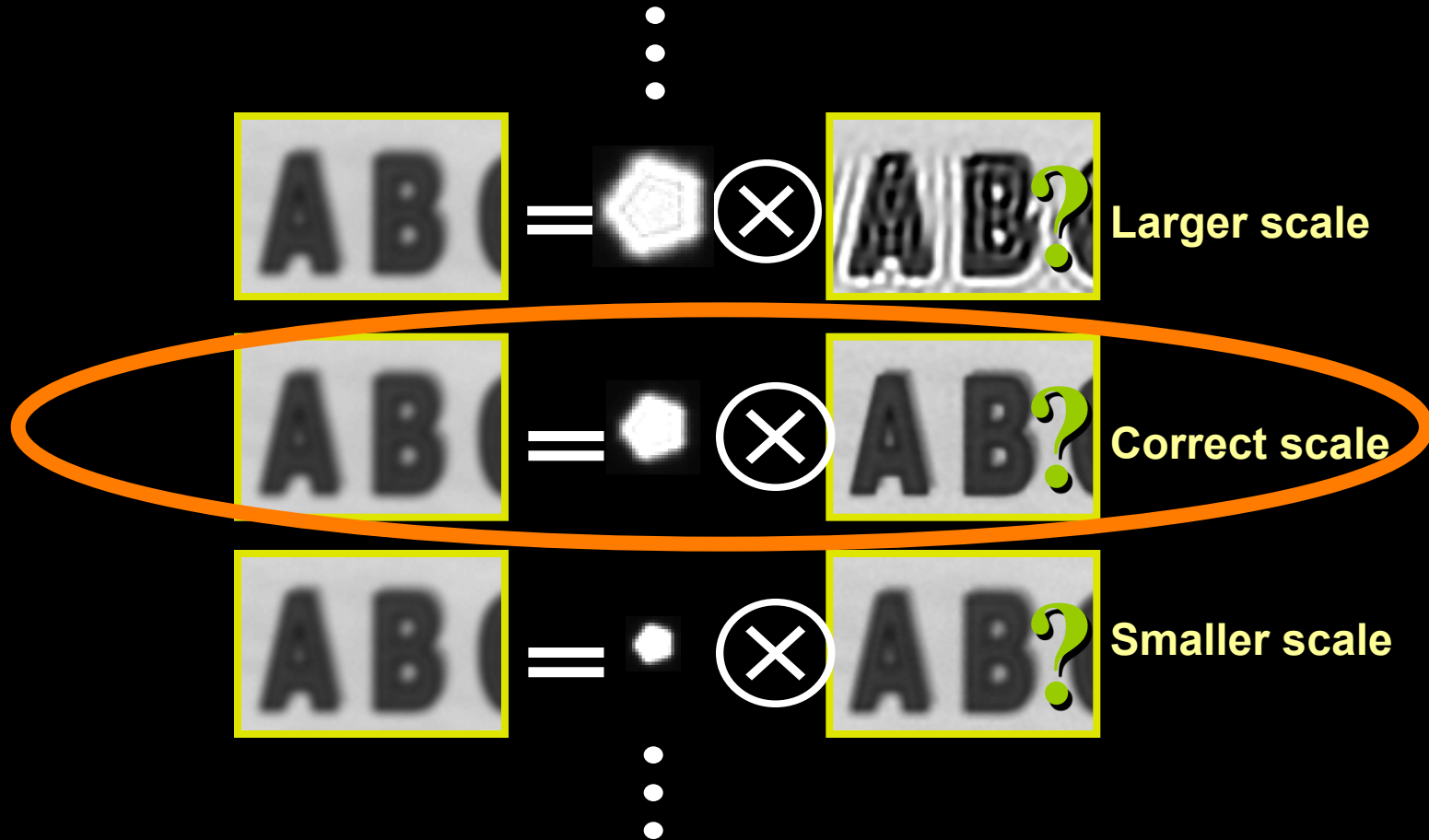


Depth  $k=3$ :



# Overview

Try deconvolving local input windows with different scaled filters:



**Somehow:** select best scale.

# Challenges

- Hard to deconvolve even when kernel is known



Input



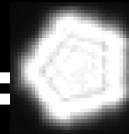
Ringing with the traditional Richardson-Lucy deconvolution algorithm

- Hard to identify correct scale:

?



=

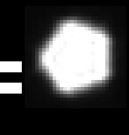


Larger scale

?



=

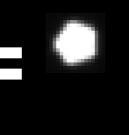


Correct scale

?



=

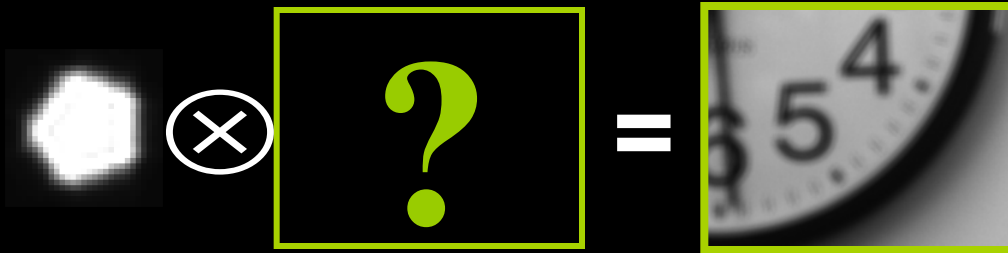


Smaller scale

# Deconvolution is ill posed

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$$f \otimes x = y$$

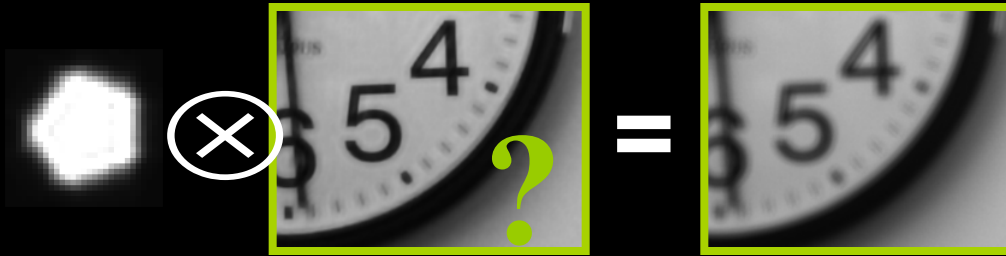


# Deconvolution is ill posed

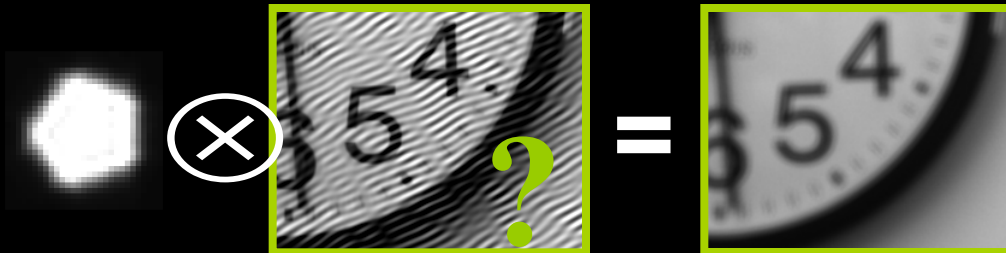
---

$$f \otimes x = y$$

**Solution 1:**



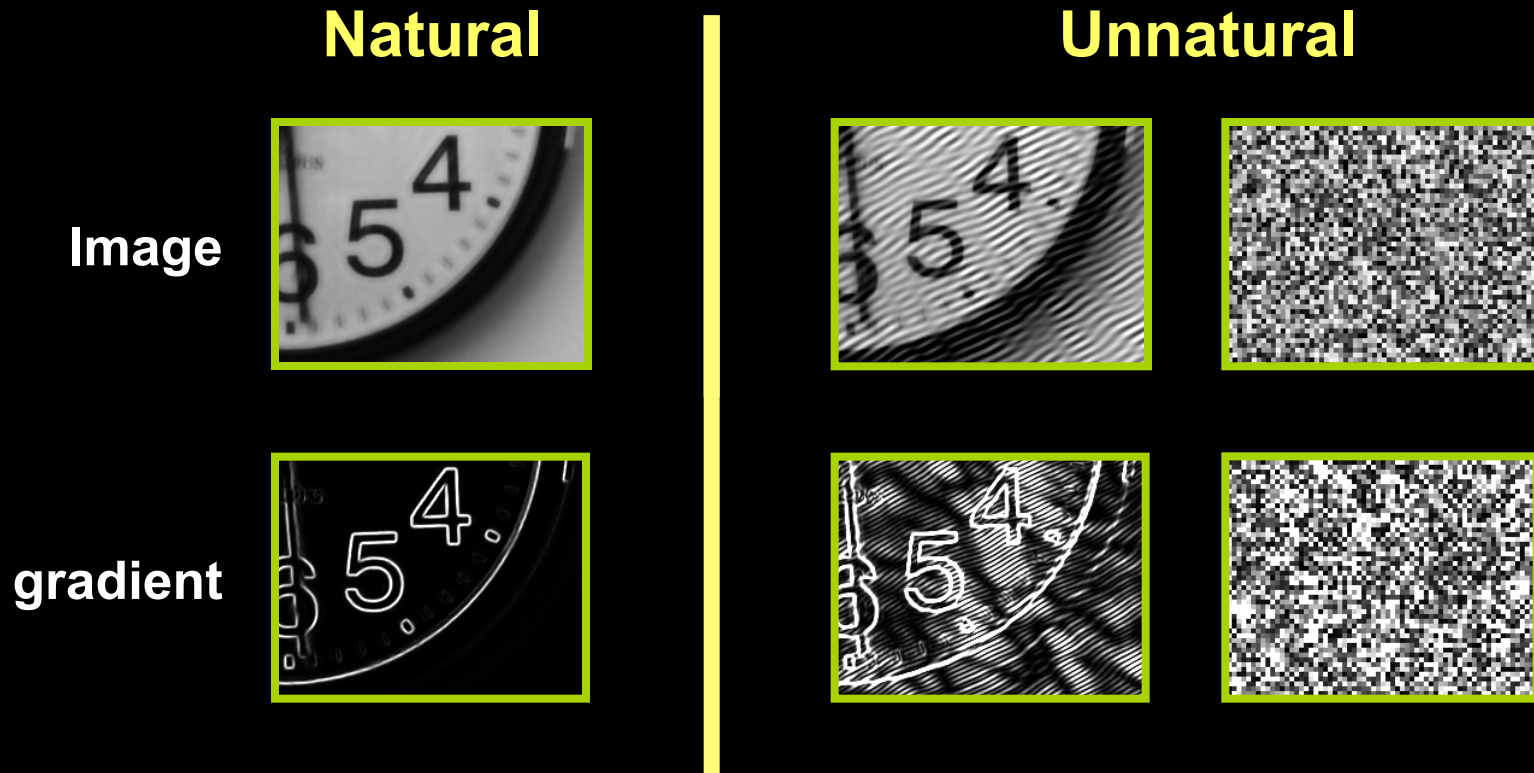
**Solution 2:**



# Idea 1: Natural images prior

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## What makes images special?



Natural images have sparse gradients

➡ put a penalty on gradients

# Deconvolution with prior

$$x = \arg \min \underbrace{\left| f \otimes x - y \right|^2}_{\text{Convolution error}} + \lambda \underbrace{\sum_i \rho(\nabla x_i)}_{\text{Derivatives prior}}$$

$$\left| \begin{array}{c} \text{Kernel} \otimes \text{Input} \end{array} - \text{Target} \right|^2 + \text{Derivatives prior}$$

Equal convolution error

Low

$$\left| \begin{array}{c} \text{Kernel} \otimes \text{Input} \end{array} - \text{Target} \right|^2 + \text{Derivatives prior}$$

High



# Comparing deconvolution algorithms

---



Input

(Non blind) deconvolution code available online: <http://groups.csail.mit.edu/graphics/CodedAperture/>

$$\rho(\nabla x) = \|\nabla x\|^2$$

“spread” gradients

$$\rho(\nabla x) = \|\nabla x\|^{0.8}$$

“localizes” gradients



Richardson-Lucy



Gaussian prior



Sparse prior

# Comparing deconvolution algorithms

---



Input

(Non blind) deconvolution code available online: <http://groups.csail.mit.edu/graphics/CodedAperture/>

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Richardson-Lucy



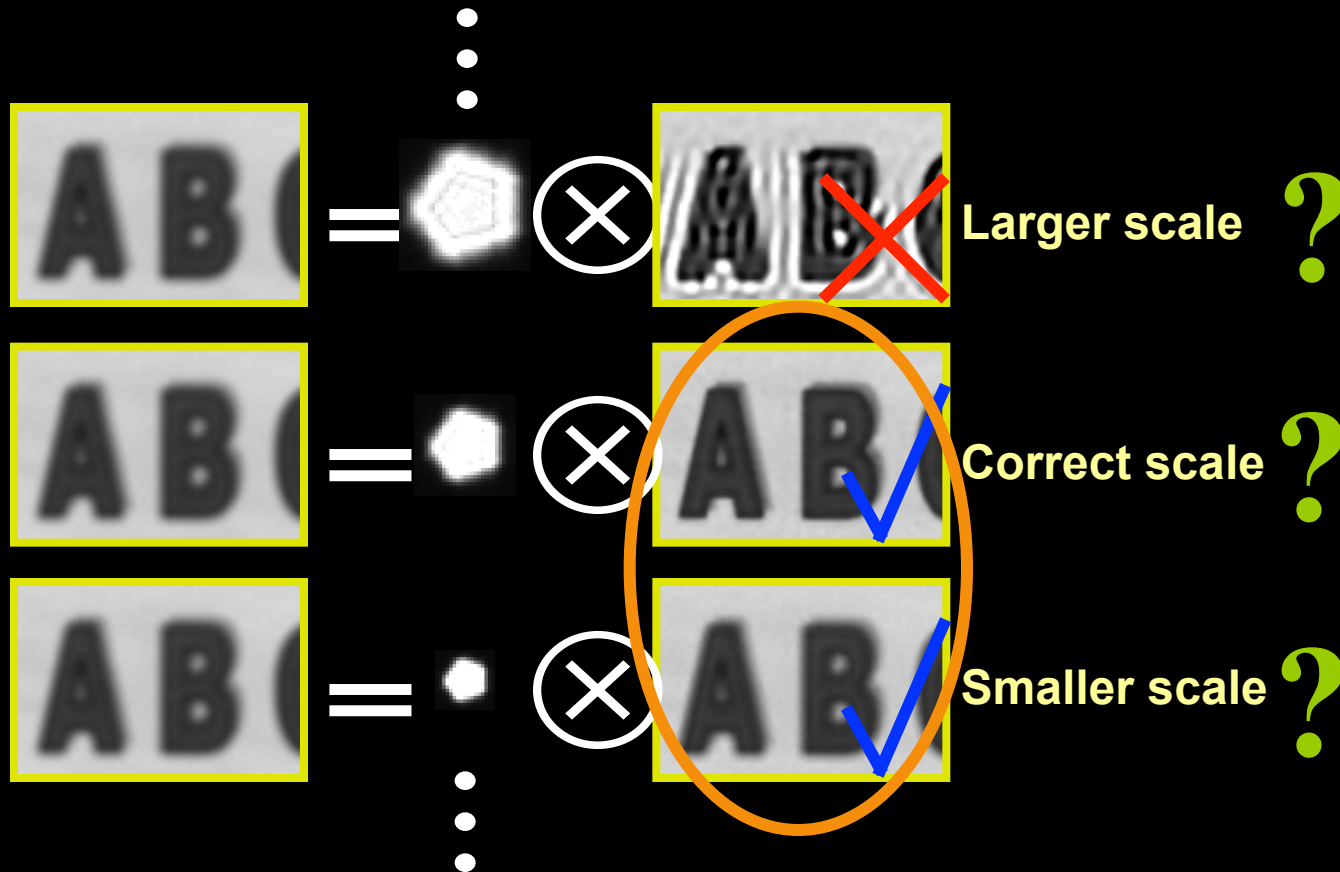
Gaussian prior



Sparse prior

# Recall: Overview

Try deconvolving local input windows with different scaled filters:



Somehow: select best scale.

Challenge: smaller scale not so different than correct

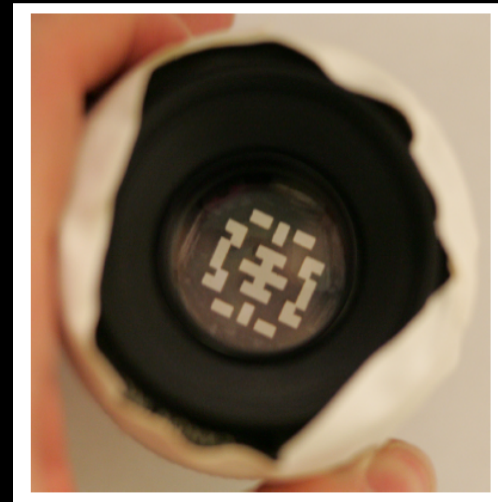
# Idea 2: Coded Aperture

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- Mask (code) in aperture plane
  - make defocus patterns different from natural images and easier to discriminate



**Conventional  
aperture**

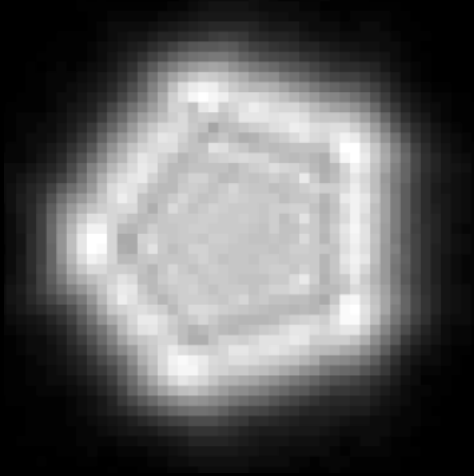


**Our coded  
aperture**

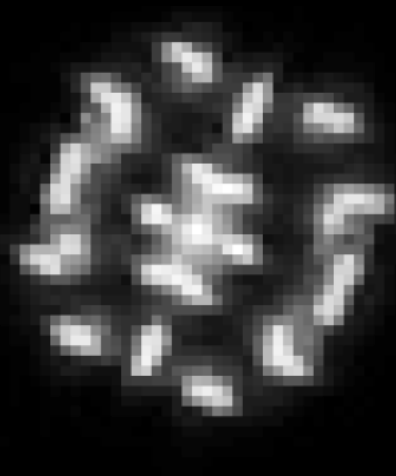
# Idea 2: Coded Aperture

---

- **Mask (code) in aperture plane**
  - make defocus patterns different from natural images and easier to discriminate



**Conventional  
aperture**

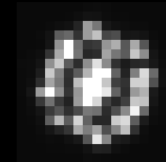
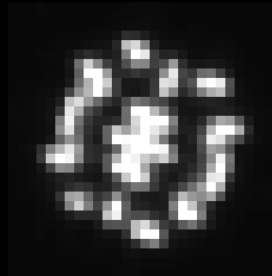
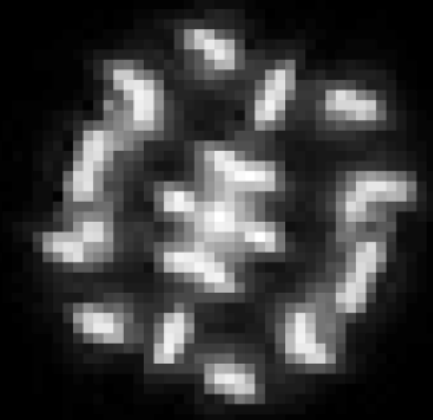


**Coded  
aperture**

# Idea 2: Coded Aperture

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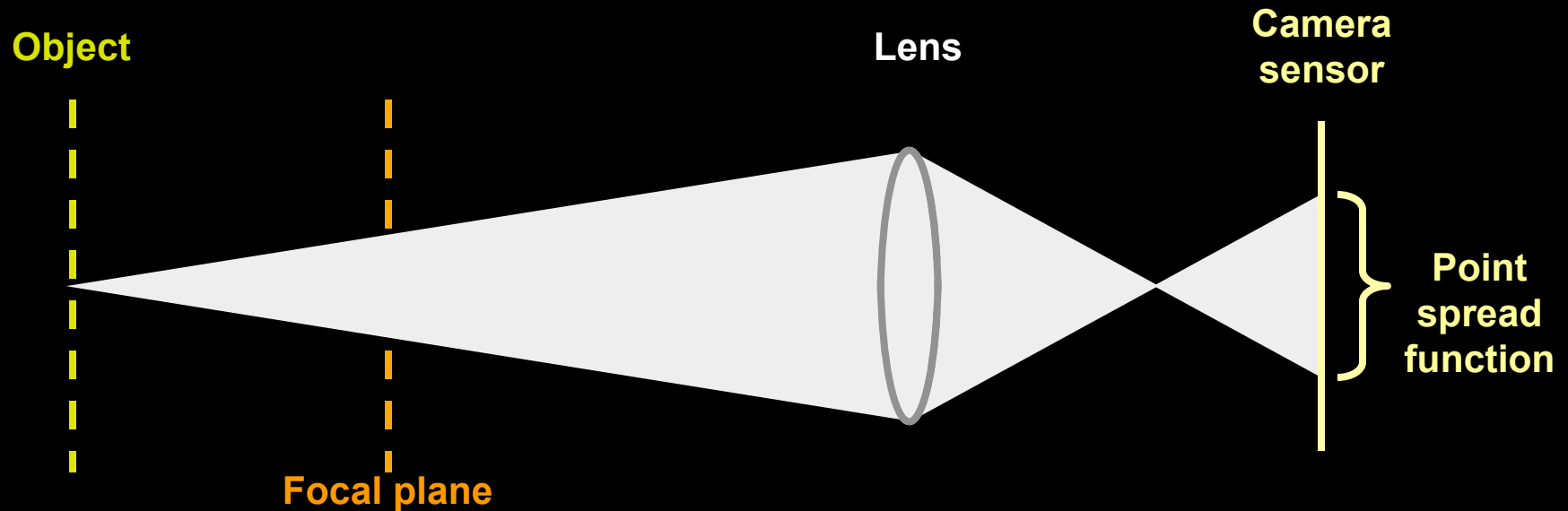
- Mask (code) in aperture plane
  - make defocus patterns different from natural images and easier to discriminate



**Coded  
aperture**

# Solution: lens with occluder

---



# Solution: lens with occluder

---

Aperture pattern

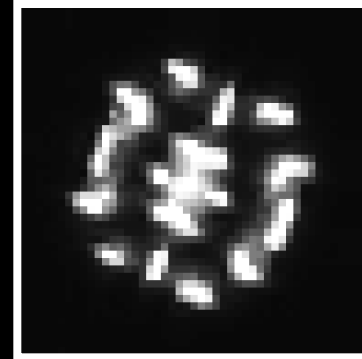
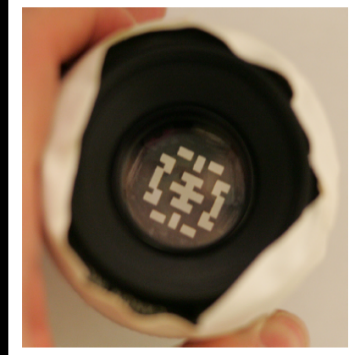


Image of a  
defocused point  
light source

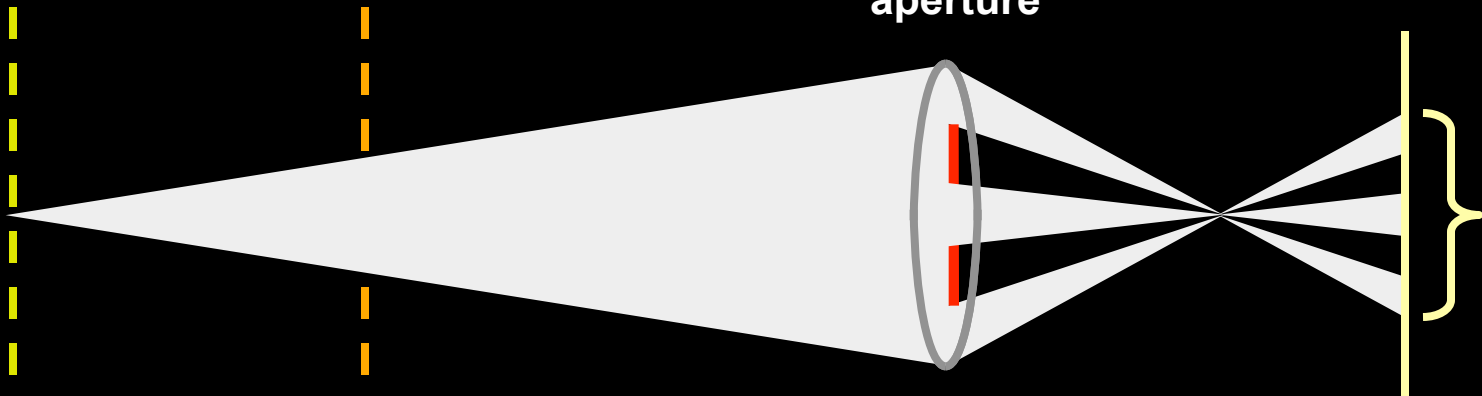
Object

Lens with coded  
aperture

Camera  
sensor

Focal plane

Point  
spread  
function





# Solution: lens with occluder

Aperture pattern

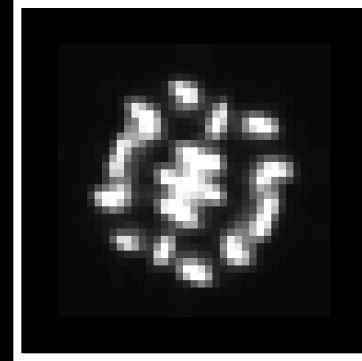
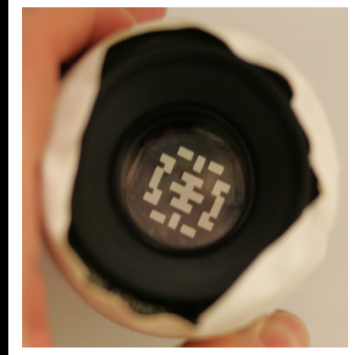
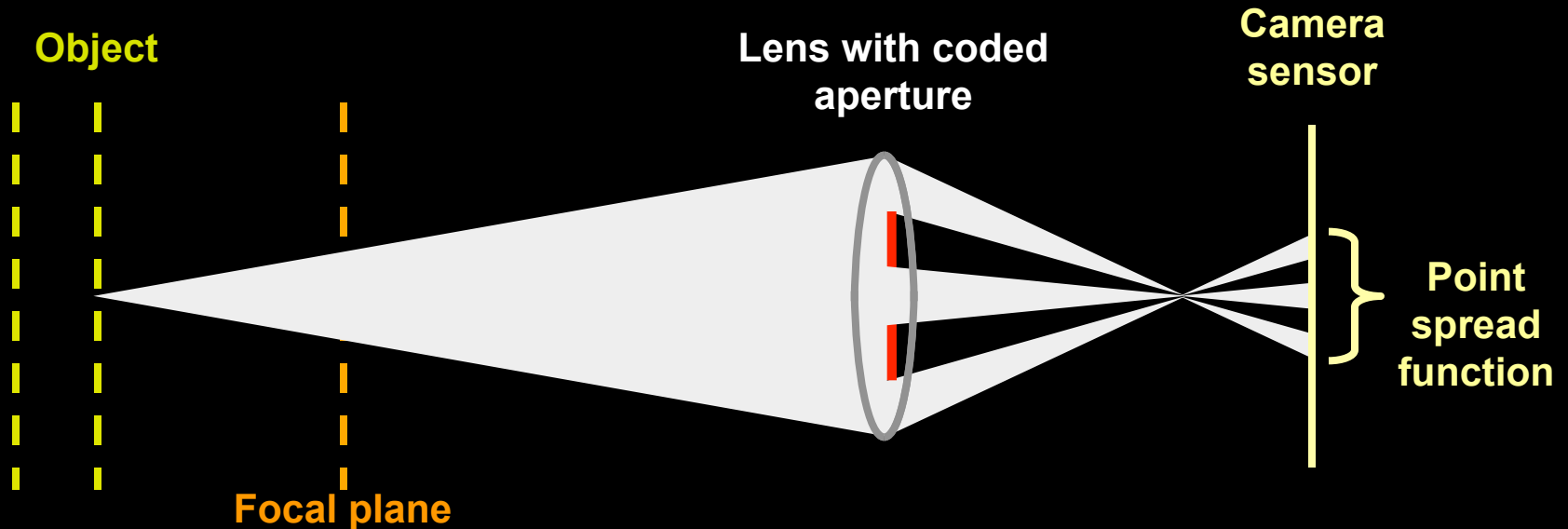


Image of a  
defocused point  
light source



# Solution: lens with occluder

---

Aperture pattern

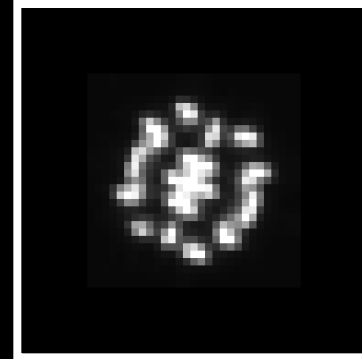
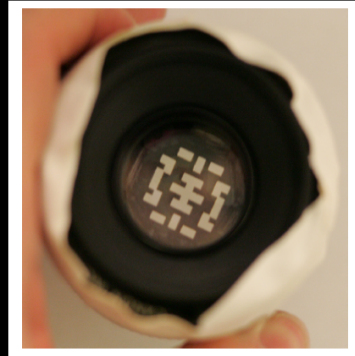
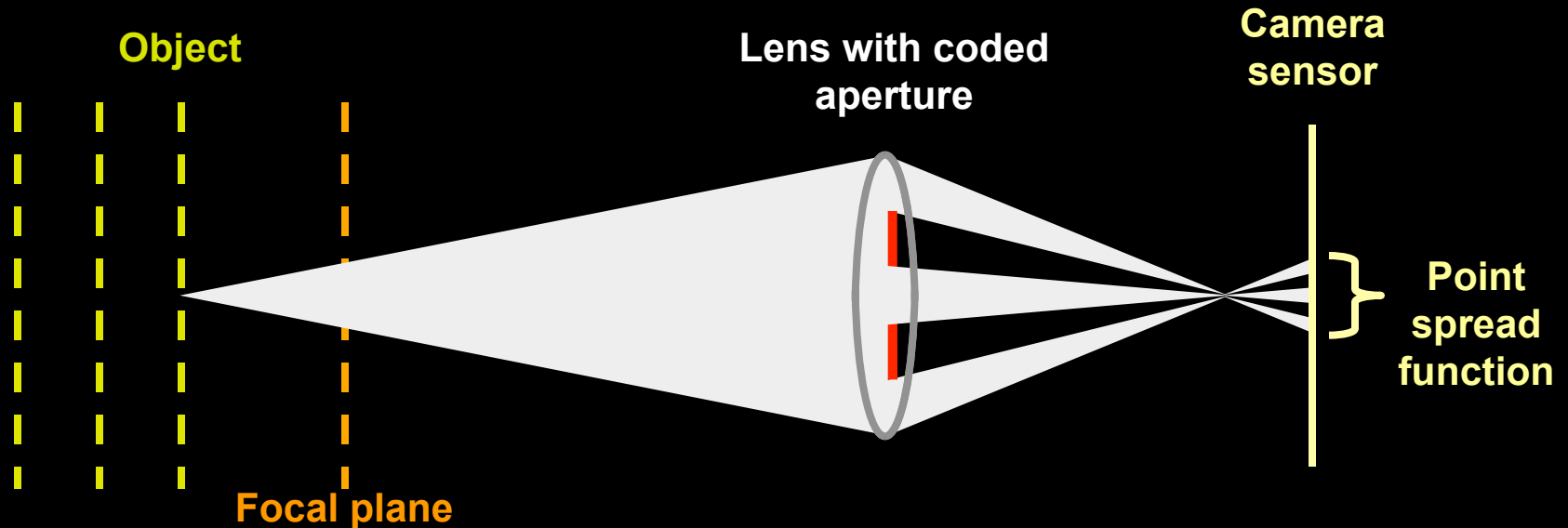


Image of a  
defocused point  
light source



# Solution: lens with occluder

---

Aperture pattern

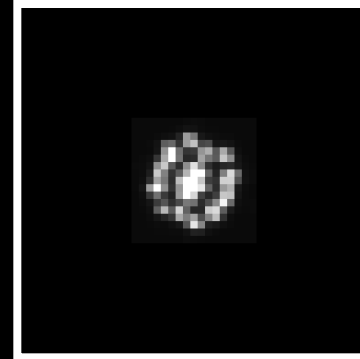
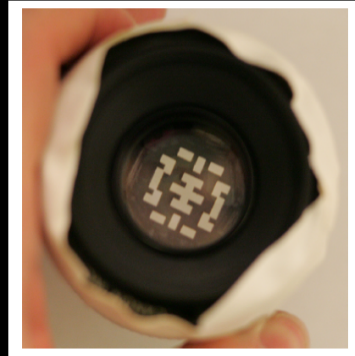
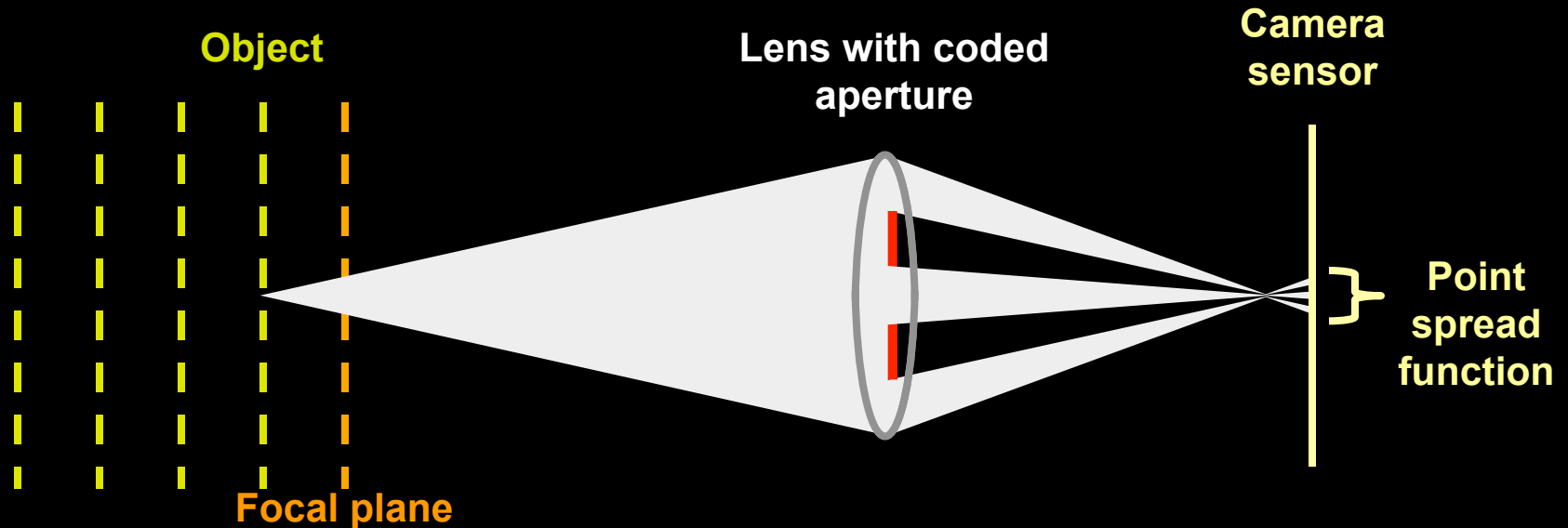


Image of a  
defocused point  
light source



# Solution: lens with occluder

Aperture pattern

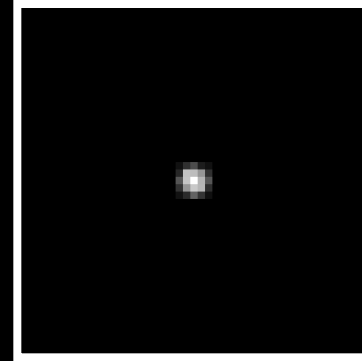
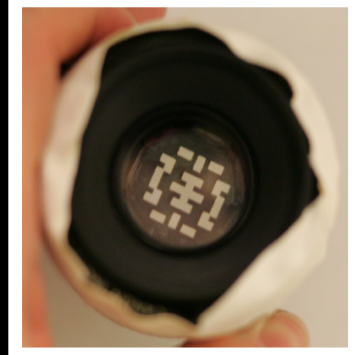
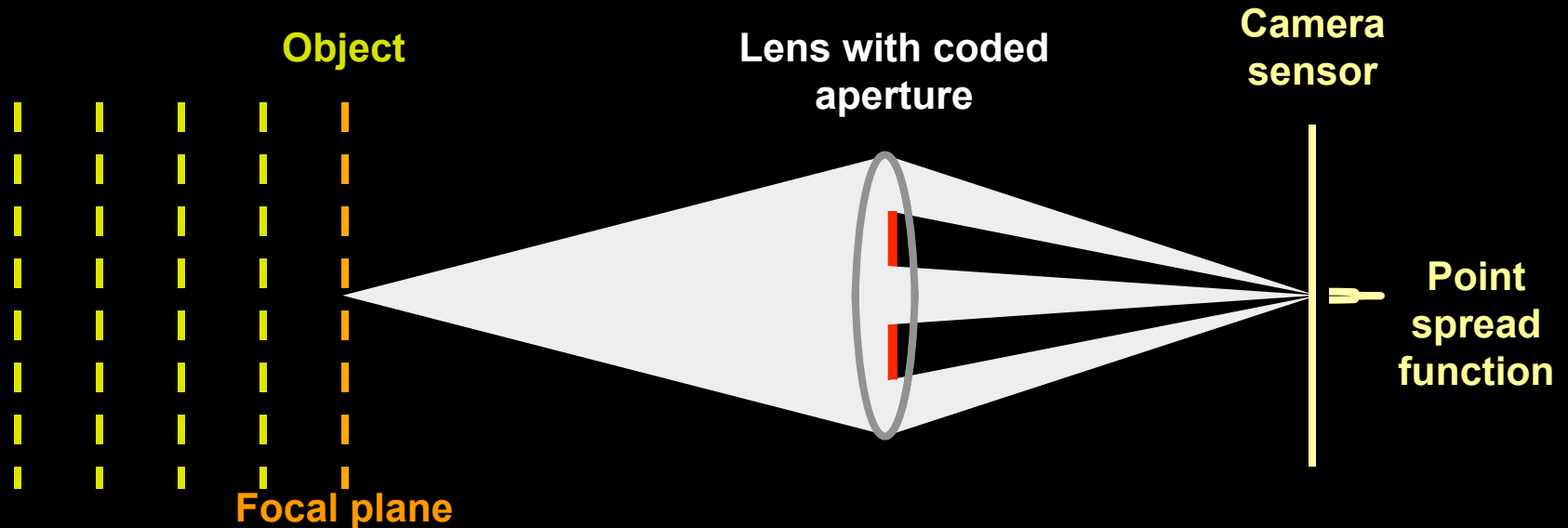


Image of a  
defocused point  
light source



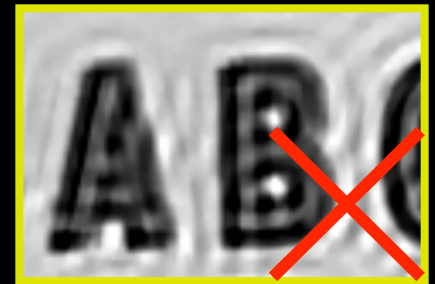
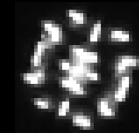
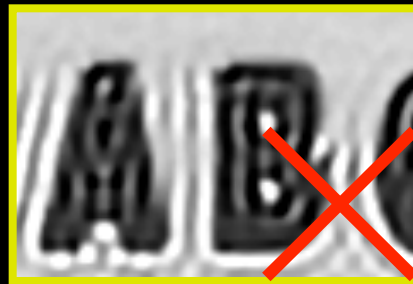
# Coded aperture reduces uncertainty in scale identification

---

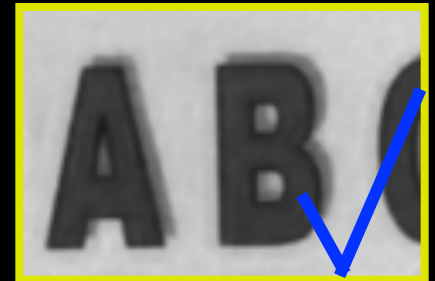
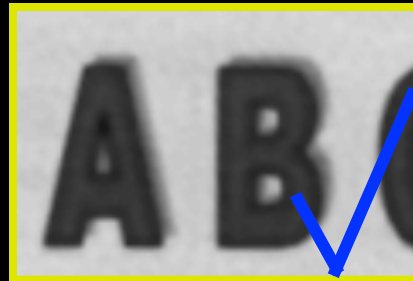
Conventional

Coded

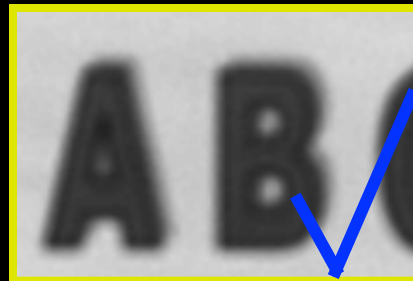
Larger scale



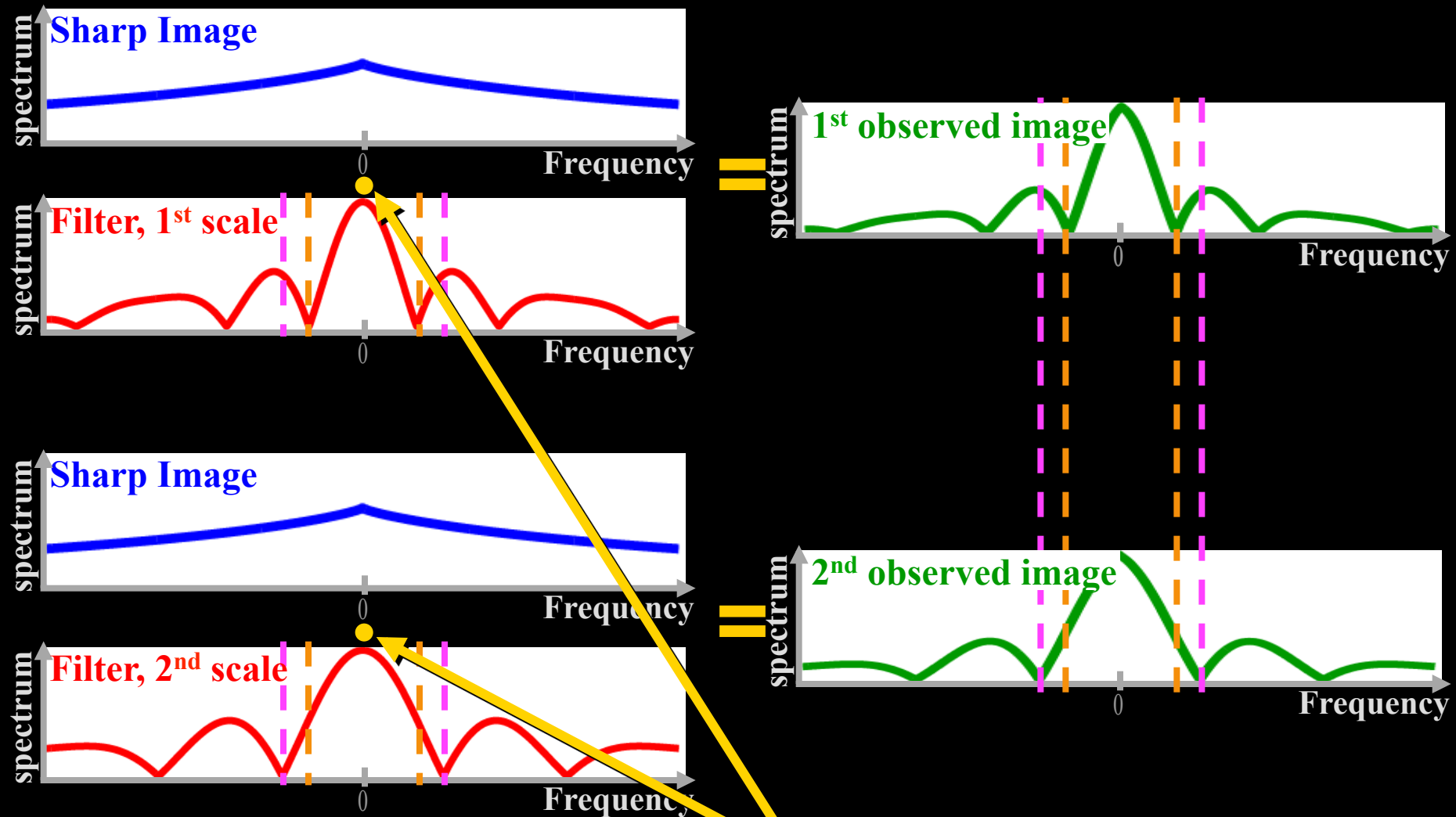
Correct scale



Smaller scale

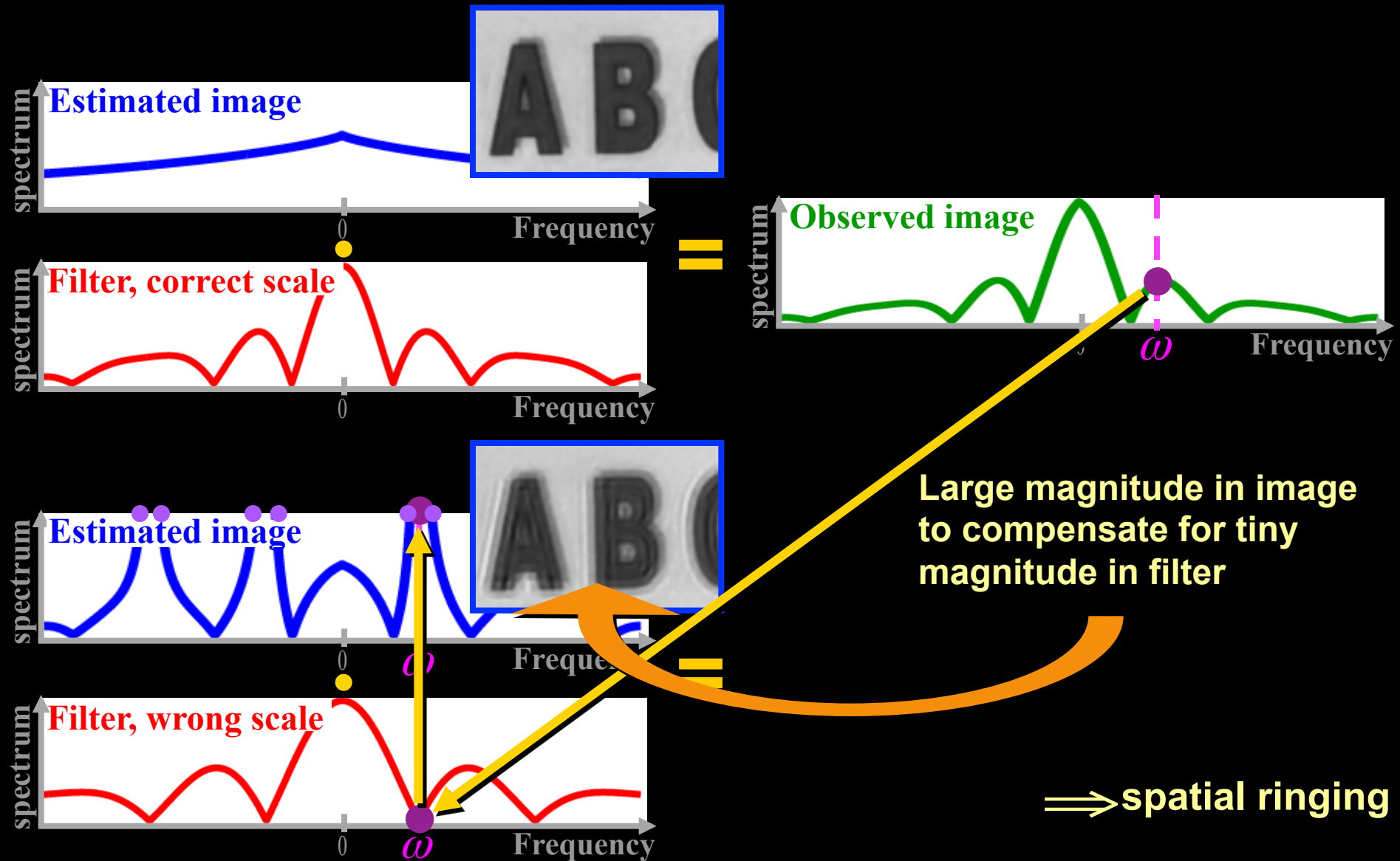


# Convolution- frequency domain representation

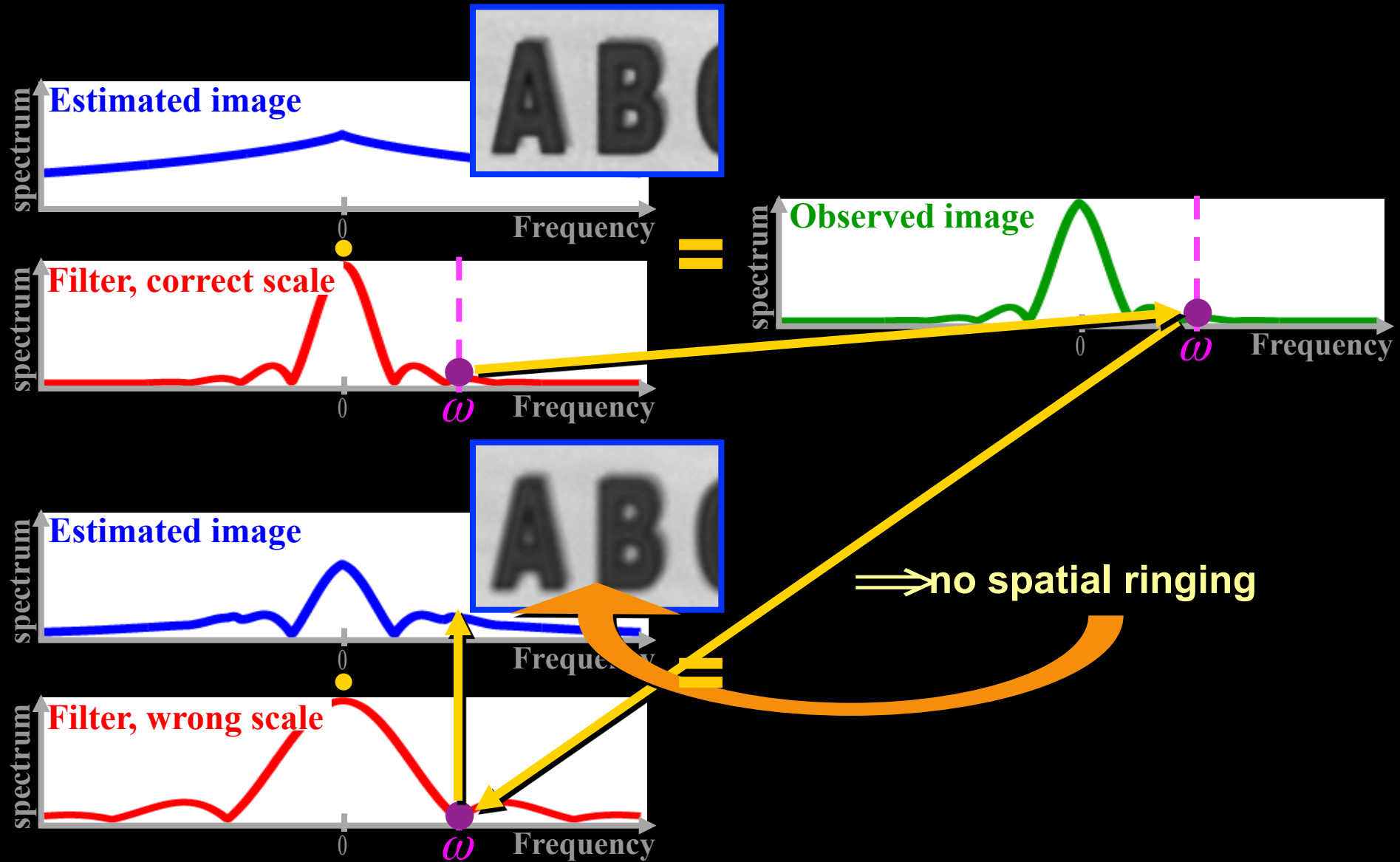


Output spectrum has zeros  
where filter spectrum has zeros

Spatial convolution  $\iff$  frequency multiplication



# Division by zero with a conventional aperture?

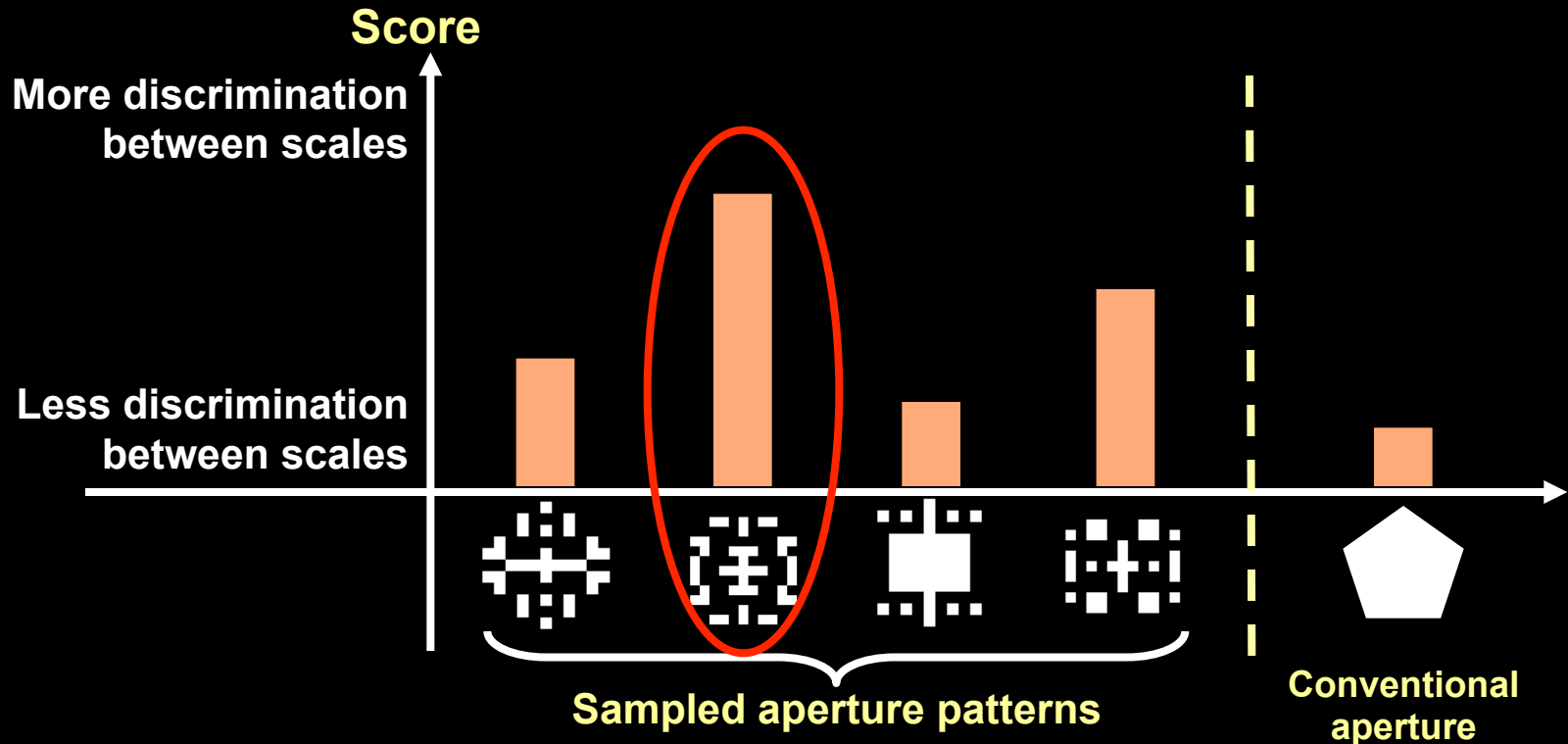




# Filter Design

Analytically search for a pattern maximizing discrimination between images at different defocus scales (*KL-divergence*)

Account for image prior and physical constraints



# Depth results

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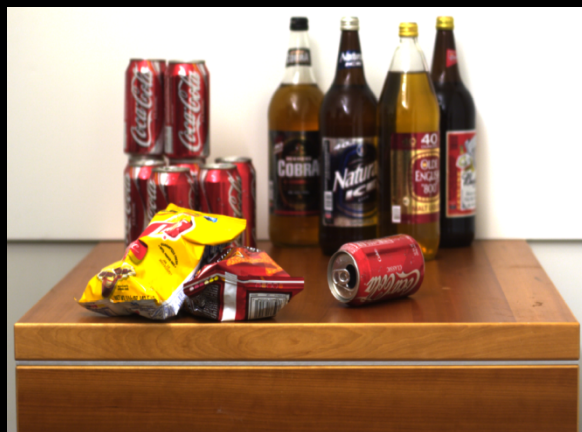
# Regularizing depth estimation

## Try deblurring with 10 different aperture scales

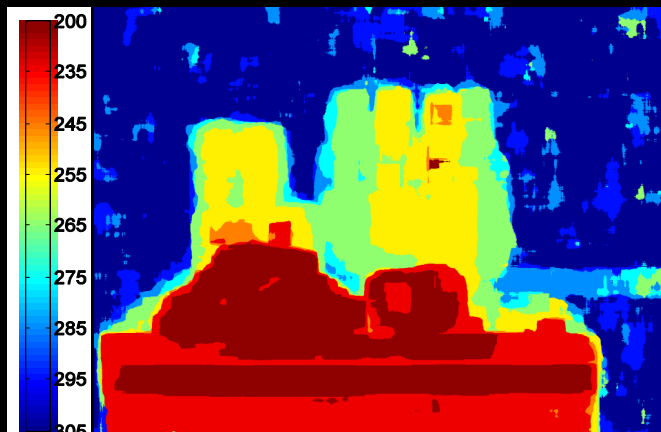
$$x = \arg \min \underbrace{|f \otimes x - y|^2}_{\text{Convolution error}} + \underbrace{\lambda \sum_i \rho(\nabla x_i)}_{\text{Derivatives prior}}$$

The diagram shows a sequence of operations: a small image of a clock face is multiplied (indicated by a circled 'X') by a larger image of the same clock face. This result is then subtracted (indicated by a minus sign) from the original larger clock face image. The difference is then squared (indicated by a superscript '2') and added (indicated by a plus sign) to the original larger clock face image, resulting in a final image where the clock face is highlighted with a green border.

## Keep minimal error scale in each local window + regularization



## Input



## Local depth estimation



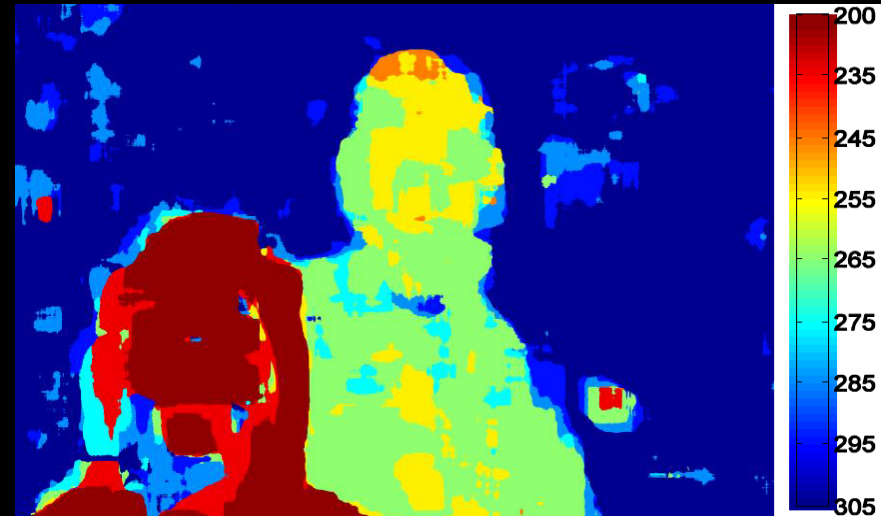
## Regularized depth

# Regularizing depth estimation

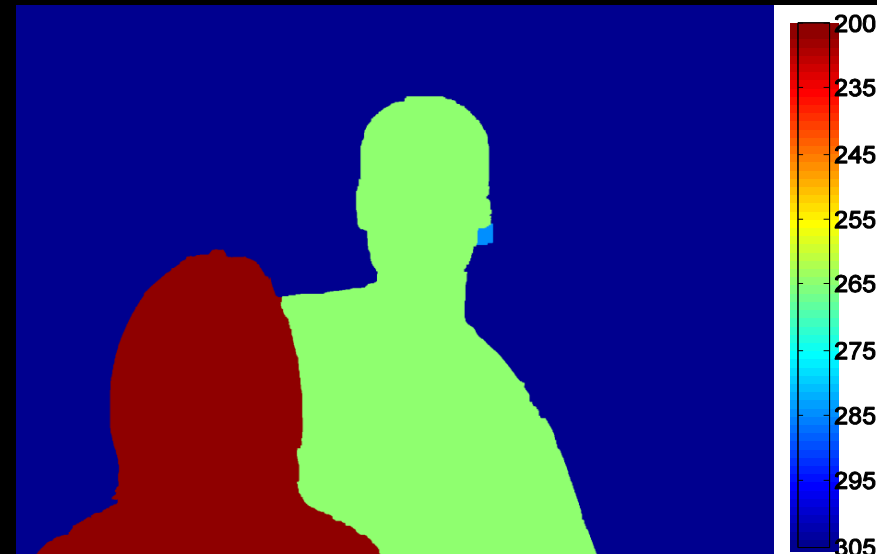
---



Input



Local depth estimation



Regularized depth

**All focused results**

---



# Input





# All-focused (deconvolved)



# Close-up

---

Original image

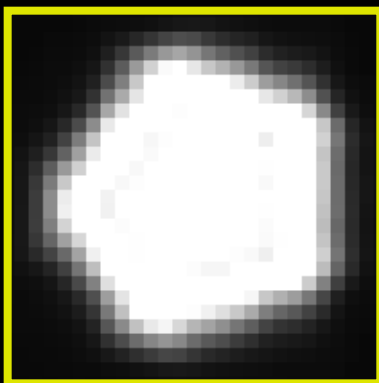


All-focus image





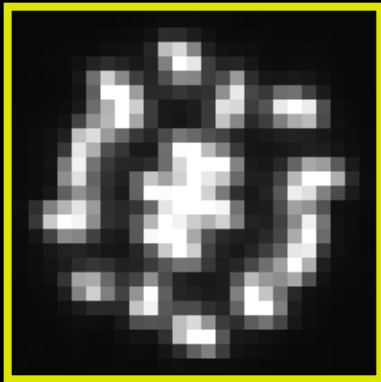
# Comparison- conventional aperture result



Ringing due to wrong scale estimation

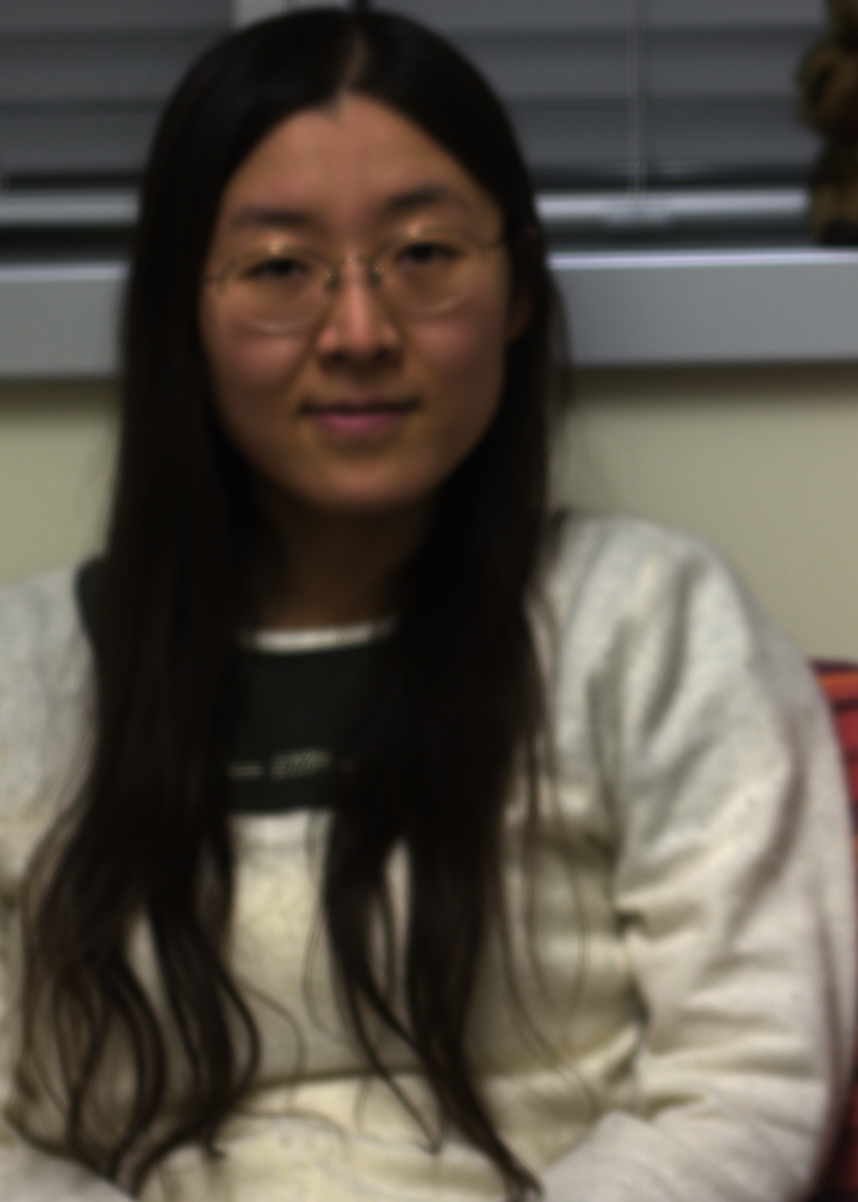


# Comparison- coded aperture result





Input





**All-focused  
(deconvolved)**



# Close-up

---



Original image



All-focus image



Naïve sharpening



# Application: Digital refocusing from a single image

---



# Application: Digital refocusing from a single image

---





# Application: Digital refocusing from a single image

---





# Application: Digital refocusing from a single image

---



# Application: Digital refocusing from a single image

---



# Application: Digital refocusing from a single image

---





# Application: Digital refocusing from a single image

---



# Coded aperture: pros and cons

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- + Image AND depth at a single shot
- + No loss of image resolution
- + Simple modification to lens
- Depth is coarse
  - unable to get depth at untextured areas, might need manual corrections.
- + But depth is a pure bonus
- Lose some light
- + But deconvolution increases depth of field





**50mm f/1.8: \$79.95**

**Cardboard: \$1**

**Tape: \$1**

**Depth acquisition: priceless**

***CodedAperture***

# Some more quick examples



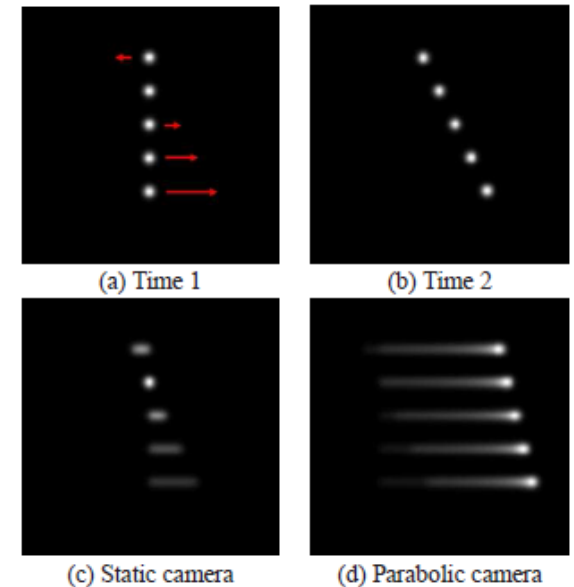
# Motion-Invariant Photography

Anat Levin   Peter Sand   Taeg Sang Cho   Frédo Durand   William T. Freeman

Massachusetts Institute of Technology, Computer Science and Artificial Intelligence Laboratory



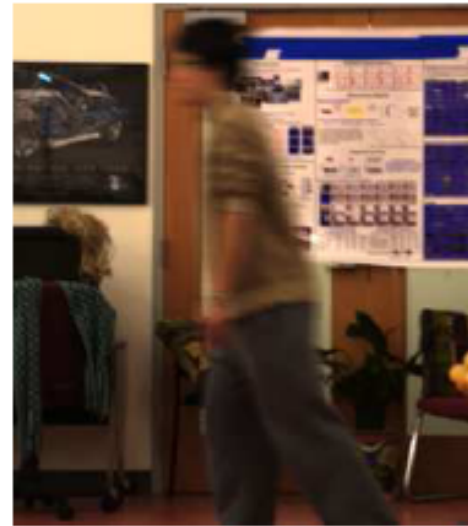
- Quickly move camera in a parabola when taking a picture
- A motion at any speed in the direction of the parabola will give the same blur kernel





# Results

Static  
Camera



Parabolic  
Camera



# Results

Static Camera



Parabolic Camera



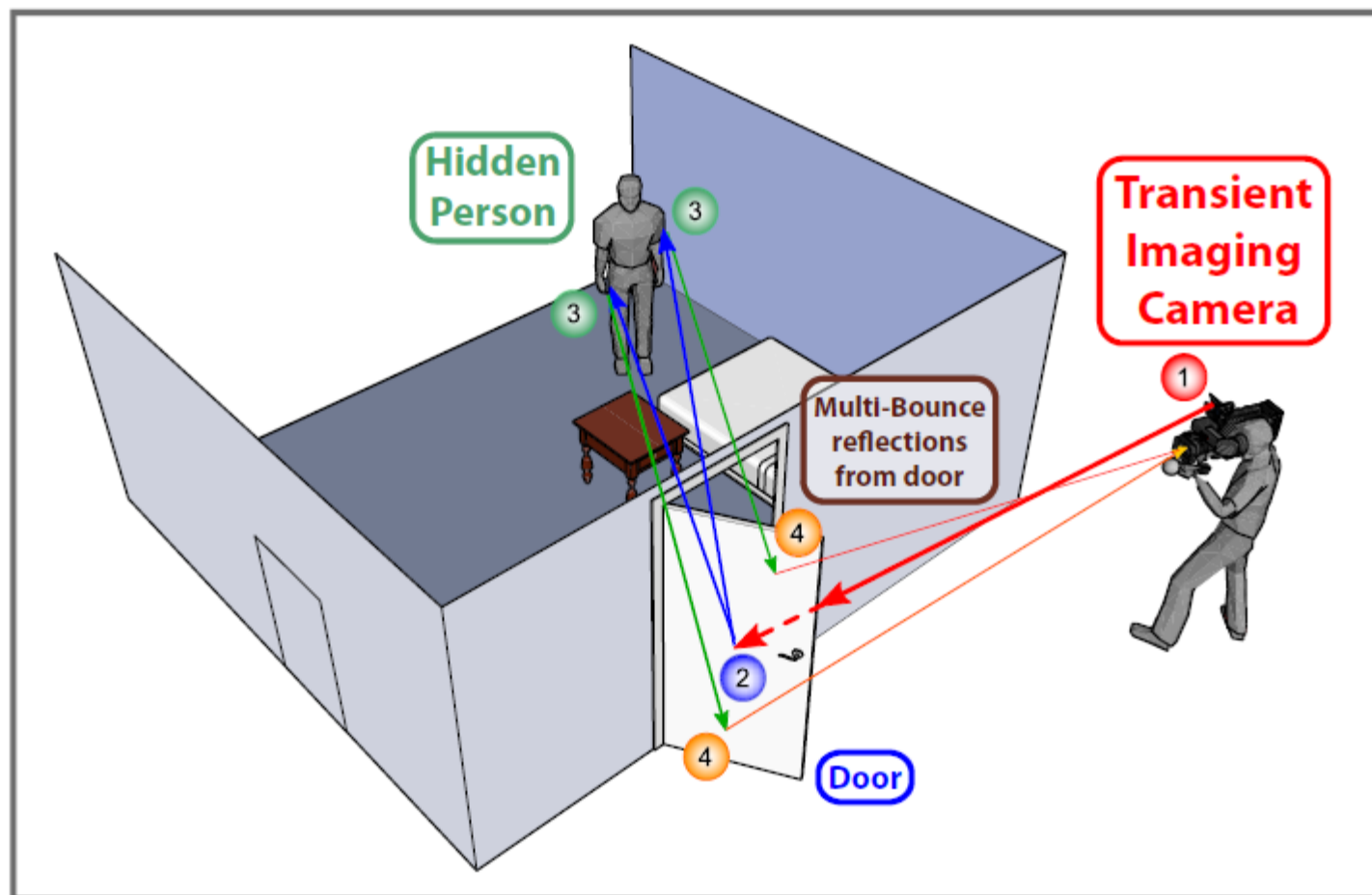
Motion in  
wrong  
direction

# Looking Around the Corner using Transient Imaging

Ahmed Kirmani <sup>\*1</sup>, Tyler Hutchison<sup>1</sup>, James Davis <sup>†2</sup>, and Ramesh Raskar<sup>‡1</sup>

<sup>1</sup>MIT Media Laboratory

<sup>2</sup> UC Santa Cruz



# Recap of questions

- How can we represent all of the information contained in light?
- What are the fundamental limitations of cameras?
- What sacrifices have we made in conventional cameras? For what benefits?
- How else can we design cameras for better focus, deblurring, multiple views, depth, etc.?

# Next class

- Exam review

