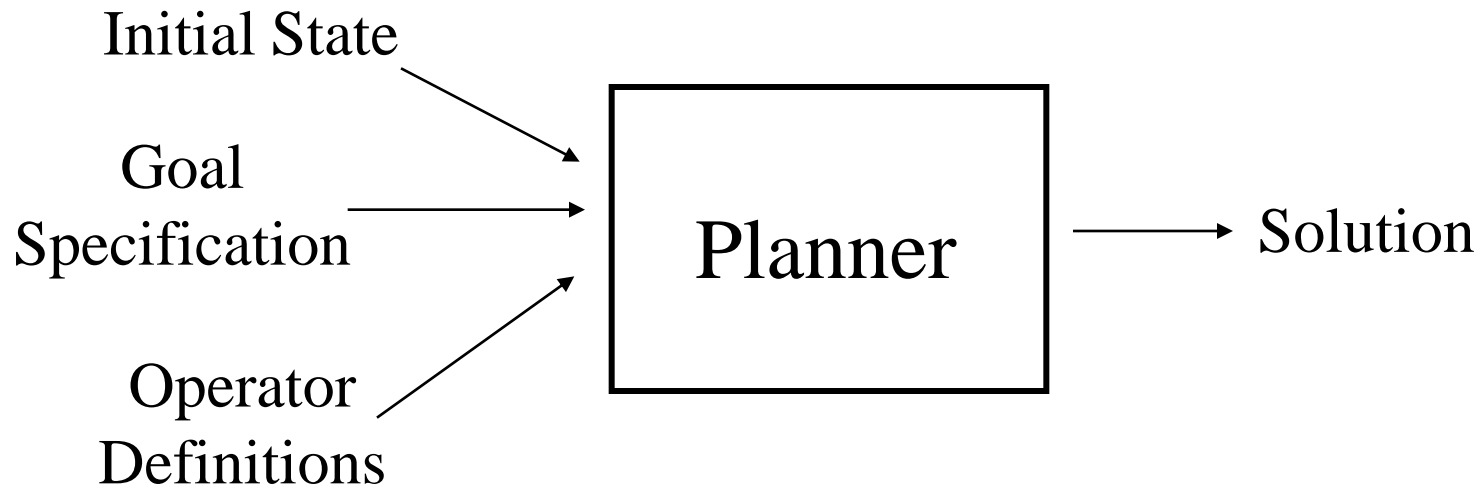


- Homework 2A due Thursday
- Planning: Today & part? of Thursday
- Next Reinforcement Learning
- Begins statistical AI
- Start reading Ch 17 & 21

# Classical Planning

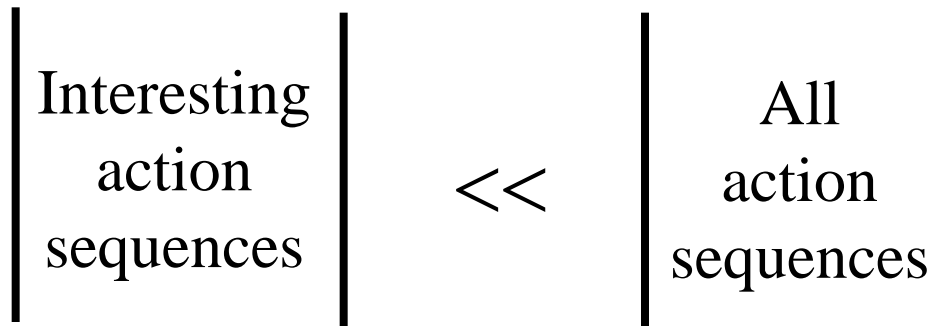
Using inference to find a sequence of operator instances (actions) that transform an initial state into a state in which the goal is satisfied.



Real World Applications:

Scheduling, Logistics, Semantic web support,  
Computer gaming, ...

# Planning vs. Search

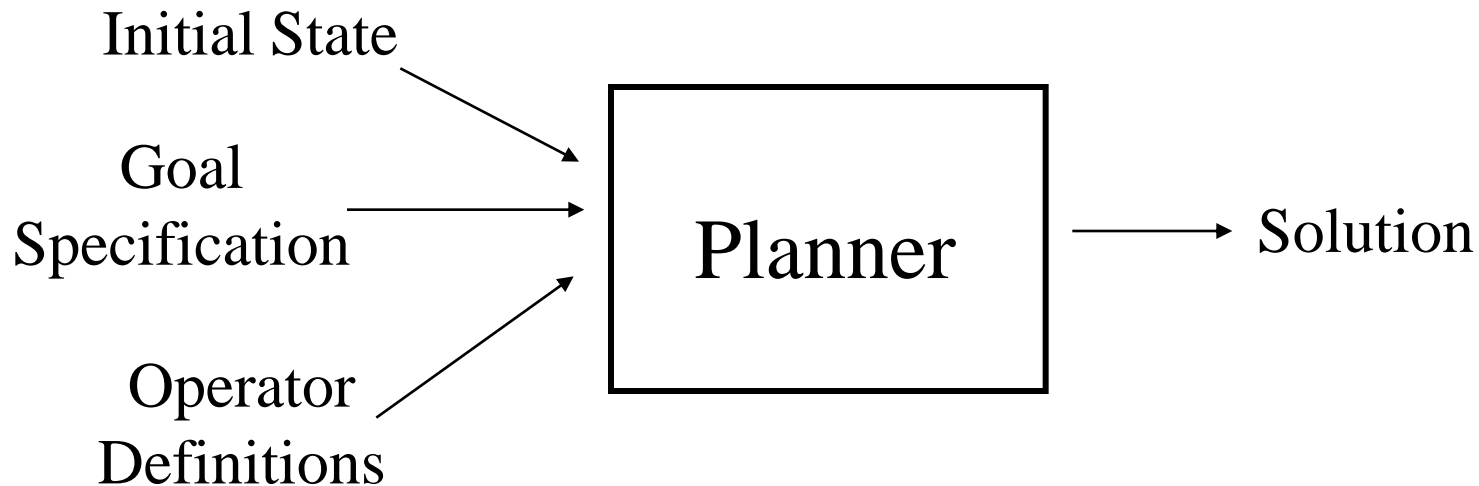


Search operators are “inferentially opaque”

Planning allows reasoning about state features

# Domain Independent Planning

- Study the planning process
  - Abstract
  - Not domain dependent
- Ontology, operators, etc. define the domain



- Operators model world dynamics
  - Situation Calculus
  - Strips Operators
  - PDDL Operators\*
- Search
  - State Space: Forward / Backward
  - Plan Space
- Heuristics
- Propositionalization

Pure FOPC



Specialized syntax

\* Ch10 R & N say PDDL but actually discuss Strips

# All Reachable Situations are Defined

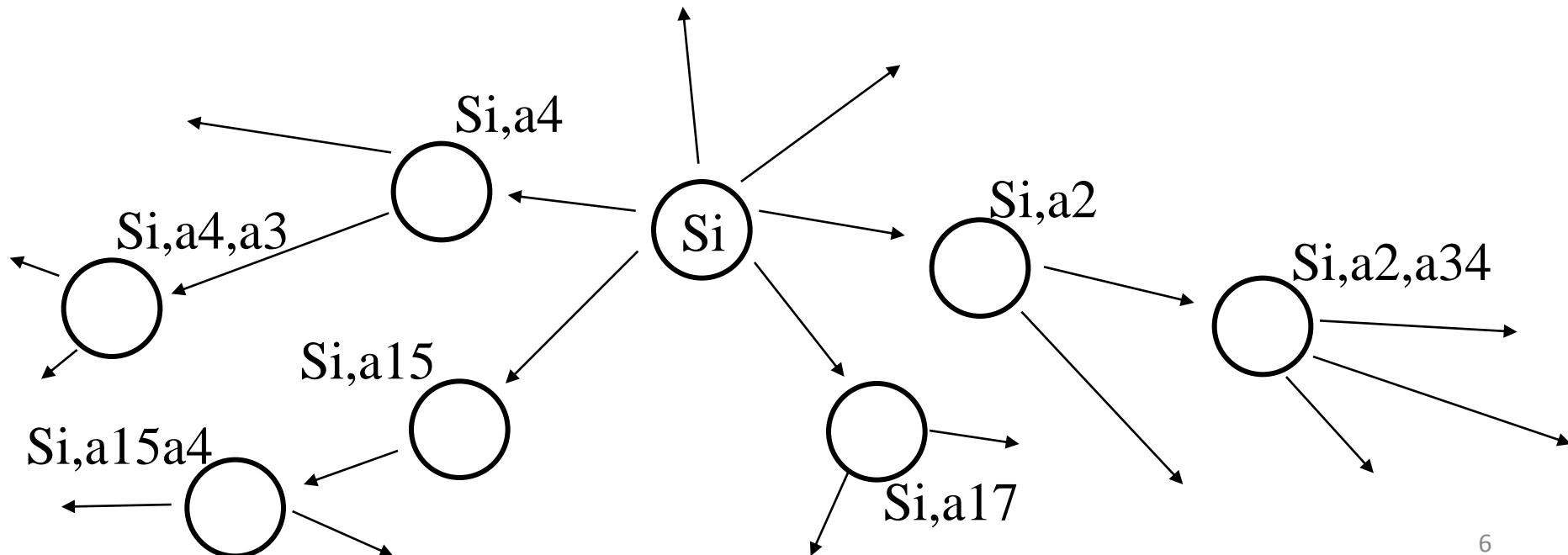
Given: 1) the Initial State

2) Axioms of World Change (operator definitions)

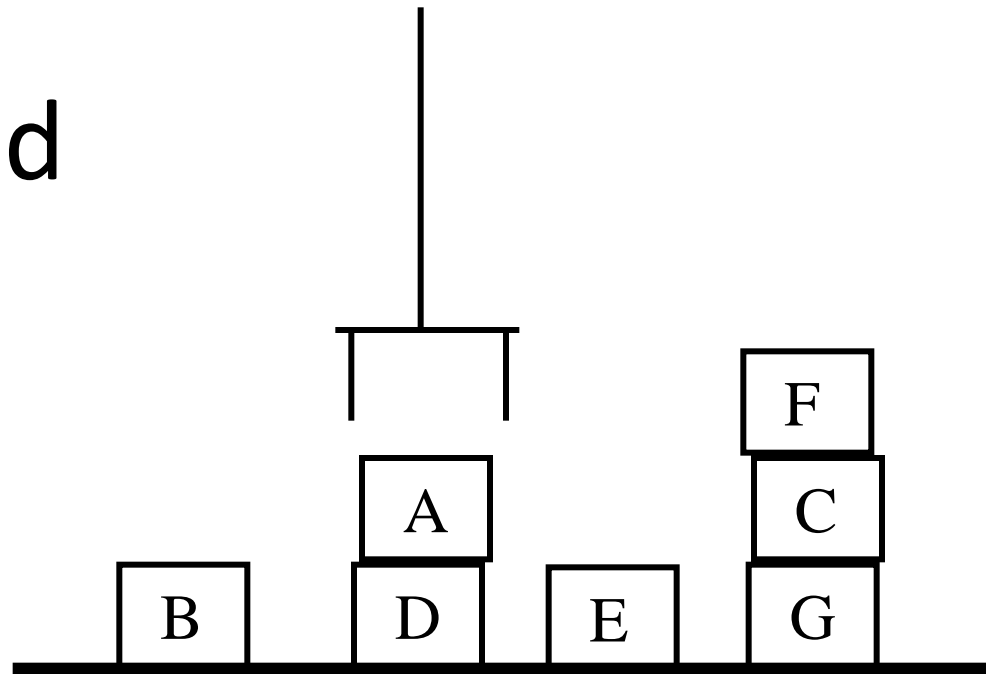
$\Delta \equiv \text{Initial State} \cup \text{Operator Definitions}$

Planning is theorem proving

Find a situation where the goal holds



# Blocks World



Several ontologies possible (ways to conceptualize the world and its changes)

Operator - General knowledge of one kind of change

Action - Ground instance of an operator

Silly domain but concisely illustrates many GENERAL planning issues

# Alternative Ontologies

change a block's position differently

Move-Block

Move-Gripper

Grasp-Block

Move-Gripper

UnGrasp-Block

Move-Gripper

Open-Gripper

Move-Gripper

Close-Gripper

...

Motor1-Velocity

Motor2-Velocity

...

Motor1-Voltage (Current, Duty Cycle)

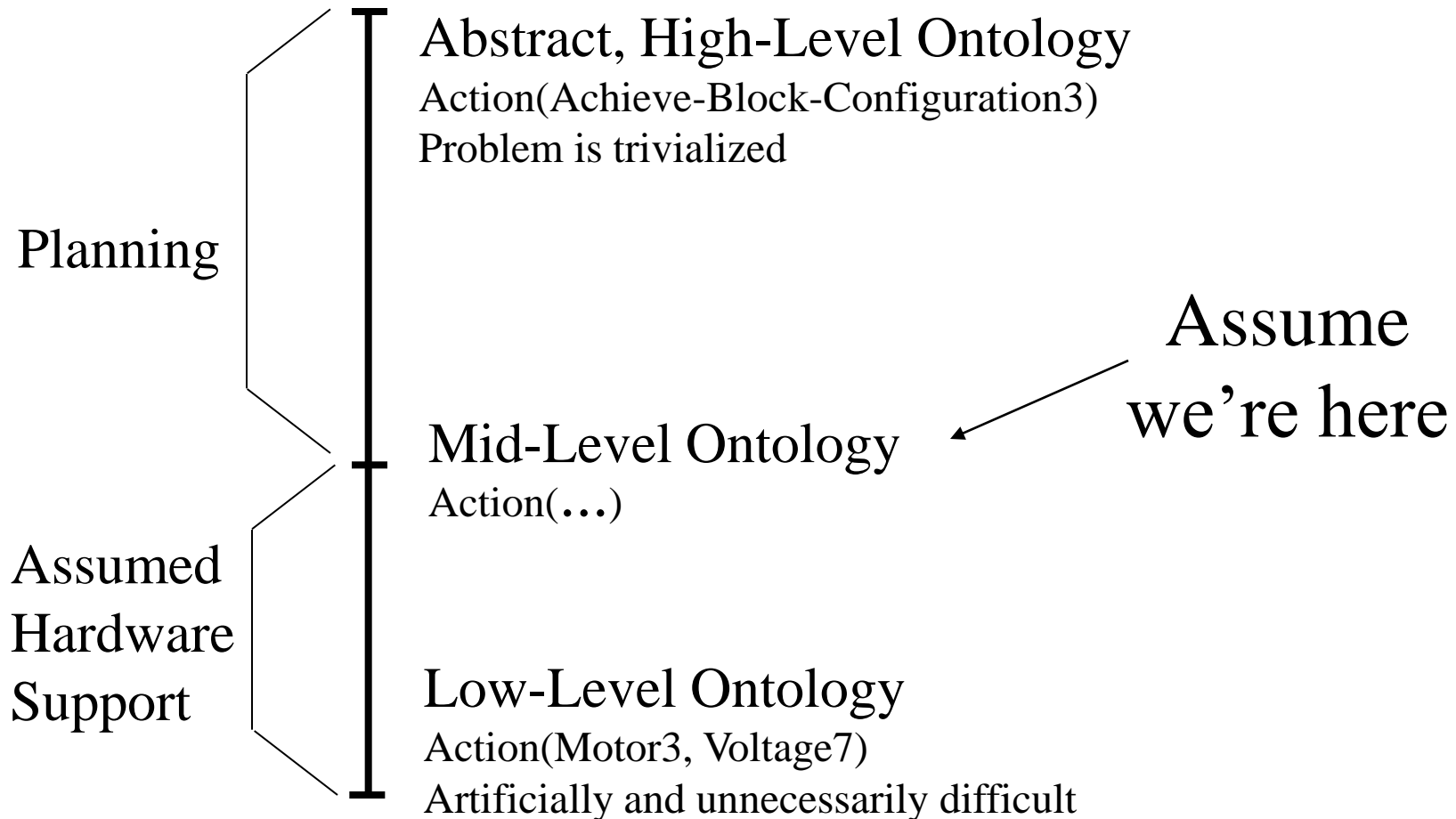
Motor2-Voltage

...

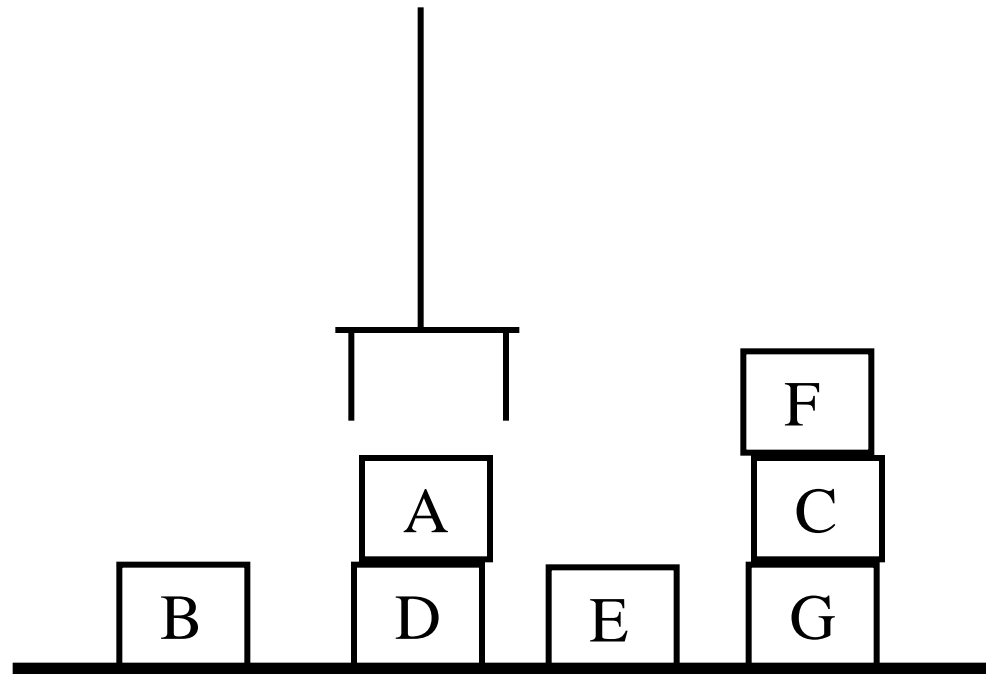
...



# Levels of Ontological Commitment



# Traditional Blocks World



Only support relationships change: On, Clr

A block can support at most one other block

The table can support any number of blocks

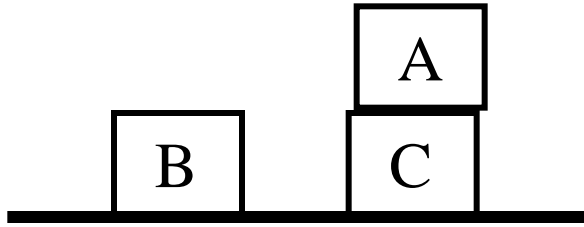
Generalized block movement – no gripper

# Operators: Situation Calculus

FOPC with some conventions

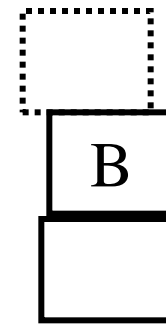
Assume a Move-Block ontology with  
at most one block directly on top of another  
a big table (always empty space available)

Move( $x, y, z$ ) operator to move  $x$  from  $y$  to  $z$



Initial State

On(A, C)  
 On(C, Tbl)  
 On(B, Tbl)  
 Blk(A)  
 Blk(B)  
 Blk(C)  
 Table(Tbl)  
 Clr(A)  
 Clr(B)  
 Clr(Tbl)



Goal

On(B, ?x)  
 Blk(?x)

Strips and PDDL can use this.  
 Situation Calculus cannot. (why?)

# FOPC Inference is Monotonic

On(A, B) and Clr(C)

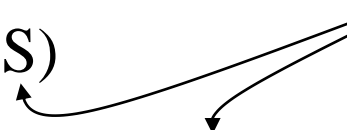
vs.

Blk(A) and Table(Tbl)

Situation Calculus solution:

On(A, B, S)  
Holds(On(A, B), S)

Situation  
Designator



The diagram shows two lines originating from the text 'Situation Designator' on the right. One line has an arrow pointing to the 'S' in 'On(A, B, S)'. The other line has an arrow pointing to the 'S' in 'Holds(On(A, B), S)'.

BTW, what's a predicate?

# Fluents

- Relationships that may be situation sensitive
- “On” & “Clr” relationships can change
- $\text{On}(x, y)$  or  $\text{On}(x, y, s)$  is a fluent
- $\text{Blk}(x)$  need not be

# The “Result” Function:

Result: Action  $\times$  Situation  $\rightarrow$  Situation

Result (Move (A, B, C), Si)

Result (Move (B, Tbl, A), Result (Move (A, B, C), Si))

*It denotes; it is not truth-valuable*

Straightforward generalization to variables:

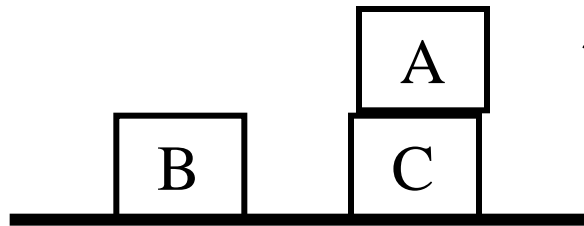
Result (Move (?x, ?y, C), Si)

denotes the set of situations where something was just moved to C from the initial state Si

Useful in “Goal Regression” planning

# World Change

Initial State:  $S_i$



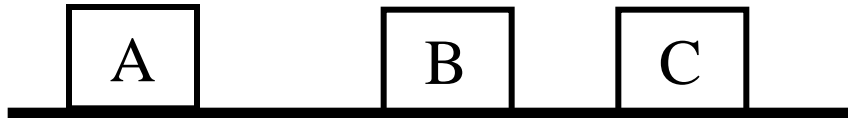
...

$\text{On}(A, C, S_i)$

...

$\text{Move}(A, C, \text{Tbl})$

Next State:  $\text{Result}(\text{Move}(A, C, \text{Tbl}), S_i)$



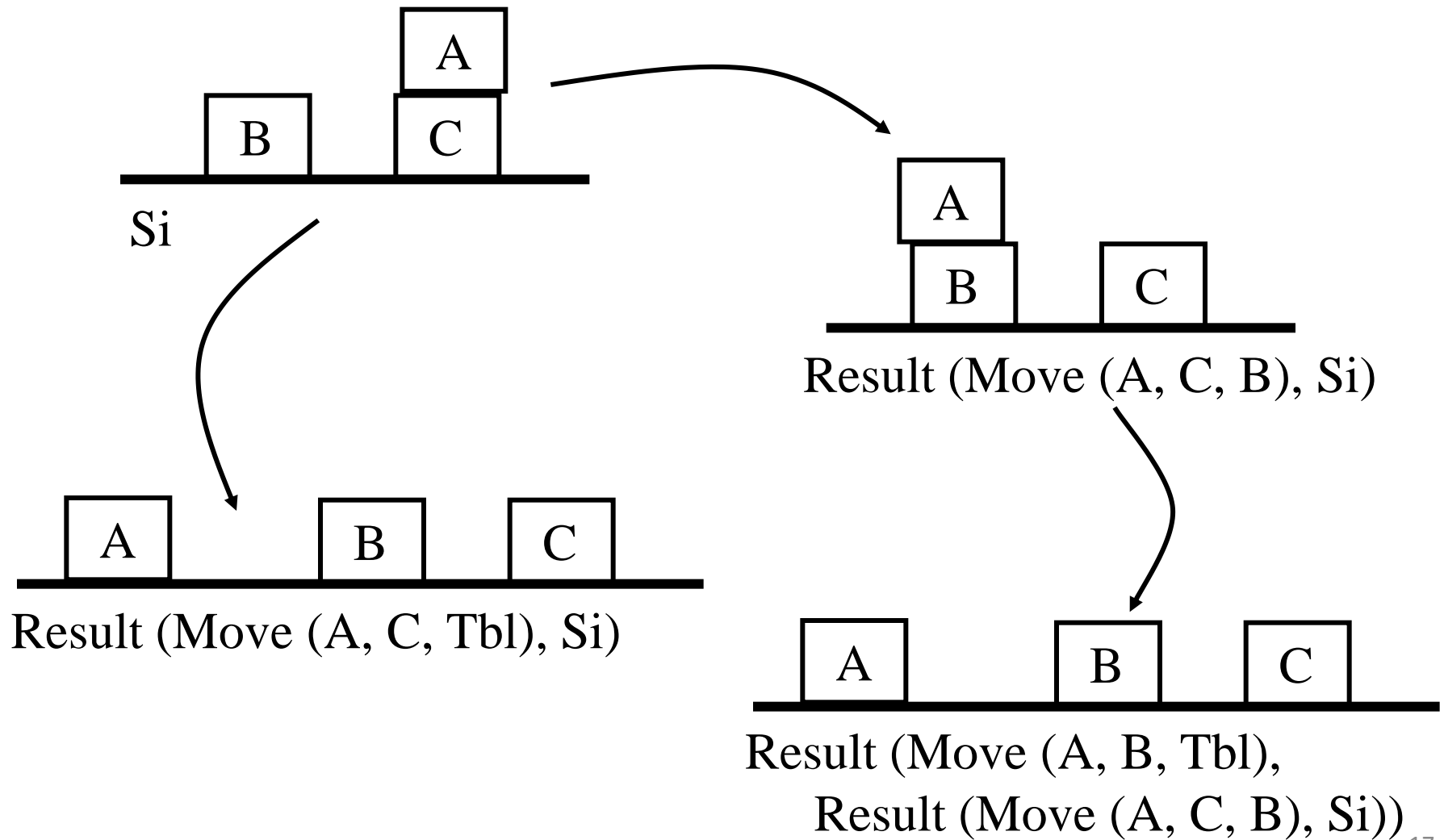
...

$\text{On}(A, \text{Tbl}, \text{Result}(\text{Move}(A, C, \text{Tbl}), S_i))$

...



# In Situation Calculus, States / Situations are Individuated by History and not Block Configuration



# the Move operator

Move(x, y, z) definition has the form:

$$\forall x \forall y \forall z \forall s \Theta \Rightarrow \Psi$$

If  $\Theta$  holds (things in s)

x is on y

z is clear

x is a block

x is clear

...

Preconditions

Then  $\Psi$  will hold (things in Result(Move(x,y,z),s))

x is on z

y is clear

...

Effects

# the Move operator

(partial)

Move(x, y, z)

$\forall x \forall y \forall z \forall s [$

$(\text{Clr}(x, s) \wedge \text{Clr}(z, s) \wedge \text{On}(x, y, s) \wedge \text{Blk}(x) \wedge \text{Diff}(x, z) \wedge \text{Diff}(y, z))$

$\Rightarrow$

$(\text{On}(x, z, \text{Result}(\text{Move}(x, y, z), s)) \wedge$

$\text{Clr}(y, \text{Result}(\text{Move}(x, y, z), s)) \wedge$

$\text{Clr}(x, \text{Result}(\text{Move}(x, y, z), s)) \wedge$

$\text{Table}(z) \Rightarrow$

$\text{Clr}(z, \text{Result}(\text{Move}(x, y, z), s)) ) ]$

Conditional  
Effect

Only Partial. Why?

Do we need to retract fluents?

On (x, y, s) - situation-specific relations

Do we need to assert negative fluents?

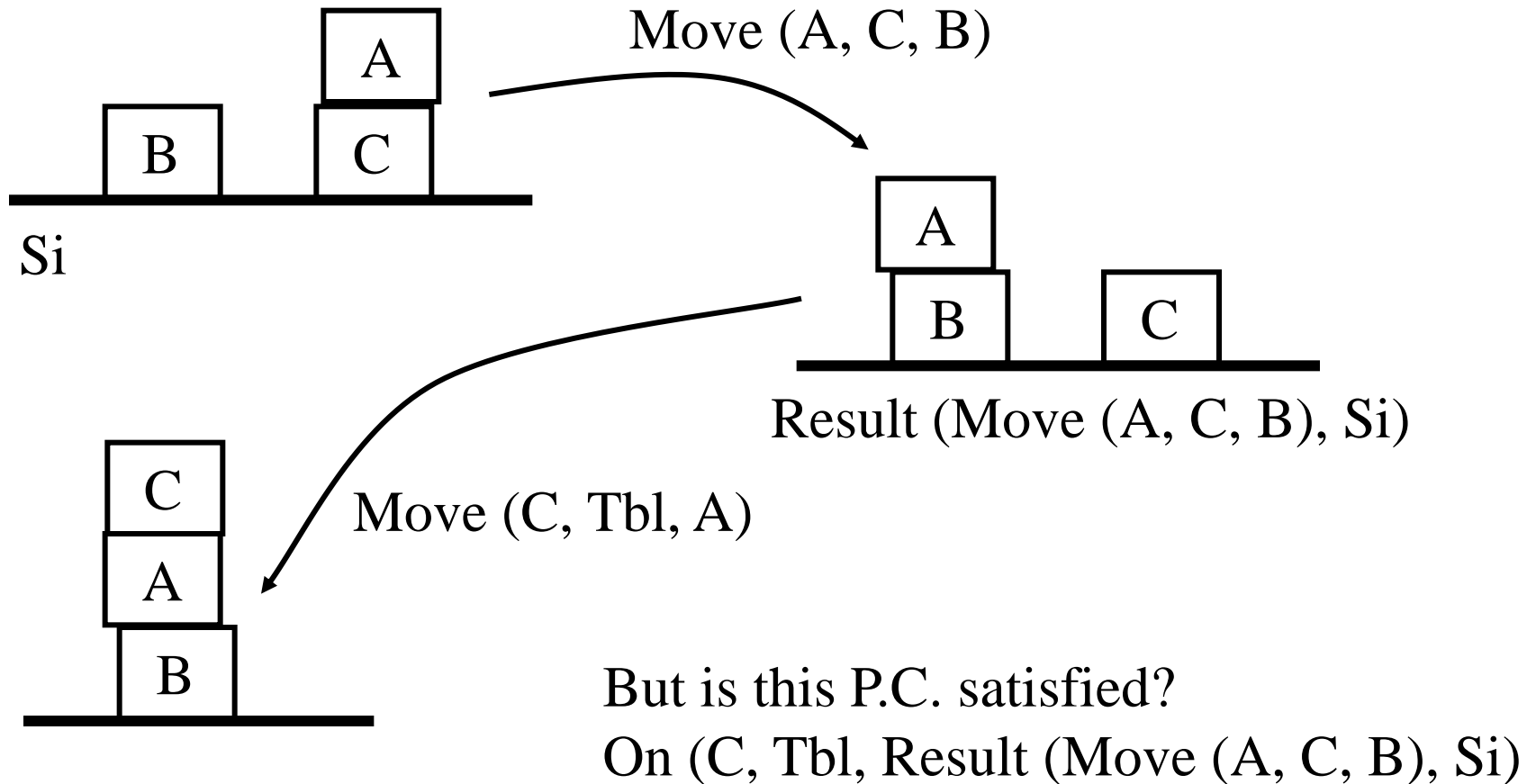
$\neg$  On (x, y, Result (Move (x, y, z), s)) ?

No, not in Situation Calculus  
(why not?)

# Frame Axioms

- Logic requires an inference path to determine that something holds
- Some relations are not involved
- May need to use these relations later
- If they don't persist through Move...

# The Need for Frame Axioms



And suppose there were other blocks: D, E, F...

# Move Frame Axioms

Move(x, y, z)

$\forall x \forall y \forall z \forall s [$

$(\text{Clr}(x, s) \wedge \text{Clr}(z, s) \wedge \text{On}(x, y, s) \wedge \text{Blk}(x) \wedge \text{Diff}(x, z))$

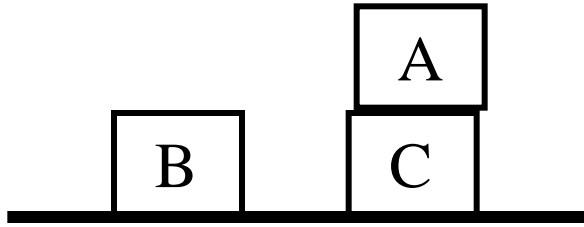
$\Rightarrow$

$([\forall v \forall w (\text{On}(v, w, s) \wedge \text{Diff}(v, x)) \Rightarrow$

$\text{On}(v, w, \text{Result}(\text{Move}(x, y, z), s)) ] \wedge$

$[\forall v (\text{Clr}(v, s) \wedge \text{Diff}(v, z)) \Rightarrow$

$\text{Clr}(v, \text{Result}(\text{Move}(x, y, z), s)) ] ) ]$



Initial State  $S_i$

$\text{On}(A, C, S_i)$

$\text{On}(C, \text{Tbl}, S_i)$

$\text{On}(B, \text{Tbl}, S_i)$

$\text{Blk}(A)$

$\text{Blk}(B)$

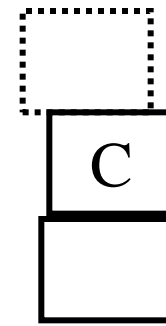
$\text{Blk}(C)$

$\text{Table}(\text{Tbl})$

$\text{Clr}(A, S_i)$

$\text{Clr}(B, S_i)$

$\text{Clr}(\text{Tbl}, S_i)$



Goal  $?s$

Find an  $?x$  and  $?s$  s.t.:

$\text{On}(C, ?x, ?s)$

$\text{Blk}(?x)$

Axioms  $\equiv$  Operator definitions  $\cup$  Initial State

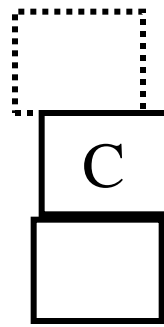
Negate Goal, add to axioms w/ Answer literal

Answer ( $?s$ ) should yield something like

Answer (Result (Move (C, Tbl, B),

Result (Move (A, C, Tbl),  $S_i$  ))





Goal ?s

Find an ?x and ?s s.t.:

On(C, ?x, ?s)

Blk(?x)

Negate Goal, add to axioms w/ Answer literal

Goal:  $\exists x \exists s [\text{On}(C, x, s) \wedge \text{Blk}(x)]$

Negated Goal  $\forall x \forall s [\neg \text{On}(C, x, s) \vee \neg \text{Blk}(x)]$

Clause form  $\{\neg \text{On}(C, ?x6, ?s8), \neg \text{Blk}(?x6), \text{Answer}(?s8)\}$   
 w/ Answer  
 literal, variables standardized apart and designated with ‘?’

# Situation Calculus

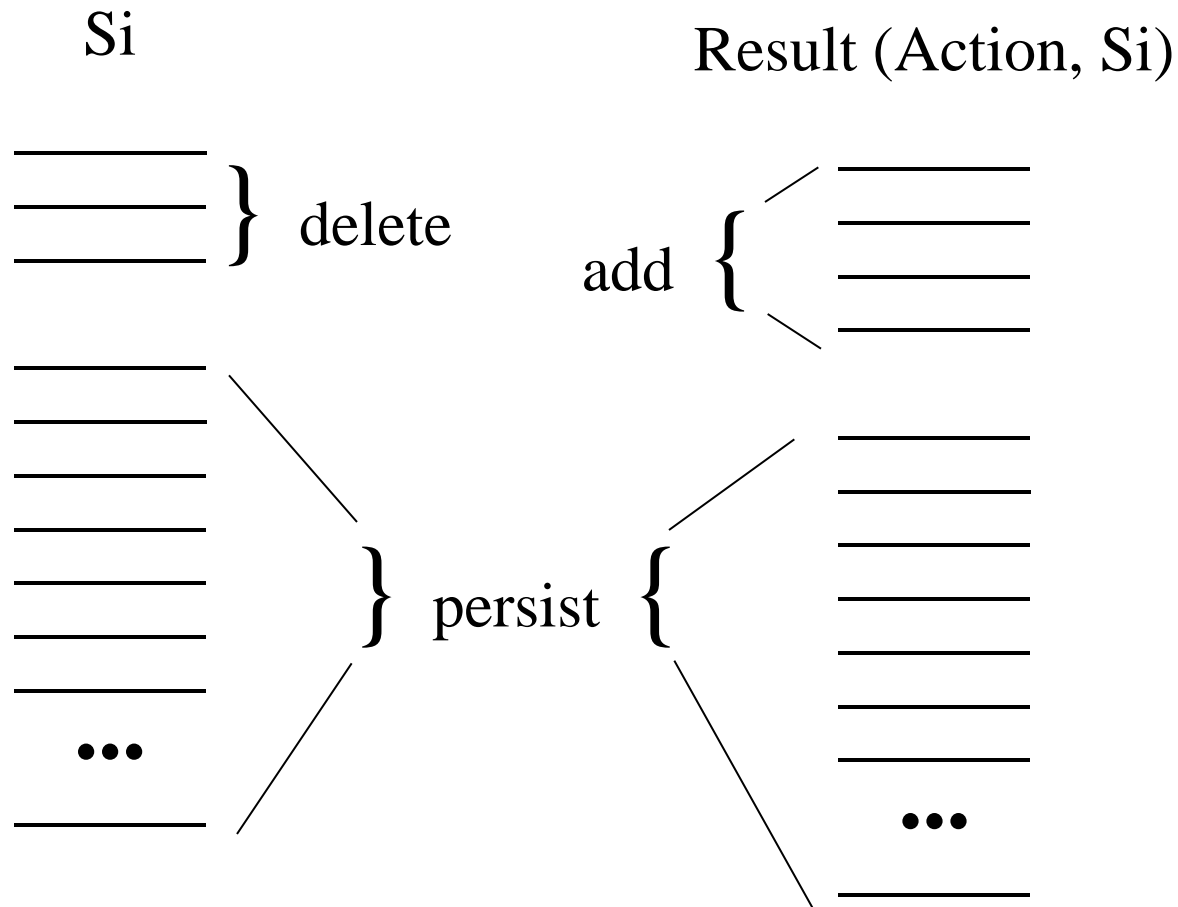
- No central operator “definition”
- Knowledge about an operator can be distributed across many WFFs
- Consider “Move” in clause form

# STRIPS Operators

- Frames from animated cartoon “frames”
- Writing them can be tedious
- Luckily relatively few things change
- Strips operators are more concise
- Historically: Stanford Research Institute  
Problem Solver

# World Changes

Action must fully define resulting world state



# Operators

## In Situation Calculus

Specify fluents

Add set

Persist set

No mention =

no inference path

By default

fluents are Deleted

## In Strips

Specify fluents

Delete set

Add set

By default

fluents Persist

More concise because usually

|Persist| >> |Delete|

# Strips Operators

- Preconditions - list of positive literals
- Effects also positive literals (N.B. below)
  - Delete list - things to be retracted
  - Add list - things to be asserted
- Effects can be combined in one list (as R & N)
  - Delete elements designated with “ $\neg$ ”
  - This is *not* logical negation (think about why)

# Representations

## In Situation Calculus

$\Delta$  contains all initial WFFs

No distinction between  
operators and initial state

Operator definitions distributed  
throughout  $\Delta$

## In Strips

Operator information is  
centralized

Operator information is stored  
separately

State information is stored  
separately for each state

No longer need a situation  
designator

Closed world assumption