CS/ECE 439: Wireless Networking

Physical Layer - Diversity

Inter-Symbol Interference

- Larger difference in path length can cause inter-symbol interference (ISI)
- Suppose the receiver can do some processing
 - Add/subtracted scaled and delayed copies of the signal



Dynamic Equalization

Combine multiple delayed copies of the signal
 ex: linear equalizer circuit



Equalization Discussion



- Use multiple delayed copies of the received signal to try to reconstruct the original signal
- Weights are set dynamically
 - Typically based on some known "training" sequence
- Effectively uses the multiple copies of the signal to reinforce each other
 - But only works for paths that differ in length by less than the depth of the pipeline



Diversity Techniques

Spatial diversity

- Exploit fact that fading is location-specific
- Use multiple nearby antennas and combine signals
 - Can be directional

Frequency diversity

- Spread signal over multiple frequencies/broader frequency band
 - For example, spread spectrum

Channel Diversity

- Distribute signal over multiple "channels"
 - "Channels" experience independent fading
 - > Reduces the error, i.e. only part of the signal is affected

Time diversity

- Spread data out over time
- Expand bit stream into a richer digital signal
 - Useful for bursty errors, e.g. slow fading
 - A specific form of channel coding



Spatial Diversity

- Use multiple antennas that pick up the signal in slightly different locations
 - Can use more than two antennas!
- Each antenna experiences different channels
 - If antennas are sufficiently separated, chances are that the signals are mostly uncorrelated
 - If one antenna experiences deep fading, chances are that the other antenna has a strong signal
 - Antennas should be separated by $\frac{1}{2}$ wavelength or more
- Applies to both transmit and receive side
 - Channels are symmetric



Receiver Diversity

Simplest solution

Selection diversity: pick antenna with best SNR

But why not use both signals?

- + More information
- Signals out of phase, e.g. kind of like multi-path
- ? Don't amplify the noise
- Maximal ratio combining: combine signals with a weight that is based on their SNR
 - Weight will favor the strongest signal (highest SNR)



Transmit Diversity

- Same as receive diversity but the transmitter has multiple antennas
- Selection diversity: transmitter picks the best antenna
 - i.e. with best channel to receiver
 - Sender "precodes" the signal
- How does transmitter learn channel?
 - Gets explicit feedback from the receiver
 - Rely on channel reciprocity

Typical Algorithm in 802.11

- Use transmit + receive selection diversity
- How to explore all channels to find the best one ... or at least the best transmit antenna
- Receiver
 - Use the antenna with the strongest signal
 - Always use the same antenna to send the acknowledgement gives feedback to the sender





Typical Algorithm in 802.11

- Use transmit + receive selection diversity
- How to explore all channels to find the best one ... or at least the best transmit antenna
- Sender
 - Pick an antenna to transmit and learn about the channel quality based on the ACK
 - Occasionally try the other antenna to explore the channel between all four channel pairs



Spread Spectrum

Spread transmission over a wider bandwidth

- Don't put all your eggs in one basket!
- Good for military
 - Jamming and interception becomes harder
- Also useful to minimize impact of a "bad" frequency in regular environments
- What can be gained from this apparent waste of spectrum?
 - Immunity from various kinds of noise and multipath distortion
 - Can be used for hiding and encrypting signals
 - Several users can independently use the same higher bandwidth with very little interference

Frequency Hopping Spread Spectrum (FHSS)

- Have the transmitter hop between a seemingly random sequence of frequencies
 - Each frequency has the bandwidth of the original signal
- Dwell time is the time spent using one frequency
- Spreading code determines the hopping sequence
 - Must be shared by sender and receiver (e.g. standardized)



Example: Original 802.11 Standard (FH)

96 channels of I MHz

- Only 78 used in US
 - Other countries used different numbers
- Each channel carried only ~1% of the bandwidth
- I or 2 Mbps per channel

Dwell time was configurable

- FCC set an upper bound of 400 msec
- Transmitter/receiver must be synchronized

Standard defined 26 orthogonal hop sequences

- Transmitter used a beacon on fixed frequency to inform the receiver of its hop sequence
- Can support multiple simultaneous transmissions use different hop sequences
 - e.g. up to 10 co-located APs with their clients



Example: Bluetooth

> 79 frequencies with a spacing of 1 MHz

- Other countries use different numbers of frequencies
- Frequency hopping rate is 1600 hops/s
- Maximum data rate is I MHz

Direct Sequence Spread Spectrum (DSSS)

- Each bit in original signal is represented by multiple bits (chips) in the transmitted signal
- Spreading code spreads signal across a wider frequency band
 - Spread is in direct proportion to number of bits used
 - e.g. exclusive-OR of the bits with the spreading code
- The resulting bit stream is used to modulate the signal





Properties

• Each bit is sent as multiple chips

- Need more bps bandwidth to send signal
- Number of chips per bit = spreading ratio
 - This is the spreading part of spread spectrum
- Need more spectral bandwidth
 - Nyquist and Shannon say so!
- Advantages
 - Transmission is more resilient.
 - DSSS signal will look like noise in a narrow band
 - Can lose some chips in a word and recover easily
 - Multiple users can share bandwidth

Example: Original 802.11 Standard (DSSS)

DSSS PHY

- I Msymbol/s rate
- II-to-I spreading ratio
- Barker chipping sequence
 - Barker sequence has low autocorrelation properties
 - $\hfill\square$ The similarity between observations as a function of the time lag between them
- Uses about 22 MHz
- Receiver decodes by counting the number of "I" bits in each word
 - 6"I" bits correspond to a 0 data bit

Data rate

- I Mbps (i.e. II Mchips/sec)
- Extended to 2 Mbps
 - Requires the detection of a $\frac{1}{4}$ phase shift



Example: 802.11b

- (Maximum) data rate
 || Mbs
- Complementary Code Keying (CCK)
 - Complementary means that the code has good autocorrelation properties
 - Want nice properties to ease recovery in the presence of noise, multipath interference, ..
 - Each word is mapped onto an 8 bit chip sequence
 - Symbol rate at 1.375 MSymbols/sec, at 8 bpS = 11 Mbps

Symbol rate

I.375 MSymbols/sec, at 8 bpS = II Mbps



Code Division Multiple Access

- Users share spectrum and time, but use different codes to spread their data over frequencies
 - DSSS where users use different spreading sequences
 - Use spreading sequences that are orthogonal, i.e. they have minimal overlap
 - Frequency hopping with different hop sequences
- The idea is that users will only rarely overlap and the inherent robustness of DSSS will allow users to recover if there is a conflict
 - Overlap = use the same the frequency at the same time
 - > The signal of other users will appear as noise



CDMA Principle

- Basic Principles of CDMA
 - D = rate of data signal
 - Break each bit into k chips user-specific fixed pattern
 - Chip data rate of new channel = kD
- If k=6 and code is a sequence of 1s and -1s
 - For a 'I' bit, A sends code as chip pattern
 - <cl, c2, c3, c4, c5, c6>
 - For a '0' bit, A sends complement of code
 - <-c1, -c2, -c3, -c4, -c5, -c6>
- Receiver knows sender's code and performs electronic decode function

 $S_u(d) = d1 \times c1 + d2 \times c2 + d3 \times c3 + d4 \times c4 + d5 \times c5 + d6 \times c6$

- < d1, d2, d3, d4, d5, d6> = received chip pattern
- <cl, c2, c3, c4, c5, c6> = sender's code



CDMA Example

- User A code = <1, -1, -1, 1, -1, 1>
 - To send a | bit = <|, -|, -|, |, -|, |>
 - To send a 0 bit = <-1, 1, 1, -1, 1, -1>
- ► User B code = < I, I, -I, I, I, I>
 - ► To send a | bit = < |, |, -|, -|, |, |>
- Receiver receiving with A's code
 - (A's code) x (received chip pattern)
 - User A 'I' bit: 6 -> I
 - User A '0' bit: -6 -> 0
 - User B'I' bit: 0 -> unwanted signal ignored

Categories of Spreading Sequences

Spreading Sequence Categories

- Pseudo-noise (PN) sequences
- Orthogonal codes
- For FHSS systems
 - PN sequences most common
- For DSSS systems not employing CDMA
 - PN sequences most common
- For DSSS CDMA systems
 - PN sequences
 - Orthogonal codes

CDMA Discussion

- CDMA does not assign a fixed bandwidth but a user's bandwidth depends on the load
 - More users = more "noise" and less throughput for each user, e.g. more information lost due to errors
 - How graceful the degradation is depends on how orthogonal the codes are
 - TDMA and FDMA have a fixed channel capacity
 - Contention based access is more flexible TDMA
- Weaker signals may be lost in the clutter
 - This will systematically put the same node pairs at a disadvantage – not acceptable
 - The solution is to add power control, i.e. nearby nodes use a lower transmission power than remote nodes

CDMA Example

- CDMA cellular standard
 Used in the US, e.g. Sprint
- Allocates 1.228 MHz for base station to mobile communication
 - Shared by 64 "code channels"
 - Used for voice (55), paging service (8), and control (1)
- Provides a lot error coding to recover from errors
 - Voice data is 8550 bps
 - Coding and FEC increase this to 19.2 kbps
 - Then spread out over 1.228 MHz using DSSS; uses QPSK



Discussion

- Spread spectrum is very widely used
- Effective against noise and multipath
 - Signal looks like noise to other nodes
 - Multiple transmitters can use the same frequency range
- FCC requires the use of spread spectrum in ISM band
 - If signal is above a certain power level
- Is also used in higher speed 802.11 versions.
 - No surprise!

Time Redundancy: Bit Stream Level

- Protect digital data by introducing redundancy in the transmitted data
 - Error detection codes: can identify certain types of errors
 - Error correction codes: can fix certain types of errors
- Block codes provide Forward Error Correction (FEC) for blocks of data
 - (n, k) code: n bits are transmitted for k information bits
 - Simplest example: parity codes
 - Many different codes exist: Hamming, cyclic, Reed-Solomon, ...
- Convolutional codes provide protection for a continuous stream of bits
 - Coding gain is n/k
 - Turbo codes: convolutional code with channel estimation

Time Diversity Example

- Spread blocks of bytes out over time
- Can use FEC or other error recovery techniques to deal with burst errors



Error Detection/Recovery

- Adds redundant information that checks for errors
 - And potentially fix them
 - If not, discard packet and resend
- Occurs at many levels
 - Demodulation of signals into symbols (analog)
 - Bit error detection/correction (digital)—our main focus
 - Within network adapter (CRC check)



Error Detection/Recovery

Analog Errors

- Example of signal distortion
- Hamming distance
 - Parity and voting
 - Hamming codes
- Error bits or error bursts?
- Digital error detection
 - Two-dimensional parity
 - Cyclic Redundancy Check (CRC)



Analog Errors

Consider the following encoding of 'Q'





Encoding isn't perfect





Encoding isn't perfect









possible binary voltage encoding symbol neighborhoods and erasure region



Symbols



QAM

- Phase and amplitude modulation
- 2-dimensional representation
 - Angle is phase shift
 - Radial distance is new amplitude

16-symbol example



Symbols





possible QAM symbol neighborhoods in green; all other space results in erasure


Digital error detection and correction

Input: decoded symbols

- Some correct
- Some incorrect
- Some erased

Output:

- Correct blocks (or codewords, or frames, or packets)
- Erased blocks



Error Detection Probabilities

Definitions

- P_b : Probability of single bit error (BER)
- P₁ : Probability that a frame arrives with no bit errors
- P₂:While using error detection, the probability that a frame arrives with one or more undetected errors
- P₃:While using error detection, the probability that a frame arrives with one or more detected bit errors but no undetected bit errors



Error Detection Probabilities

With no error detection

$$P_1 = (1 - P_b)^F$$
$$P_2 = 1 - P_1$$
$$P_3 = 0$$

F = Number of bits per frame



Error Detection Process

Transmitter

- For a given frame, an error-detecting code (check bits) is calculated from data bits
- Check bits are appended to data bits

Receiver

- Separates incoming frame into data bits and check bits
- Calculates check bits from received data bits
- Compares calculated check bits against received check bits
- Detected error occurs if mismatch



Parity

- Parity bit appended to a block of data
- Even parity
 - Added bit ensures an even number of Is
- Odd parity
 - Added bit ensures an odd number of Is

Example

- 7-bit character1110001
- Even parity
- Odd parity

|||000||0 |||000||1



Parity: Detecting Bit Flips

- I-bit error detection with parity
 - Add an extra bit to a code to ensure an even (odd) number of Is
 - Every code word has an even (odd) number of Is



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Voting: Correcting Bit Flips

- I-bit error correction with voting
 - Every codeword is transmitted n times
 - Codeword is 3 bits long



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Voting: 2-bit Erasure Correction

Every code word is copied 3 times



D

2-erasure planes in green remaining bit not ambiguous

cannot correct I-error and Ierasure



Hamming Distance

- The Hamming distance between two code words is the minimum number of bit flips to move from one to the other
 - Example:
 - 00101 and 00010
 - Hamming distance of 3



Minimum Hamming Distance

- The minimum Hamming distance of a code is the minimum distance over all pairs of codewords
 - Minimum Hamming Distance for parity
 - 2
 - Minimum Hamming Distance for voting
 - 3



Coverage

N-bit error detection

- No code word changed into another code word
- Requires Hamming distance of N+I
- N-bit error correction
 - N-bit neighborhood: all codewords within N bit flips
 - No overlap between N-bit neighborhoods
 - Requires hamming distance of 2N+I



- Linear error-correcting code
- Named after Richard Hamming
- Simple, commonly used in RAM (e.g., ECC-RAM)
- Can detect up to 2-bit errors
- Can correct up to I-bit errors



Construction

- number bits from I upward
- powers of 2 are check bits
- all others are data bits
- Check bit j: XOR of all k for which (j AND k) = j





Construction

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Construction

- number bits from I upward
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What are we trying to handle?

Worst case errors

- We solved this for I bit error
- Can generalize, but will get expensive for more bit errors
- Probability of error per bit
 - Flip each bit with some probability, independently of others

Burst model

- Probability of back-to-back bit errors
- Error probability dependent on adjacent bits
- Value of errors may have structure

Why assume bursts?

- Appropriate for some media (e.g., radio)
- Faster signaling rate enhances such phenomena



Digital Error Detection Techniques

Two-dimensional parity

- Detects up to 3-bit errors
- Good for burst errors

IP checksum

- Simple addition
- Simple in software
- Used as backup to CRC

Cyclic Redundancy Check (CRC)

- Powerful mathematics
- Tricky in software, simple in hardware
- Used in network adapter



Two-Dimensional Parity



Use I-dimensional parity

 Add one bit to a 7-bit code to ensure an even/odd number of ls

Add 2nd dimension

- Add an extra byte to frame
 - Bits are set to ensure even/odd number of 1s in that position across all bytes in frame

Comments

Catches all I-, 2- and 3-bit and most 4-bit errors



Two-Dimensional Parity

0	1	0	0	0	1	1	1	0
0	1	1	0	1	1	1	1	0
0	1	1	0	1	1	1	1	0
0	1	1	0	0	1	0	0	1
Λ	Λ	1	Δ	Δ	Δ	1	1	1
U	U		U	U	U		L	L

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What happens if...





What about 2-bit errors?





What about 2-bit errors?

Could be the dotted pair or the dashed pair. Can't correct 2-bit error.





What about 3-bit errors?

Can detect the three-bit error





What about 4-bit errors?

Are there any 4-bit errors this scheme *can* detect?

0	1	0	0	0	1	1	1	0
0	1	1	0	1	1	1	1	0
0	1	1	0	1	1	1	1	0
0	1	1	0	0	1	0	0	1
0	0	1	0	0	0	1	1	1



What about 4-bit errors?

Can you think of a 4-bit error this scheme can't detect?

	1		0	0	1	1	1	0
0	1	1	0	1	1	1	1	0
Q 1	1	X	0	1	1	1	1	0
0	1	1	0	0	1	0	0	1
	Δ		Δ	0	0	1		
U	U		U	U	U		L	



Internet Checksum

Idea

- Add up all the words
- Transmit the sum
- Use I's complement addition on I6bit codewords

Example

Codewords:	-5	-3
I's complement binary:	1010	1100

I's complement sum

Comments

- Small number of redundant bits
- Easy to implement
- Not very robust
- Eliminated in IPv6

1000



IP Checksum

}

```
u short cksum(u short *buf, int count) {
register u long sum = 0;
while (count--) {
     sum += *buf++;
     if (sum & 0xFFFF0000) {
     /* carry occurred, so wrap around */
            sum \&= 0 \times FFFF;
            sum++;
     }
}
return ~(sum & 0xFFFF);
```

What could cause this check to fail?



Simplified CRC-like protocol using regular integers

- Basic idea
 - Both endpoints agree in advance on divisor value C = 3
 - Sender wants to send message M = 10
 - Sender computes X such that C divides IOM + X
 - Sender sends codeword W = IOM + X
 - Receiver receives W' and checks whether C divides W'
 - If so, then probably no error
 - If not, then error



Simplified CRC-like protocol using regular integers

Intuition

- If C is large, it's unlikely that bits are flipped exactly to land on another multiple of C
- CRC is vaguely like this, but uses polynomials instead of numbers



Cyclic Redundancy Check (CRC)

Given

- Message M = 10011010
- Represented as Polynomial M(x)= $| *x^7 + 0 *x^6 + 0 *x^5 + | *x^4 + | *x^3 + 0 *x^2 + | *x + 0$ = $x^7 + x^4 + x^3 + x$
- Select a divisor polynomial C(x) with degree k
 - Example with k = 3:
 - $C(x) = x^3 + x^2 + I$
 - Represented as 1101
- Transmit a polynomial P(x) that is evenly divisible by

C(x)

 $P(x) = M(x) * x^{k} + k \text{ check bits}$

How can we determine these k bits?



Properties of Polynomial Arithmetic

Coefficients are modulo 2

$$(x^{3} + x) + (x^{2} + x + 1) = \dots$$
$$\dots x^{3} + x^{2} + 1$$
$$(x^{3} + x) - (x^{2} + x + 1) = \dots$$
$$\dots x^{3} + x^{2} + 1 \text{ also!}$$

- Addition and subtraction are both xor!
- Need to compute R such that C(x) divides $P(x) = M(x) \cdot x^k + R(x)$
- So R(x) = remainder of $M(x) \cdot x^k / C(x)$
 - Will find this with polynomial long division



CRC - Sender

Given

- $M(x) = 10011010 = x^7 + x^4 + x^3 + x$
- $C(x) = |10| = x^3 + x^2 + 1$
- Steps
 - $T(x) = M(x) * x^k$ (add zeros to increase deg. of M(x) by k)
 - Find remainder, R(x), from T(x)/C(x)
 - $P(x) = T(x) R(x) \Rightarrow M(x)$ followed by R(x)
- Example
 - T(x) = 10011010000
 - R(x) = 101
 - P(x) = 10011010101



CRC - Receiver

• Receive Polynomial P(x) + E(x)

- E(x) represents errors
- E(x) = 0, implies no errors
- Divide (P(x) + E(x)) by C(x)
 - If result = 0, either
 - No errors (E(x) = 0, and P(x) is evenly divisible by C(x))
 - (P(x) + E(x)) is exactly divisible by C(x), error will not be detected
 - If result = I, errors.



CRC – Example Encoding





CRC – Example Decoding – No Errors



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CRC – Example Decoding – with Errors





CRC Error Detection

Properties

- Characterize error as E(x)
- Error detected unless C(x) divides E(x)
 - (*i.e.*, E(x) is a multiple of C(x))



Example of Polynomial Multiplication

Multiply
1101 by 10110
x³ + x² + 1 by x⁴ + x² + x





CRC Error Detection

What errors can we detect?

- All single-bit errors, if x^k and x^0 have non-zero coefficients
- All double-bit errors, if C(x) has at least three terms
- All odd bit errors, if C(x) contains the factor (x + I)
- Any bursts of length < k, if C(x) includes a constant term
- Most bursts of length $\geq k$



Common Polynomials for C(x)

CRC	C(x)
CRC-8	$x^8 + x^2 + x^1 + 1$
CRC-10	$x^{10} + x^9 + x^5 + x^4 + x^1 + 1$
CRC-12	$x^{12} + x^{11} + x^3 + x^2 + x^1 + 1$
CRC-16	$x^{16} + x^{15} + x^2 + 1$
CRC-CCITT	$x^{16} + x^{12} + x^5 + 1$
CRC-32	$\begin{array}{c} x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + \\ x^4 + x^2 + x^1 + 1 \end{array}$

D



Error Detection vs. Error Correction

Detection

- Pro: Overhead only on messages with errors
- Con: Cost in bandwidth and latency for retransmissions

Correction

- Pro: Quick recovery
- Con: Overhead on all messages
- What should we use?
 - Correction if retransmission is too expensive
 - Correction if probability of errors is high
 - Detection when retransmission is easy and probability of errors is low

