

# CS 425 / ECE 428

## Distributed Systems

### Fall 2025

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*Lecture 5: Gossiping*

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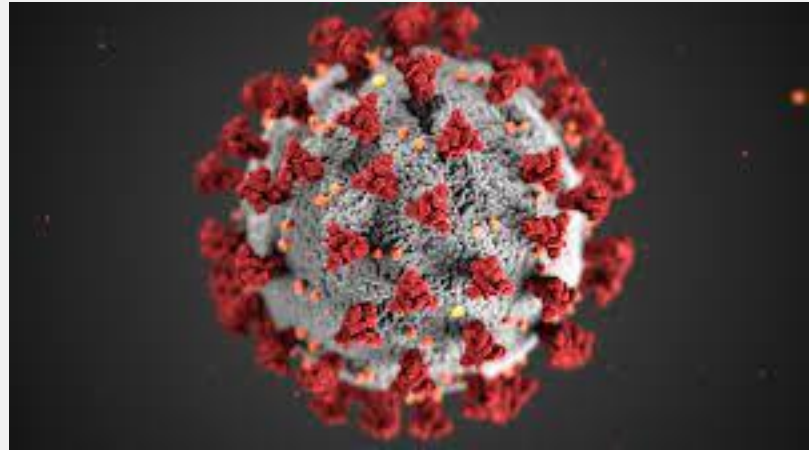
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# Today's Agenda

- Epidemics, or how to use them to your advantage (to do good things)



# Multicast

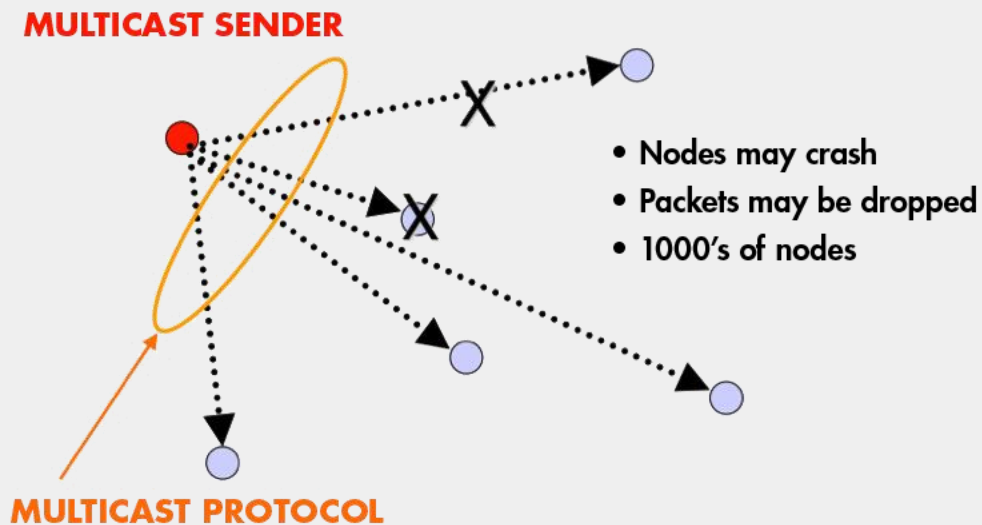
Node with a piece of information  
to be communicated to everyone



Distributed Group  
of "Nodes" =

Processes at  
Internet-based host

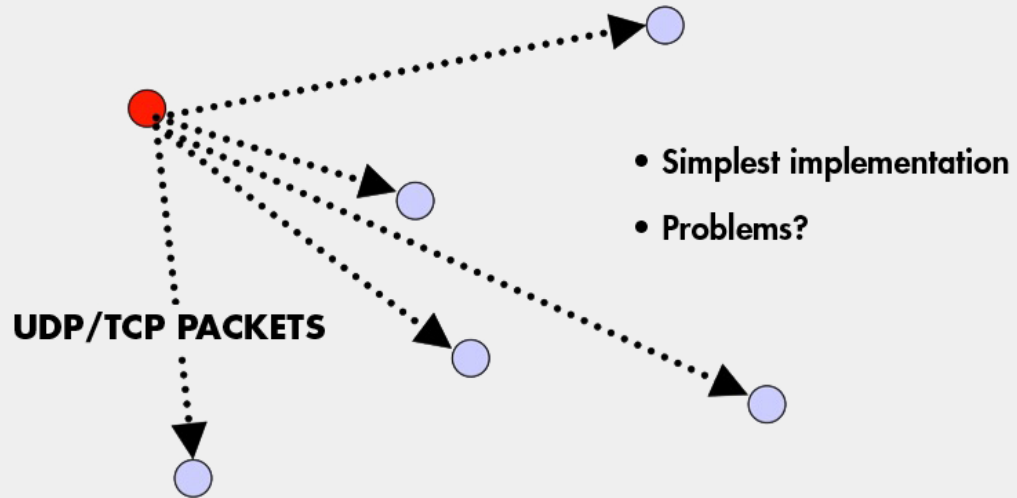
# Fault-tolerance and Scalability



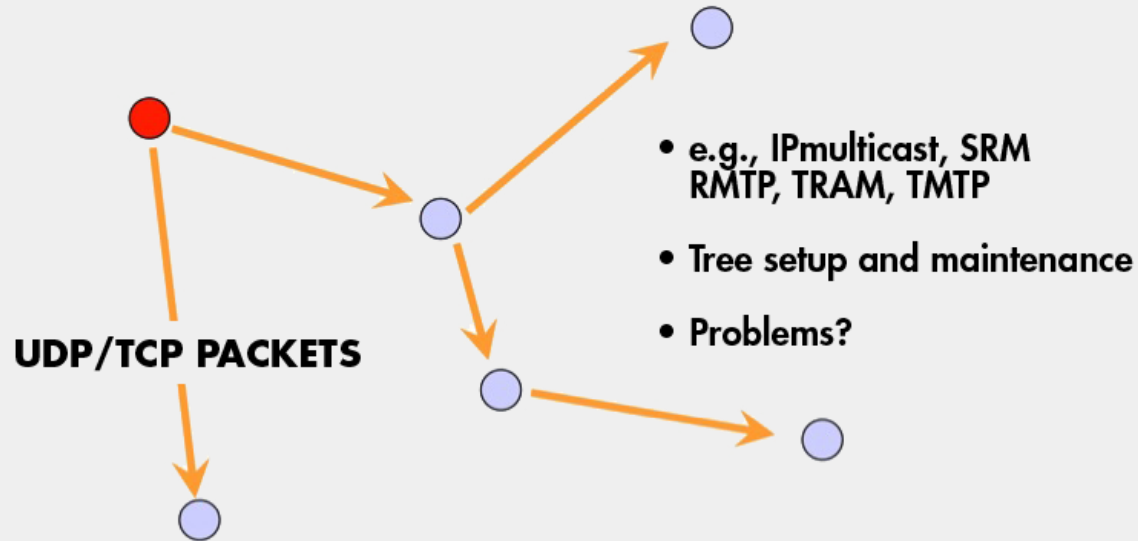
Needs:

1. Reliability (Atomicity)
  - 100% receipt
2. Speed

# Centralized



# Tree-Based



# Tree-based Multicast Protocols

- Build a spanning tree among the processes of the multicast group
- Use spanning tree to disseminate multicasts
- Use either acknowledgments (ACKs) or negative acknowledgements (NAKs) to repair multicasts not received
- SRM (Scalable Reliable Multicast)
  - Uses NAKs
  - But adds random delays, and uses exponential backoff to avoid NAK storms
  - (Do you know why SRM is called a “talented” protocol?)
- RMTP (Reliable Multicast Transport Protocol)
  - Uses ACKs
  - But ACKs only sent to designated receivers, which then re-transmit missing multicasts
- These protocols still cause an  $O(N)$  ACK/NAK overhead [Birman99]

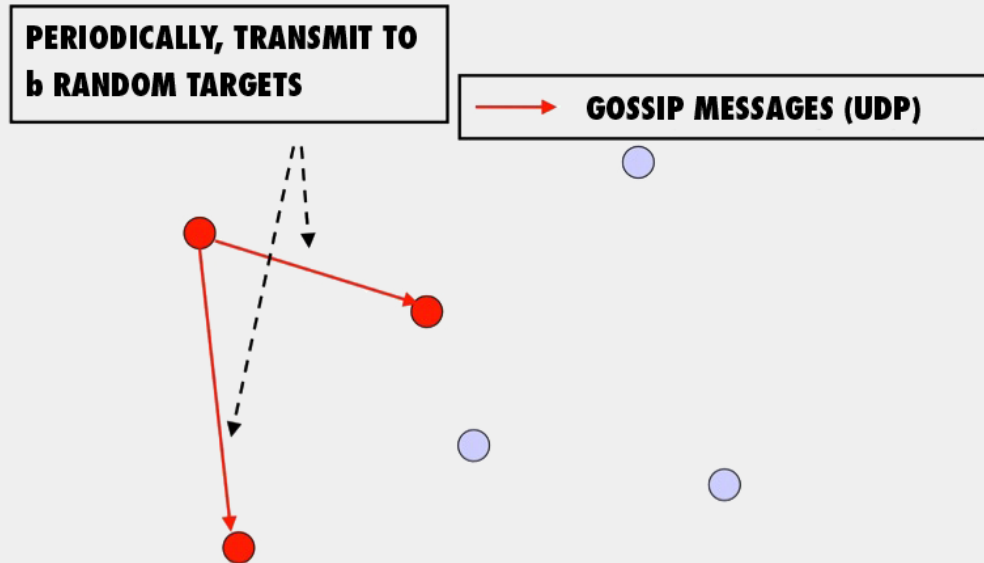


# A Third Approach

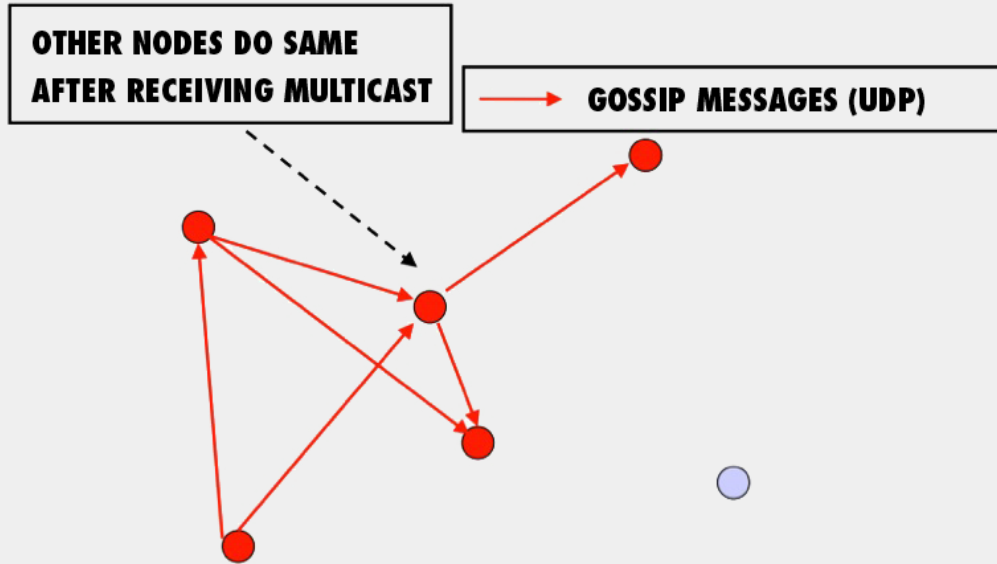
**MULTICAST SENDER**



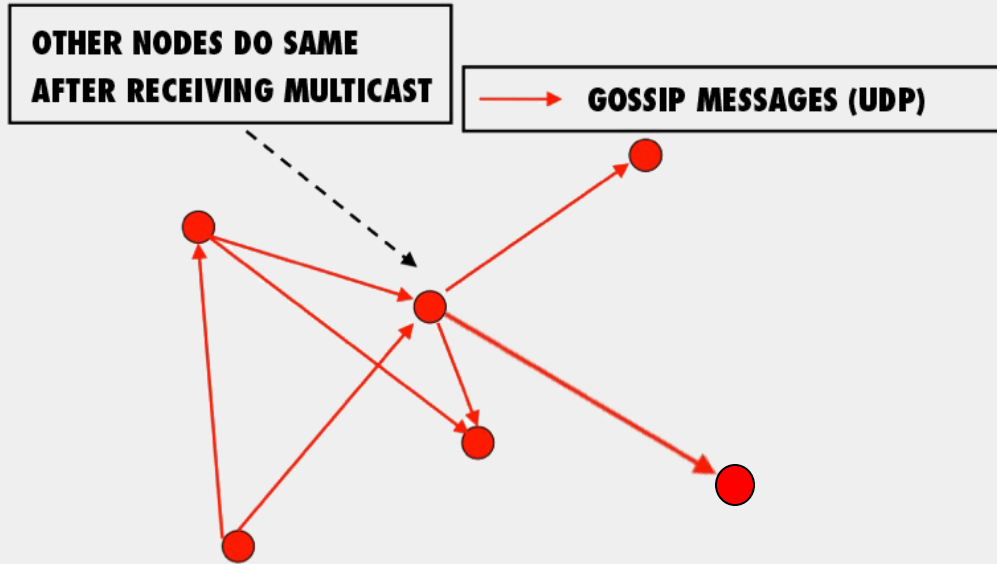
# A Third Approach



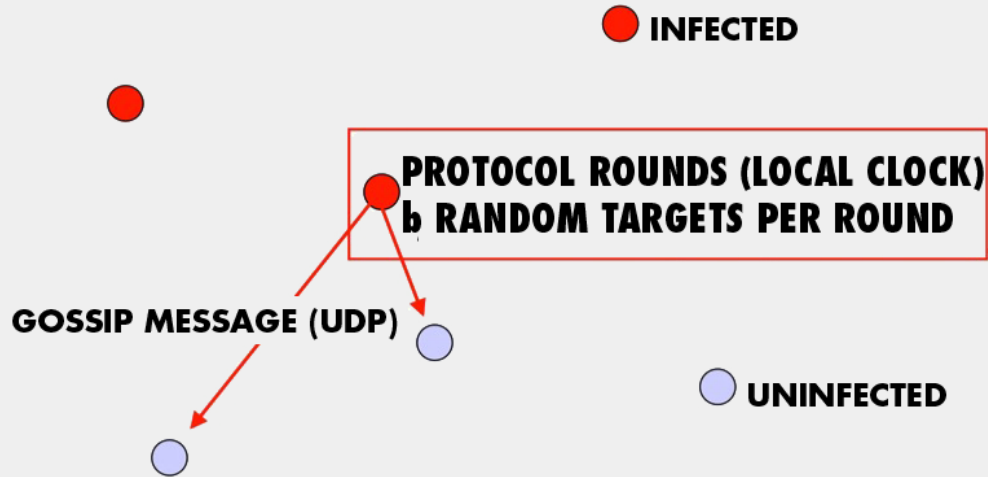
# A Third Approach



# A Third Approach



# “Epidemic” Multicast (or “Gossip”)



# Push vs. Pull

- So that was “Push” gossip
  - Once you have a multicast message, you start gossiping about it
  - Multiple messages? Gossip a random subset of them, or recently-received ones, or higher priority ones
- There’s also “Pull” gossip
  - Periodically poll a few randomly selected processes for new multicast messages that you haven’t received
  - Get those messages
- Hybrid variant: Push-Pull
  - As the name suggests

# Announcements

- MP1: Due coming Sunday 9/14, demos Monday 9/15
  - VMs distributed: see Piazza
  - Demo signup sheet: now on Piazza (sign up by Friday!)
  - Demo details: will be posted tomorrow on Piazza
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- HW1 due soon, Thu 9/18!
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# Properties

Claim that the simple Push protocol

- Is lightweight in large groups
- Spreads a multicast quickly
- Is highly fault-tolerant



# Analysis

From old mathematical branch of *Epidemiology* [Bailey 75]

- Population of  $(n+1)$  individuals mixing homogeneously
- Contact rate between any individual pair is  $\beta$
- At any time, each individual is either uninfected (numbering  $x$ ) or infected (numbering  $y$ )
- Then,  $x_0 = n, y_0 = 1$   
and at all times  $x + y = n + 1$
- Infected–uninfected contact turns latter infected, and it stays infected

# Analysis (contd.)

- Continuous time process
- Then

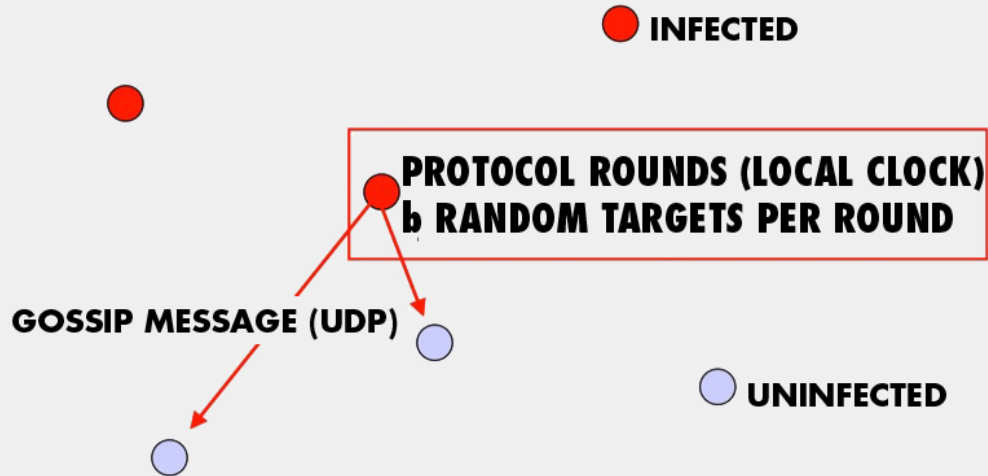
$$\frac{dx}{dt} = -\beta xy \quad (\text{why?})$$

with solution:

$$x = \frac{n(n+1)}{n + e^{\beta(n+1)t}}, y = \frac{(n+1)}{1 + ne^{-\beta(n+1)t}}$$

(can you derive it?)

# Epidemic Multicast



# Epidemic Multicast Analysis

$$\beta = \frac{b}{n} \quad (\text{why?})$$

Substituting, at time  $t=c\log(n)$ , the number of infected is

$$y \approx (n+1) - \frac{1}{n^{cb-2}}$$

(correct? can you derive it?)

# Analysis (contd.)

- Set  $c, b$  to be small numbers independent of  $n$
- Within  $c \log(n)$  rounds, [**low latency**]
  - all but  $\frac{1}{n^{cb-2}}$  number of nodes receive the multicast  
[**reliability**]
  - each node has transmitted no more than  $cb \log(n)$  gossip messages  
[**lightweight**]

# Why is $\log(N)$ low?

- $\log(N)$  is not constant in theory
- But pragmatically, it is a very slowly growing number
- Base 2
  - $\log(1000) \sim 10$
  - $\log(1M) \sim 20$
  - $\log(1B) \sim 30$
  - $\log(\text{all IPv4 addresses}) = 32$
  - $\log(\text{all IPv6 addresses}) = 128$

# Fault-tolerance

- Packet loss
  - 50% packet loss: analyze with  $b$  replaced with  $b/2$
  - To achieve same reliability as 0% packet loss, takes twice as many rounds
- Node failure
  - 50% of nodes fail: analyze with  $n$  replaced with  $n/2$  and  $b$  replaced with  $b/2$
  - Same as above

# Fault-tolerance

- With failures, is it possible that the epidemic might die out quickly?
- Possible, but improbable:
  - Once a few nodes are infected, with high probability, the epidemic will not die out
  - So the analysis we saw in the previous slides is actually behavior *with high probability*
- [Galey and Dani 98]
- Think: why do rumors spread so fast? why do infectious diseases cascade quickly into epidemics? why does a virus or worm spread rapidly?



# Pull Gossip: Analysis

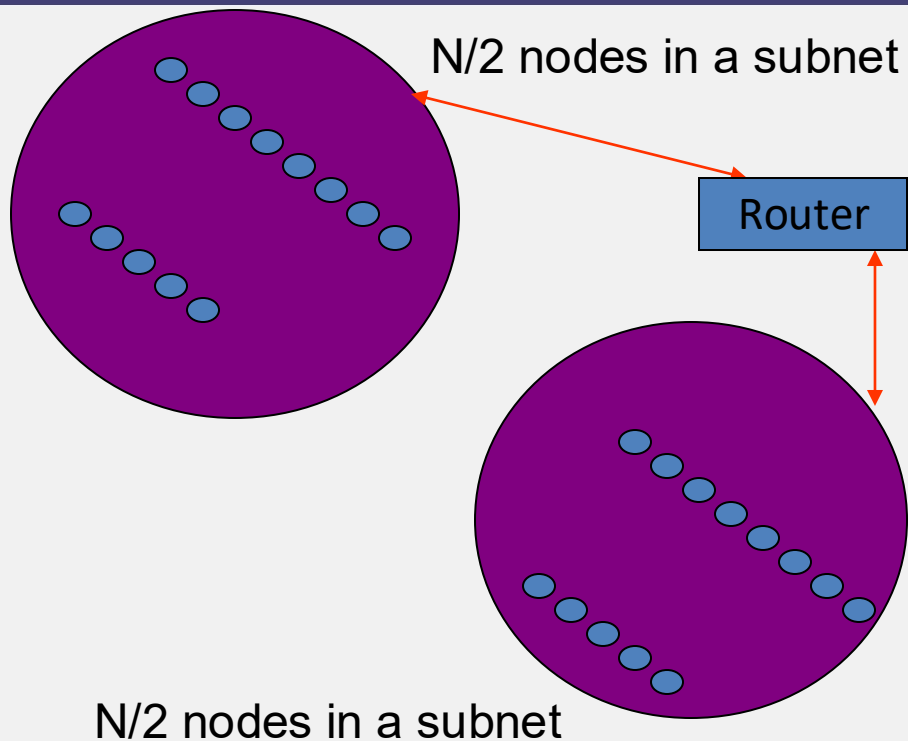
- In all forms of gossip, it takes  $O(\log(N))$  rounds before about  $N/2$  processes get the gossip
  - Why? Because that's the fastest you can spread a message – a spanning tree with fanout (degree) of constant degree has  $O(\log(N))$  total nodes (**height of tree**)
- Thereafter, pull gossip is faster than push gossip
- After the  $i$ th, round let  $p_i$  be the fraction of non-infected processes. Let each round have  $k$  pulls. Then

$$p_{i+1} = (p_i)^{k+1}$$

- This is super-exponential
- Second half of pull gossip finishes in time  $O(\log(\log(N)))$

# Topology-Aware Gossip

- Network topology is hierarchical
- Random gossip target selection => core routers face  $O(N)$  load (Why?)
- **Fix:** In subnet  $i$ , which contains  $n_i$  nodes, pick gossip target in your subnet with probability  $(1-1/n_i)$
- Router load =  $O(1)$
- Dissemination time =  $O(\log(N))$



## Answer – Push Analysis (contd.)

Using:  $\beta = \frac{b}{n}$

Substituting, at time  $t=c\log(n)$

$$\begin{aligned} y &= \frac{n+1}{1 + ne^{-\frac{b}{n}(n+1)c\log(n)}} \approx \frac{n+1}{1 + \frac{1}{n^{cb-1}}} \\ &\approx (n+1)\left(1 - \frac{1}{n^{cb-1}}\right) \\ &\approx (n+1) - \frac{1}{n^{cb-2}} \end{aligned}$$

# SO,...

- Is this all theory and a bunch of equations?
- Or are there implementations yet?

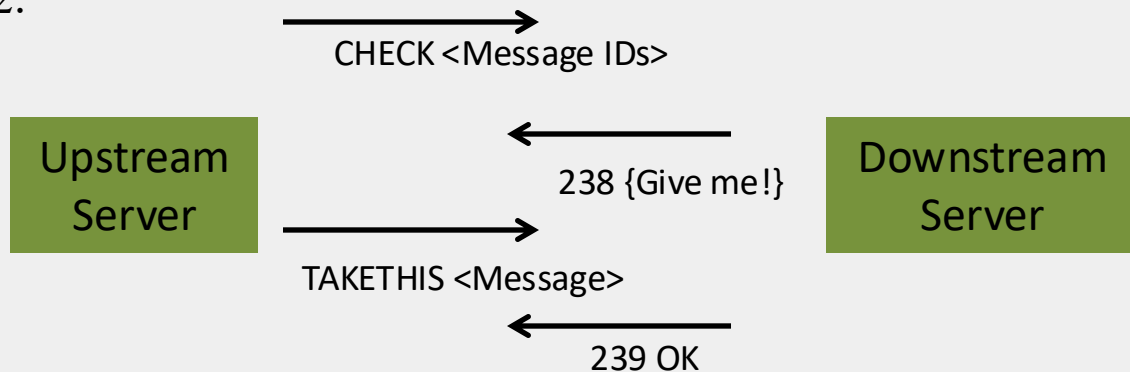
# Some implementations

- Clearinghouse and Bayou projects: email and database transactions [PODC '87]
- refDBMS system [Usenix '94]
- Bimodal Multicast [ACM TOCS '99]
- Sensor networks [Li Li et al, Infocom '02, and PBBF, ICDCS '05]
- AWS EC2 and S3 Cloud (rumored). [ '00s]
- Cassandra key-value store (and others) use gossip for maintaining membership lists
- Usenet NNTP (Network News Transport Protocol) [ '79]

# NNTP Inter-server Protocol

1. Each client uploads and downloads news posts from a news server

2.



Server retains news posts for a while,  
transmits them lazily, deletes them after a while.

# Summary

- Multicast is an important problem
- Tree-based multicast protocols
- When concerned about scale and fault-tolerance, gossip is an attractive solution
- Also known as epidemics
- Fast, reliable, fault-tolerant, scalable, topology-aware

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