

CS 425 / ECE 428
Distributed Systems
Fall 2016

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Lecture 23: Structure of Networks

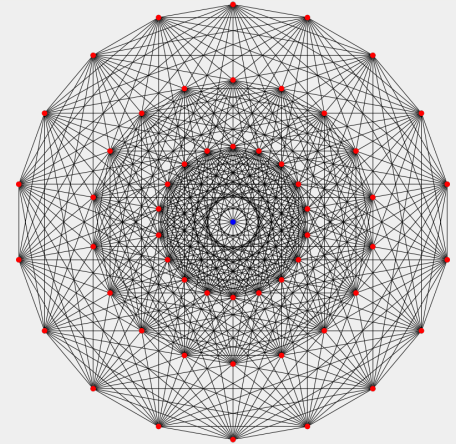
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WHAT'S A NETWORK/GRAPH?

- Has **vertices** (i.e., nodes)
 - E.g., in the Facebook graph, each user = a vertex (or a node)
- Has **edges** that connect pairs of vertices
 - E.g., in the Facebook graph, a friend relationship = an edge

LOTS OF GRAPHS/NETWORKS

- Large graphs/network are all around us
 - Internet : vertices are routers/switches and edges are links
 - World Wide Web: vertices are webpages, and edges are URL links on a webpage pointing to another webpage
 - Called “Directed” graph as edges are uni-directional
 - Social networks: Facebook, Twitter, LinkedIn
 - Biological networks: DNA interaction graphs, ecosystem graphs, etc.



Source: Wikimedia Commons

COMPLEXITY OF NETWORKS

- **Structural:** *human population has ~7 B nodes, there are millions of computers on the Internet...*
- **Evolution:** *people make new friends all the time, ISP's change hands all the time...*
- **Diversity:** *some people are more popular, some friendships are more important...*
- **Node Complexity:** *Endpoints have different CPUs, Windows is a complicated OS, Mobile devices ...*
- **Emergent phenomena:** *simple end behavior → leads to → complex system-wide behavior.*
 - *If we understand the basics of climate change, why is the weather so unpredictable?*

NETWORK STRUCTURE

- “Six degrees of Kevin Bacon”
- Milgram’s experiment in 1970

- Recent work on shows similarities between the structures of: Internet, WWW, human social networks, p2p overlays, Electric power grid, protein networks
- These networks have “evolved naturally”
- Many of these are “small world networks”

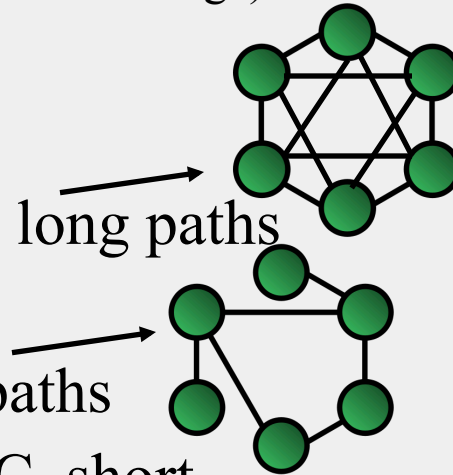
TWO IMPORTANT NETWORK PROPERTIES

1. Clustering Coefficient: CC

$\Pr(\text{A-B edge, given an A-C edge and a C-B edge})$

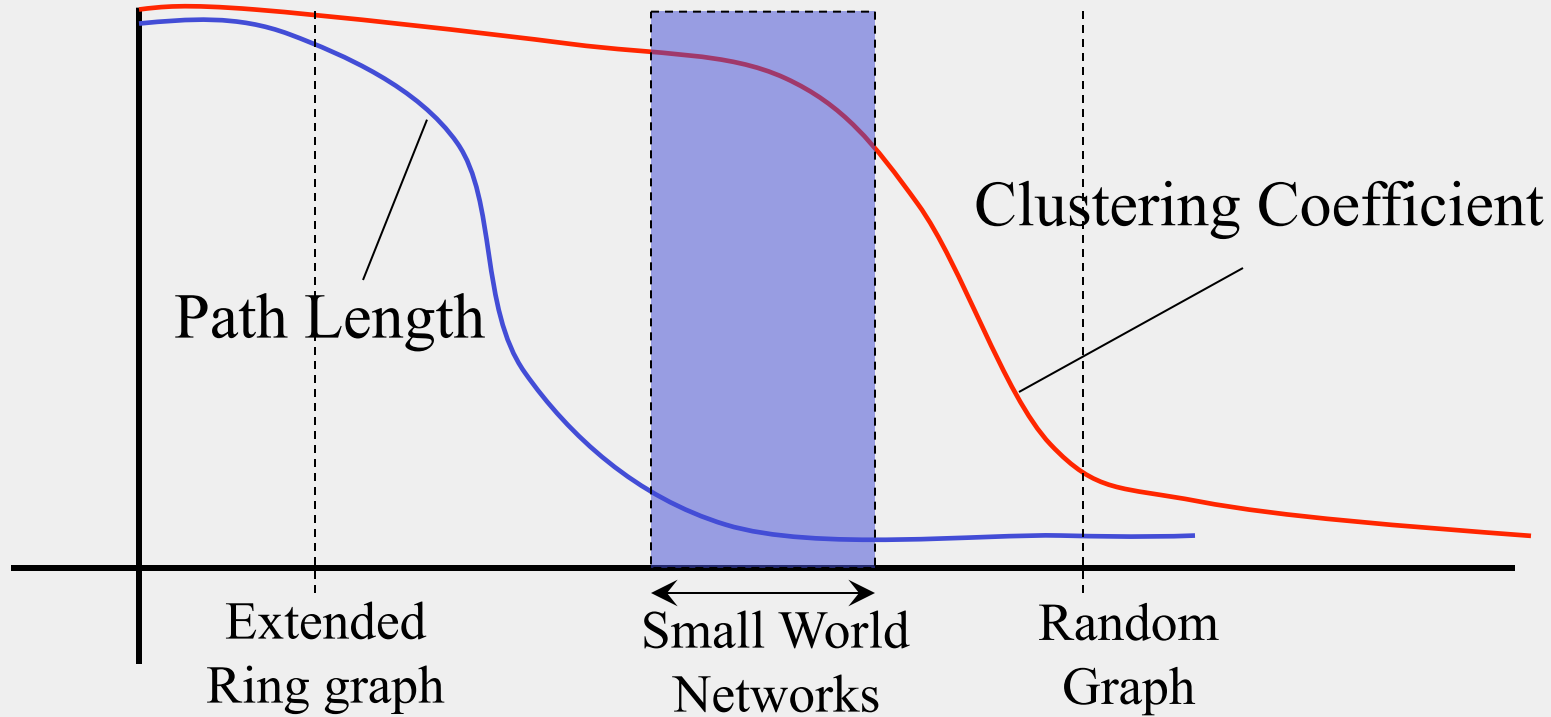
2. Path Length of shortest path

- Extended Ring graph: high CC, long paths
- Random graph: low CC, short paths
- Small World Networks: high CC, short paths



DERIVING SMALL-WORLD GRAPHS

Convert more and more edges to point to random nodes



SMALL-WORLD NETWORKS ALL AROUND

Most “natural evolved” networks are small world

- Network of actors → six degrees of Kevin Bacon
- Network of humans → Milgram’s experiment
- Co-authorship network → “Erdos Number”
- World Wide Web, the Internet, ...

Many of these networks also “grow incrementally”

“Preferential” model of growth

- When adding a vertex to graph, connect it to existing vertex v with probability proportional to $\text{num_neighbors}(v)$

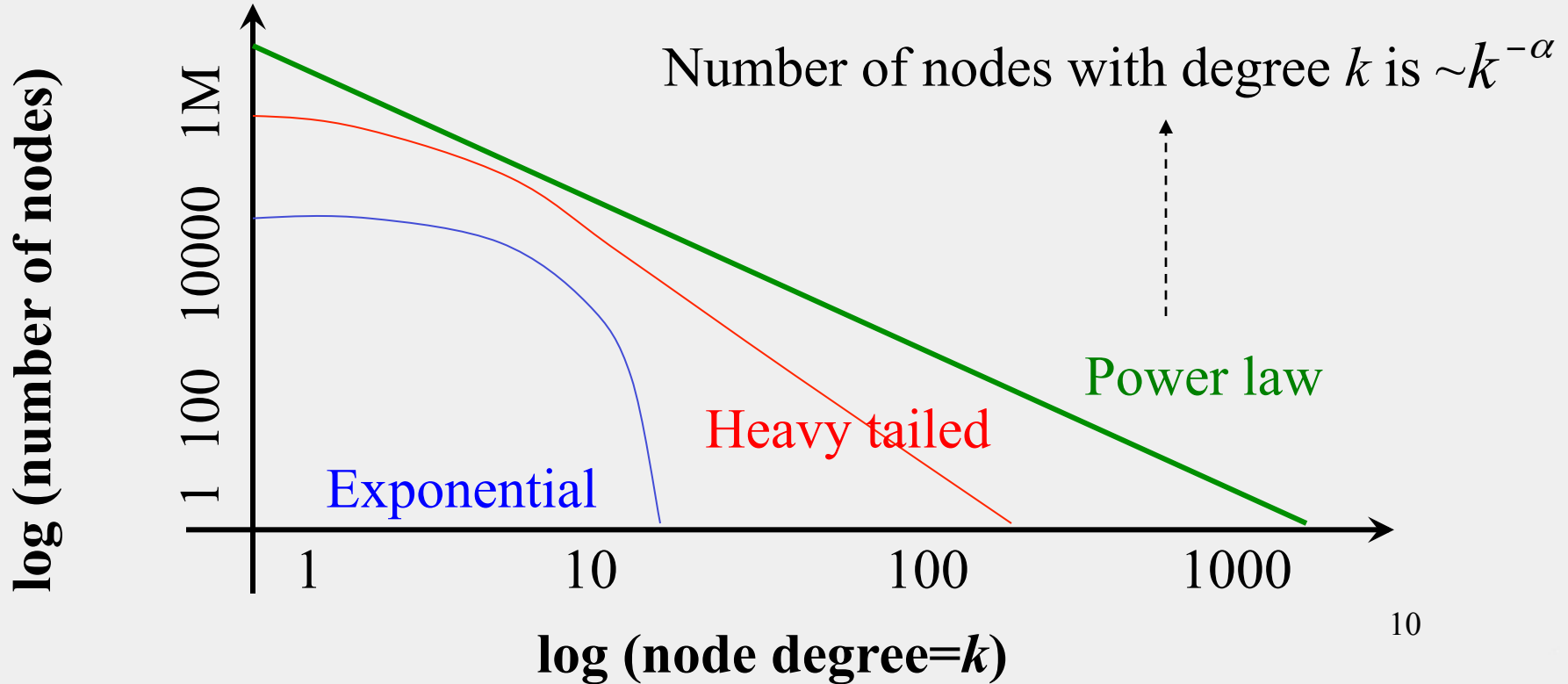
DEGREES

Degree of a vertex = number of its immediate neighbor vertices

Degree distribution – what is the probability of a given node having k edges (neighbors, friends, ...)

- Regular graph: all nodes same degree
- **Gaussian**
- Random graph: **Exponential** $e^{-k.c}$
- **Power law:** $k^{-\alpha}$

POWER LAW GRAPHS



SMALL-WORLD AND POWER-LAW

- A lot of small world networks are power law graphs
 - Internet backbone, telephone call graph, protein networks
 - WWW is a small-world graph and also a power-law graph with $\alpha=2.1-2.4$
 - Gnutella p2p system network has heavy-tailed degree distribution
- Power law networks also called *scale-free*
 - Gnutella has 3.4 edges per vertex, *independent of scale* (i.e., number of vertices)

SMALL-WORLD \neq POWER-LAW

- Not all small world networks are power law
 - E.g., co-author networks
- Not all power-law networks are small world
 - E.g., Disconnected power-law networks

RESILIENCE OF SMALL-WORLD+POWER-LAW

Most nodes have small degree, but a few nodes have high degree

Attacks on small world networks

- Killing a large number of randomly chosen nodes does not disconnect graph
- Killing a few high-degree nodes will disconnect graph

“A few (of the many thousand) nutrients are very important to your body”

“The Electric Grid is very vulnerable to attacks”

ROUTING IN SMALL-WORLD/POWER-LAW NETWORKS

- Build shortest-path routes between every pair of vertices
- => Most of these routes will pass via the few high-degree vertices in the graphs
 - => High-degree vertices are heavily overloaded
 - High-degree vertices more likely to suffer congestions or crash
- Same phenomenon in Electric power grid
- Solution may be to introduce some randomness in path selection; don't always use shortest path

SUMMARY

- Networks (graphs) are all around us
 - Man-made networks like Internet, WWW, p2p
 - Natural networks like protein networks, human social network
- Yet, many of these have common characteristics
 - Small-world
 - Power-law
- Useful to know this: when designing distributed systems that run on such networks
 - Can better predict how these networks might behave

ANNOUNCEMENTS

- HW4, MP4 released: Start NOW
 - Last HW and MP (yay!)
- HW3 solutions released