Computer Science 425
Distributed Systems

CS 425 / CSE 424 / ECE 428

Fall 2012

Indranil Gupta (Indy)

November 15, 2012

Lecture 24

Self-Stabilization

Reading: Handout from Ghosh's textbook

Motivation

- As the number of computing elements increase in distributed systems failures become more common
- We desire that fault-tolerance should be automatic, without external intervention
- Two kinds of fault tolerance
  - masking: application layer does not see faults, e.g., redundancy and replication
  - non-masking: system deviates, deviation is detected and then corrected: e.g., roll back and recovery
- Self-stabilization is a general technique for non-masking distributed systems
- We deal only with transient failures which corrupt data, but <u>not</u> crash-stop failures

Self-stabilization

- **Technique for spontaneous healing**
- **Guarantees eventual safety following failures**

Feasibility demonstrated by Dijkstra (CACM `74)

E. Dijkstra

Self-stabilizing systems

- Recover from any initial configuration to a legitimate configuration in a bounded number of steps, as long as the processes are not corrupted

- Assumption:

  Failures affect the state (and data) but not the program code

Self-stabilizing systems

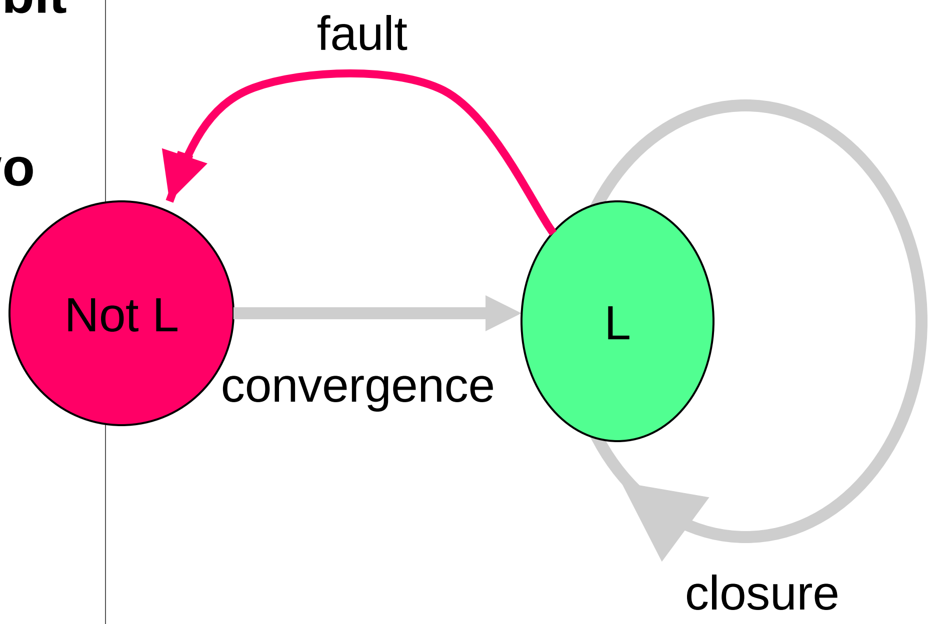
- **The ability to spontaneously recover from any initial state implies that <u>no initialization is ever required</u>.**

- **Such systems can be deployed ad hoc, and are guaranteed to function properly within bounded number of steps**

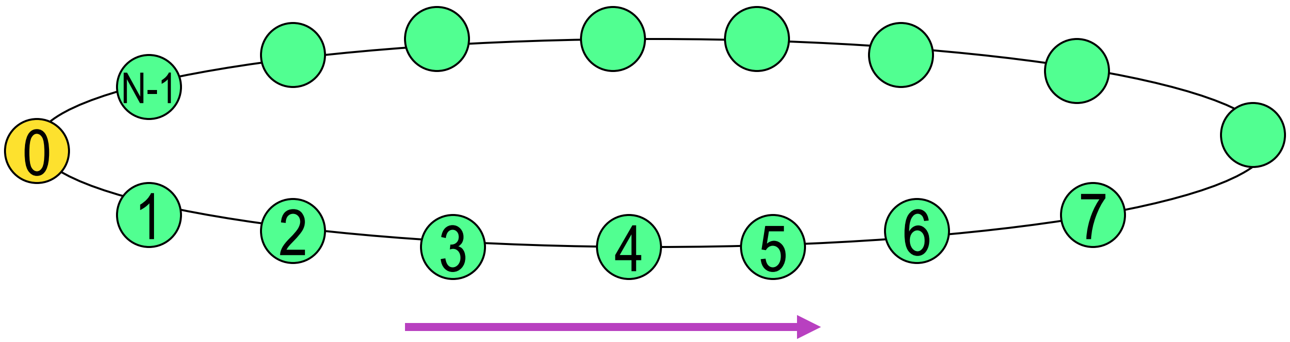
- **Guarantees-fault tolerance when the mean time between failures (MTBF) >> mean time to recovery (MTTR)**

Self-stabilizing systems

- **Self-stabilizing systems exhibit non-masking fault-tolerance**
- **They satisfy the following two criteria**
  - **Convergence**
  - **Closure**



Example 1: Stabilizing mutual exclusion in unidirectional ring



Consider a unidirectional ring of processes.

Counter-clockwise ring.

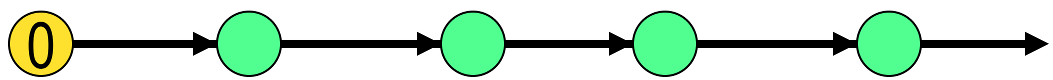
One special process (yellow above) is process with id=0

Legal configuration = exactly one token in the ring (Safety)

Desired "normal" behavior: single token circulates in the ring

Dijkstra's stabilizing mutual exclusion

N processes: 0, 1, …, N-1
state of process j is x[j] $\in$ {0, 1, 2, K-1}, where K > N



p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

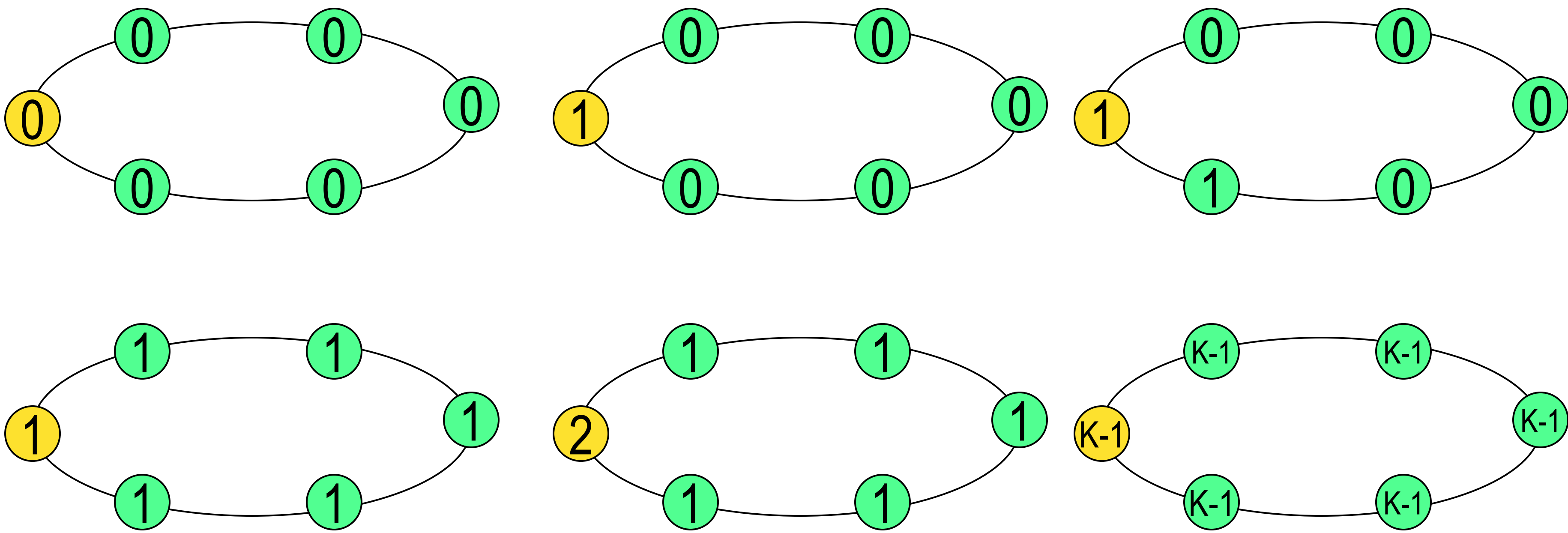
p_j j > 0 **if** x[j] $\neq$ x[j -1] **then** x[j] := x[j-1]

TOKEN is @ a process p = "if" condition is true @ process p

Legal configuration: only one process has token

Can start the system from an arbitrary initial configuration

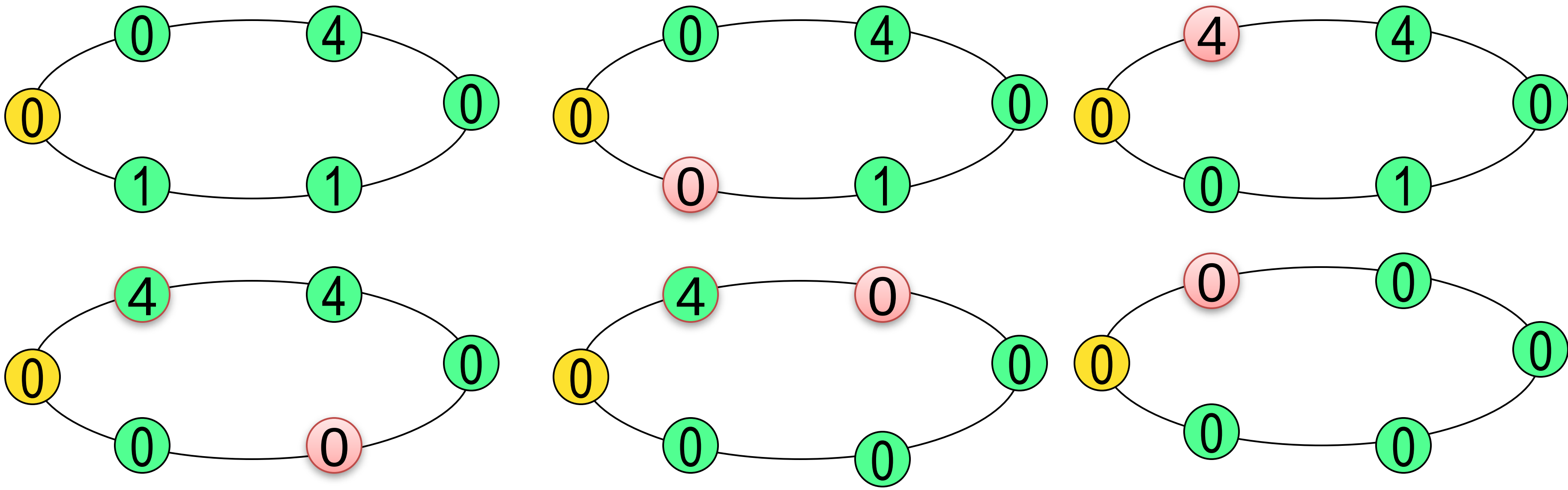
Example execution



p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

p_j j > 0 **if** x[j] ≠ x[j -1] **then** x[j] := x[j-1]

Stabilizing execution

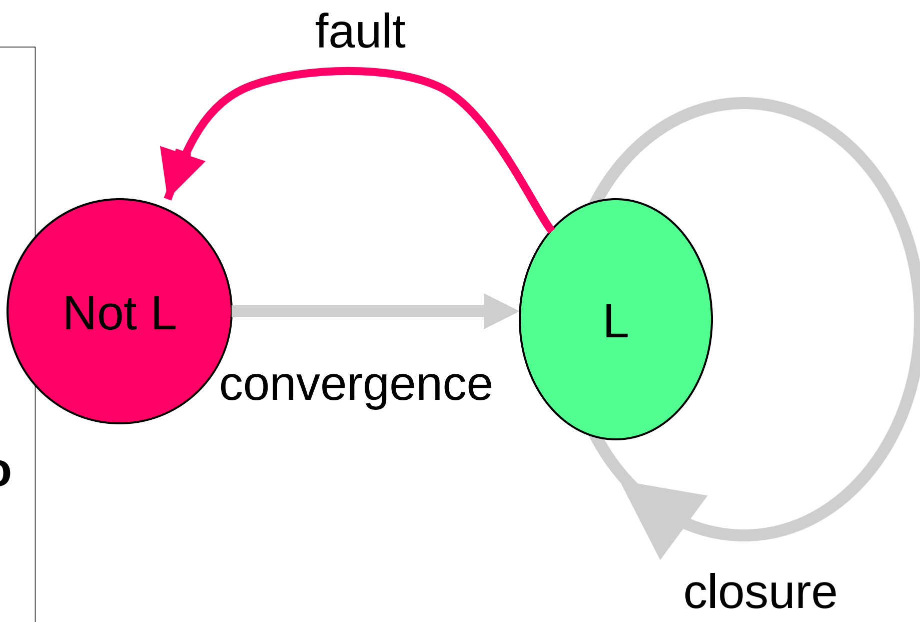


p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

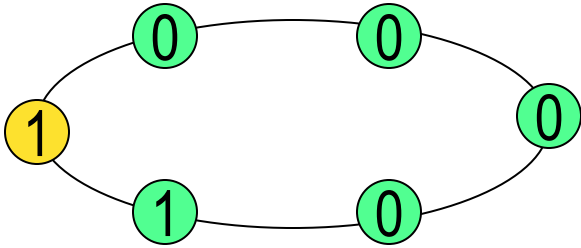
p_j j > 0 **if** x[j] ≠ x[j -1] **then** x[j] := x[j-1]

What Happens

- **Legal configuration = a configuration with a single token**
- **Perturbations or failures take the system to configurations with multiple tokens**
  - **e.g. mutual exclusion property may be violated**
- **Within finite number of steps, if no further failures occur, then the system returns to a legal configuration**

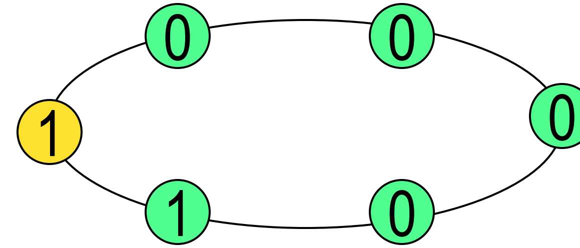


Why does it work ?



1. At any configuration, at least one process can make a move (has token)
2. Set of legal configurations is closed under all moves
3. Total number of possible moves from (successive configurations) never increases
4. Any illegal configuration C converges to a legal configuration in a finite number of moves

Why does it work ?

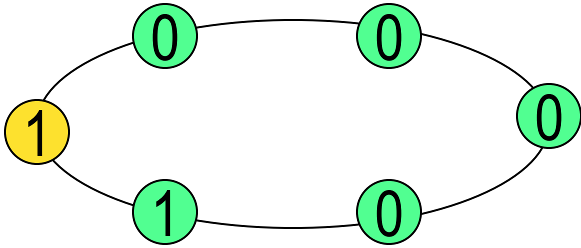


1. **At any configuration, at least one process can make a move (has token), i.e., if condition is false at all processes**
   - **Proof by contradiction: suppose no one can make a move**
   - **Then $p_1,\ldots,p_{N-1}$ cannot make a move**
   - **Then x[N-1] = x[N-2] = … x[0]**
   - **But this means that p_0 can make a move => contradiction**

p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

p_j j > 0 **if** x[j] ≠ x[j -1] **then** x[j] := x[j-1]

Why does it work ?



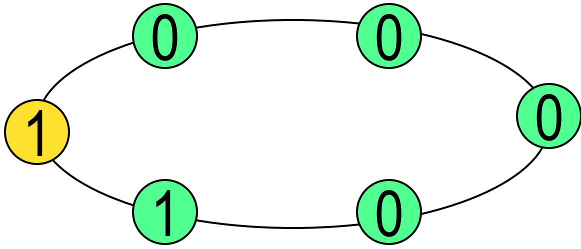
1. At any configuration, at least one process can make a move (has token)
2. Set of legal configurations is <u>closed</u> under all moves
   - If only p_0 can make a move, then for all i,j: x[i] = x[j]. After p_0's move, only p_1 can make a move
   - If only pi (i≠0) can make a move
     » for all j < i, x[j] = x[i-1]
     » for all k ≥ i, x[k] = x[i], and
     » x[i-1] ≠ x[i]

     in this case, after p_i's move only p_{i+1} can move

p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

p_j j > 0 **if** x[j] ≠ x[j -1] **then** x[j] := x[j-1]

Why does it work ?

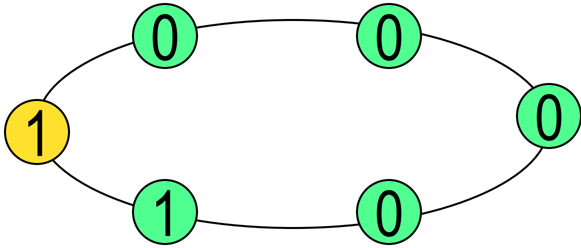


1. **At any configuration, at least one process can make a move (has token)**
2. **Set of legal configurations is closed under all moves**
3. **Total number of possible moves from (successive configurations) never increases**
   - **any move by p_i either enables a move for p_{i+1} or none at all**

p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

p_j j > 0 **if** x[j] ≠ x[j -1] **then** x[j] := x[j-1]

Why does it work ?



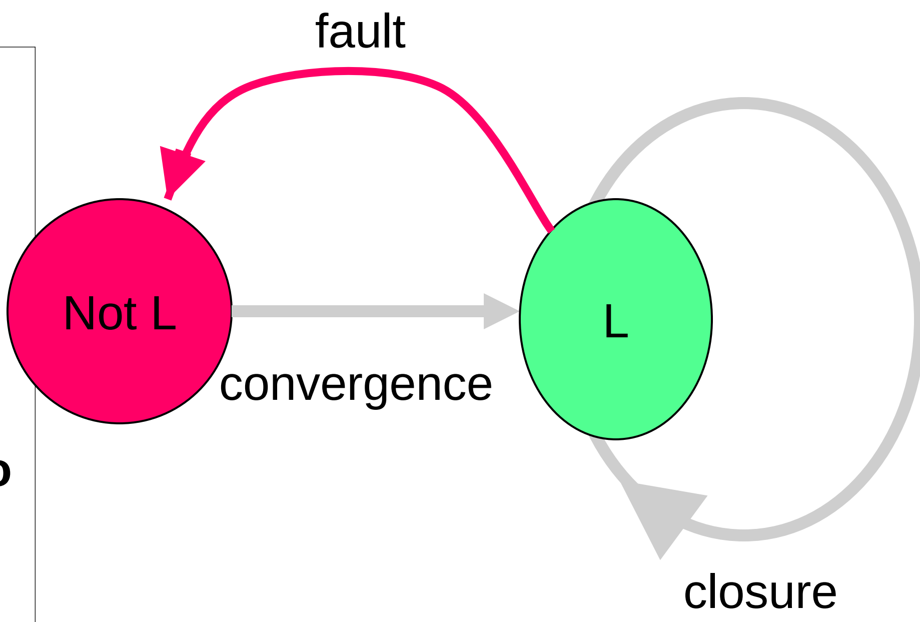
1. At any configuration, at least one process can make a move (has token)
2. Set of legal configurations is closed under all moves
3. Total number of possible moves from (successive configurations) never increases
4. Any illegal configuration C converges to a legal configuration in a finite number of moves
   - There must be a value, say v, that does not appear in C (since K > N)
   - Except for p_0, none of the processes create new values (since they only copy values)
   - Thus p_0 takes infinitely many steps, and since it only self-increments, it eventually sets x[0] = v (within K steps)
   - Soon after, all other processes copy value v and a legal configuration is reached in N-1 steps

p_0 **if** x[0] = x[N-1] **then** x[0] := x[0] + 1

p_j j > 0 **if** x[j] ≠ x[j -1] **then** x[j] := x[j-1]

Putting it All Together

- **Legal configuration = a configuration with a single token**
- **Perturbations or failures take the system to configurations with multiple tokens**
  - **e.g. mutual exclusion property may be violated**
- **Within finite number of steps, if no further failures occur, then the system returns to a legal configuration**



Summary

- **Many more self-stabilizing algorithms**
  - Self-stabilizing distributed spanning tree
  - Self-stabilizing distributed graph coloring
  - Not covered in the course – look them up on the web!
- **Reading for this lecture: Ghosh's textbook chapter**
  - But only what's on the slides is material
- **Have a good Thanksgiving break!**
- **HW4 and MP4 have been released - due soon after break (but not immediately after)!**