

## Energy

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To Turn-off or not to Turn-off

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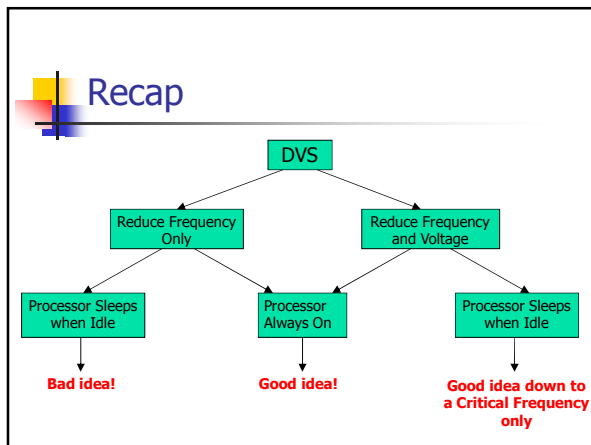
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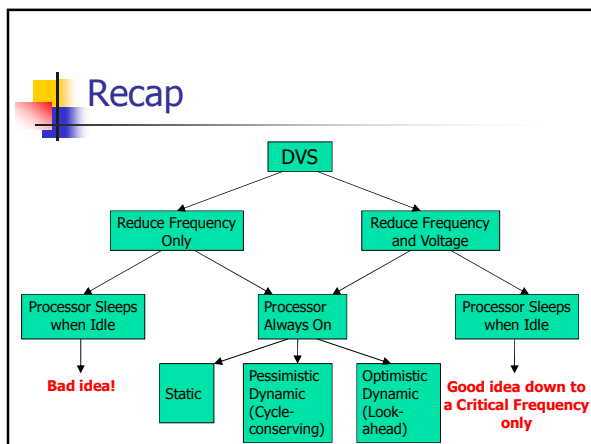
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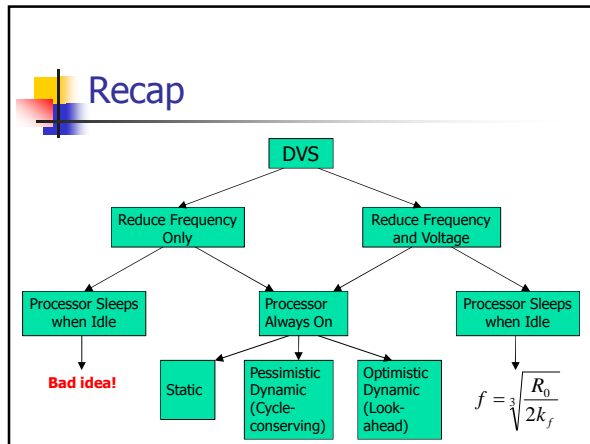
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**Turning Processors Off  
The Cost of Wakeup**

- Energy expended on wakeup,  $E_{wake}$
- To sleep or not to sleep?

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**Turning Processors Off  
The Cost of Wakeup**

- Energy expended on wakeup,  $E_{wake}$
- To sleep or not to sleep?
  - Not to sleep (for time  $t$ ):  

$$E_{no-sleep} = (k_v V^2 f + R_0) t$$
  - To sleep (for time  $t$ ) then wake up:  

$$E_{sleep} = P_{sleep} t + E_{wake}$$

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## Turning Processors Off The Cost of Wakeup

- Energy expended on wakeup,  $E_{wake}$
- To sleep or not to sleep?
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$$E_{no-sleep} = (k_v V^2 f + R_0) t$$
  - To sleep (for time  $t$ ) then wake up:
 
$$E_{sleep} = P_{sleep} t + E_{wake}$$
  - To save energy by sleeping:  $E_{sleep} < E_{no-sleep}$ 

$$t > \frac{E_{wake}}{k_v V^2 f + R_0 - P_{sleep}}$$

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## Turning Processors Off The Cost of Wakeup

- Energy expended on wakeup,  $E_{wake}$
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$$t > \frac{E_{wake}}{k_v V^2 f + R_0 - P_{sleep}}$$
- ← Minimum sleep interval

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## Dynamic Power Management

- DPM refers to turning devices off (or putting them in deep sleep modes)
- Device wakeup has a cost that imposes a minimum sleep interval (a breakeven time)
- DPM must maximize power savings due to sleep while maintaining schedulability

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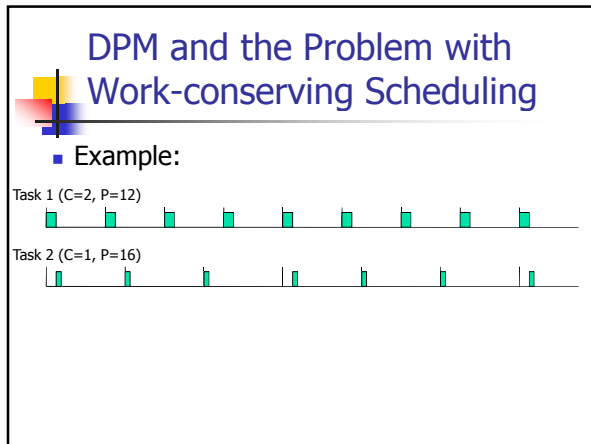
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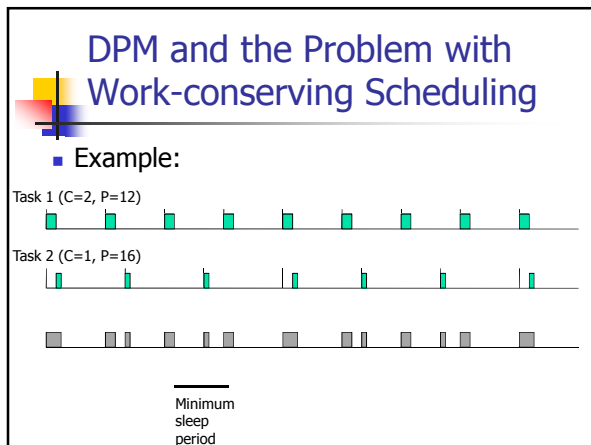
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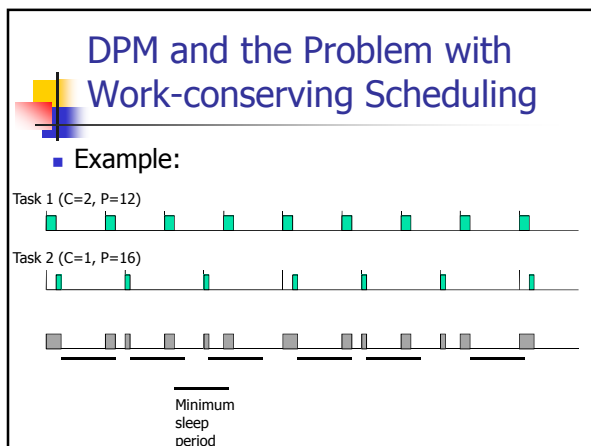
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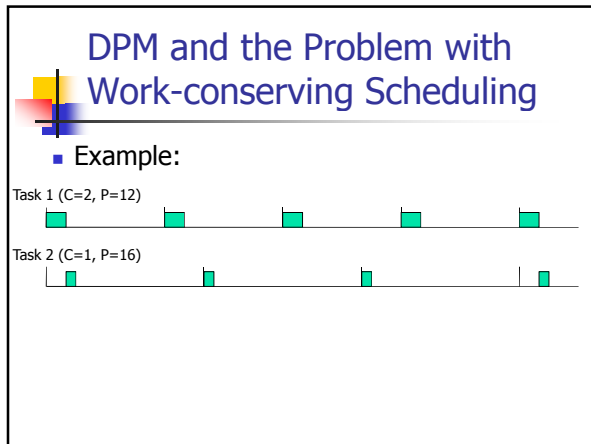
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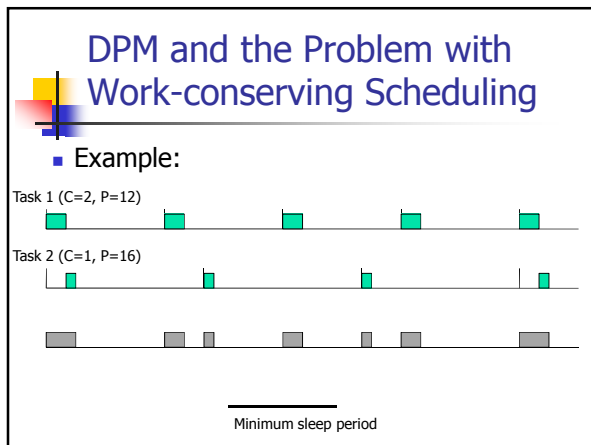
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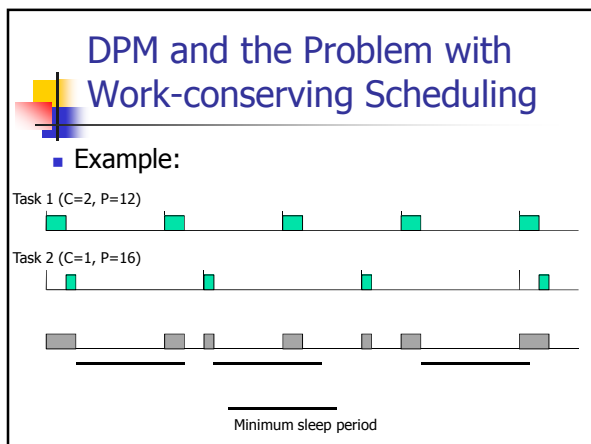
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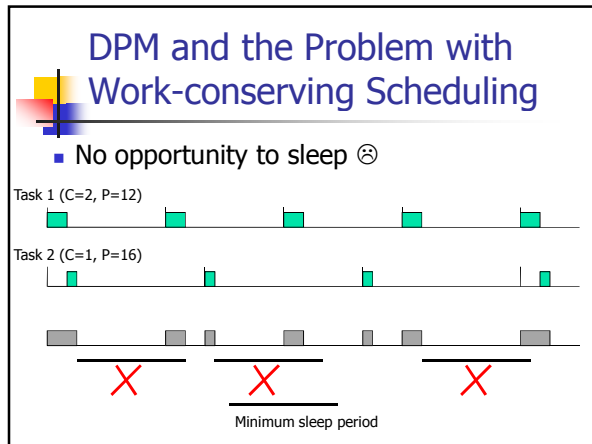
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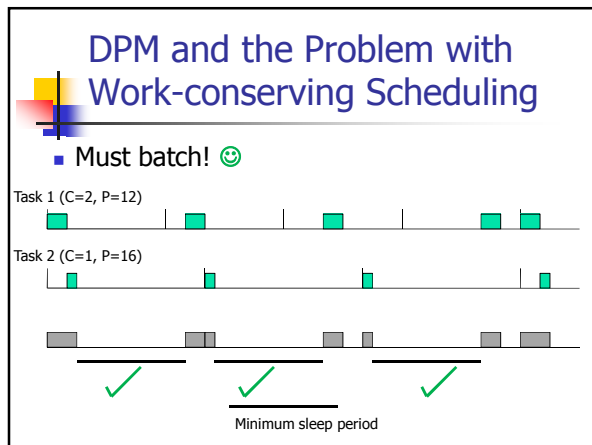
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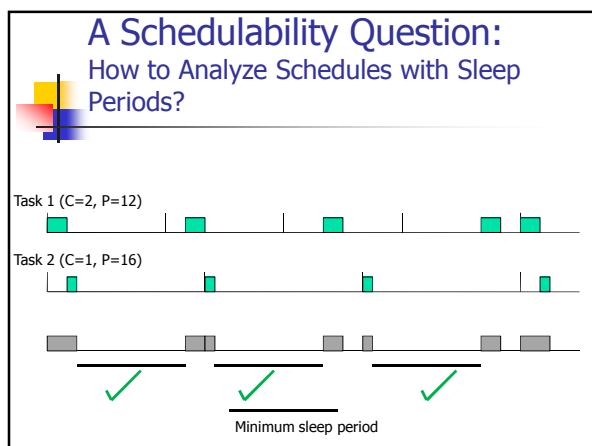
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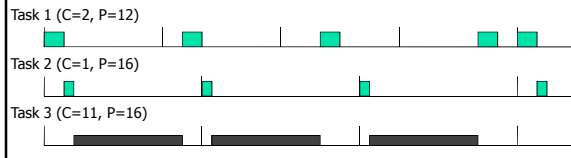
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### A Schedulability Question: How to Analyze Schedules with Sleep Periods?

- Option 1: Treat sleep periods like a sporadic task. Use the Liu and Layland utilization bound for schedulability. Problems?




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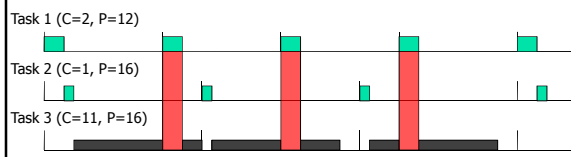
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### A Schedulability Question: How to Analyze Schedules with Sleep Periods?

- Option 1: Treat sleep periods like a sporadic task. Use the Liu and Layland utilization bound for schedulability. Problems?
  - Does not work because the "sleep task" cannot be preempted, whereas the rest of the tasks are preemptible. The utilization bound works only for fully preemptive scheduling.




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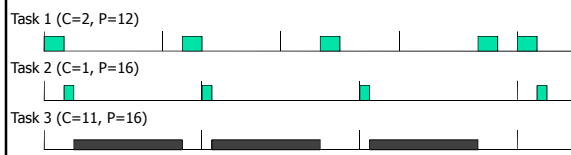
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### A Schedulability Question: How to Analyze Schedules with Sleep Periods?

- Option 2: Treat sleep periods like the *highest-priority* sporadic task. Use the Liu and Layland utilization bound for schedulability. Problems?




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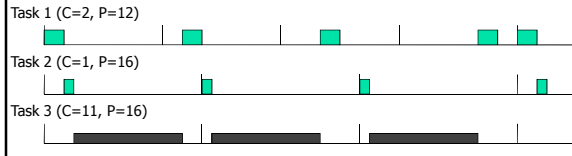
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## A Schedulability Question: How to Analyze Schedules with Sleep Periods?

- Option 2: Treat sleep periods like the *highest-priority* sporadic task. Use the Liu and Layland utilization bound for schedulability. Problems?
  - Does not work because the "sleep task" may need to have a larger period than the actual top-priority task, which contradicts rate-monotonic scheduling. The bound does not work.




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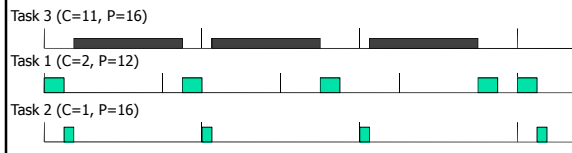
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## A Schedulability Question: How to Analyze Schedules with Sleep Periods?

- Option 3: Treat sleep periods like the *highest-priority* sporadic task. Use *response time analysis* for schedulability. Problems?




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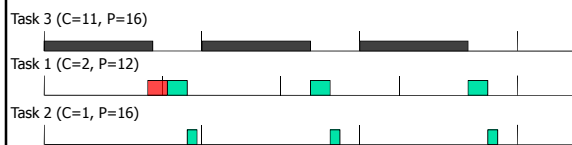
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## Device Forbidden Regions

- Option 3: Treat sleep periods like the *highest-priority* sporadic task. Use *response time analysis* for schedulability. Problems?
  - A Valid solution, but pessimistic. (Called: Device Forbidden Regions. Published in RTAS 2008.)




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## DVS on Homogeneous Multiprocessors

- Consider a set of tasks, where task  $i$  has period  $P_i$  and total number of cycles  $C_i$ 
  - Sort tasks from largest to smallest utilization  $C_i/P_i$
  - Assign tasks one at a time (largest-first) to the least utilized processor
  - Apply one of the previous algorithms on each processor separately

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## Question

- From the perspective of minimizing energy, is it always a good idea to use up all processors?

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## How Many Processors to Use?

- Consider using one processor at frequency  $f$  versus two at frequency  $f/2$
- Case 1: Total power for one processor
  - $k_f f^3 + R_0$
- Case 2: Total power for two processors
  - $2 \{k_f (f/2)^3 + R_0\} = k_f f^3/4 + 2 R_0$

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### How Many Processors to Use?

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- Case 1: Total power for one processor
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- Case 2: Total power for two processors
  - $2 \{k_f (f/2)^3 + R_0\} = k_f f^3/4 + 2 R_0$
- The general case:  $n$  processors
  - $n \{k_f (f/n)^3 + R_0\} = k_f f^3/n^2 + n R_0$

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### How Many Processors to Use?

- The general case:  $n$  processors
  - $\text{Power} = n \{k_f (f/n)^3 + R_0\} = k_f f^3/n^2 + n R_0$
  - $d\text{Power}/dn = -2 k_f f^3/n^3 + R_0 = 0$

$$n = \sqrt[3]{\frac{2k_f f^3}{R_0}}$$

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### How Many Processors to Use?

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- What if  $n$  is not an integer?

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### Advanced Configuration and Power Interface (ACPI Standard)

- C-states (idle states)
- P-states (dynamic voltage and frequency scaling)

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### Turning a Processor Off

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