Objectives

You should be able to...

Partial Evaluation

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- ► Explain the difference between Interpreters and Compilers mathematically
- ► Annotate a program according to the expression binding times
- Explain the difference between online and offline partial evaluation
- ► Specialize a simple program according to its static input
- ► Describe the three Futamura projections





Interpreters and Compilers

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An Interpreter

Notations

- \blacktriangleright Let $\mathcal S$ be a language.
- ▶ Let M be a program in language S.
- \blacktriangleright Let lower case letters be values in \mathcal{S} .
- \blacktriangleright An S-interpreter is a program I such that

$$I(M,s,d) \rightarrow x$$

 \blacktriangleright An S-partial evaluator is a program

$$P(M,s) \rightarrow M_s$$

such that

$$M_s(d) = M(s,d)$$

Some examples

$$P(\texttt{printf}, \texttt{"%s"}) \rightarrow \texttt{puts}$$

$$P(\mathtt{pow(n,x)},2) \to \lambda \mathtt{x}$$
 . \mathtt{x} * \mathtt{x}

P()

Basic Operation

Online

- ▶ Like eval, but distinguishes between "known" and "unknown" values.
- ► Expressions that have all known sub-expressions are specialized.
- ► Everything else is residualized.
- More aggressive, but can cause instability.

Offline

- ► A preprocessor called a *binding time analyser* annotates the source program.
 - ▶ Everything that is known for sure is marked as known.
 - ► Everything else is marked as unknown.
- ▶ The partial evaluator then follows the annotations.
- ► Can lose opportunity to specializes, but more stability.



BTA Example

- We underline the things that are known.
- ▶ We start with the input n.
- ► We annotate the "leaves"
- ▶ If all subexpressions are known, so is the expression.
- ▶ It will unroll functions that the inputs are partially known.

```
1 pow n x =
if n > 0
  then x * pow (n-1) x
  else 1
```

```
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Binding Time Analyzer

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The First Futamura Projection

$$P(I,S) \mapsto I_S$$

where $I_S(D) = I(S,D)$

Compilation

- ▶ We have fed an interpreter to our parial evaluator.
- ▶ The result is I_S ... this is a compiled program!
- ► I_S usually runs 4–10 times faster than I(S, P).

The Second Futamura Projection

$$P(P,I) \mapsto P_I$$

where $P_I(S) = P(I,S)$
and $P(I,S)(D) = I_S(D) = I(S,D)$

Producing a Compiler

- ▶ Notice what P_I actually does.
- ▶ We wrote an interpeter, and got a compiler...
- ▶ ... for free.

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The Third Futamura Projection

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and $P(I,S)(D) = I_S(D) = I(S,D)$

Compiler Generator

- ▶ Well, maybe not entirely free. It costs something to run P(P, I).
- ▶ But, we can specialize P to run these, so that P_P is faster.
- ▶ This is called a *code generator* or *compiler generator*.

