Programming Languages and Compilers (CS 421)



Grigore Rosu 2110 SC, UIUC

http://courses.engr.illinois.edu/cs421

Slides by Elsa Gunter, based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

4/10/2014

Semantics

- Expresses the meaning of syntax
- Static semantics
 - Meaning based only on the form of the expression without executing it
 - Usually restricted to type checking / type inference

4/10/2014



Dynamic semantics



- Method of describing meaning of executing a program
- Several different types:
 - Operational Semantics
 - Axiomatic Semantics
 - Denotational Semantics

4/10/2014

Dynamic Semantics



- Different languages better suited to different types of semantics
- Different types of semantics serve different purposes

4/10/2014



Operational Semantics



- Start with a simple notion of machine
- Describe how to execute (implement) programs of language on virtual machine, by describing how to execute each program statement (ie, following the structure of the program)
- Meaning of program is how its execution changes the state of the machine
- Useful as basis for implementations

4/10/2014

Axiomatic Semantics

- Also called Floyd-Hoare Logic
- Based on formal logic (first order predicate calculus)
- Axiomatic Semantics is a logical system built from *axioms* and *inference rules*
- Mainly suited to simple imperative programming languages



Axiomatic Semantics

- Used to formally prove a property (post-condition) of the state (the values of the program variables) after the execution of program, assuming another property (pre-condition) of the state before execution
- Written : {Precondition} Program {Postcondition}
- Source of idea of loop invariant

4/10/2014



Denotational Semantics

- Construct a function M assigning a mathematical meaning to each program construct
- Lambda calculus often used as the range of the meaning function
- Meaning function is compositional: meaning of construct built from meaning of parts
- Useful for proving properties of programs

4/10/2014



Natural Semantics



- Aka Structural Operational Semantics, aka "Big Step Semantics"
- Provide value for a program by rules and derivations, similar to type derivations
- Rule conclusions look like

(C, m) \ \ m' or (E, m) ↓ v

4/10/2014



Simple Imperative Programming Language

- *I* ∈ *Identifiers*
- N ∈ Numerals
- *B* ::= true | false | *B* & *B* | *B* or *B* | not *B* |E < E|E = E
- E::= N / I / E + E / E * E / E E / E
- C::= skip | C,C | I::= E | if B then Celse Cfi | while B do Cod

4/10/2014



4/10/2014

Natural Semantics of Atomic Expressions

- Identifiers: $(I,m) \downarrow m(I)$
- Numerals are values: $(N,m) \downarrow N$
- Booleans: (true, m) \(\psi\$ true (false m) \downarrow false

Booleans:

$$\frac{(\textit{B},\textit{m}) \Downarrow \text{ false}}{(\textit{B} \& \textit{B}',\textit{m}) \Downarrow \text{ false}} \frac{(\textit{B},\textit{m}) \Downarrow \text{ true } (\textit{B}',\textit{m}) \Downarrow \textit{b}}{(\textit{B} \& \textit{B}',\textit{m}) \Downarrow \textit{b}}$$



Relations

$$\underbrace{(E, m) \Downarrow U \quad (E', m) \Downarrow V \quad U \sim V = b}_{(E \sim E', m) \Downarrow b}$$

- By $U \sim V = b$, we mean does (the meaning of) the relation \sim hold on the meaning of Uand V
- May be specified by a mathematical expression/equation or rules matching U and

4/10/2014 13



Arithmetic Expressions

$$\frac{(E, m) \Downarrow U \quad (E', m) \Downarrow V \quad U \ op \ V = N}{(E \ op \ E', \ m) \Downarrow N}$$

where *N* is the specified value for *U op V*

4/10/2014

14



Commands

(skip, m) $\downarrow m$ Skip:

Assignment:

 $\frac{(E,m) \Downarrow V}{(I::=E,m) \Downarrow m[I < -- V]}$

Sequencing: $(C,m) \Downarrow m' (C',m') \Downarrow m''$ $(C;C',m) \Downarrow m''$



If Then Else Command

 $\frac{(B,m) \Downarrow \text{true } (C,m) \Downarrow m'}{(\text{if } B \text{ then } C \text{ else } C' \text{fi, } m) \Downarrow m'}$

 $\underbrace{(B,m) \Downarrow \text{ false } (C',m) \Downarrow m'}_{\text{(if } B \text{ then } C \text{ else } C' \text{fi, } m) \Downarrow m'}$

4/10/2014

16



4/10/2014

While Command

(B,m) ↓ false (while $B \text{ do } C \text{ od}, m) \downarrow m$

(B,m) \forall true (C,m) \forall m' (while B do C od, m') \forall m''(while B do C od, m) $\downarrow m''$

4/10/2014



15

17

Example: If Then Else Rule

(if
$$x > 5$$
 then $y := 2 + 3$ else $y := 3 + 4$ fi,
 $\{x -> 7\}$) \downarrow ?

4/10/2014





Example: Arith Relation

$$(x > 5, \{x \to 7\})$$
 (if $x > 5$ then $y := 2 + 3$ else $y := 3 + 4$ fi, $\{x \to 7\}$) ?

? > ? = ?

$$\frac{(x,\{x->7\}) \ \ }{(x,\{x->7\}) \ \ }?}{(x > 5, \{x -> 7\}) \ \)?}$$
(if x > 5 then y:= 2 + 3 else y:=3 + 4 fi,

$$\{x -> 7\}) \ \ \ \$$
?

4/10/2014 19

4/10/2014

20

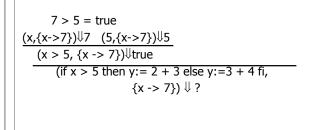
22



Example: Identifier(s)

Example: Arith Relation

7 > 5 = true $\frac{(x,\{x->7\}) \forall 7 \quad (5,\{x->7\}) \forall 5}{(x > 5, \{x -> 7\}) \forall ?}$ (if x > 5 then y:= 2 + 3 else y:= 3 + 4 fi, $\{x -> 7\}) \ \forall \ ?$



-

4/10/2014

4/10/2014

Example: If Then Else Rule

If then eise Ruie

4/10/2014

4/10/2014

21

Example: Assignment

7 > 5 = true $(x,(x->7)) \forall 7 \quad (5,(x->7)) \forall 5$ $(x > 5, (x -> 7)) \forall \text{true}$ (if x > 5 then y := 2 + 3 else y := 3 + 4 fi, $(x -> 7) \forall ?$



4/10/2014 25



$$2 + 3 = 5$$

$$(2,\{x->7\}) \lor 2 \quad (3,\{x->7\}) \lor 3$$

$$7 > 5 = \text{true} \qquad (2+3,\{x->7\}) \lor ?$$

$$(x,\{x->7\}) \lor 7 \quad (5,\{x->7\}) \lor 5 \qquad (y:= 2+3,\{x->7\})$$

$$(x > 5, \{x -> 7\}) \lor \text{true} \qquad \lor ?$$

$$(if x > 5 \text{ then } y:= 2+3 \text{ else } y:=3+4 \text{ fi,}$$

$$\{x -> 7\}) \lor ?$$

4/10/2014 26

Example: Arith Op

4/10/2014 27

Example: Assignment

$$\begin{array}{c}
2 + 3 = 5 \\
(2,\{x->7\}) \downarrow 2 \quad (3,\{x->7\}) \downarrow 3 \\
7 > 5 = \text{true} \qquad (2+3,\{x->7\}) \downarrow 5 \\
(x,\{x->7\}) \downarrow 7 \quad (5,\{x->7\}) \downarrow 5 \\
(x > 5, \{x -> 7\}) \downarrow \text{true} \qquad \downarrow \{x->7, y->5\} \\
(if x > 5 \text{ then } y:= 2 + 3 \text{ else } y:= 3 + 4 \text{ fi,} \\
(x -> 7\}) \downarrow ?
\end{array}$$

4/10/2014

28



Example: If Then Else Rule

$$2 + 3 = 5$$

$$\underbrace{(2,\{x->7\}) \downarrow 2 \quad (3,\{x->7\}) \downarrow 3}$$

$$7 > 5 = \text{true} \qquad \underbrace{(2+3, \{x->7\}) \downarrow 5}$$

$$\underbrace{(x,\{x->7\}) \downarrow 7 \quad (5,\{x->7\}) \downarrow 5}$$

$$\underbrace{(x > 5, \{x -> 7\}) \downarrow \text{true}}$$

$$\underbrace{(x > 5, \{x -> 7\}) \downarrow \text{true}}$$

$$\underbrace{(x > 5, \{x -> 7\}) \downarrow \text{true}}$$

$$\underbrace{(x > 7, y->5)}$$

$$\underbrace{(x > 7, y->5)}$$

$$\underbrace{(x -> 7, y->5)}$$

4/10/2014 29



Let in Command

$$\frac{(E,m) \ \forall v \ (C,m[I < -v]) \ \forall \ m'}{(\text{let } I = E \text{ in } C, \ m) \ \forall \ m''}$$

Where m''(y) = m'(y) for $y \neq I$ and m''(I) = m(I) if m(I) is defined, and m''(I) is undefined otherwise

4/10/2014



4/10/2014



4/10/2014 32



Comment

- Simple Imperative Programming Language introduces variables implicitly through assignment
- The let-in command introduces scoped variables explictly
- Clash of constructs apparent in awkward semantics

4/10/2014



31

33

Interpretation Versus Compilation

- A compiler from language L1 to language L2 is a program that takes an L1 program and for each piece of code in L1 generates a piece of code in L2 of same meaning
- An interpreter of L1 in L2 is an L2 program that executes the meaning of a given L1 program
- Compiler would examine the body of a loop once; an interpreter would examine it every time the loop was executed

4/10/2014

34



Interpreter

- An Interpreter represents the operational semantics of a language L1 (source language) in the language of implementation L2 (target language)
- Built incrementally
 - Start with literals
 - Variables
 - Primitive operations
 - Evaluation of expressions
 - Evaluation of commands/declarations

4/10/2014

35



Interpreter

- Takes abstract syntax trees as input
 - In simple cases could be just strings
- One procedure for each syntactic category (nonterminal)
 - eq one for expressions, another for commands
- If Natural semantics used, tells how to compute final value from code
- If Transition semantics used, tells how to compute next "state"
 - To get final value, put in a loop

4/10/2014

36

4

Natural Semantics Example

- compute_exp (Var(v), m) = look_up v m
- compute_exp (Int(n), _) = Num (n)
- ...
- compute_com(IfExp(b,c1,c2),m) =
 if compute_exp (b,m) = Bool(true)
 then compute_com (c1,m)
 else compute_com (c2,m)

4/10/2014



Natural Semantics Example

- compute_com(While(b,c), m) =
 if compute_exp (b,m) = Bool(false)
 then m
 else compute_com
 (While(b,c), compute_com(c,m))
- May fail to terminate exceed stack limits
- Returns no useful information then

4/10/2014

37

38