

Programming Languages and Compilers (CS 421)

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<http://courses.engr.illinois.edu/cs421>

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

10/19/23

1

LR Parsing

- Read tokens left to right (L)
- Create a rightmost derivation (R)
- How is this possible?
- Start at the bottom (left) and work your way up
- Last step has only one non-terminal to be replaced so is right-most
- Working backwards, replace mixed strings by non-terminals
- Always proceed so that there are no non-terminals to the right of the string to be replaced

10/19/23

2

Example: $\langle \text{Sum} \rangle = 0 \mid 1 \mid (\langle \text{Sum} \rangle)$
| $\langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\langle \text{Sum} \rangle \Rightarrow$

$= 0 + 1 + 0$ shift

10/19/23

3

Example: $\langle \text{Sum} \rangle = 0 \mid 1 \mid (\langle \text{Sum} \rangle)$
| $\langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\langle \text{Sum} \rangle \Rightarrow$

$= (0 + 1) + 0$ shift
 $= 0 + 1 + 0$ shift

10/19/23

4

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| $\langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\langle \text{Sum} \rangle \Rightarrow$

$\Rightarrow (0 + 1) + 0$ reduce
 $= (0 + 1) + 0$ shift
 $= 0 + 1 + 0$ shift

10/19/23

5

Example: $\langle \text{Sum} \rangle = 0 \mid 1 \mid (\langle \text{Sum} \rangle)$
| $\langle \text{Sum} \rangle + \langle \text{Sum} \rangle$


$\langle \text{Sum} \rangle \Rightarrow$

$= (\langle \text{Sum} \rangle + 1) + 0$ shift
 $\Rightarrow (0 + 1) + 0$ reduce
 $= (0 + 1) + 0$ shift
 $= 0 + 1 + 0$ shift

10/19/23

6


Example

$$(0 + 1) + 0$$


10/19/23

19


Example

$$(\textcircled{0} + 1) + 0$$


10/19/23

20


Example

$$(\textcircled{0} + 1) + 0$$


10/19/23

21


Example

$$(\textcircled{0} + 1) + 0$$


10/19/23

22


Example

$$(\textcircled{0} + \textcircled{1}) + 0$$


10/19/23

23

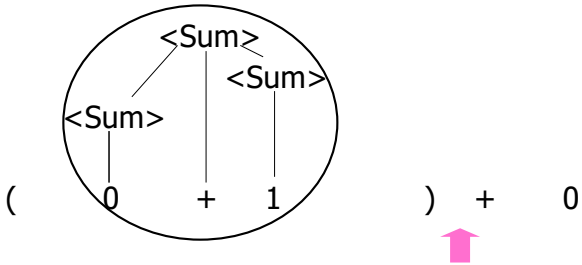
Example

$$(\textcircled{0} + \textcircled{1}) + 0$$


10/19/23

24

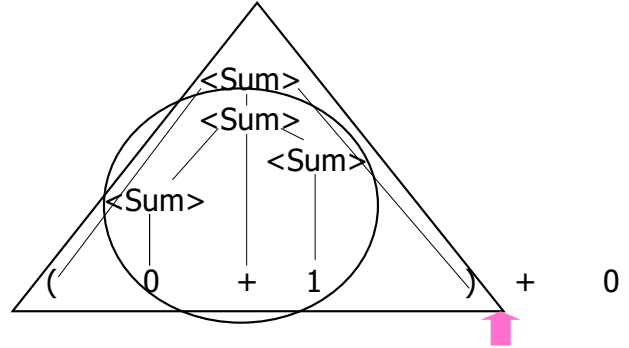
Example



10/19/23

25

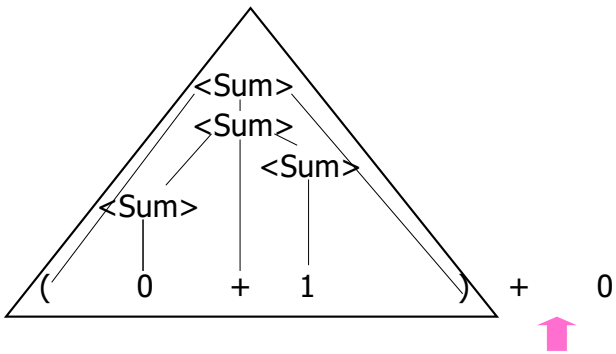
Example



10/19/23

26

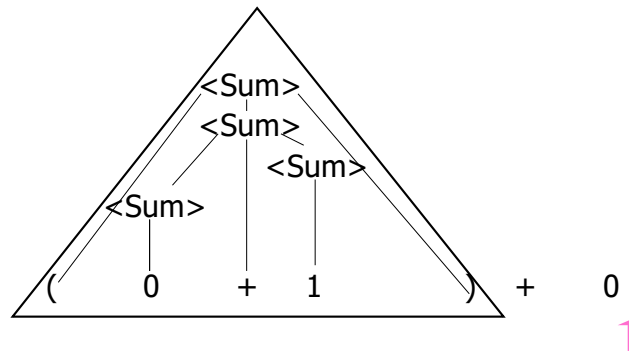
Example



10/19/23

27

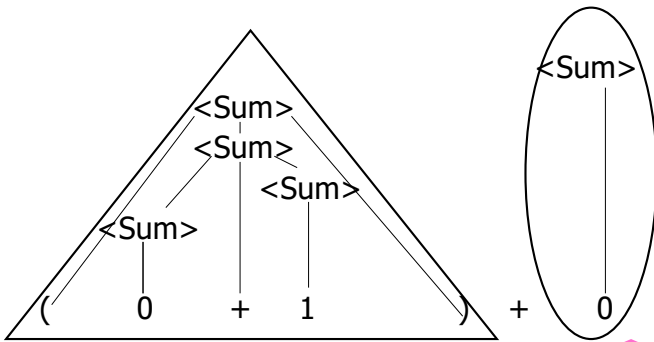
Example



10/19/23

28

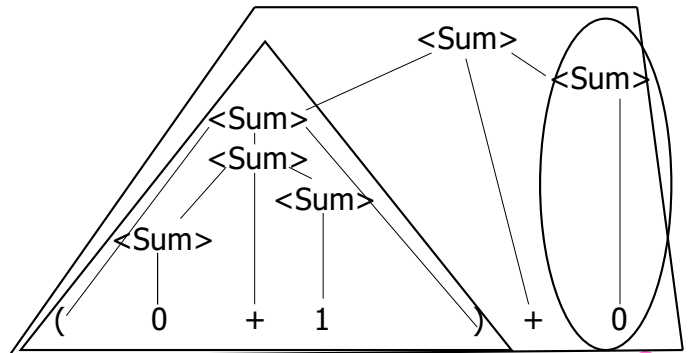
Example



10/19/23

29

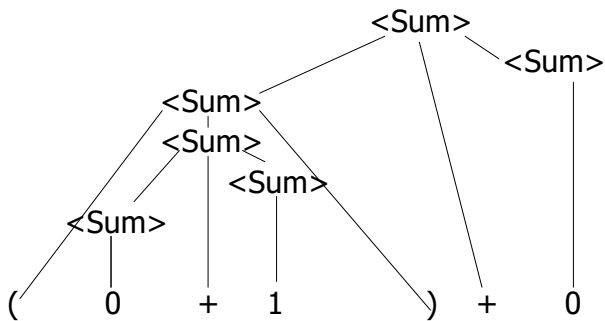
Example



10/19/23

30

Example



10/19/23

31

LR Parsing Tables

- Build a pair of tables, Action and Goto, from the grammar
 - This is the hardest part, we omit here
 - Rows labeled by states
 - For Action, columns labeled by terminals and “end-of-tokens” marker
 - (more generally strings of terminals of fixed length)
 - For Goto, columns labeled by non-terminals

10/19/23

32

Action and Goto Tables

- Given a state and the next input, Action table says either
 - **shift** and go to state n , or
 - **reduce** by production k (explained in a bit)
 - **accept or error**
- Given a state and a non-terminal, Goto table says
 - go to state m

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33

LR(i) Parsing Algorithm

- Based on push-down automata
- Uses states and transitions (as recorded in Action and Goto tables)
- Uses a stack containing states, terminals and non-terminals

10/19/23

34

LR(i) Parsing Algorithm

0. Insure token stream ends in special “end-of-tokens” symbol
1. Start in state 1 with an empty stack
2. Push **state**(1) onto stack
- 3. Look at next i tokens from token stream ($toks$) (don't remove yet)
4. If top symbol on stack is **state**(n), look up action in Action table at ($n, toks$)

10/19/23

35

LR(i) Parsing Algorithm

5. If action = **shift** m ,
 - a) Remove the top token from token stream and push it onto the stack
 - b) Push **state**(m) onto stack
 - c) Go to step 3

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36

LR(i) Parsing Algorithm

6. If action = **reduce** k where production k is $E ::= u$
- Remove $2 * \text{length}(u)$ symbols from stack (u and all the interleaved states)
 - If new top symbol on stack is **state**(m), look up new state p in $\text{Goto}(m, E)$
 - Push E onto the stack, then push **state**(p) onto the stack
 - Go to step 3

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37

LR(i) Parsing Algorithm

7. If action = **accept**
- Stop parsing, return success
8. If action = **error**,
- Stop parsing, return failure

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38

Adding Synthesized Attributes

- Add to each **reduce** a rule for calculating the new synthesized attribute from the component attributes
- Add to each non-terminal pushed onto the stack, the attribute calculated for it
- When performing a **reduce**,
 - gather the recorded attributes from each non-terminal popped from stack
 - Compute new attribute for non-terminal pushed onto stack

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39

Shift-Reduce Conflicts

- Problem:** can't decide whether the action for a state and input character should be **shift** or **reduce**
- Caused by ambiguity in grammar
- Usually caused by lack of associativity or precedence information in grammar

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40

Example: $\langle \text{Sum} \rangle = 0 \mid 1 \mid (\langle \text{Sum} \rangle)$
 $\mid \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\bullet 0 + 1 + 0$ shift
 $\rightarrow 0 \bullet + 1 + 0$ reduce
 $\rightarrow \langle \text{Sum} \rangle \bullet + 1 + 0$ shift
 $\rightarrow \langle \text{Sum} \rangle + \bullet 1 + 0$ shift
 $\rightarrow \langle \text{Sum} \rangle + 1 \bullet + 0$ reduce
 $\rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \bullet + 0$

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41

Example - cont

- Problem:** shift or reduce?
- You can shift-shift-reduce-reduce or reduce-shift-shift-reduce
- Shift first - right associative
- Reduce first- left associative

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42

Reduce - Reduce Conflicts

- **Problem:** can't decide between two different rules to reduce by
- Again caused by ambiguity in grammar
- **Symptom:** RHS of one production suffix of another
- Requires examining grammar and rewriting it
- Harder to solve than shift-reduce errors

Example

- $S ::= A \mid aB$ $A ::= abc$ $B ::= bc$

● abc shift
a ● bc shift
ab ● c shift
abc ●

- Problem: reduce by $B ::= bc$ then by $S ::= aB$, or by $A ::= abc$ then $S ::= A$?