



Quiz 4



Midterm 2 ADT, Second Chance

```
type `a option =  
| None  
| Some of `a
```



Programming Languages and Compilers (CS 421)

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<https://courses.grainger.illinois.edu/cs421/fa2023/>

Based heavily on slides by Elsa Gunter, which were based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha



Objectives for Today

- **Reminder:** We want to turn strings (code) into computer instructions
- Done in **phases**
 - Turn strings into abstract syntax trees (**parse**)
 - Translate abstract syntax trees into executable instructions (**interpret** or **compile**)
- Last week we started the first step of parsing, which is **lexing** those input strings into **tokens**
- Today we will finish **lexing** and move on to the rest of **parsing**



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Questions from last week?



Recap



Example : using generated file

```
# #use "test.ml";;
```

```
...
```

```
val main : Lexing.lexbuf -> result = <fun>
```

```
val __ocaml_lex_main_rec :
```

```
Lexing.lexbuf -> int -> result = <fun>
```

```
hi there 234 5.2
```

```
- : result = String "hi"
```



Example : using generated file

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hi there 234 5.2
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```
- : result = String "hi"
```

What happened to the rest?

Example : using generated file

```
# let b = Lexing.from_channel stdin;;
```

```
# main b;;
```

```
hi 673 there
```

```
- : result = String "hi"
```

```
# main b;;
```

```
- : result = Int 673
```

```
# main b;;
```

```
- : result = String "there"
```

Recall the hidden argument of type `lexbuf`



Example : using generated file

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# let b = Lexing.from_channel stdin;;
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```
# main b;;
```

```
- : result = String "there"
```

Recall the hidden argument of type `lexbuf`



Fancy Lexing



Problem

- How to get lexer to look at **more than the first token** at one time?
- **Answer: *action*** has to tell it to – **recursive calls**
- **Downside:** *Not* what you want to sew this together with ocaml yacc (parser generator)
- **Side Benefit:** can add “**state**” into lexing
- **Note:** already used this with the `_` case



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Example: Old Version

```
rule main = parse
| (digits)'. 'digits as f
  { Float (float_of_string f) }
| digits as n
  { Int (int_of_string n) }
| letters as s
  { String s }
| _ { main lexbuf }
```



Example: WIP New Version

rule main = parse

| (digits)'. 'digits as f

{ Float (float_of_string f) :: **main lexbuf** }

| digits as n

{ Int (int_of_string n) :: **main lexbuf** }

| letters as s

{ String s :: **main lexbuf** }

| _ { **main lexbuf** }



Example: New Version

rule main = parse

| (digits)'. 'digits as f

{ Float (float_of_string f) :: **main lexbuf** }

| digits as n

{ Int (int_of_string n) :: **main lexbuf** }

| letters as s

{ String s :: **main lexbuf** }

| **eof** { [] }

| **_** { **main lexbuf** }



Example Results

hi there 234 5.2

- : result list =

[String "hi"; String "there"; Int 234; Float 5.2]

Used Ctrl-d to send the end-of-file signal



Questions so far?



Dealing with Comments (No Nesting)

```
let open_comment = "("*
```

```
let close_comment = "*")"
```

```
rule main = parse
```

```
... (* same as last time *)
```

```
| open_comment { comment lexbuf }
```

```
| eof { [] }
```

```
| _ { main lexbuf }
```

```
and comment = parse
```

```
| close_comment { main lexbuf }
```

```
| _ { comment lexbuf }
```



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| open_comment { comment lexbuf }
| eof { [] }
| _ { main lexbuf }
and comment = parse
| close_comment { main lexbuf }
| _ { comment lexbuf }
```



Questions so far?



Dealing with Nested Comments

```
rule main = parse
```

```
...
```

```
| open_comment { comment 1 lexbuf }
```

```
| eof { [] }
```

```
| _ { main lexbuf }
```

```
and comment depth = parse
```

```
| open_comment { comment (depth+1) lexbuf }
```

```
| close_comment { if depth = 1 then main lexbuf  
  else comment (depth - 1) lexbuf }
```

```
| _ { comment depth lexbuf }
```



Dealing with Nested Comments

rule main = parse

...

| open_comment { comment 1 lexbuf }

| eof { [] }

| _ { main lexbuf }

and comment depth = parse

| **open_comment** { comment (depth + 1) lexbuf }

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Dealing with Nested Comments

rule main = parse

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```
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```



Note: No Longer Regular!



Often easier to defer non-regular things to the parser generator.



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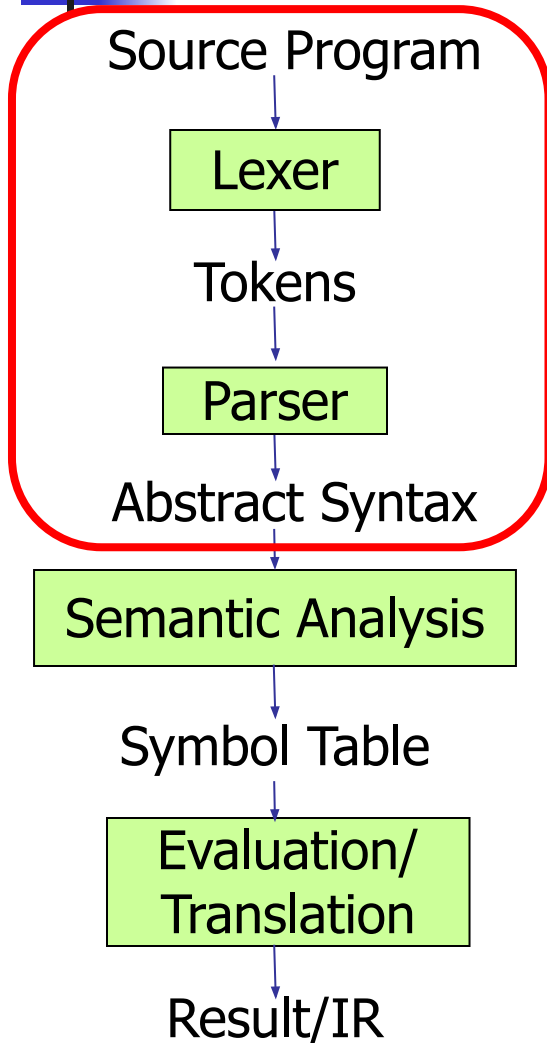


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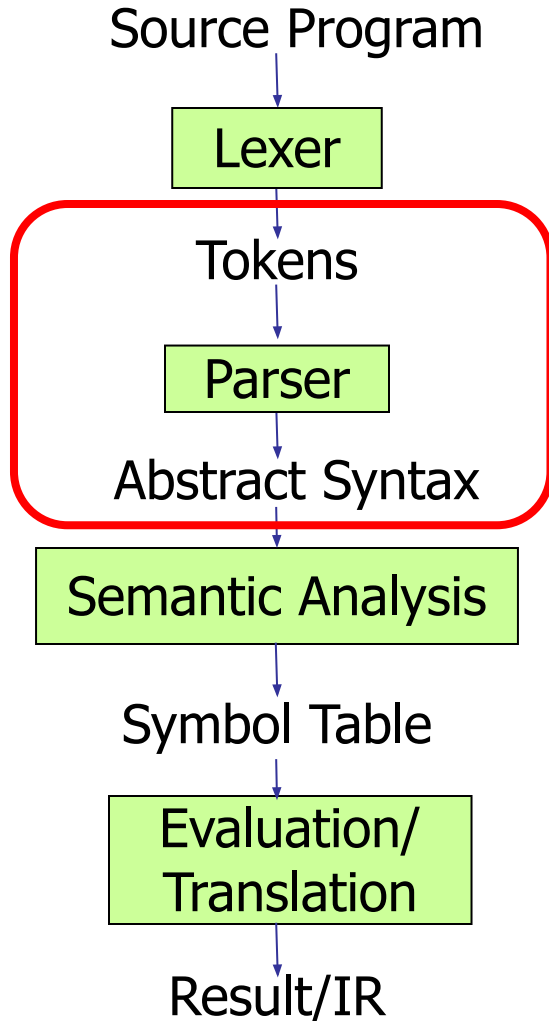


Parsing

Lexing and Parsing

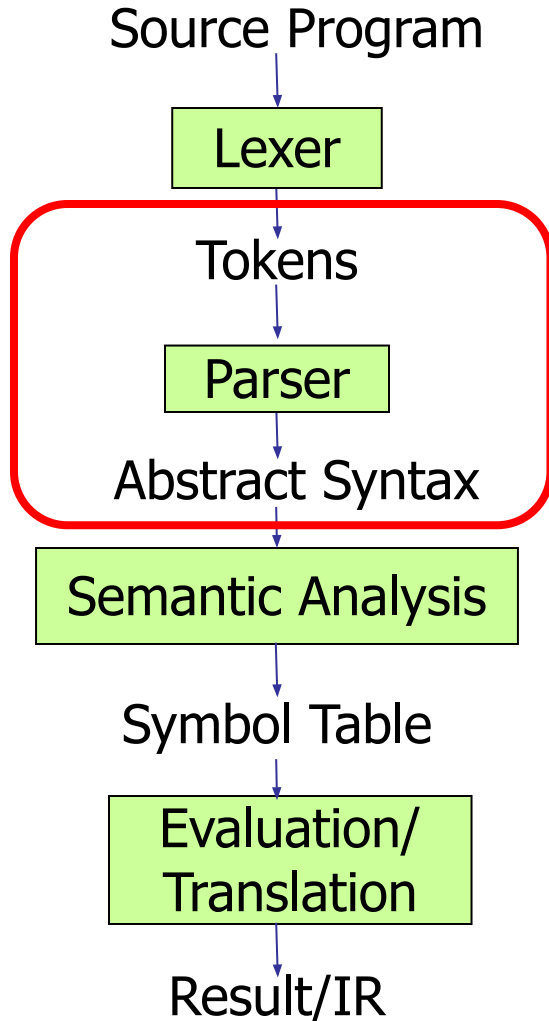


Lexing and Parsing



To **parse** our source program and get **abstract syntax**, we need a **grammar** defined in terms of the kinds of **tokens** we get out of our lexer.

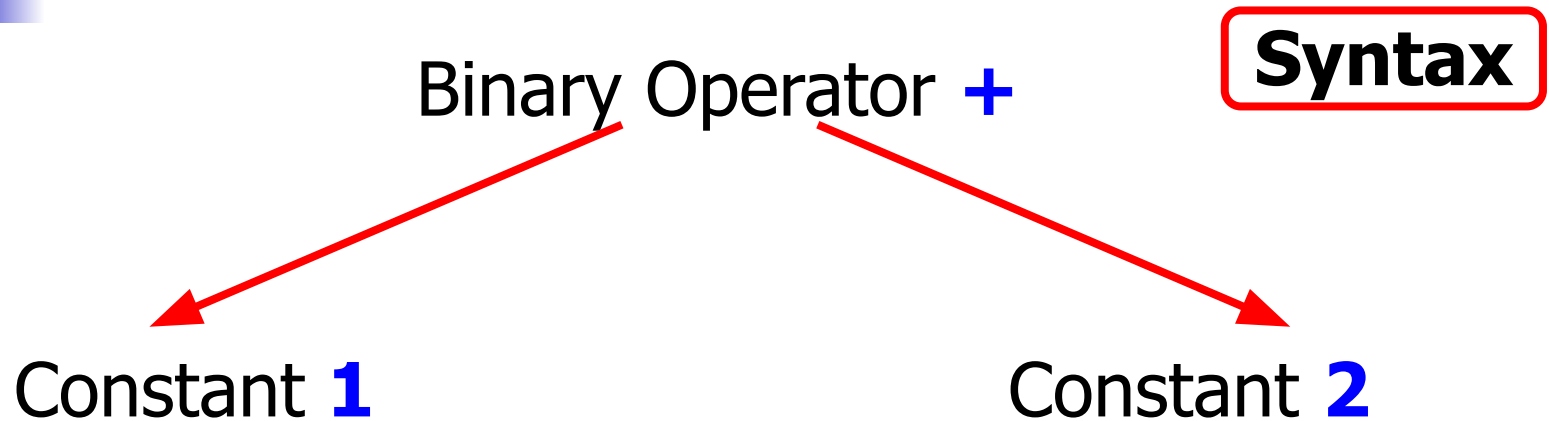
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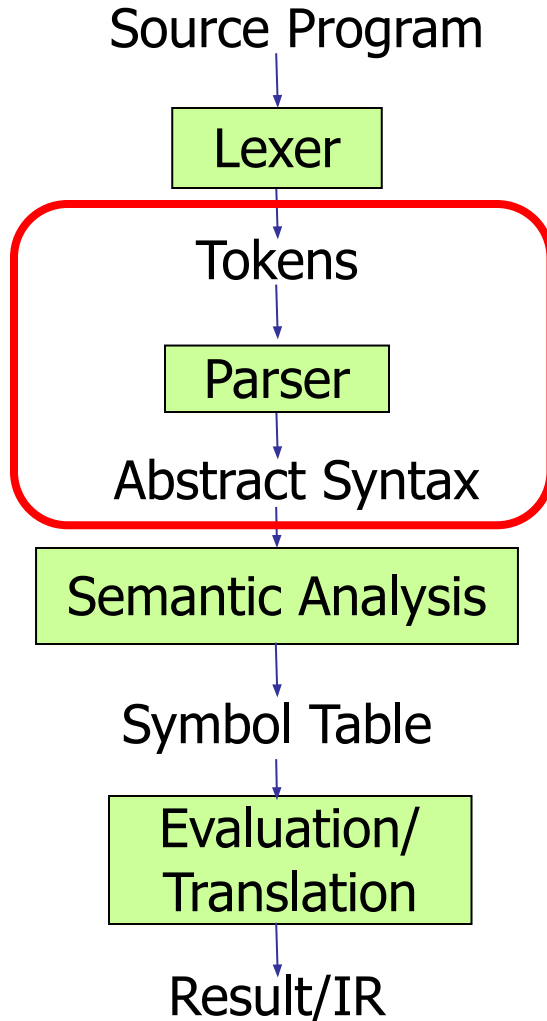
The output, an **abstract syntax tree**, will track not just categories, but also **structure**.

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Sample Grammar

- Language: Parenthesized sums of 0's and 1's

$\langle \text{Sum} \rangle ::= 0$

$\langle \text{Sum} \rangle ::= 1$

$\langle \text{Sum} \rangle ::= \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\langle \text{Sum} \rangle ::= (\langle \text{Sum} \rangle)$

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Context-Free Grammars



BNF Grammars

- A notation for a **context-free grammar**
- Start with a set of characters **a, b, ... (terminals)**
- Add different characters **X, Y, ... (nonterminals)**
- One special **nonterminal S** called **start symbol**
- BNF rules (aka **productions**) have form
$$\mathbf{X} ::= \mathbf{y}$$
where **X** is any nonterminal and **y** is a string of terminals and nonterminals
- BNF **grammar** is a set of BNF rules such that every nonterminal appears on the left of some rule

Context-Free Grammars



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Context-Free Grammars



Sample BNF Grammar

- Terminals: 0 1 + ()
- Nonterminals: <Sum>
- Start symbol = <Sum>

<Sum> ::= 0

<Sum> ::= 1

<Sum> ::= <Sum> + <Sum>

<Sum> ::= (<Sum>)



Sample BNF Grammar

- Terminals: 0 1 + ()
- Nonterminals: <Sum>
- Start symbol = <Sum>

<Sum> ::= 0

<Sum> ::= 1

<Sum> ::= <Sum> + <Sum>

<Sum> ::= (<Sum>)

Can be abbreviated as

<Sum> ::= 0 | 1 | <Sum> + <Sum> | (<Sum>)

Context-Free Grammars



Questions so far?



BNF Semantics

- **Question:** What does a BNF grammar **mean**?
- **Answer:** The **meaning** of a BNF grammar is the **set of all strings** consisting only of **terminals** that can be derived from the **Start** symbol
- **Question:** How do we determine that set?



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- **Question:** How do we determine that set?

BNF Derivations

- Given rules

$$\mathbf{X} ::= \mathbf{yZw} \text{ and } \mathbf{Z} ::= \mathbf{v}$$

we may replace \mathbf{Z} by \mathbf{v} to say

$$\mathbf{X} \Rightarrow \mathbf{yZw} \Rightarrow \mathbf{yvw}$$

- Sequence of such replacements called **derivation**
- Derivation called **right-most** if always replace the right-most non-terminal



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we may replace \mathbf{Z} by v to say

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- Sequence of such replacements called **derivation**
- Derivation called **right-most** if always replace the right-most non-terminal



BNF Derivations

Start with the start symbol:

$\langle \text{Sum} \rangle \Rightarrow$



BNF Derivations

Pick a non-terminal:

<Sum> =>

BNF Derivations

Pick a rule and substitute:

- $\langle \text{Sum} \rangle ::= \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$



BNF Derivations

Pick a non-terminal:

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

BNF Derivations

Pick a rule and substitute:

- $\langle \text{Sum} \rangle ::= (\langle \text{Sum} \rangle)$

$$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$$

$$\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$$



BNF Derivations

Pick a non-terminal:

$$\begin{aligned} \langle \text{Sum} \rangle & \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \\ & \Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle \end{aligned}$$

BNF Derivations

Pick a rule and substitute:

- $\langle \text{Sum} \rangle ::= \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + \langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$



BNF Derivations

Pick a non-terminal:

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BNF Derivations

Pick a rule and substitute:

- $\langle \text{Sum} \rangle ::= 1$

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + \langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + 1) + \langle \text{Sum} \rangle$

BNF Derivations

Pick a non-terminal:

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + \langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + 1) + \langle \text{Sum} \rangle$

BNF Derivations

Pick a rule and substitute:

- $\langle \text{Sum} \rangle ::= 0$

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + \langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + 1) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + 1) + 0$



BNF Derivations

Pick a non-terminal:

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BNF Derivations

Pick a rule and substitute

- $\langle \text{Sum} \rangle ::= 0$

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + \langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + 1) + \langle \text{Sum} \rangle$

$\Rightarrow (\langle \text{Sum} \rangle + 1) 0$

$\Rightarrow (0 + 1) + 0$

Context-Free Grammars



BNF Derivations

$(0 + 1) + 0$ is generated by the grammar.

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$
 $\Rightarrow (\langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$
 $\Rightarrow (\langle \text{Sum} \rangle + \langle \text{Sum} \rangle) + \langle \text{Sum} \rangle$
 $\Rightarrow (\langle \text{Sum} \rangle + 1) + \langle \text{Sum} \rangle$
 $\Rightarrow (\langle \text{Sum} \rangle + 1) + 0$
 $\Rightarrow (0 + 1) + 0$



Questions so far?



Extended BNF Grammars

- **Alternatives:** allow rules of form $X ::= y \mid z$
 - Abbreviates $X ::= y, X ::= z$
- **Options:** $X ::= y[v]z$
 - Abbreviates $X ::= yvz, X ::= yz$
- **Repetition:** $X ::= y\{v\}^*z$
 - Can be eliminated by adding new nonterminal V and rules $X ::= yz, X ::= yVz, V ::= v, V ::= vV$

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Questions?



Next Class: From Tokens to ASTs



Next Class

- **EC2 is up**
- **WA7** due **Thursday**
- **MP8** due next **Tuesday**
- All deadlines can be found on **course website**
- Use **office hours** and **class forums** for help