## Programming Languages and Compilers (CS 421)

# Talia Ringer (they/them) 4218 SC, UIUC



https://courses.grainger.illinois.edu/cs421/fa2023/

Based heavily on slides by Elsa Gunter, which were based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

#### **Objectives for Today**

- We want to turn strings (code) into computer instructions
- Done in **phases** 
  - Turn strings into abstract syntax trees (parse)
  - Translate abstract syntax trees into executable instructions (interpret or compile)
- Today we will learn the first step of parsing, which is **lexing** those raw input strings into **tokens**

#### Questions from last week?



#### Meta-discourse

#### Language Syntax and Semantics

- Syntax: form
  - Regular Expressions, DFSAs and NDFSAs
  - Grammars
- Semantics: meaning
  - Natural Semantics
  - Transition Semantics
- Compilers and interpreters (when correctly implemented) map from the syntax of programs (as written) to their semantics (as executed)



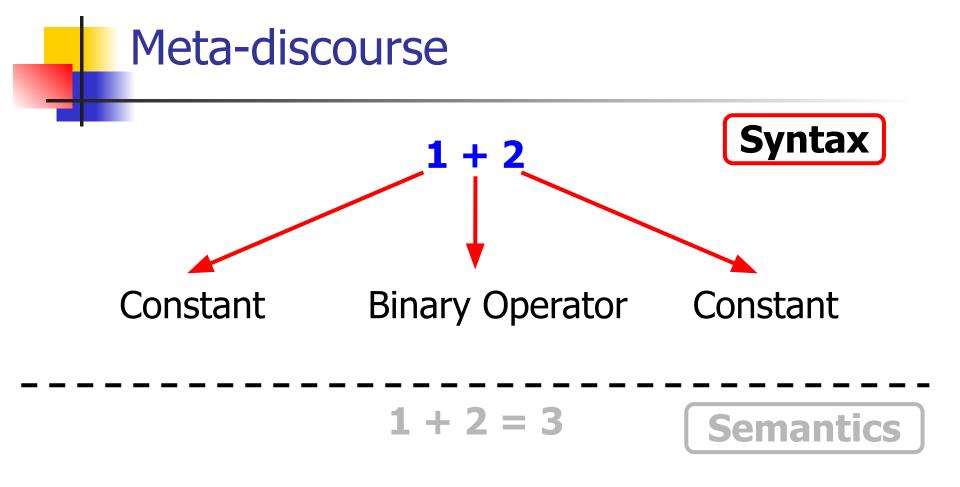
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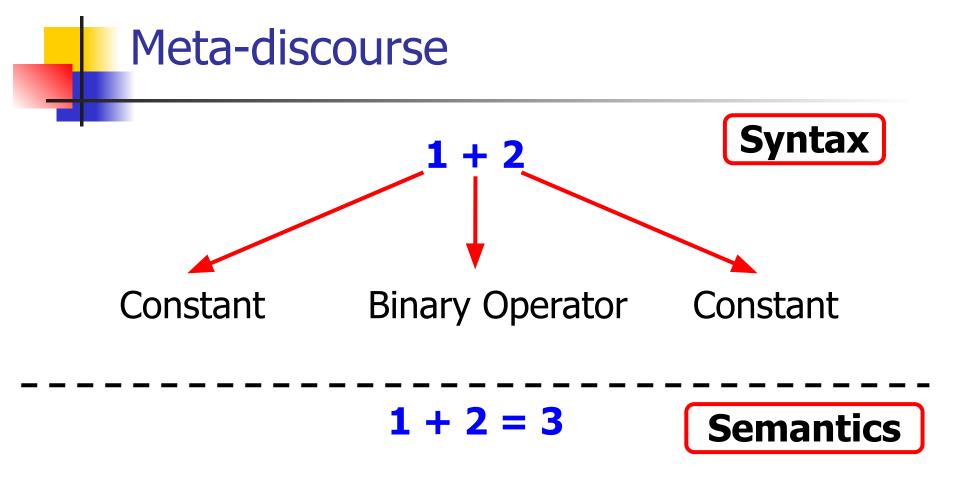


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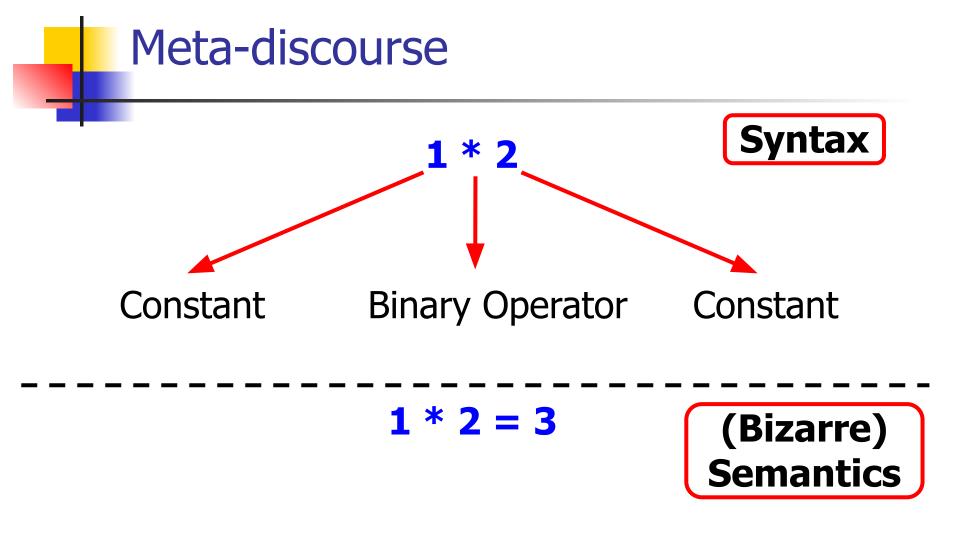
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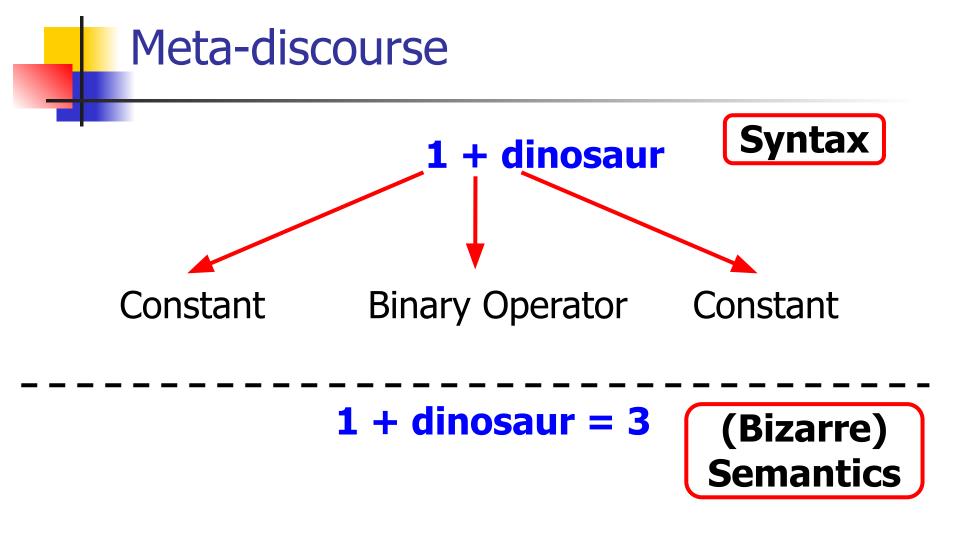




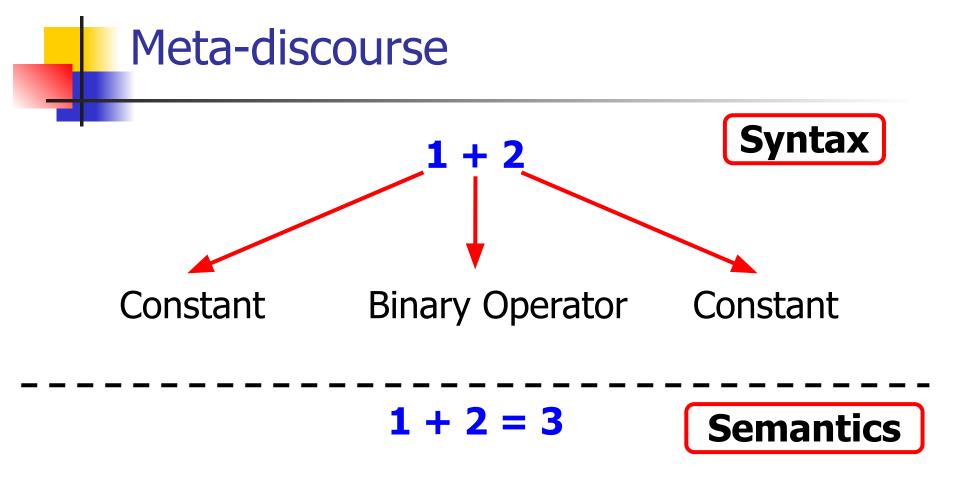




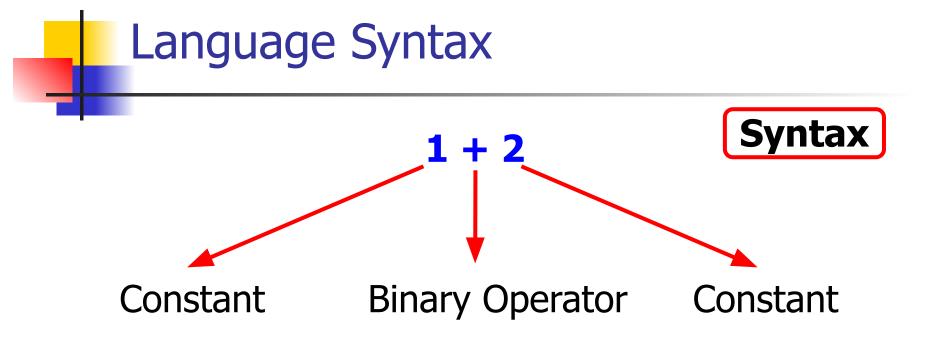












#### Language Syntax

- Syntax describe which strings of symbols are meaningful expressions in a language
- It takes more than syntax to understand a language; need meaning (semantics) too
- Syntax is the entry point





Converting strings (representing programs) to abstract syntax trees done in two phases:

- Lexing: Converting strings (or streams of characters) into lists/streams of tokens (the "words" of the language)
  - Specification Technique: Regular Expressions
- Parsing: Convert lists/streams of tokens into abstract syntax trees

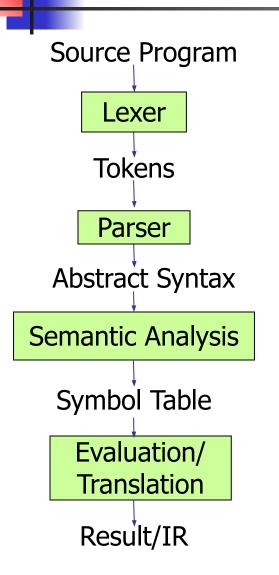
Specification Technique: BNF Grammars



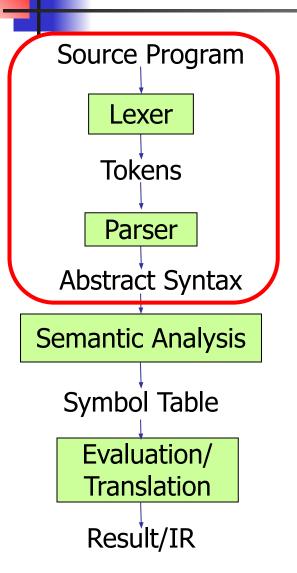
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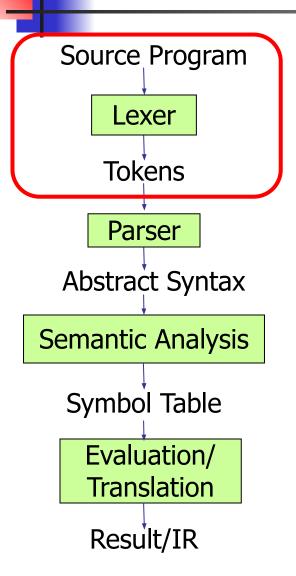
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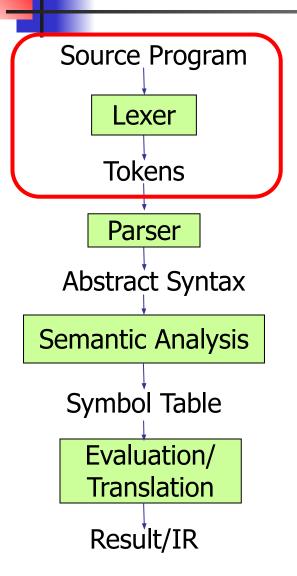




Lexing 21



To **lex** our source program and get **tokens**, we need **regular expressions**, **automata**, and a specific kind of **grammar**.



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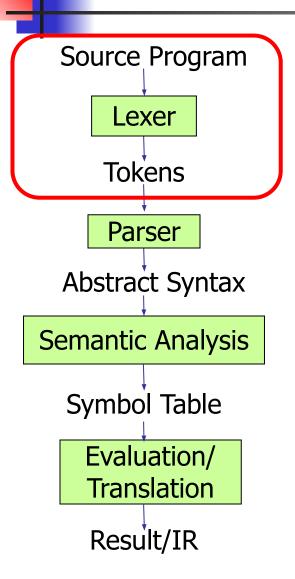
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## Lexing and Parsing 1 + 2 Syntax Constant Binary Operator Constant

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**Tokens** just tell us what category each part of the input falls into.



## **Regular Expressions**

- Start with given character set (alphabet):
   For example, {a, b, c, ... }
- Empty Set:
  - $\blacksquare L(\Phi) = \{ \}$
- Empty String:
  - $\blacksquare L(\mathbf{\epsilon}) = \{ ``'' \}$
  - Literals: Each character is a regular expression
    - Represents the set of one string containing just that character
    - *L*(**a**) = {a}

#### Regular Expressions

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   For example (a b c )
  - For example, {a, b, c, ... }
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$$\blacksquare L(\mathbf{\epsilon}) = \{ "" \}$$

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If **x** and **y** are regular expressions, then their **concatenation xy** is a regular expression

- Represents the set of strings made from first a string described by x then a string described by y
- L(xy) = L(x) × L(y). e.g., if L(x) = {a, ab} and L(y) = {c, d}, then L(xy) = {ac, ad, abc, abd}
   If x and y are regular expressions, then their alternation x ∨ y (sometimes x | y) is too
  - Represents the set of strings described by x or y
  - L(x ∨ y) = L(x) ∪ L(y). e.g., if L(x) = {a, ab} and L(y) = {c, d}, then L(x ∨ y) = {a, ab, c, d} Regular Expressions

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## Grouping: If x is a regular expression, so is (x) Represents the same thing as x

**Repeat:** If **x** is a regular expression, then so is **x**\*

- It represents strings made from concatenating zero or more strings from x
- $L(x^*) = L(\varepsilon) \cup L(x) \cup (L(x) \times L(x)) \cup ... e.g.,$ if  $L(x) = \{a, ab\}$ , then  $L(x^*) = \{$ "", a, ab, aa, aab, abab, ...}

#### Regular Expressions

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#### Aside for Math Nerds

On a given alphabet, these form a semiring:

- is 0 (additive identity)
- **ε** is **1 (multiplicative identity)**
- $\mathbf{x} \lor \mathbf{y}$  is  $\mathbf{x} + \mathbf{y}$  (addition)
- xy is x y (multiplication)
  - If curious, try proving the semiring laws :)
- Special kind—a (star-continuous) Kleene algebra:
  - The Kleene star x\* can be viewed as the infinite sum of powers of x (the closure)
  - Furthermore, we have x + x = x (idempotence)
     Imposes a partial ordering and other goodies!

#### **Regular Expressions**

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Regular Expressions

■ **(0**∨1)\*1

Set of all strings of 0s and 1s ending in 1
 {1, 01, 11,...}

a\*b(a\*)

- Set of all strings of **a**s and **b**s with exactly one **b**
- **((01)** \(10))\*

You tell me

Regular expressions (equivalently, regular grammars) important for lexing, breaking strings into recognized words

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**Regular Expressions** 



Regular Expressions



Regular Expressions 42

#### **Right Regular Grammars**

- Subclass of BNF (covered in detail soon)
- Only rules of form

<nonterminal> ::= <terminal><nonterminal> or <nonterminal> ::= <terminal> or <nonterminal> ::= ε

- Defines same class of languages as regular expressions
- Important for writing lexers (programs that convert strings of characters into strings of tokens)

Connection to nondeterministic finite state automata: nonterminals ≅ states; rule ≅ edge Regular Expressions

#### Example

# Right regular grammar: <Balanced> ::= ε <Balanced> ::= 0<OneAndMore> <Balanced> ::= 1<ZeroAndMore> <OneAndMore> ::= 1<Balanced> <ZeroAndMore> ::= 0<Balanced>

Generates even length strings where every initial substring of even length has same number of 0s as 1s

Regular Expressions

#### Example

## Right regular grammar: <Balanced> ::= ɛ <Balanced> ::= 0<OneAndMore> <Balanced> ::= 1<ZeroAndMore> <OneAndMore> ::= 1<Balanced> <ZeroAndMore> ::= 0<Balanced>

Generates even length strings where every initial substring of even length has same number of 0s as 1s

#### **Implementing Regular Expressions**

- Regular expressions can be good for generating strings in language
- They are not so good for recognizing when a string is in language
- Problems:
  - Which option to choose?
  - How many repetitions to make?
- Answer: finite state automata
- Should have seen in CS374

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#### **Implementing Regular Expressions**

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- They are not so good for recognizing when a string is in language

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- **Answer**: finite state automata
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#### Example: Lexing

 Regular expressions good for describing lexemes (words) in a programming language

- Identifier =
- Digit =  $(0 \lor 1 \lor ... \lor 9)$
- Number =
  - $0 \lor (1 \lor ... \lor 9)(0 \lor ... \lor 9)* \lor \sim (1 \lor ... \lor 9)(0 \lor ... \lor 9)*$

**Keywords**: if = if, while = while,...

#### Lexing

Different syntactic categories of "words": tokens
Example:

- Convert sequence of characters into sequence of strings, integers, and floating point numbers
- "asd 123 jkl 3.14" will become: [String "asd"; Int 123; String "jkl"; Float 3.14] Could write the regular expression, then translate
- to DFA by hand, but this is a lot of work
- Better: Write program to translate automatically
- Lex is such a program (ocamllex for ocaml)

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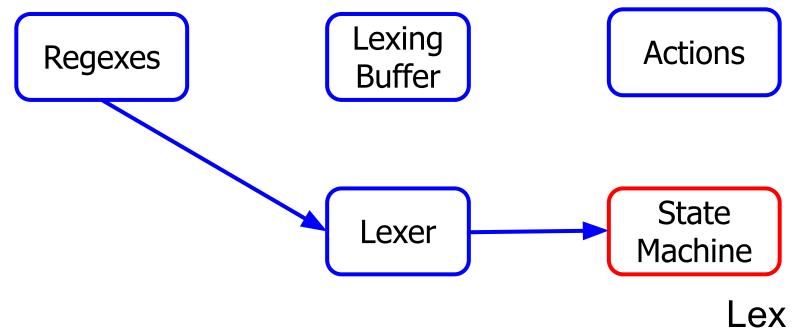
- A way to identify input strings (a lexing buffer)
- A set of **regular expressions** to match against
- A corresponding set of actions to take



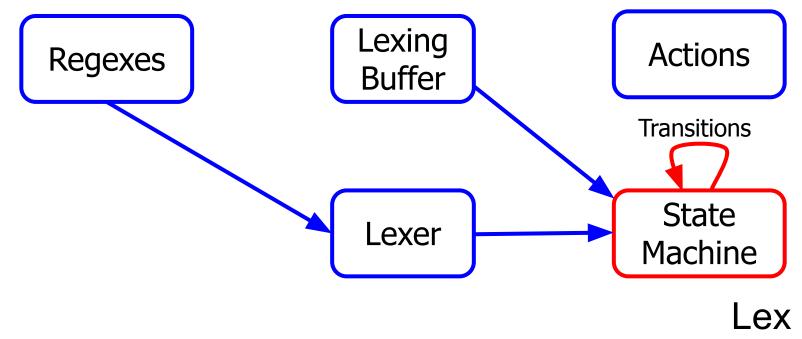




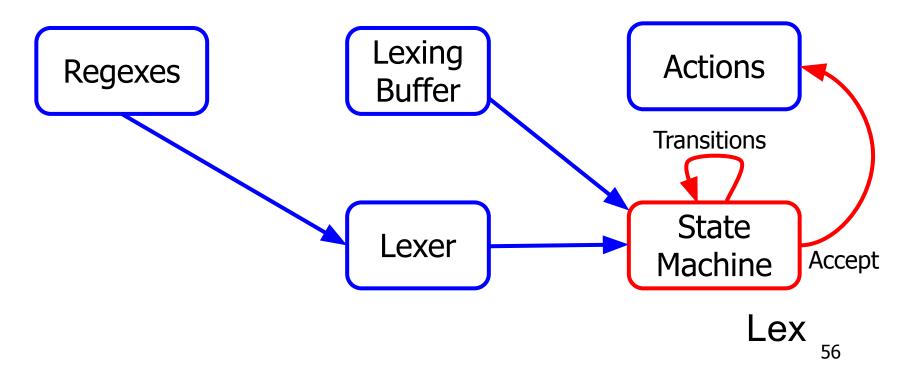
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#### **Ocamllex Mechanics**

Put table of regular expressions and corresponding actions (in OCaml) into a file: <*filename*>.mll

Call:

ocamllex < filename>.mll

#### Produces OCaml code for a lexical analyzer in *<filename>.*ml

#### Sample Input

```
rule main = parse
| ['0'-'9']+ { print_string "Int\n"}
| ['0'-'9']+'.'['0'-'9']+ { print_string "Float\n"}
| ['a'-'z']+ { print_string "String\n"}
| _ { main lexbuf }
{
```

let newlexbuf = Lexing.from\_channel stdin in main newlexbuf

#### Sample Input

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rule main = parse
['0'-'9']+ { print string "Int\n"}
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{ main lexbuf }
 let newlexbuf = Lexing.from channel stdin in
 main newlexbuf
```

#### Sample Input

```
let digits = ['0'-'9']+
let chars = ['a'-'z']+
rule main = parse
digits { print_string "Int\n"}
digits'.'digits { print_string "Float\n"}
chars { print_string "String\n"}
{ main lexbuf }
 let newlexbuf = Lexing.from_channel stdin in
 main newlexbuf
```



```
let ident = regexp ...
rule entrypoint [arg1... argn] = parse
| regexp { action }
| ...
| regexp { action }
and entrypoint [arg1... argn] = parse
```



These contain **arbitrary ocaml code** put at top and bottom of *<filename>*.ml



{ header }

let *ident* = *regexp* ...

rule entrypoint [arg1... argn] = parse
| regexp { action }

```
. . .
```

regexp { action }

and *entrypoint* [*arg1*... *argn*] = parse

and ... { *trailer* }

## This **introduces a variable** *ident* for use in later regular expressions



{ header }

let *ident* = *regexp* ...

rule entrypoint [arg1... argn] = parse
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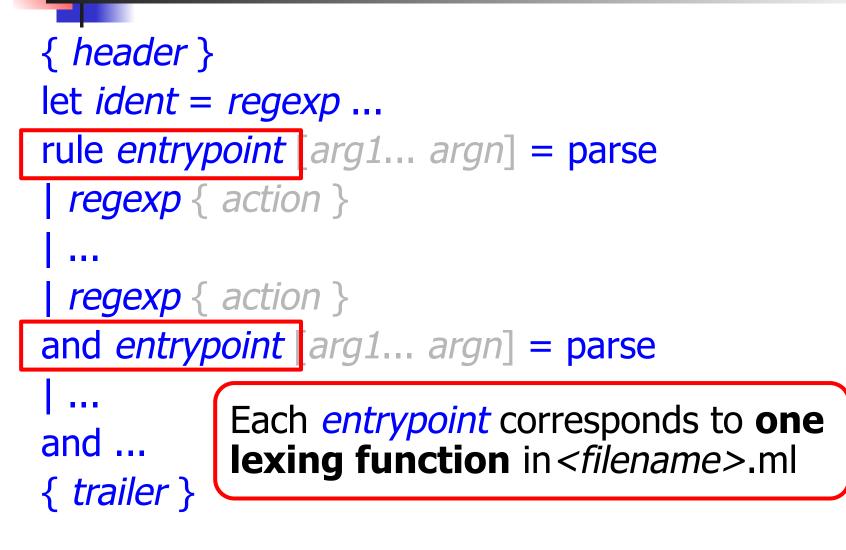
*regexp* { *action* }

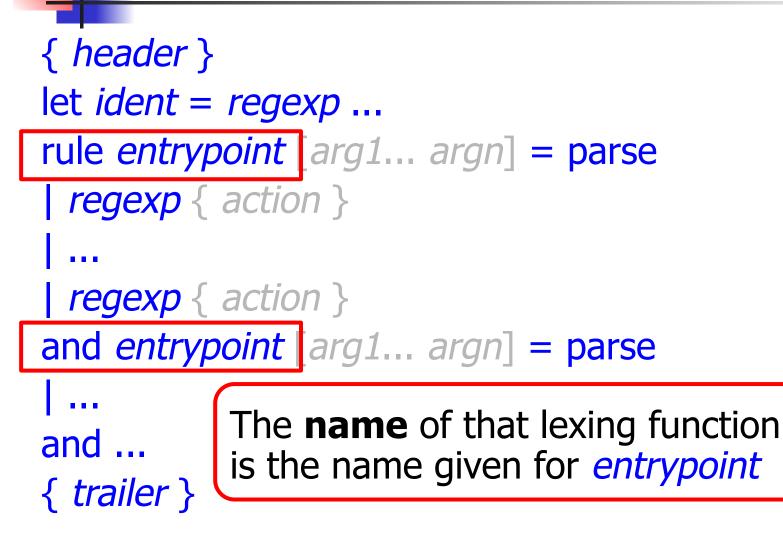
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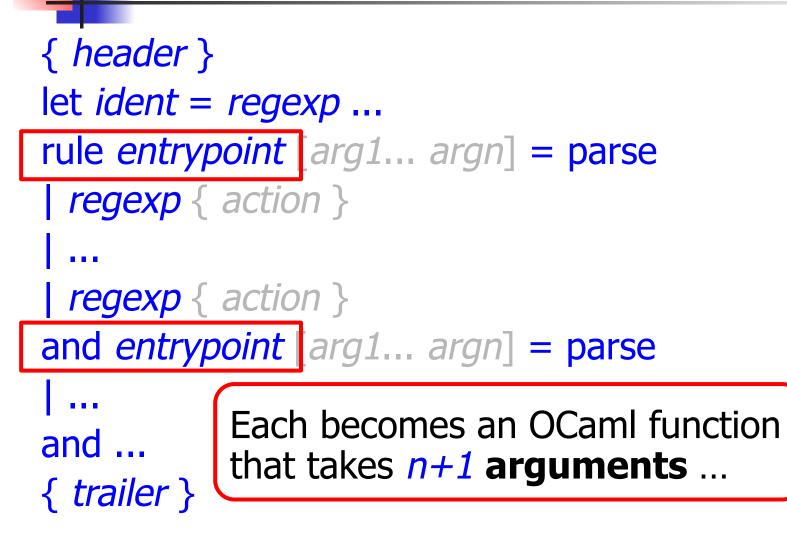
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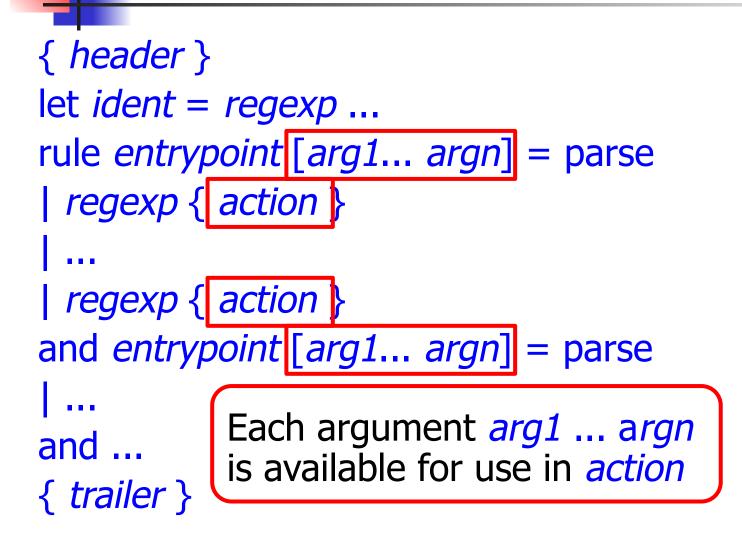








```
{ header }
let ident = regexp ...
rule entrypoint [arg1... argn] = parse
regexp { action }
 regexp { action }
and entrypoint [arg1... argn] = parse
             The first n arguments are those defined here explicitly.
and ...
{ trailer }
```



```
{ header }
let ident = regexp ...
rule entrypoint [arg1... argn] = parse
| regexp { action }
regexp { action }
and entrypoint [arg1... argn] = parse
            The extra implicit last argument has type Lexing.lexbuf
and ...
{ trailer }
```

#### **Ocamllex Regular Expression**

- Single quoted characters for letters: `a'
- \_: (underscore) matches any letter
- Eof: special "end\_of\_file" marker
- Concatenation same as usual
- *string*: concatenation of sequence of characters
- $e_1 | e_2$ : choice what was  $e_1 \vee e_2$
- [c<sub>1</sub> c<sub>2</sub>]: choice of any character between first and second inclusive, as determined by character codes
- $[^{c_1} c_2]$ : choice of any character NOT in set

Lex

#### **Ocamllex Regular Expression**

- e\*: same as before
- e+: same as e e\*
- e?: option was  $e \vee \epsilon$
- *e*<sub>1</sub> # *e*<sub>2</sub>: the characters in *e*<sub>1</sub> but not in *e*<sub>2</sub>; *e*<sub>1</sub> and *e*<sub>2</sub> must describe just sets of characters
- **ident**: abbreviation for earlier reg exp in let *ident* 
  - = regexp
  - e<sub>1</sub> as *id*: binds the result of e<sub>1</sub> to *id* to be used in the associated *action*

#### **Ocamllex Manual**

More details can be found at:

https://v2.ocaml.org/releases/4.14/htmlman/lexyacc.html

```
(* header *)
 type result = Int of int | Float of float | String of string
}
(* variables for reference in later regular expressions *)
let digit = ['0'-'9']
let digits = digit +
let lower case = ['a'-'z']
let upper case = ['A'-'Z']
let letter = upper_case | lower_case
let letters = letter +
                                                    Lex
```

73

\*

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                                                    Lex
```

rule main = parse (\* entrypoint called "main" \*)
| (digits)'.'digits as f { Float (float\_of\_string f) }
| digits as n { Int (int\_of\_string n) }
| letters as s { String s}
|\_\_ { main lexbuf }

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rule main = parse (\* entrypoint called "main" \*) (digits)'.'digits as f { Float (float\_of\_string f) } { Int (int\_of\_string n) } digits as n letters as s { String s} { main lexbuf } (\* trailer \*) let newlexbuf = (Lexing.from\_channel stdin) in print\_newline (); main newlexbuf

# #use "test.ml";;

```
val main : Lexing.lexbuf -> result = <fun>
val __ocaml_lex_main_rec :
  Lexing.lexbuf -> int -> result = <fun>
hi
```

- : result = String "hi"

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hi there 234 5.2
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hi there 234 5.2

- : result = String "hi"

What happened to the rest?

- # let b = Lexing.from\_channel stdin;; # main b;; hi 673 there
- : result = String "hi"
- # main b;;
- -: result = Int 673
- # main b;;
- : result = String "there"

Recall the hidden argument of type lexbuf

- # let b = Lexing.from\_channel stdin;;
  # main b;;
  hi 673 there
- : result = String "hi"
- # main b;;
- : result = Int 673
- # main b;;
- : result = String "there"

Recall the hidden argument of type lexbuf

- # let b = Lexing.from\_channel stdin;;
  # main b;;
  hi 673 there
- : result = String "hi"
- # main b;;
- -: result = Int 673
- # main b;;
- : result = String "there"

Recall the hidden argument of type lexbuf



## Your Turn

#### Work on MP8

- Add a few keywords
- Implement booleans and unit
- Implement Ints and Floats
- Implement identifiers



#### Next Class

- EC2 is up
- Quiz 4 on MP7 is Tuesday
  - Please show up!
  - Extra chance for ADT midterm question!
- WA7 due next Thursday
- All deadlines can be found on course website
- Use office hours and class forums for help