

Programming Languages and Compilers (CS 421)

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<http://courses.engr.illinois.edu/cs421>

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

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Example

Before:

```
let rec mem (y,lst) =
  match lst with
  [ ] -> false
  | x :: xs ->
    if (x = y)
    then true
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =
  (* rule 1 *)
```

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Example

Before:

```
let rec mem (y,lst) =
  match lst with
  [ ] -> false
  | x :: xs ->
    if (x = y)
    then true
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =
  (* rule 1 *)
  k false (* rule 2 *)
  k true (* rule 2 *)
```

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Example

Before:

```
let rec mem (y,lst) =
  match lst with
  [ ] -> false
  | x :: xs ->
    if (x = y)
    then true
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =
  (* rule 1 *)
  k false (* rule 2 *)
  k true (* rule 2 *)
  memk (y, xs) k (* rule 3 *)
```

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Example

Before:

```
let rec mem (y,lst) =
  match lst with
  [ ] -> false
  | x :: xs ->
    if (x = y)
    then true
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =
  (* rule 1 *)
  k false (* rule 2 *)
  eqk (x, y)
  (fun b -> b (* rule 4 *)
   k true (* rule 2 *)
   memk (y, xs) (* rule 3 *))
```

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Example

Before:

```
let rec mem (y,lst) =
  match lst with
  [ ] -> false
  | x :: xs ->
    if (x = y)
    then true
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =
  (* rule 1 *)
  k false (* rule 2 *)
  eqk (x, y)
  (fun b -> if b (* rule 4 *)
   then k true (* rule 2 *)
   else memk (y, xs) (* rule 3 *))
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
 | x :: xs ->  
   if (x = y)  
   then true  
   else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  match lst with  
  | [ ] -> k false (* rule 2 *)  
  | x :: xs ->  
    eqk (x, y)  
    (fun b -> if b (* rule 4 *)  
    then k true (* rule 2 *)  
    else memk (y, xs) k (* rule 3 *))
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
 | x :: xs ->  
   if (x = y)  
   then true  
   else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  match lst with  
  | [ ] -> k false (* rule 2 *)  
  | x :: xs ->  
    eqk (x, y)  
    (fun b -> if b (* rule 4 *)  
    then k true (* rule 2 *)  
    else memk (y, xs) k (* rule 3 *))
```

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Data type in Ocaml: lists

- Frequently used lists in recursive program
- Matched over two structural cases
 - `[]` - the empty list
 - `(x :: xs)` a non-empty list
- Covers all possible lists
- `type 'a list = [] | (::) of 'a * 'a list`
 - Not quite legitimate declaration because of special syntax

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Variants - Syntax (slightly simplified)

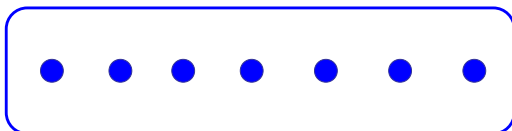
- `type name = C1 [of ty1] | . . . | Cn [of tyn]`
- Introduce a type called *name*
- `(fun x -> Ci x) : tyi -> name`
- *C_i* is called a *constructor*; if the optional type argument is omitted, it is called a *constant*
- Constructors are the basis of almost all pattern matching

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Enumeration Types as Variants

An enumeration type is a collection of distinct values



In C and Ocaml they have an order structure; order by order of input

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Enumeration Types as Variants

```
# type weekday = Monday | Tuesday | Wednesday  
  | Thursday | Friday | Saturday | Sunday;;  
type weekday =  
  Monday  
  | Tuesday  
  | Wednesday  
  | Thursday  
  | Friday  
  | Saturday  
  | Sunday
```

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Functions over Enumerations

```
# let day_after day = match day with
  Monday -> Tuesday
  | Tuesday -> Wednesday
  | Wednesday -> Thursday
  | Thursday -> Friday
  | Friday -> Saturday
  | Saturday -> Sunday
  | Sunday -> Monday;;
val day_after : weekday -> weekday = <fun>
```

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Functions over Enumerations

```
# let rec days_later n day =
  match n with 0 -> day
  | _ -> if n > 0
    then day_after (days_later (n - 1) day)
    else days_later (n + 7) day;;
val days_later : int -> weekday -> weekday
= <fun>
```

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Functions over Enumerations

```
# days_later 2 Tuesday;;
- : weekday = Thursday
# days_later (-1) Wednesday;;
- : weekday = Tuesday
# days_later (-4) Monday;;
- : weekday = Thursday
```

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Problem:

```
# type weekday = Monday | Tuesday |
  Wednesday
  | Thursday | Friday | Saturday | Sunday;;
■ Write function is_weekend : weekday -> bool
let is_weekend day =
```

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Problem:

```
# type weekday = Monday | Tuesday |
  Wednesday
  | Thursday | Friday | Saturday | Sunday;;
■ Write function is_weekend : weekday -> bool
let is_weekend day =
  match day with Saturday -> true
  | Sunday -> true
  | _ -> false
```

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Example Enumeration Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp

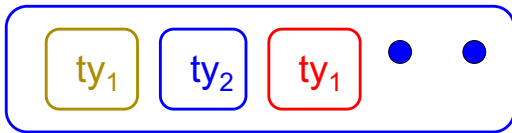
# type mon_op = HdOp | TIOp | FstOp
  | SndOp
```

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Disjoint Union Types

- Disjoint union of types, with some possibly occurring more than once



- We can also add in some new singleton elements

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Disjoint Union Types

```
# type id = DriversLicense of int
| SocialSecurity of int | Name of string;;
type id = DriversLicense of int | SocialSecurity
of int | Name of string
# let check_id id = match id with
  DriversLicense num ->
    not (List.mem num [13570; 99999])
  | SocialSecurity num -> num < 900000000
  | Name str -> not (str = "John Doe");;
val check_id : id -> bool = <fun>
```

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Problem

- Create a type to represent the currencies for US, UK, Europe and Japan

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Problem

- Create a type to represent the currencies for US, UK, Europe and Japan

```
type currency =
  Dollar of int
| Pound of int
| Euro of int
| Yen of int
```

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Example Disjoint Union Type

```
# type const =
  BoolConst of bool
| IntConst of int
| FloatConst of float
| StringConst of string
| NilConst
| UnitConst
```

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Example Disjoint Union Type

```
# type const = BoolConst of bool
| IntConst of int | FloatConst of float
| StringConst of string | NilConst
| UnitConst
```

- How to represent 7 as a const?
- Answer: `IntConst 7`

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Polymorphism in Variants

- The type `'a option` gives us something to represent non-existence or failure

```
# type 'a option = Some of 'a | None;;  
type 'a option = Some of 'a | None
```

- Used to encode partial functions
- Often can replace the raising of an exception

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Functions producing option

```
# let rec first p list =  
  match list with [ ] -> None  
  | (x::xs) -> if p x then Some x else first p xs;;  
val first : ('a -> bool) -> 'a list -> 'a option = <fun>  
# first (fun x -> x > 3) [1;3;4;2;5];;  
- : int option = Some 4  
# first (fun x -> x > 5) [1;3;4;2;5];;  
- : int option = None
```

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Functions over option

```
# let result_ok r =  
  match r with None -> false  
  | Some _ -> true;;  
val result_ok : 'a option -> bool = <fun>  
# result_ok (first (fun x -> x > 3) [1;3;4;2;5]);;  
- : bool = true  
# result_ok (first (fun x -> x > 5) [1;3;4;2;5]);;  
- : bool = false
```

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Problem

- Write a `hd` and `tl` on lists that doesn't raise an exception and works at all types of lists.

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Problem

- Write a `hd` and `tl` on lists that doesn't raise an exception and works at all types of lists.

```
■ let hd list =  
  match list with [] -> None  
  | (x::xs) -> Some x  
■ let tl list =  
  match list with [] -> None  
  | (x::xs) -> Some xs
```

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Mapping over Variants

```
# let optionMap f opt =  
  match opt with None -> None  
  | Some x -> Some (f x);;  
val optionMap : ('a -> 'b) -> 'a option -> 'b option = <fun>  
# optionMap  
  (fun x -> x - 2)  
  (first (fun x -> x > 3) [1;3;4;2;5]);;  
- : int option = Some 2
```

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Folding over Variants

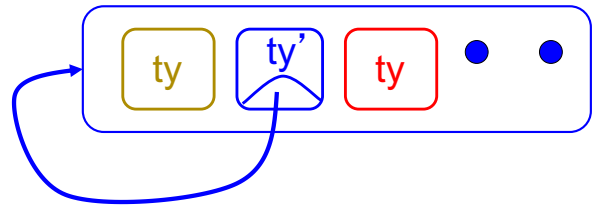
```
# let optionFold someFun noneVal opt =  
  match opt with None -> noneVal  
    | Some x -> someFun x;;  
val optionFold : ('a -> 'b) -> 'b -> 'a option ->  
'b = <fun>  
# let optionMap f opt =  
  optionFold (fun x -> Some (f x)) None opt;;  
val optionMap : ('a -> 'b) -> 'a option -> 'b  
option = <fun>
```

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Recursive Types

- The type being defined may be a component of itself



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Recursive Data Types

```
# type int_Bin_Tree =  
  Leaf of int | Node of (int_Bin_Tree *  
  int_Bin_Tree);;
```

```
type int_Bin_Tree = Leaf of int | Node of  
(int_Bin_Tree * int_Bin_Tree)
```

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Recursive Data Type Values

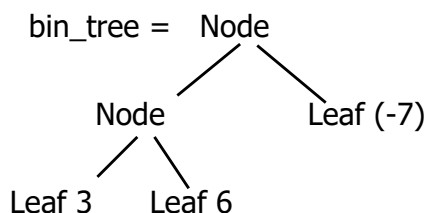
```
# let bin_tree =  
  Node(Node(Leaf 3, Leaf 6),Leaf (-7));;
```

```
val bin_tree : int_Bin_Tree = Node (Node  
(Leaf 3, Leaf 6), Leaf (-7))
```

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Recursive Data Type Values



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Recursive Data Types

```
# type exp =  
  VarExp of string  
  | ConstExp of const  
  | MonOpAppExp of mon_op * exp  
  | BinOpAppExp of bin_op * exp * exp  
  | IfExp of exp * exp * exp  
  | AppExp of exp * exp  
  | FunExp of string * exp
```

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent 6 as an exp?

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent 6 as an exp?
- Answer: ConstExp (IntConst 6)

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent (6, 3) as an exp?

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent (6, 3) as an exp?
- BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3))

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent [(6, 3)] as an exp?
- BinOpAppExp (ConsOp, BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3)), ConstExp NilConst))

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Recursive Functions

```
# let rec first_leaf_value tree =
  match tree with (Leaf n) -> n
  | Node (left_tree, right_tree) ->
    first_leaf_value left_tree;;
val first_leaf_value : int_Bin_Tree -> int =
  <fun>
# let left = first_leaf_value bin_tree;;
val left : int = 3
```

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Problem

```
type int_Bin_Tree = Leaf of int
| Node of (int_Bin_Tree * int_Bin_Tree);;
■ Write sum_tree : int_Bin_Tree -> int
■ Adds all ints in tree
let rec sum_tree t =
```

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Problem

```
type int_Bin_Tree = Leaf of int
| Node of (int_Bin_Tree * int_Bin_Tree);;
■ Write sum_tree : int_Bin_Tree -> int
■ Adds all ints in tree
let rec sum_tree t =
  match t with Leaf n -> n
  | Node(t1,t2) -> sum_tree t1 + sum_tree t2
```

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Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
■ How to count the number of variables in an exp?
```

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Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
■ How to count the number of variables in an exp?
# let rec varCnt exp =
  match exp with VarExp x ->
  | ConstExp c ->
  | BinOpAppExp (b, e1, e2) ->
  | FunExp (x,e) ->
  | AppExp (e1, e2) ->
```

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Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
■ How to count the number of variables in an exp?
# let rec varCnt exp =
  match exp with VarExp x -> 1
  | ConstExp c -> 0
  | BinOpAppExp (b, e1, e2) -> varCnt e1 + varCnt e2
  | FunExp (x,e) -> 1 + varCnt e
  | AppExp (e1, e2) -> varCnt e1 + varCnt e2
```

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Your turn now

Try Problem 3 on MP5

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Mapping over Recursive Types

```
# let rec ibtreeMap f tree =  
  match tree with (Leaf n) -> Leaf (f n)  
  | Node (left_tree, right_tree) ->  
    Node (ibtreeMap f left_tree,  
          ibtreeMap f right_tree);;  
val ibtreeMap : (int -> int) -> int_Bin_Tree ->  
int_Bin_Tree = <fun>
```

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Mapping over Recursive Types

```
# ibtreeMap ((+) 2) bin_tree;;  
  
- : int_Bin_Tree = Node (Node (Leaf 5, Leaf  
8), Leaf (-5))
```

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Folding over Recursive Types

```
# let rec ibtreeFoldRight leafFun nodeFun tree =  
  match tree with Leaf n -> leafFun n  
  | Node (left_tree, right_tree) ->  
    nodeFun  
    (ibtreeFoldRight leafFun nodeFun left_tree)  
    (ibtreeFoldRight leafFun nodeFun right_tree);;  
val ibtreeFoldRight : (int -> 'a) -> ('a -> 'a -> 'a) ->  
int_Bin_Tree -> 'a = <fun>
```

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Folding over Recursive Types

```
# let tree_sum =  
  ibtreeFoldRight (fun x -> x) (+);;  
val tree_sum : int_Bin_Tree -> int = <fun>  
# tree_sum bin_tree;;  
  
- : int = 2
```

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Mutually Recursive Types

```
# type 'a tree = TreeLeaf of 'a  
  | TreeNode of 'a treeList  
and 'a treeList = Last of 'a tree  
  | More of ('a tree * 'a treeList);;  
type 'a tree = TreeLeaf of 'a | TreeNode of 'a  
treeList  
and 'a treeList = Last of 'a tree | More of ('a  
tree * 'a treeList)
```

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Mutually Recursive Types - Values

```
# let tree =  
  TreeNode  
  (More (TreeLeaf 5,  
        (More (TreeNode  
              (More (TreeLeaf 3,  
                    Last (TreeLeaf 2))),  
                Last (TreeLeaf 7)))));;
```

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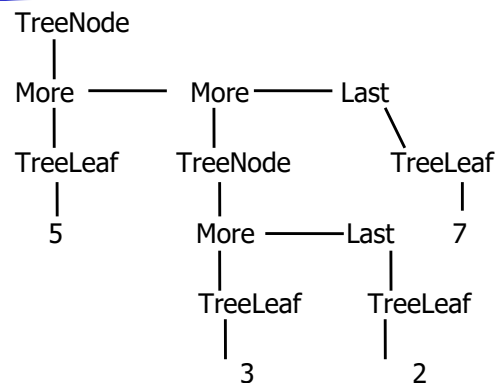
Mutually Recursive Types - Values

```
val tree : int tree =
  TreeNode
    (More
      (TreeLeaf 5,
        More
          (TreeNode (More (TreeLeaf 3, Last
            (TreeLeaf 2))), Last (TreeLeaf 7))))
```

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Mutually Recursive Types - Values

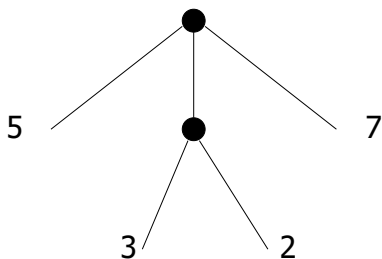


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Mutually Recursive Types - Values

A more conventional picture



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Mutually Recursive Functions

```
# let rec fringe tree =
  match tree with (TreeLeaf x) -> [x]
  | (TreeNode list) -> list_fringe list
and list_fringe tree_list =
  match tree_list with (Last tree) -> fringe tree
  | (More (tree,list)) ->
    (fringe tree) @ (list_fringe list);;
```

```
val fringe : 'a tree -> 'a list = <fun>
val list_fringe : 'a treeList -> 'a list = <fun>
```

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Mutually Recursive Functions

```
# fringe tree;;
- : int list = [5; 3; 2; 7]
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
let rec tree_size t =
  match t with TreeLeaf _ ->
  | TreeNode ts ->
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
and treeList_size ts =
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
and treeList_size ts =
  match ts with Last t ->
  | More t ts' ->
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
and treeList_size ts =
  match ts with Last t -> tree_size t
  | More t ts' -> tree_size t + treeList_size ts'
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
and treeList_size ts =
  match ts with Last t -> tree_size t
  | More t ts' -> tree_size t + treeList_size ts'
```

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Nested Recursive Types

```
# type 'a labeled_tree =
  TreeNode of ('a * 'a labeled_tree
list);;
type 'a labeled_tree = TreeNode of ('a
* 'a labeled_tree list)
```

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Nested Recursive Type Values

```
# let ltree =
  TreeNode(5,
  [TreeNode (3, []);
  TreeNode (2, [TreeNode (1, []);
  TreeNode (7, [])]);
  TreeNode (5, [])];;
```

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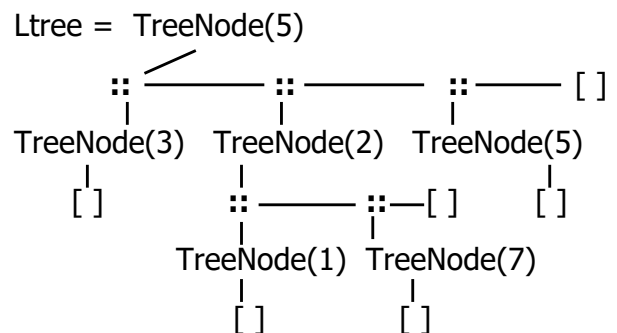
Nested Recursive Type Values

```
val ltree : int labeled_tree =
  TreeNode
  (5,
  [TreeNode (3, []); TreeNode (2,
  [TreeNode (1, []); TreeNode (7, [])]);
  TreeNode (5, [])])
```

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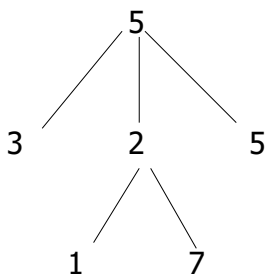
Nested Recursive Type Values



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Nested Recursive Type Values



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Mutually Recursive Functions

```
# let rec flatten_tree labtree =
  match labtree with TreeNode (x,treelist)
  -> x::flatten_tree_list treelist
  and flatten_tree_list treelist =
  match treelist with [] -> []
  | labtree::labtrees
  -> flatten_tree labtree
  @ flatten_tree_list labtrees;;
```

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Mutually Recursive Functions

```
val flatten_tree : 'a labeled_tree -> 'a list =
  <fun>
val flatten_tree_list : 'a labeled_tree list -> 'a
  list = <fun>
# flatten_tree ltree;;
- : int list = [5; 3; 2; 1; 7; 5]
```

- Nested recursive types lead to mutually recursive functions

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Infinite Recursive Values

```
# let rec ones = 1::ones;;
val ones : int list =
  [1; 1; 1; 1; ...]
# match ones with x::_ -> x;;
Characters 0-25:
Warning: this pattern-matching is not exhaustive.
Here is an example of a value that is not matched:
[]
  match ones with x::_ -> x;;
  ^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^
- : int = 1
```

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Infinite Recursive Values

```
# let rec lab_tree = TreeNode(2, tree_list)
  and tree_list = [lab_tree; lab_tree];;
val lab_tree : int labeled_tree =
  TreeNode (2, [TreeNode(...); TreeNode(...)])
val tree_list : int labeled_tree list =
  [TreeNode (2, [TreeNode(...);
  TreeNode(...)]);
  TreeNode (2, [TreeNode(...);
  TreeNode(...)])]
```

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Infinite Recursive Values

```
# match lab_tree
  with TreeNode (x, _) -> x;;
- : int = 2
```

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Records

- Records serve the same programming purpose as tuples
- Provide better documentation, more readable code
- Allow components to be accessed by label instead of position
 - Labels (aka *field names*) must be unique
 - Fields accessed by suffix dot notation

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Record Types

- Record types must be declared before they can be used in OCaml
- ```
type person = { name : string; ss : (int * int * int); age : int };;
type person = { name : string; ss : int * int * int; age : int; }
```
- person is the type being introduced
  - name, ss and age are the labels, or fields

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## Record Values

- Records built with labels; order does not matter

```
let teacher = {name = "Elsa L. Gunter";
age = 102; ss = (119,73,6244)};;
val teacher : person =
{name = "Elsa L. Gunter"; ss = (119, 73,
6244); age = 102}
```

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## Record Pattern Matching

```
let {name = elsa; age = age; ss =
(_,_,s3)} = teacher;;
val elsa : string = "Elsa L. Gunter"
val age : int = 102
val s3 : int = 6244
```

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## Record Field Access

```
let soc_sec = teacher.ss;;
val soc_sec : int * int * int = (119,
73, 6244)
```

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## Record Values

```
let student = {ss=(325,40,1276);
name="Joseph Martins"; age=22};;
val student : person =
{name = "Joseph Martins"; ss = (325, 40,
1276); age = 22}
student = teacher;;
- : bool = false
```

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## New Records from Old

```
let birthday person = {person with age =
person.age + 1};;
val birthday : person -> person = <fun>
birthday teacher;;
- : person = {name = "Elsa L. Gunter"; ss =
(119, 73, 6244); age = 103}
```

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## New Records from Old

```
let new_id name soc_sec person =
{person with name = name; ss = soc_sec};;
val new_id : string -> int * int * int -> person
-> person = <fun>
new_id "Guieseppe Martin" (523,04,6712)
student;;
- : person = {name = "Guieseppe Martin"; ss
= (523, 4, 6712); age = 22}
```

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