Programming Languages and Compilers (CS 421)

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http://courses.engr.illinois.edu/cs421

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

Data type in Ocaml: lists

- Frequently used lists in recursive program
- Matched over two structural cases
 - [] the empty list
 - (x :: xs) a non-empty list
- Covers all possible lists
- type 'a list = [] | (::) of 'a * 'a list
 - Not quite legitimate declaration because of special syntax

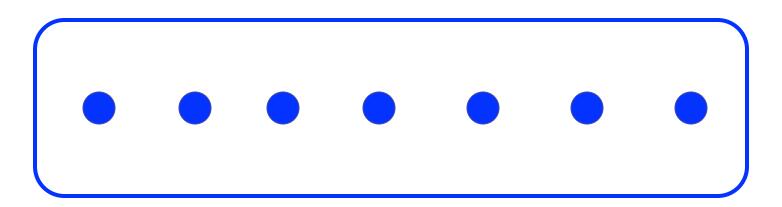
Variants - Syntax (slightly simplified)

- type $name = C_1 [of ty_1] | \dots | C_n [of ty_n]$
- Introduce a type called name
- (fun x -> C_i x) : ty_1 -> name
- C_i is called a constructor, if the optional type argument is omitted, it is called a constant
- Constructors are the basis of almost all pattern matching



Enumeration Types as Variants

An enumeration type is a collection of distinct values



In C and Ocaml they have an order structure; order by order of input

Enumeration Types as Variants

```
# type weekday = Monday | Tuesday | Wednesday
  | Thursday | Friday | Saturday | Sunday;;
type weekday =
  Monday
 | Tuesday
 | Wednesday
  Thursday
  Friday
 | Saturday
 | Sunday
```

Functions over Enumerations

```
# let day_after day = match day with
   Monday -> Tuesday
 | Tuesday -> Wednesday
 | Wednesday -> Thursday
 | Thursday -> Friday
  Friday -> Saturday
 | Saturday -> Sunday
 | Sunday -> Monday;;
val day after: weekday -> weekday = <fun>
```

Functions over Enumerations

```
# let rec days_later n day =
    match n with 0 -> day
    |_ -> if n > 0
        then day_after (days_later (n - 1) day)
        else days_later (n + 7) day;;
val days_later : int -> weekday -> weekday
        = <fun>
```

Functions over Enumerations

```
# days_later 2 Tuesday;;
-: weekday = Thursday
# days_later (-1) Wednesday;;
-: weekday = Tuesday
# days_later (-4) Monday;;
-: weekday = Thursday
```

Problem:

- # type weekday = Monday | Tuesday |
 Wednesday
 - | Thursday | Friday | Saturday | Sunday;;
- Write function is_weekend : weekday -> bool let is_weekend day =

Problem:

```
# type weekday = Monday | Tuesday |
 Wednesday
  | Thursday | Friday | Saturday | Sunday;;
Write function is weekend: weekday -> bool
let is weekend day =
   match day with Saturday -> true
    | Sunday -> true
    -> false
```

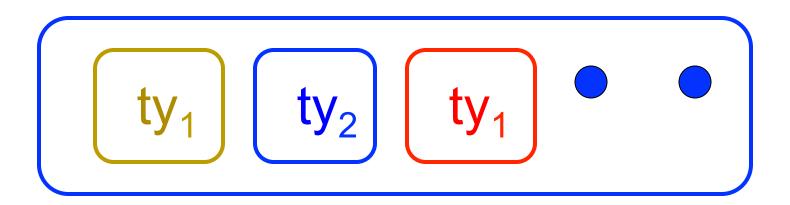


Example Enumeration Types



Disjoint Union Types

Disjoint union of types, with some possibly occurring more than once



 We can also add in some new singleton elements

Disjoint Union Types

```
# type id = DriversLicense of int
  | SocialSecurity of int | Name of string;;
type id = DriversLicense of int | SocialSecurity
 of int | Name of string
# let check id id = match id with
    DriversLicense num ->
     not (List.mem num [13570; 99999])
  | SocialSecurity num -> num < 900000000
  | Name str -> not (str = "John Doe");;
val check id : id -> bool = <fun>
```

Problem

 Create a type to represent the currencies for US, UK, Europe and Japan

Problem

 Create a type to represent the currencies for US, UK, Europe and Japan

type currency =

Dollar of int

| Pound of int

| Euro of int

| Yen of int



Example Disjoint Union Type

- # type const =

 BoolConst of bool
 - | IntConst of int
 - | FloatConst of float
 - | StringConst of string
 - | NilConst
 - | UnitConst



Example Disjoint Union Type

- How to represent 7 as a const?
- Answer: IntConst 7

Polymorphism in Variants

 The type 'a option is gives us something to represent non-existence or failure

```
# type 'a option = Some of 'a | None;;
type 'a option = Some of 'a | None
```

- Used to encode partial functions
- Often can replace the raising of an exception

Functions producing option

```
# let rec first p list =
    match list with [] -> None
    | (x::xs) -> if p x then Some x else first p xs;;
val first : ('a -> bool) -> 'a list -> 'a option = <fun>
# first (fun x -> x > 3) [1;3;4;2;5];;
- : int option = Some 4
# first (fun x -> x > 5) [1;3;4;2;5];;
- : int option = None
```

Functions over option

```
# let result ok r =
  match r with None -> false
  | Some _ -> true;;
val result ok : 'a option -> bool = <fun>
# result_ok (first (fun x -> x > 3) [1;3;4;2;5]);;
-: bool = true
# result_ok (first (fun x -> x > 5) [1;3;4;2;5]);;
-: bool = false
```

Problem

Write a hd and tl on lists that doesn't raise an exception and works at all types of lists.

Problem

Write a hd and tl on lists that doesn't raise an exception and works at all types of lists.

```
    let hd list =
        match list with [] -> None
        | (x::xs) -> Some x
    let tl list =
        match list with [] -> None
        | (x::xs) -> Some xs
```

Mapping over Variants

```
# let optionMap f opt =
   match opt with None -> None
   | Some x \rightarrow Some (f x);;
val optionMap: ('a -> 'b) -> 'a option -> 'b
  option = <fun>
# optionMap
 (fun x -> x - 2)
 (first (fun x -> x > 3) [1;3;4;2;5]);;
- : int option = Some 2
```

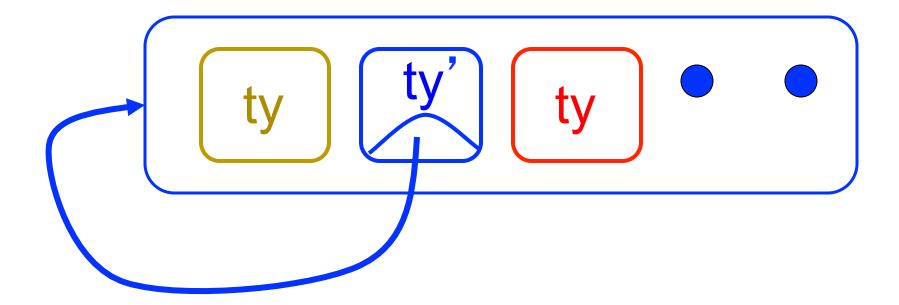
Folding over Variants

```
# let optionFold someFun noneVal opt =
  match opt with None -> noneVal
   | Some x -> someFun x;;
val optionFold : ('a -> 'b) -> 'b -> 'a option ->
  'b = <fun>
# let optionMap f opt =
  optionFold (fun x \rightarrow Some (f x)) None opt;;
val optionMap: ('a -> 'b) -> 'a option -> 'b
 option = <fun>
```



Recursive Types

 The type being defined may be a component of itself



Recursive Data Types

```
# type int_Bin_Tree =
Leaf of int | Node of (int_Bin_Tree *
  int_Bin_Tree);;
```

```
type int_Bin_Tree = Leaf of int | Node of (int_Bin_Tree * int_Bin_Tree)
```

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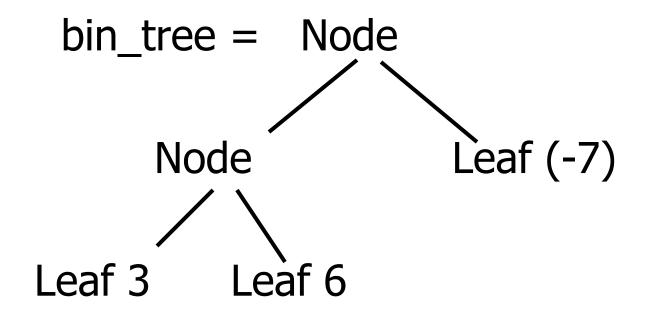
Recursive Data Type Values

```
# let bin_tree =
Node(Node(Leaf 3, Leaf 6),Leaf (-7));;
```

```
val bin_tree : int_Bin_Tree = Node (Node (Leaf 3, Leaf 6), Leaf (-7))
```



Recursive Data Type Values



Recursive Data Types

```
# type exp =
   VarExp of string
  | ConstExp of const
  | MonOpAppExp of mon_op * exp
  | BinOpAppExp of bin_op * exp * exp
  | IfExp of exp* exp * exp
  AppExp of exp * exp
  | FunExp of string * exp
```

Recursive Data Types

How to represent 6 as an exp?

Recursive Data Types

- How to represent 6 as an exp?
- Answer: ConstExp (IntConst 6)

Recursive Data Types

How to represent (6, 3) as an exp?

Recursive Data Types

- How to represent (6, 3) as an exp?
- BinOpAppExp (CommaOp, ConstExp (IntConst 6),
 ConstExp (IntConst 3))

Recursive Data Types

- How to represent [(6, 3)] as an exp?
- BinOpAppExp (ConsOp, BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3)), ConstExp NilConst)));;

Recursive Functions

```
# let rec first leaf value tree =
   match tree with (Leaf n) -> n
   | Node (left_tree, right_tree) ->
   first_leaf_value left tree;;
val first leaf value : int Bin Tree -> int =
  <fun>
# let left = first leaf value bin tree;;
val left: int = 3
```

Problem

```
type int_Bin_Tree =Leaf of int
| Node of (int_Bin_Tree * int_Bin_Tree);;
```

- Write sum_tree : int_Bin_Tree -> int
- Adds all ints in treelet rec sum_tree t =

```
type int_Bin_Tree = Leaf of int
| Node of (int_Bin_Tree * int_Bin_Tree);;
```

- Write sum_tree : int_Bin_Tree -> int
- Adds all ints in tree

```
let rec sum_tree t =
    match t with Leaf n -> n
    | Node(t1,t2) -> sum_tree t1 + sum_tree t2
```



Recursion over Recursive Data Types

How to count the number of variables in an exp?

Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
```

How to count the number of variables in an exp?

```
# let rec varCnt exp =
  match exp with VarExp x ->
  | ConstExp c ->
  | BinOpAppExp (b, e1, e2) ->
  | FunExp (x,e) ->
  | AppExp (e1, e2) ->
```

Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
```

How to count the number of variables in an exp?

```
# let rec varCnt exp =
  match exp with VarExp x -> 1
  | ConstExp c -> 0
  | BinOpAppExp (b, e1, e2) -> varCnt e1 + varCnt e2
  | FunExp (x,e) -> 1 + varCnt e
  | AppExp (e1, e2) -> varCnt e1 + varCnt e2
```



Your turn now

Try Problem 3 on MP3

Mapping over Recursive Types

Mapping over Recursive Types

```
# ibtreeMap ((+) 2) bin_tree;;
```

-: int_Bin_Tree = Node (Node (Leaf 5, Leaf 8), Leaf (-5))

Folding over Recursive Types

```
# let rec ibtreeFoldRight leafFun nodeFun tree =
    match tree with Leaf n -> leafFun n
    | Node (left_tree, right_tree) ->
        nodeFun
        (ibtreeFoldRight leafFun nodeFun left_tree)
        (ibtreeFoldRight leafFun nodeFun right_tree);;
val ibtreeFoldRight: (int -> 'a) -> ('a -> 'a -> 'a) ->
        int_Bin_Tree -> 'a = <fun>
```

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Folding over Recursive Types

```
# let tree_sum =
   ibtreeFoldRight (fun x -> x) (+);;
val tree_sum : int_Bin_Tree -> int = <fun>
# tree_sum bin_tree;;
- : int = 2
```

Mutually Recursive Types

```
# type 'a tree = TreeLeaf of 'a
  | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree
  | More of ('a tree * 'a treeList);;
type 'a tree = TreeLeaf of 'a | TreeNode of 'a
  treeList
and 'a treeList = Last of 'a tree | More of ('a
 tree * 'a treeList)
```

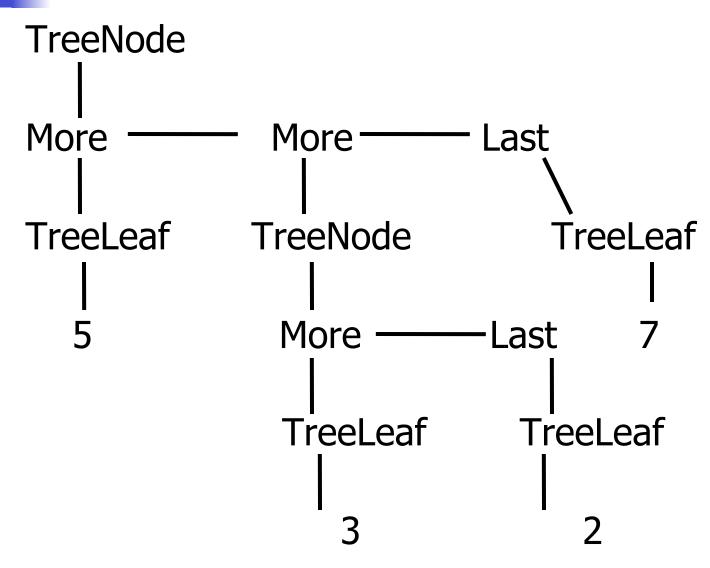


```
# let tree =
 TreeNode
  (More (TreeLeaf 5,
       (More (TreeNode
            (More (TreeLeaf 3,
                 Last (TreeLeaf 2))),
            Last (TreeLeaf 7)))));;
```



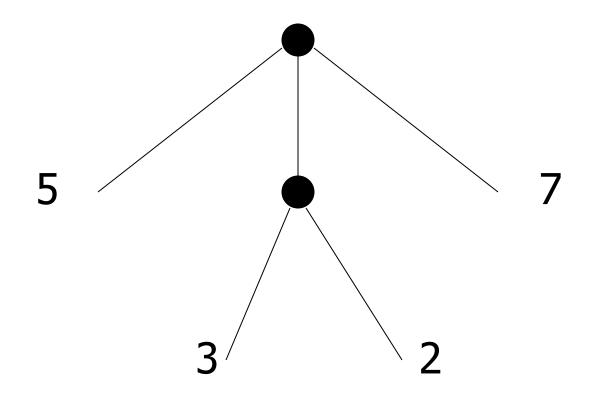
```
val tree : int tree =
  TreeNode
  (More
    (TreeLeaf 5,
        More
        (TreeNode (More (TreeLeaf 3, Last
        (TreeLeaf 2))), Last (TreeLeaf 7))))
```







A more conventional picture



Mutually Recursive Functions

```
# let rec fringe tree =
   match tree with (TreeLeaf x) -> [x]
 | (TreeNode list) -> list fringe list
and list_fringe tree_list =
   match tree_list with (Last tree) -> fringe tree
 | (More (tree, list)) ->
   (fringe tree) @ (list_fringe list);;
val fringe: 'a tree -> 'a list = <fun>
val list_fringe : 'a treeList -> 'a list = <fun>
```

Mutually Recursive Functions

```
# fringe tree;;
- : int list = [5; 3; 2; 7]
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
let rec tree_size t =
    match t with TreeLeaf _ ->
    | TreeNode ts ->
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
let rec tree_size t =
    match t with TreeLeaf _ -> 1
    | TreeNode ts -> treeList_size ts
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
    match t with TreeLeaf _ -> 1
    | TreeNode ts -> treeList_size ts
and treeList_size ts =
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree size and treeList size
let rec tree size t =
     match t with TreeLeaf -> 1
     | TreeNode ts -> treeList size ts
and treeList size ts =
     match ts with Last t ->
     | More t ts' ->
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree size and treeList size
let rec tree size t =
    match t with TreeLeaf -> 1
     | TreeNode ts -> treeList size ts
and treeList size ts =
    match ts with Last t -> tree size t
     | More t ts' -> tree size t + treeList size ts'
```

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree size and treeList size
let rec tree size t =
    match t with TreeLeaf -> 1
     | TreeNode ts -> treeList size ts
and treeList size ts =
    match ts with Last t -> tree size t
     | More t ts' -> tree size t + treeList size ts'
```

Nested Recursive Types

```
# type 'a labeled_tree =
  TreeNode of ('a * 'a labeled_tree
  list);;
type 'a labeled_tree = TreeNode of ('a
  * 'a labeled_tree list)
```

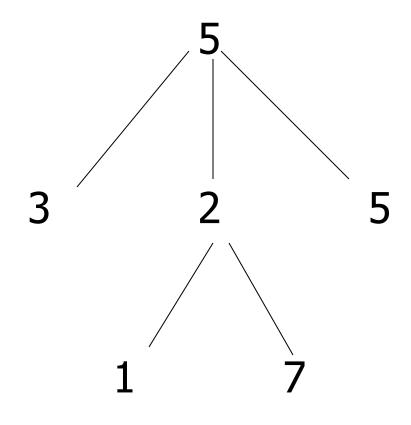


```
val ltree : int labeled_tree =
  TreeNode
  (5,
    [TreeNode (3, []); TreeNode (2,
    [TreeNode (1, []); TreeNode (7, [])]);
    TreeNode (5, [])])
```



```
Ltree = TreeNode(5)
TreeNode(3) TreeNode(2) TreeNode(5)
          TreeNode(1) TreeNode(7)
```





Mutually Recursive Functions

```
# let rec flatten_tree labtree =
  match labtree with TreeNode (x,treelist)
    -> x::flatten tree list treelist
  and flatten tree list treelist =
  match treelist with [] -> []
   | labtree::labtrees
    -> flatten tree labtree
      @ flatten tree list labtrees;;
```

Mutually Recursive Functions

 Nested recursive types lead to mutually recursive functions

Infinite Recursive Values

```
# let rec ones = 1::ones;;
val ones : int list =
 [1; 1; 1; 1; ...]
# match ones with x::_ -> x;;
Characters 0-25:
Warning: this pattern-matching is not exhaustive.
Here is an example of a value that is not matched:
 match ones with x::_ -> x;;
 -: int = 1
```

Infinite Recursive Values

```
# let rec lab tree = TreeNode(2, tree list)
  and tree list = [lab tree; lab tree];;
val lab tree : int labeled tree =
 TreeNode (2, [TreeNode(...); TreeNode(...)])
val tree list : int labeled tree list =
 [TreeNode (2, [TreeNode(...);
 TreeNode(...)]);
  TreeNode (2, [TreeNode(...);
 TreeNode(...)])]
```

Infinite Recursive Values

```
# match lab_tree
  with TreeNode (x, _) -> x;;
- : int = 2
```

Records

- Records serve the same programming purpose as tuples
- Provide better documentation, more readable code
- Allow components to be accessed by label instead of position
 - Labels (aka field names must be unique)
 - Fields accessed by suffix dot notation

Record Types

 Record types must be declared before they can be used in OCaml

```
# type person = {name : string; ss : (int * int
  * int); age : int};;

type person = { name : string; ss : int * int *
  int; age : int; }
```

- person is the type being introduced
- name, ss and age are the labels, or fields

Record Values

 Records built with labels; order does not matter

```
# let teacher = {name = "Elsa L. Gunter";
   age = 102; ss = (119,73,6244)};;
val teacher : person =
   {name = "Elsa L. Gunter"; ss = (119, 73,
   6244); age = 102}
```

Record Pattern Matching

```
# let {name = elsa; age = age; ss =
  (_,_,s3)} = teacher;;
val elsa : string = "Elsa L. Gunter"
val age : int = 102
val s3 : int = 6244
```

Record Field Access

```
# let soc_sec = teacher.ss;;
val soc_sec : int * int * int = (119,
73, 6244)
```

Record Values

```
# let student = {ss=(325,40,1276);
  name="Joseph Martins"; age=22};;
val student : person =
  {name = "Joseph Martins"; ss = (325, 40, 1276); age = 22}
# student = teacher;;
- : bool = false
```

New Records from Old

```
# let birthday person = {person with age =
    person.age + 1};;
val birthday : person -> person = <fun>
# birthday teacher;;
- : person = {name = "Elsa L. Gunter"; ss =
    (119, 73, 6244); age = 103}
```

New Records from Old

```
# let new_id name soc_sec person =
{person with name = name; ss = soc_sec};;
val new id: string -> int * int * int -> person
 -> person = <fun>
# new id "Guieseppe Martin" (523,04,6712)
 student;;
-: person = {name = "Guieseppe Martin"; ss
 = (523, 4, 6712); age = 22
```