# Programming Languages and Compilers (CS 421)



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Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

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- Start with a set of characters, **a,b,c,...** 
  - We call these *terminals*
- Add a set of different characters, X,Y,Z,
  - We call these *nonterminals*
- One special nonterminal S called start symbol

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#### **BNF Grammars**

BNF rules (aka productions) have form

$$X := v$$

where X is any nonterminal and y is a string of terminals and nonterminals

 BNF grammar is a set of BNF rules such that every nonterminal appears on the left of some rule

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# Sample Grammar

- Terminals: 0 1 + ( )
- Nonterminals: <Sum>
- Start symbol = <Sum>
- <Sum> ::= 0
- <Sum >::= 1
- <Sum> ::= <Sum> + <Sum>
- <Sum> ::= (<Sum>)
- Can be abbreviated as

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#### **BNF** Deriviations

Given rules

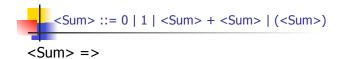
$$X::= yZw$$
 and  $Z::=v$ 

we may replace  $\mathbf{Z}$  by  $\mathbf{v}$  to say

$$X => yZw => yvw$$

- Sequence of such replacements called derivation
- Derivation called *right-most* if always replace the right-most non-terminal

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#### **BNF Semantics**

 The meaning of a BNF grammar is the set of all strings consisting only of terminals that can be derived from the Start symbol

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# Regular Grammars

- Subclass of BNF
- Only rules of form
  - <nonterminal>::=<terminal><nonterminal> or <nonterminal>::=<terminal> or
  - <nonterminal $>::= \varepsilon$
- Defines same class of languages as regular expressions
- Important for writing lexers (programs that convert strings of characters into strings of tokens)

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#### Example

- Regular grammar:
  - <Balanced $> ::= \epsilon$
  - <Balanced> ::= 0<OneAndMore>
  - <Balanced> ::= 1<ZeroAndMore>
  - <OneAndMore> ::= 1<Balanced>
  - <ZeroAndMore> ::= 0<Balanced>
- Generates even length strings where every initial substring of even length has same number of 0's as 1's

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## **Extended BNF Grammars**

- Alternatives: allow rules of from X::= y/z
  - Abbreviates X::= y, X::= z
- Options: X := y[v]z
  - Abbreviates X::= yvz, X::= yz
- Repetition: X::= y{ v}\*z
  - Can be eliminated by adding new nonterminal V and rules X::= yz, X::= yVz, V::= v, V::= vW

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#### Parse Trees

- Graphical representation of derivation
- Each node labeled with either non-terminal or terminal
- If node is labeled with a terminal, then it is a leaf (no sub-trees)
- If node is labeled with a non-terminal, then it has one branch for each character in the right-hand side of rule used to substitute for it

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#### Example

Consider grammar:

Problem: Build parse tree for 1 \* 1 + 0 as an <exp>



# Example cont.

■ 1 \* 1 + 0: <exp>

<exp> is the start symbol for this parse tree

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# Example cont.

Use rule: <exp> ::= <factor>

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# Example cont.

Use rule: <factor> ::= <bin> \* <exp>

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# Example cont.

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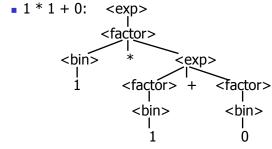
# Example cont.

Use rule: <factor> ::= <bin>

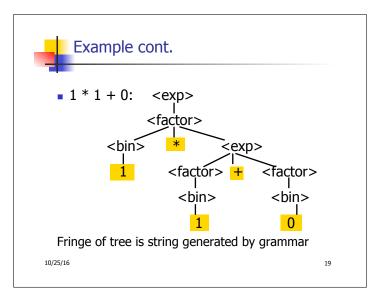
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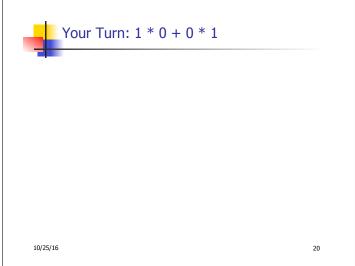
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# Example cont.



Use rules: <bin> ::= 1 | 0







#### Parse Tree Data Structures

- Parse trees may be represented by OCaml datatypes
- One datatype for each nonterminal
- One constructor for each rule
- Defined as mutually recursive collection of datatype declarations

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Recall grammar:

<exp> ::= <factor> | <factor> + <factor>
<factor> ::= <bin> | <bin> \* <exp>

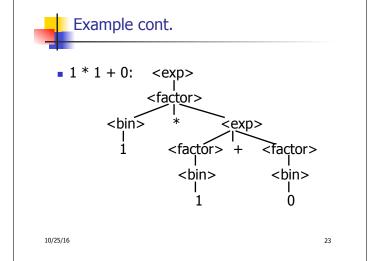
<br/><br/><br/><br/><br/>1 = 0 | 1

type exp = Factor2Exp of factor | Plus of factor \* factor

and factor = Bin2Factor of bin | Mult of bin \* exp

and bin = Zero | One

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# Example cont.

Can be represented as

Factor2Exp (Mult(One, Plus(Bin2Factor One, Bin2Factor Zero)))



#### **Ambiguous Grammars and Languages**

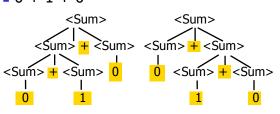
- A BNF grammar is <u>ambiguous</u> if its language contains strings for which there is more than one parse tree
- If all BNF's for a language are ambiguous then the language is *inherently ambiguous*

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# Example: Ambiguous Grammar

0 + 1 + 0



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#### Example

What is the result for:

$$3 + 4 * 5 + 6$$

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# Example

What is the result for:

$$3 + 4 * 5 + 6$$

Possible answers:

- 41 = ((3 + 4) \* 5) + 6
- 47 = 3 + (4 \* (5 + 6))
- 29 = (3 + (4 \* 5)) + 6 = 3 + ((4 \* 5) + 6)
- 77 = (3 + 4) \* (5 + 6)

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# Example

What is the value of:

$$7 - 5 - 2$$



# Example

What is the value of:

$$7 - 5 - 2$$

- Possible answers:
  - In Pascal, C++, SML assoc. left

$$7-5-2=(7-5)-2=0$$

In APL, associate to right

$$7-5-2=7-(5-2)=4$$

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# Two Major Sources of Ambiguity

- Lack of determination of operator precedence
- Lack of determination of operator assoicativity
- Not the only sources of ambiguity

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# Disambiguating a Grammar

• Given ambiguous grammar G, with start symbol S, find a grammar G' with same start symbol, such that

language of G = language of G'

- Not always possible
- No algorithm in general

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## Disambiguating a Grammar

- Idea: Each non-terminal represents all strings having some property
- Identify these properties (often in terms of things that can't happen)
- Use these properties to inductively guarantee every string in language has a unique parse

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## Steps to Grammar Disambiguation

- Identify the rules and a smallest use that display ambiguity
- Decide which parse to keep; why should others be thrown out?
- What syntactic restrictions on subexpressions are needed to throw out the bad (while keeping the good)?
- Add a new non-terminal and rules to describe this set of restricted subexpressions (called stratifying, or refactoring)
- Replace old rules to use new non-terminals
- Rinse and repeat

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#### Example

Ambiguous grammar:

String with more then one parse:

$$0 + 1 + 0$$
  
 $1 * 1 + 1$ 

Sourceof ambiuity: associativity and precedence

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# Two Major Sources of Ambiguity

- Lack of determination of operator precedence
- Lack of determination of operator assoicativity
- Not the only sources of ambiguity

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# How to Enforce Associativity

- Have at most one recursive call per production
- When two or more recursive calls would be natural leave right-most one for right assoicativity, left-most one for left assoiciativity

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# Example

- Becomes
  - <Sum> ::= <Num> | <Num> + <Sum>
  - < Num> ::= 0 | 1 | (<Sum>)

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# **Operator Precedence**

- Operators of highest precedence evaluated first (bind more tightly).
- Precedence for infix binary operators given in following table
- Needs to be reflected in grammar

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# Precedence Table - Sample

	Fortan	Pascal	C/C++	Ada	SML
highest	**	*, /, div, mod	++,	**	div, mod, / , *
	*,/	+, -	*,/, %	*, /, mod	+, -,
	+, -		+, -	+, -	::

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# First Example Again

- In any above language, 3 + 4 \* 5 + 6 = 29
- In APL, all infix operators have same precedence
  - Thus we still don't know what the value is (handled by associativity)
- How do we handle precedence in grammar?

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# Predence in Grammar

- Higher precedence translates to longer derivation chain
- Example:

Becomes

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## Ocamlyacc Input

File format:

%{

<header>

%}

<declarations>

%%

<rules>

%%

<trailer>

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# Ocamlyacc < header>

- Contains arbitrary Ocaml code
- Typically used to give types and functions needed for the semantic actions of rules and to give specialized error recovery
- May be omitted
- < footer> similar. Possibly used to call parser

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# Ocamlyacc <declarations>

- %token symbol ... symbol
- Declare given symbols as tokens
- %token <type> symbol ... symbol
- Declare given symbols as token constructors, taking an argument of type <type>
- %start symbol ... symbol
- Declare given symbols as entry points; functions of same names in < grammar>.ml

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# Ocamlyacc < declarations>

- %type <type> symbol ... symbol Specify type of attributes for given symbols. Mandatory for start symbols
- %left symbol ... symbol
- %right symbol ... symbol
- %nonassoc symbol ... symbol
   Associate precedence and associativity to given symbols. Same line, same precedence;

given symbols. Same line, same precedence; earlier line, lower precedence (broadest scope)

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#### Ocamlyacc < rules>

```
nonterminal:
```

```
symbol ... symbol { semantic_action }
| ...
| symbol ... symbol { semantic_action }
```

- Semantic actions are arbitrary Ocaml expressions
- Must be of same type as declared (or inferred) for nonterminal
- Access semantic attributes (values) of symbols by position: \$1 for first symbol, \$2 to second ...

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# -

#### Example - Base types

```
(* File: expr.ml *)

type expr =
    Term_as_Expr of term
    | Plus_Expr of (term * expr)
    | Minus_Expr of (term * expr)
and term =
    Factor_as_Term of factor
    | Mult_Term of (factor * term)
    | Div_Term of (factor * term)
and factor =
    Id_as_Factor of string
    | Parenthesized_Expr_as_Factor of expr
```

```
Example - Parser (exprparse.mly)

%{ open Expr
%}
%token <string> Id_token
%token Left_parenthesis Right_parenthesis
%token Times_token Divide_token
%token Plus_token Minus_token
%token EOL
%start main
%type <expr> main
%%
```

```
expr:
term
{ Term_as_Expr $1 }
| term Plus_token expr
{ Plus_Expr ($1, $3) }
| term Minus_token expr
{ Minus_Expr ($1, $3) }
```

```
term:
factor
{ Factor_as_Term $1 }
| factor Times_token term
{ Mult_Term ($1, $3) }
| factor Divide_token term
{ Div_Term ($1, $3) }
```

```
factor:

Id_token

{ Id_as_Factor $1 }

| Left_parenthesis expr Right_parenthesis

{ Parenthesized_Expr_as_Factor $2 }

main:

| expr EOL

{ $1 }
```

```
# #use "expr.ml";;
...
# #use "exprparse.ml";;
...
# #use "exprlex.ml";;
...
# let test s =
let lexbuf = Lexing.from_string (s^"\n") in
main token lexbuf;;

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```

```
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```

# Example - Using Parser

```
# test "a + b";;
-: expr =
Plus_Expr
(Factor_as_Term (Id_as_Factor "a"),
   Term_as_Expr (Factor_as_Term
   (Id_as_Factor "b")))
```