
HW 8 – Regular Expressions

CS 421 – Fall 2015

Revision 1.0

Assigned October 20, 2015

Due October 28, 2015, 23:59

Extension 48 hours (20% penalty)

1 Change Log

1.0 Initial Release.

2 Turn-In Procedure

Answer the problem below, save your work as a PDF (either scanned if handwritten or converted from a program), add the PDF to the subversion repository (`svn add hw8-submission.pdf`) and commit it (`svn commit -m ""`). Your file should be named `hw8-submission.pdf` and committed in your `assignments/hw8` directory.

3 Objectives and Background

The purpose of this HW is to test your understanding of regular expressions and remind you of their connection to regular grammars.

4 Problems

1. (15 points) For this problem, you will be given regular expressions describing given languages, and asked to write regular grammars defining the same language.

1. `let V rec V in`

2. `(a V b V c) (a V b V c) *`

3. `(0 V 1 V 8 V 9) (0 V 1 V 8 V 9)* (.) (0 V 1 V 8 V 9)*`

Solution:

1. `S = lL | rR | iI`

`L = eE`

`E = t`

`R = eF`

`F = c`

`I = n`

$$2. \begin{aligned} S &= aT \mid bT \mid cT \\ T &= aT \mid bT \mid cT \mid \epsilon \end{aligned}$$

$$3. \begin{aligned} S &= 0A \mid 1A \mid 8A \mid 9A \\ A &= 0A \mid 1A \mid 8A \mid 9A \mid .B \\ B &= 0B \mid 1B \mid 8B \mid 9B \mid \epsilon \end{aligned}$$

2. (10 points) For this problem, you will be given regular grammars with start symbol S describing given languages, and asked to write regular expressions defining the same language.

$$1. \begin{aligned} S &= aA \mid bB \\ A &= a \\ B &= bB \mid bA \end{aligned}$$

$$2. \begin{aligned} S &= aS \mid bS \mid cC \\ C &= aS \mid cC \mid c \end{aligned}$$

Solution:

1. $(aa) \vee (b(b)^*ba)$
2. $(a \vee b)^*c(c \vee a(a \vee b)^*c)^*c$